

Dynamika układów kwantowych i wprowadzenie do pakietu QuTiP (Quantum Toolbox in Python)

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Ewolucja czasowa układów kwantowych

Zależne od czasu równanie Schroedingera

$$i\hbar \frac{\partial \Psi(\mathbf{r}, t)}{\partial t} = H\Psi(\mathbf{r}, t) = H \begin{pmatrix} \psi_{\uparrow}(\mathbf{r}, t) \\ \psi_{\downarrow}(\mathbf{r}, t) \end{pmatrix}$$

Separacja części przestrzennej i spinowej/orbitalnej

$$\Psi(\mathbf{r}, t) = \begin{pmatrix} \psi_{\uparrow}(\mathbf{r}, t) \\ \psi_{\downarrow}(\mathbf{r}, t) \end{pmatrix} = \Psi(\mathbf{r}) \begin{pmatrix} \alpha_{\uparrow}(t) \\ \alpha_{\downarrow}(t) \end{pmatrix}$$

Ewolucja czasowa układów kwantowych

Zależne od czasu równanie Schroedingera

$$i\hbar \frac{d}{dt} |\Psi(t)\rangle = \hat{H}(t) |\Psi(t)\rangle$$

Dla pojedynczego kubitu

$$|\Psi(t)\rangle = a(t)|0\rangle + b(t)|1\rangle = \begin{pmatrix} a(t) \\ b(t) \end{pmatrix} \quad \hat{H} = \begin{pmatrix} h_{11}(t) & h_{12}(t) \\ h_{21}(t) & h_{22}(t) \end{pmatrix}$$

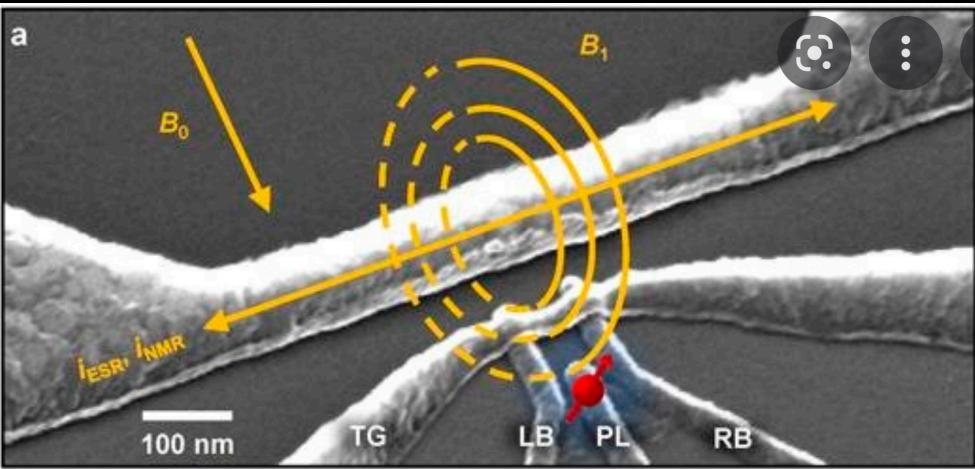
Układ równań różniczkowych zwyczajnych na $a(t)$ i $b(t)$

$$\begin{cases} i\hbar \dot{a}(t) = h_{11}(t)a(t) + h_{12}(t)b(t) \\ i\hbar \dot{b}(t) = h_{21}(t)a(t) + h_{22}(t)b(t) \end{cases}$$

Przykład Oscylacje Rabiego – Rezonans NMR (Nuclear Magnetic Resonance)

$$\hat{H} = -\vec{\mu} \cdot \vec{B}$$

$$\vec{\mu} = \frac{1}{2}\gamma_p \vec{\sigma}, \quad \gamma_p = 5.59 \frac{q_p \hbar}{2m_p}$$



$$\vec{B}_1(t) = (\cos(\omega t), -\sin(\omega t), 0)$$

$$\vec{B}_0(t) = (0, 0, B_0)$$

$$\vec{B}(t) = (\cos(\omega t), -\sin(\omega t), B_0)$$

$$\hat{H}(t) = -\frac{1}{2}\gamma_p B_0 \sigma_z - \frac{1}{2}\gamma_p B_1 (\cos(\omega t)\sigma_x - \sin(\omega t)\sigma_y)$$

Przykład Oscylacje Rabiego – Rezonans NMR (Nuclear Magnetic Resonance)

$$\hat{H}(t) = -\frac{1}{2}\gamma_p B_0 \sigma_z - \frac{1}{2}\gamma_p B_1 (\cos(\omega t)\sigma_x - \sin(\omega t)\sigma_y)$$

$$\hbar\omega_0 = \gamma_p B_0 \quad \hbar\omega_1 = \gamma_p B_1$$

$$\frac{\hbar\omega_0}{2} \quad |1\rangle = |\downarrow\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$



$$-\frac{\hbar\omega_0}{2} \quad |0\rangle = |\uparrow\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$\hat{H}(t) = -\frac{\hbar}{2}\omega_0 \sigma_z - \frac{\hbar}{2}\omega_1 (\cos(\omega t)\sigma_x - \sin(\omega t)\sigma_y)$$

Przykład Oscylacje Rabiego – Rezonans NMR (Nuclear Magnetic Resonance)

$$\hat{H}(t) = -\frac{\hbar}{2} \begin{pmatrix} \omega_0 & \omega_1 e^{i\omega t} \\ \omega_1 e^{-i\omega t} & -\omega_0 \end{pmatrix}$$

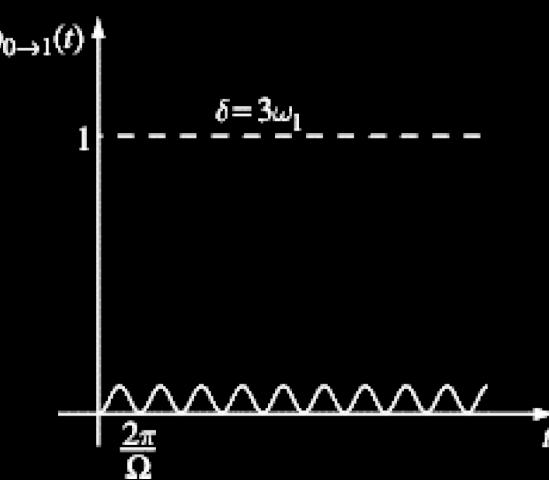
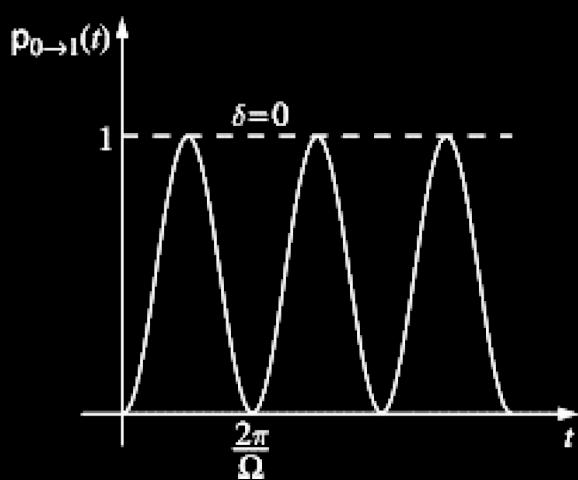
$$|\Psi(t)\rangle = a(t)|0\rangle + b(t)|1\rangle = \begin{pmatrix} a(t) \\ b(t) \end{pmatrix}$$

$$P_{|0\rangle \rightarrow |1\rangle}(t) = \left(\frac{\omega_1}{\Omega}\right)^2 \sin^2\left(\frac{\Omega t}{2}\right) \quad \Omega = \sqrt{(\omega - \omega_0)^2 + \omega_1^2}$$

Przykład Oscylacje Rabiego – Rezonans NMR (Nuclear Magnetic Resonance)

$$P_{|0\rangle \rightarrow |1\rangle}(t) = \left(\frac{\omega_1}{\Omega}\right)^2 \sin^2\left(\frac{\Omega t}{2}\right) \quad \Omega = \sqrt{(\omega - \omega_0)^2 + \omega_1^2}$$

$$P_{|0\rangle \rightarrow |1\rangle}(t) = \sin^2\left(\frac{\omega_1 t}{2}\right), \quad \omega = \omega_0$$



$$\frac{\omega_1 t}{2} = \frac{\pi}{2}, \quad t = \frac{\pi}{\omega_1}$$

$$\frac{\omega_1 t}{2} = \frac{\pi}{4}, \quad t = \frac{\pi}{2\omega_1}$$

Figure 3.4 Rabi oscillations. The *detuning* δ is defined as $\delta = \omega - \omega_0$.

Ewolucja czasowa układów kwantowych

Zależne od czasu równanie Schroedingera

$$i\hbar \frac{d}{dt} |\Psi(t)\rangle = \hat{H}(t) |\Psi(t)\rangle$$

Dla n kubitów

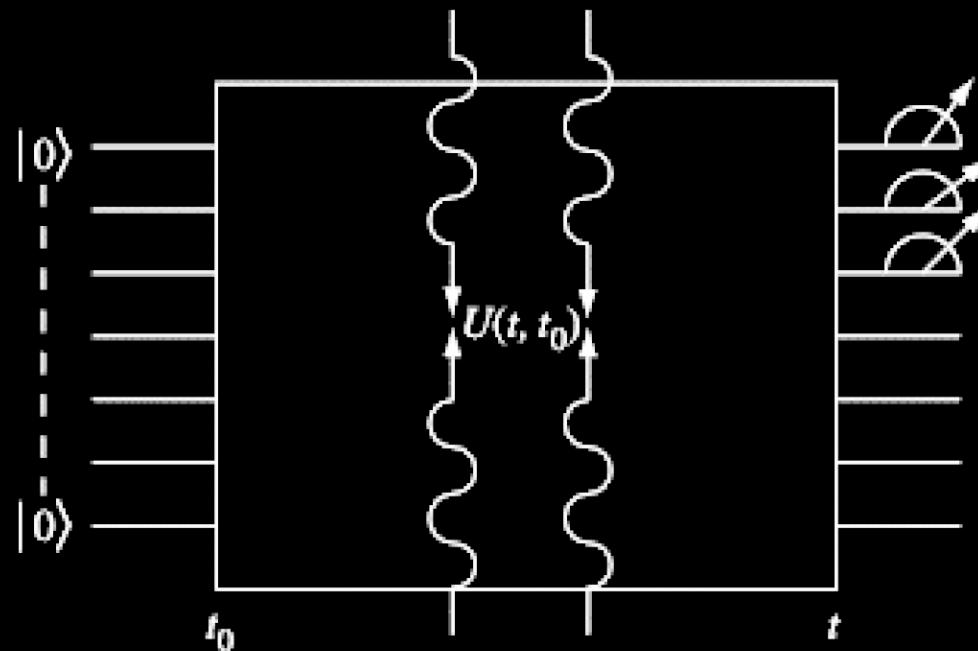
$$|\Psi(t)\rangle = \sum_{j=1}^{2^n} a_j |j\rangle$$

Układ 2^n równań różniczkowych zwyczajnych na $a_i(t)$, $i=1,2, \dots, 2^n$

$$i\hbar \begin{pmatrix} \dot{a}_1(t) \\ \dot{a}_2(t) \\ \vdots \\ \dot{a}_{2^n}(t) \end{pmatrix} = \begin{pmatrix} h_{11}(t) & h_{12}(t) & \dots & h_{12^n}(t) \\ h_{21}(t) & h_{22}(t) & \dots & h_{22^n}(t) \\ \vdots & \vdots & \ddots & \vdots \\ h_{2^n1}(t) & h_{2^n2}(t) & \dots & h_{2^n2^n}(t) \end{pmatrix} \begin{pmatrix} a_1(t) \\ a_2(t) \\ \vdots \\ a_{2^n}(t) \end{pmatrix}$$

Operator ewolucji czasowej, a bramki kwantowe

$$\hat{U}(t, t_0) = \exp \left[-\frac{i}{\hbar} \int_{t_0}^t dt' \hat{H}(t') \right]$$

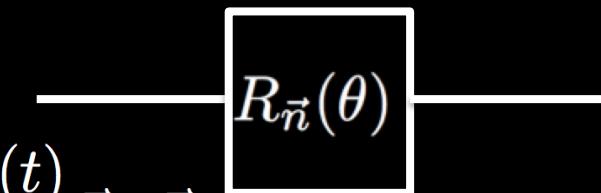


Operator ewolucji czasowej - impulsy generujące kwantowe bramki logiczne obrotu

$$\hat{U}(t, t_0) = \exp \left[-\frac{i}{\hbar} \int_{t_0}^t dt' \hat{H}(t') \right]$$

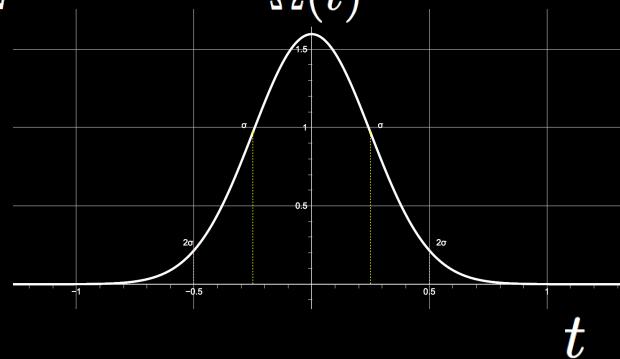
Hamiltonian cząstki o spinie $\frac{1}{2}$ w polu magnetycznym \mathbf{B} :

$$\hat{H}(t) = g\mu_B \vec{B}(t) \cdot \vec{S} = \frac{\hbar}{2} g\mu_B B_0(t) \vec{n} \cdot \vec{\sigma} = \frac{\hbar\Omega(t)}{2} \vec{n} \cdot \vec{\sigma}$$



$$\hat{U}(t, t_0) = \exp \left[-i \underbrace{\frac{1}{\hbar} \int_{-\infty}^{\infty} dt'}_{\text{underbrace}} \frac{\hbar\Omega(t')}{2} \vec{n} \cdot \vec{\sigma} \right]$$

$$R_{\vec{n}}(\theta) \equiv \exp \left(-i \vec{n} \cdot \vec{\sigma} \frac{\theta}{2} \right) = I \cos(\theta/2) - i(\vec{n} \cdot \vec{\sigma}) \sin(\theta/2)$$



Macierz gestości

$$\rho(t) = \begin{pmatrix} \rho_{00}(t) & \rho_{01}(t) \\ \rho_{10}(t) & \rho_{11}(t) \end{pmatrix}$$

Stany czyste

$$\rho(t) = |\Psi(t)\rangle\langle\Psi(t)| = \begin{pmatrix} |\alpha_0(t)|^2 & \alpha_0^*(t)\alpha_1(t) \\ \alpha_0(t)\alpha_1^*(t) & |\alpha_1(t)|^2 \end{pmatrix} \quad \rho^2 = \rho$$

Stany mieszane

Liouville–von Neumann equations

$$\rho = \sum_j \lambda_j |j\rangle\langle j|$$

$$\frac{d}{dt}\rho(t) = -\frac{i}{\hbar}[H, \rho(t)]$$

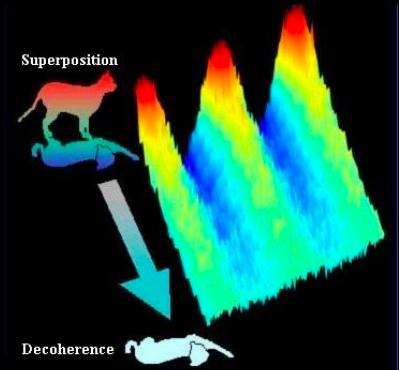
The Lindblad Master equation - decoherence

$$\dot{\rho}_{\text{tot}}(t) = -\frac{i}{\hbar} [H_{\text{tot}}, \rho_{\text{tot}}(t)]$$

$$H_{\text{tot}} = H_{\text{sys}} + H_{\text{env}} + H_{\text{int}}$$

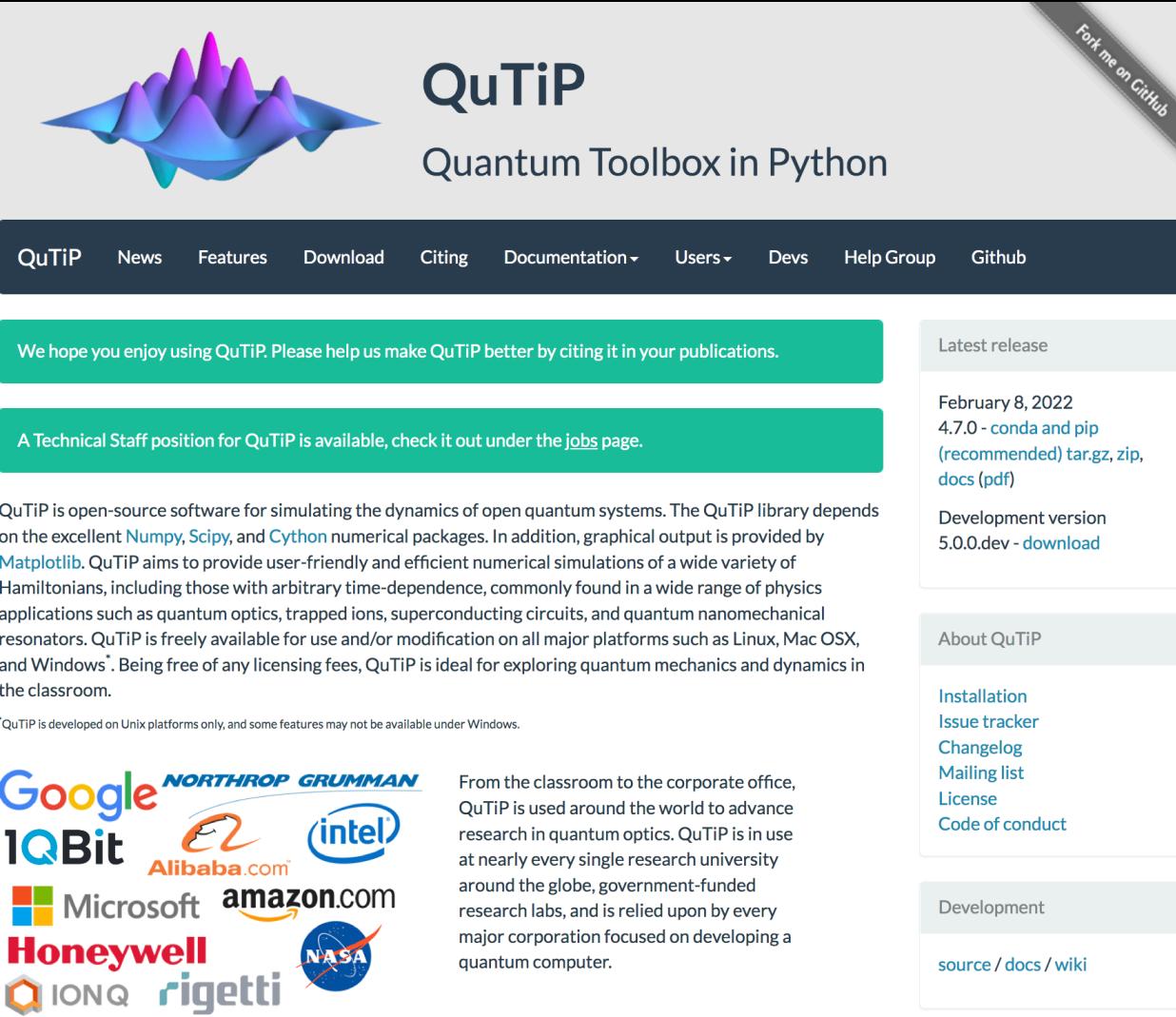
$$\rho = \text{Tr}_{\text{env}}[\rho_{\text{tot}}] \quad \rho_{\text{tot}}(t) \approx \rho(t) \otimes \rho_{\text{env}}$$

$$\dot{\rho}(t) = -\frac{i}{\hbar} [H(t), \rho(t)] + \sum_n \frac{1}{2} [2C_n \rho(t) C_n^\dagger - \rho(t) C_n^\dagger C_n - C_n^\dagger C_n \rho(t)]$$



$$C_n = \sqrt{\gamma_n} A_n$$

QuTiP <https://qutip.org/>



The screenshot shows the official website for QuTiP, a quantum toolbox in Python. The header features a 3D surface plot of a quantum state and the text "Fork me on GitHub". The main navigation bar includes links for QuTiP, News, Features, Download, Citing, Documentation, Users, Devs, Help Group, and Github. A teal banner at the top encourages citation, and another below it announces a job opening. The central content area describes QuTiP as open-source software for simulating quantum dynamics, mentioning dependencies like Numpy, Scipy, and Cython, and various applications such as quantum optics and nanomechanical resonators. It notes that QuTiP is freely available and ideal for classroom use. A small note states that QuTiP is developed on Unix platforms only. To the right, a sidebar provides links to the latest release (February 8, 2022), development version (5.0.0.dev), and detailed sections about QuTiP, including installation, issue tracking, and mailing lists. Logos of supporting organizations like Google, Northrop Grumman, IQBit, Alibaba, Intel, Microsoft, Amazon, Honeywell, NASA, IonQ, and Rigetti are displayed at the bottom.

We hope you enjoy using QuTiP. Please help us make QuTiP better by citing it in your publications.

A Technical Staff position for QuTiP is available, check it out under the [jobs](#) page.

QuTiP is open-source software for simulating the dynamics of open quantum systems. The QuTiP library depends on the excellent [Numpy](#), [Scipy](#), and [Cython](#) numerical packages. In addition, graphical output is provided by [Matplotlib](#). QuTiP aims to provide user-friendly and efficient numerical simulations of a wide variety of Hamiltonians, including those with arbitrary time-dependence, commonly found in a wide range of physics applications such as quantum optics, trapped ions, superconducting circuits, and quantum nanomechanical resonators. QuTiP is freely available for use and/or modification on all major platforms such as Linux, Mac OSX, and Windows*. Being free of any licensing fees, QuTiP is ideal for exploring quantum mechanics and dynamics in the classroom.

*QuTiP is developed on Unix platforms only, and some features may not be available under Windows.

From the classroom to the corporate office, QuTiP is used around the world to advance research in quantum optics. QuTiP is in use at nearly every single research university around the globe, government-funded research labs, and is relied upon by every major corporation focused on developing a quantum computer.

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[IONQ](#) [rigetti](#)

Latest release
February 8, 2022
4.7.0 - [conda](#) and [pip](#)
(recommended) tar.gz, zip,
docs (pdf)

Development version
5.0.0.dev - [download](#)

About QuTiP
[Installation](#)
[Issue tracker](#)
[Changelog](#)
[Mailing list](#)
[License](#)
[Code of conduct](#)

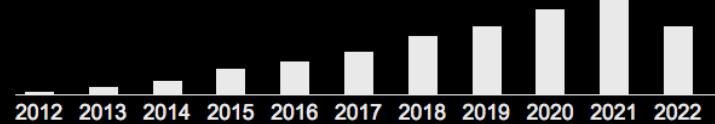
Development
[source / docs / wiki](#)

QuTiP Contributors and papers

J. R. Johansson, P. D. Nation, and F. Nori: "QuTiP 2: A Python framework for the dynamics of open quantum systems.", Comp. Phys. Comm. 184, 1234 (2013) [DOI: 10.1016/j.cpc.2012.11.019].

J. R. Johansson, P. D. Nation, and F. Nori: "QuTiP: An open-source Python framework for the dynamics of open quantum systems.", Comp. Phys. Comm. 183, 1760–1772 (2012) [DOI: 10.1016/j.cpc.2012.02.021].

Cited by 1998



Paul Nation
IBM Q
Library designer
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Library designer and
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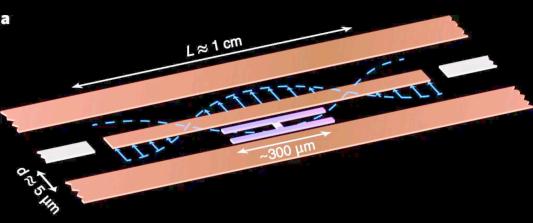


Franco Nori
RIKEN / University
of Michigan

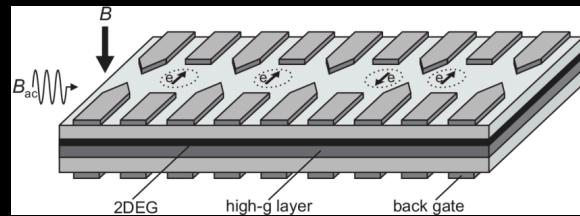
<https://qutip.org/devs.html>

Układy fizyczne, których dynamikę można symulować przy użyciu pakietu QuTiP

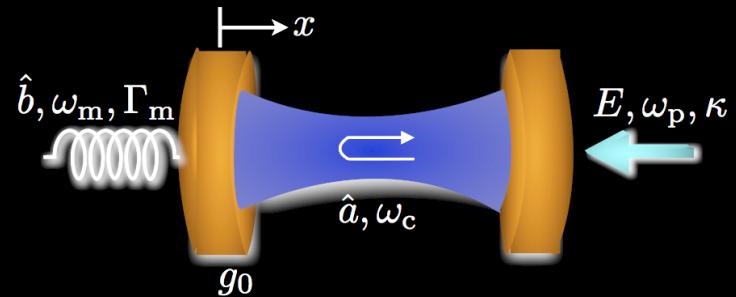
circuit QED



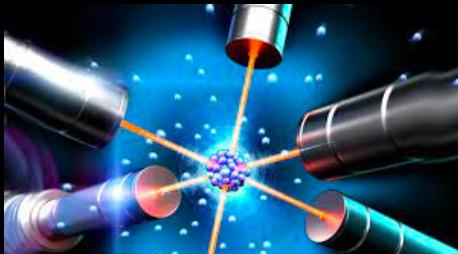
Spin chain



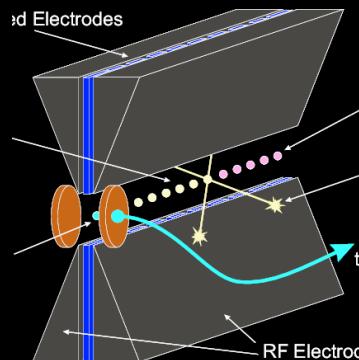
Optomechanical Systems



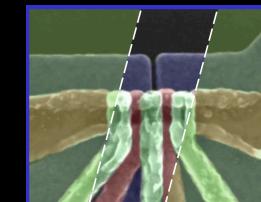
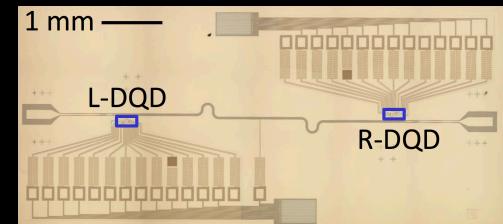
Quantum optics



Ion traps



Light matter interaction



Przykłady użycia pakietu QuTiP

Probing many-body dynamics on a 51-atom quantum simulator

Hannes Bernien, Sylvain Schwartz, Alexander Keesling, Harry Levine, Ahmed Omran, Hannes Pichler, Soonwon Choi, Alexander S. Zibrov, Manuel Endres, Markus Greiner  Vladan Vuletić  & Mikhail D. Lukin 

Nature 551, 579–584 (2017) | [Cite this article](#)

36k Accesses | 978 Citations | 432 Altmetric | [Metrics](#)

Unconditional quantum teleportation between distant solid-state quantum bits

W. PFAFF, B. J. HENSEN, H. BERNIEN, S. B. VAN DAM, M. S. BLOK, T. H. TAMINIAU, M. J. TIGGELMAN, R. N. SCHOUTEN, M. MARKHAM, [...] R. HANSON

+2 authors

[Authors Info & Affiliations](#)

SCIENCE • 29 May 2014 • Vol 345, Issue 6196 • pp. 532-535 • [DOI: 10.1126/science.1253512](#)

Entanglement-based single-shot detection of a single magnon with a superconducting qubit

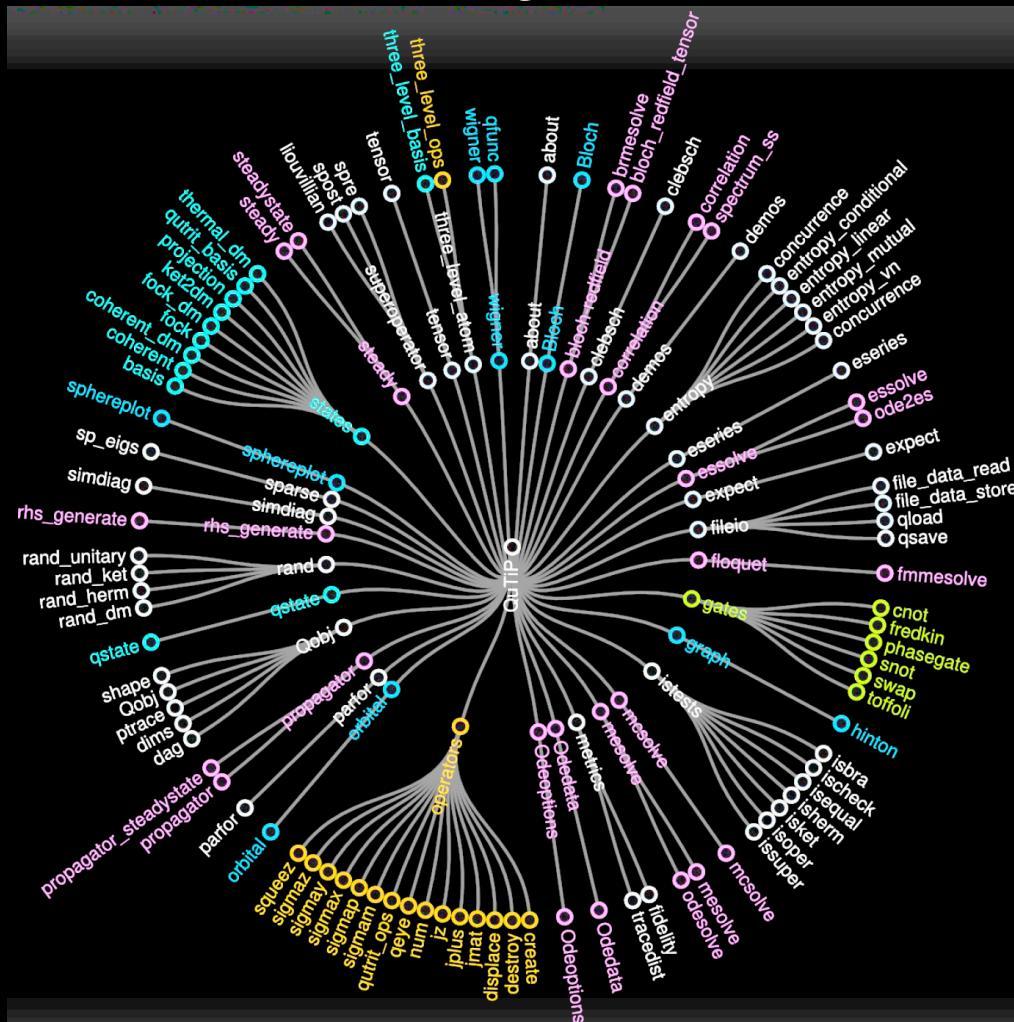
DANY LACHANCE-QUIRION , SAMUEL PIOTR WOLSKI , YUTAKA TABUCHI , SHINGO KONO , KOJI USAMI, AND YASUNOBU NAKAMURA 

[Authors Info & Affiliations](#)

SCIENCE • 24 Jan 2020 • Vol 367, Issue 6476 • pp. 425-428 • [DOI: 10.1126/science.aaz9236](#)



Funkcjonalność



<https://qutip.org/downloads/4.7.0/qutip-doc-4.7.pdf>

Stany - klasa Qobj

States	Command (# means optional)	Inputs
Fock state ket vector	basis (N, #m) / fock (N, #m)	N = number of levels in Hilbert space, m = level containing excitation (0 if no m given)
Fock density matrix (outer product of basis)	fock_dm (N, #p)	same as basis(N,m) / fock(N,m)
Coherent state	coherent (N, alpha)	alpha = complex number (eigenvalue) for requested coherent state
Coherent density matrix (outer product)	coherent_dm (N, alpha)	same as coherent(N,alpha)
Thermal density matrix (for n particles)	thermal_dm (N, n)	n = particle number expectation value

Operatory

Operators	Command (# means optional)	Inputs
Charge operator	charge (N, M=-N)	Diagonal operator with entries from M..0..N.
Commutator	commutator (A, B, kind)	Kind = ‘normal’ or ‘anti’.
Diagonals operator	qdiags (N)	Quantum object created from arrays of diagonals at given offsets.
Displacement operator (Single-mode)	displace (N, alpha)	N=number of levels in Hilbert space, alpha = complex displacement amplitude.
Higher spin operators	jmat (j, #s)	j = integer or half-integer representing spin, s = ‘x’, ‘y’, ‘z’, ‘+’, or ‘-’
Identity	qeye (N)	N = number of levels in Hilbert space.
Lowering (destruction) operator	destroy (N)	same as above
Momentum operator	momentum (N)	same as above
Number operator	num (N)	same as above
Phase operator (Single-mode)	phase (N, phi0)	Single-mode Pegg-Barnett phase operator with ref phase phi0.
Position operator	position (N)	same as above
Raising (creation) operator	create (N)	same as above
Squeezing operator (Single-mode)	squeeze (N, sp)	N=number of levels in Hilbert space, sp = squeezing parameter.
Squeezing operator (Generalized)	squeezing (q1, q2, sp)	q1,q2 = Quantum operators (Qobj) sp = squeezing parameter.
Sigma-X	sigmax ()	
Sigma-Y	sigmay ()	
Sigma-Z	sigmaz ()	
Sigma plus	sigmap ()	
Sigma minus	sigmam ()	
Tunneling operator	tunneling (N, m)	Tunneling operator with elements of the form $ N\rangle\langle N+m + N+m\rangle\langle N $.

Funkcje

Function	Command	Description
Check Hermiticity	<code>Q.check_herm()</code>	Check if quantum object is Hermitian
Conjugate	<code>Q.conj()</code>	Conjugate of quantum object.
Cosine	<code>Q.cosm()</code>	Cosine of quantum object.
Dagger (adjoint)	<code>Q.dag()</code>	Returns adjoint (dagger) of object.
Diagonal	<code>Q.diag()</code>	Returns the diagonal elements.
Diamond Norm	<code>Q.dnorm()</code>	Returns the diamond norm.
Eigenenergies	<code>Q.eigenenergies()</code>	Eigenenergies (values) of operator.
Eigenstates	<code>Q.eigenstates()</code>	Returns eigenvalues and eigenvectors.
Eliminate States	<code>Q.eliminate_states(inds)</code>	Returns quantum object with states in list <code>inds</code> removed.
Exponential	<code>Q.expm()</code>	Matrix exponential of operator.
Extract States	<code>Q.extract_states(inds)</code>	<code>Qobj</code> with states listed in <code>inds</code> only.
Full	<code>Q.full()</code>	Returns full (not sparse) array of <code>Q</code> 's data.
Groundstate	<code>Q.groundstate()</code>	Eigenval & eigket of <code>Qobj</code> groundstate.
Matrix Element	<code>Q.matrix_element(bra, ket)</code>	Matrix element $\langle \text{bra} Q \text{ket} \rangle$
Norm	<code>Q.norm()</code>	Returns L2 norm for states, trace norm for operators.
Overlap	<code>Q.overlap(state)</code>	Overlap between current <code>Qobj</code> and a given state.
Partial Trace	<code>Q.ptrace(sel)</code>	Partial trace returning components selected using 'sel' parameter.
Permute	<code>Q.permute(order)</code>	Permutes the tensor structure of a composite object in the given order.
Projector	<code>Q.proj()</code>	Form projector operator from given ket or bra vector.
Sine	<code>Q.sinm()</code>	Sine of quantum operator.
Sqrt	<code>Q.sqrtm()</code>	Matrix sqrt of operator.
Tidyup	<code>Q.tidyup()</code>	Removes small elements from <code>Qobj</code> .
Trace	<code>Q.tr()</code>	Returns trace of quantum object.
Transform	<code>Q.transform(inpt)</code>	A basis transformation defined by matrix or list of kets 'inpt' .
Transpose	<code>Q.trans()</code>	Transpose of quantum object.
Truncate Neg	<code>Q.trunc_neg()</code>	Truncates negative eigenvalues
Unit	<code>Q.unit()</code>	Returns normalized (unit) vector $Q/Q.\text{norm}()$.

Ewolucja czasowa wektorów stanu i macierzy gęstości - solvers

```
def mesolve(H, rho0, tlist, c_ops=None, e_ops=None, args=None, options=None, progress_bar=None, _safe_mode=True):
```

```
def mcsolve(H, psi0, tlist, c_ops=[], e_ops=[], ntraj=0, args={}, options=None, progress_bar=True, map_func=parallel_map, map_kwargs={}, _safe_mode=True):
```

```
def sesolve(H, psi0, tlist, e_ops=None, args=None, options=None, progress_bar=None, _safe_mode=True):
```

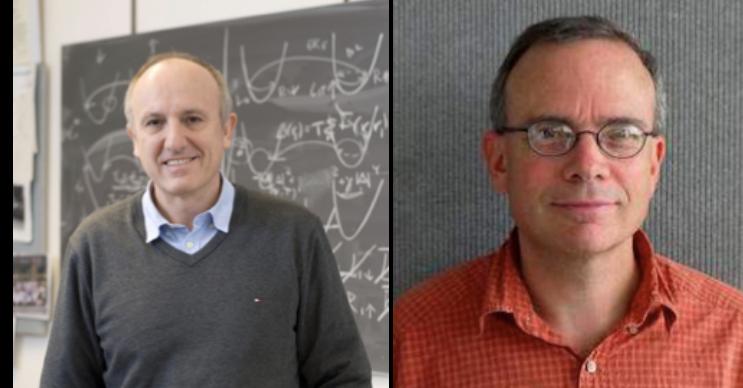
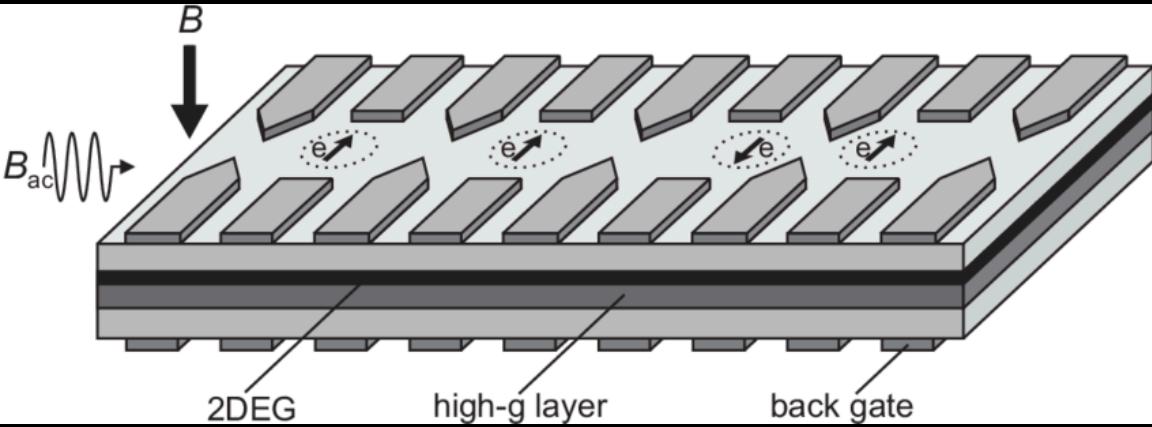
```
def brmesolve(H, psi0, tlist, a_ops=[], e_ops=[], c_ops=[], args={}, use_secular=True, sec_cutoff = 0.1, tol=qset.atol, spectra_cb=None, options=None, progress_bar=None, _safe_mode=True, verbose=False):
```

```
def ssesolve(H, psi0, times, sc_ops=[], e_ops=[], _safe_mode=True, args={}, **kwargs):
```

<https://qutip.org/docs/latest/modules/index.html>

I wiecej...

Spin w kropkach kwantowych



Daniel Loss

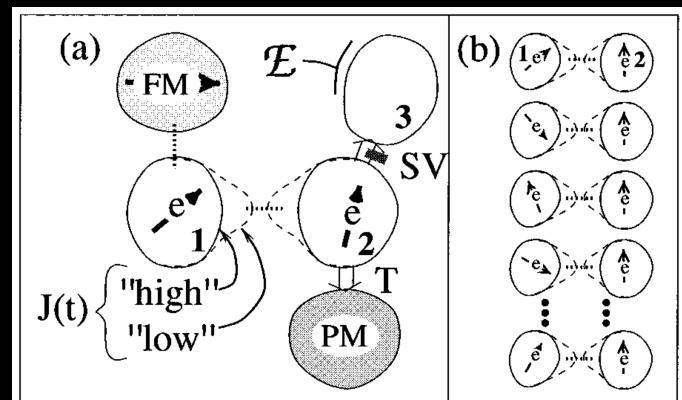
DP DiVincenzo

$$H = \sum_{\langle ij \rangle} J_{ij}(t) S_i \cdot S_j + \sum_i (g_i \mu_B B_i)(t) \cdot S_i$$

$$|\Psi\rangle = \alpha |\uparrow\rangle + \beta |\downarrow\rangle \quad |1\rangle = |\downarrow\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$S_i = \frac{\hbar}{2} \sigma_i$$

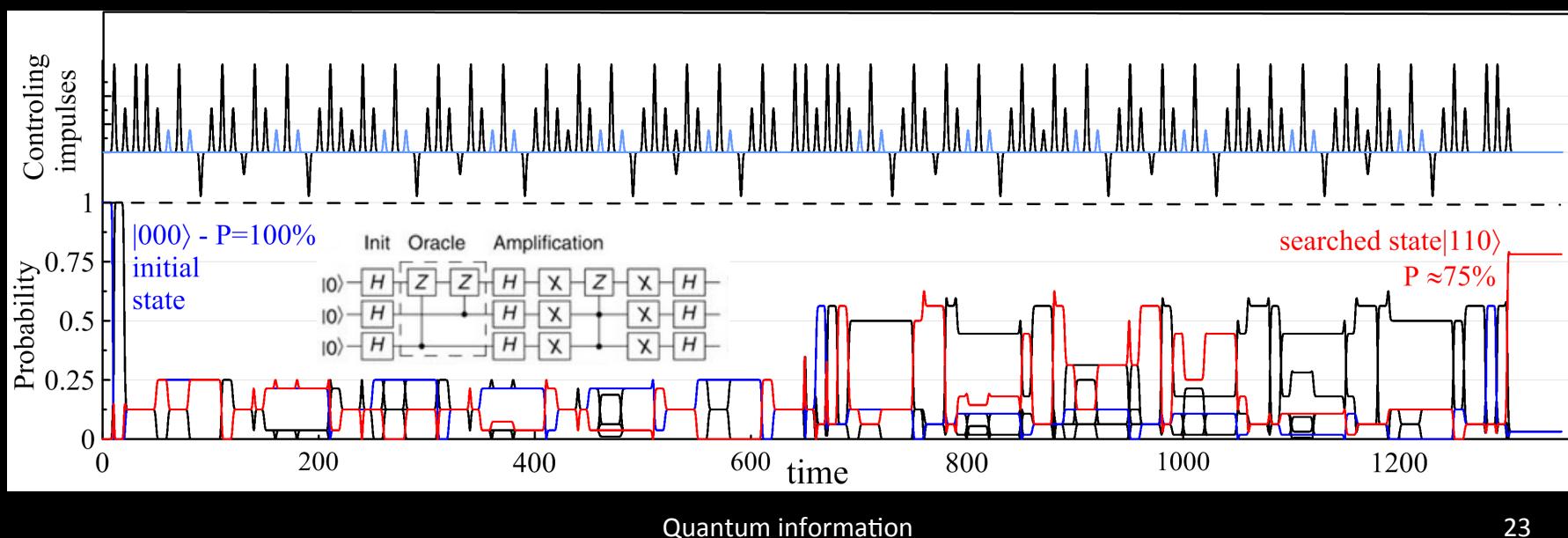
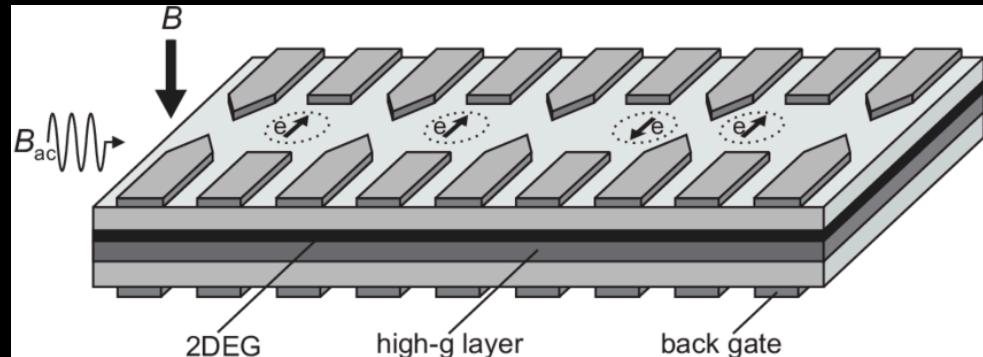
$$|0\rangle = |\uparrow\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$



Quantum computation with quantum dots
D Loss, DP DiVincenzo PRA **57** (1), 120 (1997)

Symulacja algorytmu Grovera

$$\begin{aligned}
 H(t) = & \vec{B}_1(t) \cdot \vec{\sigma}_1 \otimes I \otimes I \\
 & + \vec{B}_2(t) \cdot I \otimes \vec{\sigma}_2 \otimes I \\
 & + \vec{B}_3(t) \cdot I \otimes I \otimes \vec{\sigma}_3 \\
 & + J_{12}(t) \cdot \vec{\sigma}_1 \otimes \vec{\sigma}_2 \otimes I \\
 & + J_{23}(t) \cdot I \otimes I \otimes \vec{\sigma}_2 \otimes \vec{\sigma}_3
 \end{aligned}$$



Obliczenia kwantowe -Oprogramowanie

- <https://github.com/qosf/awesome-quantum-software>
- <https://quantumcomputingreport.com/tools/>
- <https://github.com/desireevl/awesome-quantum-computing>

Qiskit (IBM) - <https://qiskit.org/>

[Overview](#)[Learn](#)[Community](#) ▾[Documentation](#)

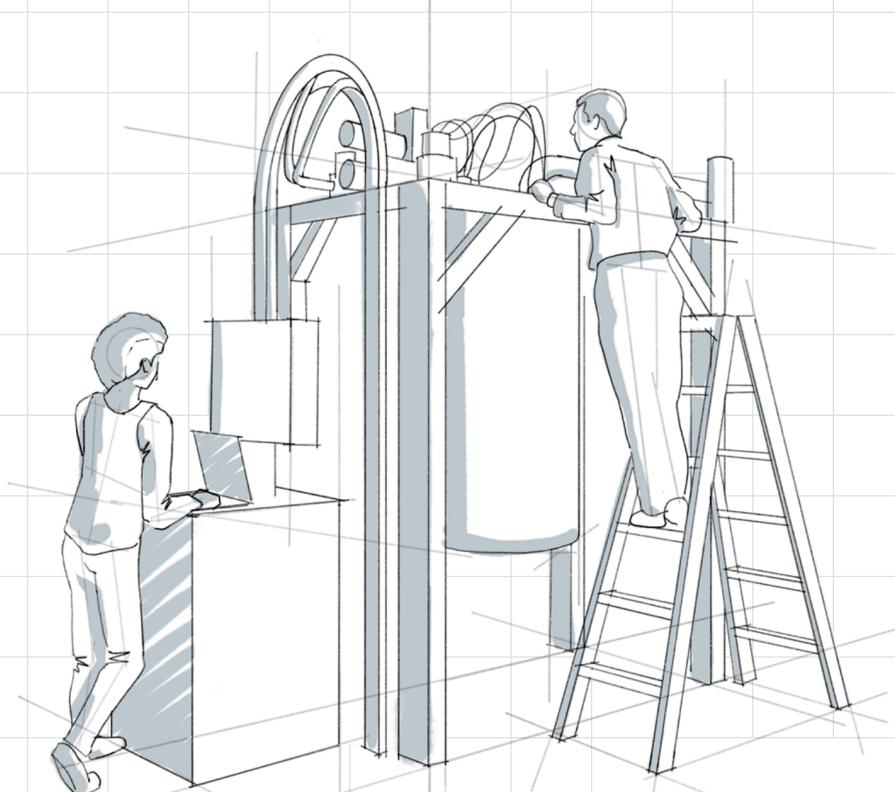
Start building with Qiskit runtime. Leverage the new programming model and execution framework to efficiently execute circuits.

[Learn more](#)

 qiskit 0.36.2
[see release notes](#)

Open-Source Quantum Development

Qiskit [kiss-kit] is an open-source SDK for working with quantum computers at the level of pulses, circuits, and application modules.

[Get started](#)

Q #(#Microsoft) - <https://azure.microsoft.com/en-us/resources/development-kit/quantum-computing/>

The screenshot shows the Azure Quantum Development Kit landing page. At the top, there's a navigation bar with the Azure logo, a search bar, and links for Docs, Support, Contact Sales, a Free account button, and Sign in. Below the navigation is a breadcrumb trail: Home / Resources / Development Kit. The main section features a large title "Q# and the Quantum Development Kit" with a subtitle "All the tools you need to develop quantum applications and formulate optimization problems". There are two buttons: "Get started" (blue) and "Access learning resources >". To the right is a 3D wireframe cube icon. At the bottom, there's a navigation bar with "Quantum Development Kit" (selected), Overview, Features, Get started, Resources, and FAQs.

The development kit for quantum computing

The open-source Quantum Development Kit for [Azure Quantum](#) offers tools for durable quantum application development on hardware-accelerated compute resources in Azure. Program your quantum algorithms and formulate optimization solutions, then apply those quantum solutions within the existing Azure platform to achieve real-world impacts now, before the development of a scalable [quantum computer](#) in the future.

Cirq (Google) -<https://quantumai.google/cirq>

Google Quantum AI Software ▾ Hardware ▾ Research ▾ Education Team ▾ Search

Cirq

Overview Guide Tutorials Experiments Reference

We're celebrating World Quantum Day 2022! [Join us](#)



Cirq

An open source framework for programming quantum computers

Cirq is a Python software library for writing, manipulating, and optimizing quantum circuits, and then running them on quantum computers and quantum simulators. Cirq provides useful abstractions for dealing with today's noisy intermediate-scale quantum computers, where details of the hardware are vital to achieving state-of-the-art results.

[Get started with Cirq](#) [GitHub repository](#)

```
import cirq

# Pick a qubit.
qubit = cirq.GridQubit(0, 0)

# Create a circuit
circuit = cirq.Circuit(
    cirq.X(qubit)**0.5, # Square root of NOT.
    cirq.measure(qubit, key='m') # Measurement.
)
print("Circuit:")
print(circuit)

# Simulate the circuit several times.
simulator = cirq.Simulator()
result = simulator.run(circuit, repetitions=20)
print("Results:")
print(result)
```



Forest (Rigetti)- <https://docs.rigetti.com/qcs/>

The screenshot shows the homepage of the Rigetti Quantum Cloud Services (QCS) documentation. The page has a dark header with the Rigetti logo and a search bar. A sidebar on the left contains a navigation menu with links to 'Welcome to Quantum Cloud Services', 'Getting Started', 'Guides', and 'References'. The main content area features a large title 'Welcome to Quantum Cloud Services' and a paragraph about QCS being Rigetti's quantum-first cloud computing platform. It includes a callout box with a checkmark icon and the text: 'If you don't already have a QCS account, you can [request one](#)'. Below this, there is a section titled 'Forest SDK' with a description of what it is and its components: pyQuil, quilc, and QVM. There is also a 'Try it!' section with a link to a Binder tutorial. The footer includes a 'Powered By GitBook' logo and a GitHub link: [GitHub: rigetti/forest-notebook/3-consolidate-tutorials](https://github.com/rigetti/forest-notebook/3-consolidate-tutorials). On the right side, there are additional links for 'Copy link', 'CONTENTS', 'Forest SDK', and 'Try it!'. The footer also contains a 'Quantum information' link.

Silq (ETH Zurich) - <https://silq.ethz.ch/>



What is Silq?

+ Overview

Comparison to Q#

+ Examples

+ Documentation

Installing Silq

Contact

News

About

Silq: Abstract

What is Silq?

[GitHub](#)

[ETH zürich](#)

Silq is a new high-level programming language for quantum computing with a strong static type system, developed at ETH Zürich. Silq was originally published at [PLDI'20](#).



More intuitive semantics

[Overview on Grover's Algorithm](#)



Reduce & simplify code

[Comparison to Q#](#)



Prevent errors

[Examples of prevented errors](#)



Safe automatic uncomputation

[Discussion of Uncomputation](#)



Physicality

[Examples of rejected unphysical programs](#)



Download Silq

[Installation instructions](#)



High-Level Quantum Programming

Watch later Share

Quantum information

Amazon Braket <https://aws.amazon.com/braket/>

The screenshot shows the Amazon Braket homepage with a dark background and blue header. The header includes navigation links: Amazon Braket, Overview (which is underlined), Features, Pricing, FAQs, Getting Started, Quantum Computers, and Customers. A blue banner at the top says "Free AWS Training | Advance your career with AWS Cloud Practitioner Essentials—a free, six-hour, foundational course »". Below the banner, the page title "Amazon Braket" and subtitle "Accelerate quantum computing research" are displayed. A prominent orange button says "Get Started with Amazon Braket". To the right, a callout box highlights "1 free hour of simulation time per month for a year with AWS Free Tier". Four main features are listed in boxes: "Easily work with different types of quantum computers and circuit simulators using a consistent set of development tools.", "Build quantum projects on a trusted cloud with simple pricing and management controls for both quantum and classical workloads.", "Run hybrid quantum-classical algorithms faster with priority access to quantum computers and no classical infrastructure to manage.", and "Innovate quickly with expert guidance and tech support, or collaborate with consultants in the Amazon Quantum Solutions Lab.". Below these, a section titled "How it works" explains the process: "Amazon Braket is a fully managed quantum computing service designed to help speed up scientific research and software development for quantum computing." It shows a flowchart with five steps: 1. "Build" (laptop icon) - "Build your quantum algorithms on managed Jupyter notebooks or in your own development environment". 2. "Test" (atom icon) - "Test your algorithms on a local simulator or a choice of fully managed, high-performance simulators". 3. "Run" (chip icons) - "Run your algorithms on your choice of different quantum computers. Combine classical and quantum computing resources for hybrid algorithms". 4. "Analyze" (graph icon) - "Analyze results after your algorithm has completed".

Amazon Braket
Get started with quantum computing

Build
Build your quantum algorithms on managed Jupyter notebooks or in your own development environment

Test
Test your algorithms on a local simulator or a choice of fully managed, high-performance simulators

Run
Run your algorithms on your choice of different quantum computers. Combine classical and quantum computing resources for hybrid algorithms

Analyze
Analyze results after your algorithm has completed

Quantum information

Dziękuję za uwagę



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