Zestaw 2

Katarzyna Sowa

1N

Rozwiązać równanie AX=e za pomoca metody Gaussa-Seidela oraz gradientów sprzężonych.

Metoda Gaussa-Seidela: wyniki:

```
||xk - x(k-1)|| = 4.347526282501
||xk - x(k-1)|| = 1.430748983160
||xk - x(k-1)|| = 0.471072861006
||xk - x(k-1)|| = 0.154869041634
||xk - x(k-1)|| = 0.051372333179
||xk - x(k-1)|| = 0.017263732423
||xk - x(k-1)|| = 0.006242350825
||xk - x(k-1)|| = 0.002642480878
||xk - x(k-1)|| = 0.001439319880
||xk - x(k-1)|| = 0.000915965548
||xk - x(k-1)|| = 0.000625614674
||xk - x(k-1)|| = 0.000437571586
||xk - x(k-1)|| = 0.000310315435
||xk - x(k-1)|| = 0.000222012213
||xk - x(k-1)|| = 0.000160001310
||xk - x(k-1)|| = 0.000116009217
||xk - x(k-1)|| = 0.000084551844
||xk - x(k-1)|| = 0.000061903004
||xk - x(k-1)|| = 0.000045499954
||xk - x(k-1)|| = 0.000033559499
||xk - x(k-1)|| = 0.000024828561
||xk - x(k-1)|| = 0.000018419295
||xk - x(k-1)|| = 0.000013697926
||xk - x(k-1)|| = 0.000010209164
||xk - x(k-1)|| = 0.000007624073
||xk - x(k-1)|| = 0.000005703819
||xk - x(k-1)|| = 0.000004274222
||xk - x(k-1)|| = 0.000003207749
||xk - x(k-1)|| = 0.000002410698
||xk - x(k-1)|| = 0.000001813999
||xk - x(k-1)|| = 0.000001366602
||xk - x(k-1)|| = 0.000001030672
||xk - x(k-1)|| = 0.000000778106
||xk - x(k-1)|| = 0.000000587987
||xk - x(k-1)|| = 0.000000444713
||xk - x(k-1)|| = 0.000000336629
||xk - x(k-1)|| = 0.000000255011
||xk - x(k-1)|| = 0.000000193322
||xk - x(k-1)|| = 0.000000146656
x0 = 0.194276803143
x1 = 0.130930197375
x2 = 0.146794905195
x3 = 0.162311327101
x4 = 0.091962599350
x5 = 0.135207496702
x6 = 0.119578852038
x7 = 0.111997198113
x8 = 0.140353962114
x9 = 0.116698372525
x10 = 0.127684994343
x11 = 0.129767053859
x12 = 0.117925997315
x13 = 0.129960046367
x14 = 0.123215743391
x15 = 0.123323606434
x16 = 0.128214932301
x17 = 0.122319713141
x18 = 0.126168377920
```

Metoda gradientów sprzężonych: wyniki:

```
||xk - x(k-1)|| = 0.332773183960
||xk - x(k-1)|| = 0.074073759768
||xk - x(k-1)|| = 0.023176288362
||xk - x(k-1)|| = 0.010205400914
||xk - x(k-1)|| = 0.004870100518
||xk - x(k-1)|| = 0.002793505377
||xk - x(k-1)|| = 0.002110760773
||xk - x(k-1)|| = 0.001485902085
||xk - x(k-1)|| = 0.000884308742
||xk - x(k-1)|| = 0.000429385951
||xk - x(k-1)|| = 0.000211693992
||xk - x(k-1)|| = 0.000117530404
||xk - x(k-1)|| = 0.000073097644
||xk - x(k-1)|| = 0.000049650735
||xk - x(k-1)|| = 0.000030263434
||xk - x(k-1)|| = 0.000016614641
||xk - x(k-1)|| = 0.000008596052
||xk - x(k-1)|| = 0.000004698531
||xk - x(k-1)|| = 0.000002881458
||xk - x(k-1)|| = 0.000001584908
||xk - x(k-1)|| = 0.000000554669
||xk - x(k-1)|| = 0.000000363768
||xk - x(k-1)|| = 0.000000129328
||xk - x(k-1)|| = 0.000000049167
||xk - x(k-1)|| = 0.000000026565
||xk - x(k-1)|| = 0.000000019393
||xk - x(k-1)|| = 0.000000013728
||xk - x(k-1)|| = 0.000000005886
||xk - x(k-1)|| = 0.000000002334
||xk - x(k-1)|| = 0.000000000821
||xk - x(k-1)|| = 0.000000000521
||xk - x(k-1)|| = 0.000000000328
||xk - x(k-1)|| = 0.000000000238
||xk - x(k-1)|| = 0.000000000097
||xk - x(k-1)|| = 0.000000000044
||xk - x(k-1)|| = 0.000000000021
||xk - x(k-1)|| = 0.000000000011
||xk - x(k-1)|| = 0.000000000005
||xk - x(k-1)|| = 0.000000000003
x0 = 0.194276795444
x1 = 0.130930202478
x2 = 0.146794908343
x3 = 0.162311315286
x4 = 0.091962615745
x5 = 0.135207486300
x6 = 0.119578848862
x7 = 0.111997214768
x8 = 0.140353939990
x9 = 0.116698387716
x10 = 0.127684995141
x11 = 0.129767036788
x12 = 0.117926021811
x13 = 0.129960027706
x14 = 0.123215746070
x15 = 0.123323621125
x16 = 0.128214908273
x17 = 0.122319733580
x18 = 0.126168371747
```

x19 = 0.125507835221
x20 = 0.123570968833
x21 = 0.126377778548
x22 = 0.124283199980
x23 = 0.124905712643
x24 = 0.125615565858
x25 = 0.124315015689
x26 = 0.125415325979
x27 = 0.124970544514
x28 = 0.124746049459
x29 = 0.125331256117
x30 = 0.124769941940
x31 = 0.125050735124
x32 = 0.125098428297
x33 = 0.124843977875
x34 = 0.125122908307
x35 = 0.124958145590
x36 = 0.124965529538
x37 = 0.125071487401
x38 = 0.124936308568
x39 = 0.125028242411
x40 = 0.125009816653
x41 = 0.124968242394
x42 = 0.125032120003
x43 = 0.124982762309
x44 = 0.124998722958
x45 = 0.125013597920
x46 = 0.124984214534
x47 = 0.125009863339
x48 = 0.124998925855
x49 = 0.124994438122
x50 = 0.125007553103
x51 = 0.124994643745
x52 = 0.125001280596
x53 = 0.125002159325
x54 = 0.124996497314
x55 = 0.125002732188
x56 = 0.124999136052
x57 = 0.124999159324
x58 = 0.125001562962
x59 = 0.124998784148
x60 = 0.125000301168
x61 = 0.125000491374
x62 = 0.124999305590
x63 = 0.125000284379
x64 = 0.125000361480
x65 = 0.124999280122
x66 = 0.125000447690
x67 = 0.125000385643
x68 = 0.124998714759
x69 = 0.125001570478
x70 = 0.124999220377
x71 = 0.124999044921
x72 = 0.125002794116
x73 = 0.124996506330
x74 = 0.125002082721
x75 = 0.125001377485
x76 = 0.124994588335
x77 = 0.125007530068
x78 = 0.124994527652
x79 = 0.124998824174
x80 = 0.125009913805
x81 = 0.124984248180
x82 = 0.125013498730
x83 = 0.124998828368
x84 = 0.124982714825
x85 = 0.125032079743
x86 = 0.124968347493
x87 = 0.125009708804
x88 = 0.125028288914
x89 = 0.124936351228
x90 = 0.125071380468

x19 = 0.125507824368
x20 = 0.123570990391
x21 = 0.126377757954
x22 = 0.124283208997
x23 = 0.124905719266
x24 = 0.125615547841
x25 = 0.124315035216
x26 = 0.125415315047
x27 = 0.124970541729
x28 = 0.124746063762
x29 = 0.125331238295
x30 = 0.124769953871
x31 = 0.125050735008
x32 = 0.125098417087
x33 = 0.124843993972
x34 = 0.125122896169
x35 = 0.124958147283
x36 = 0.124965538910
x37 = 0.125071472559
x38 = 0.124936320200
x39 = 0.125028240784
x40 = 0.125009807432
x41 = 0.124968256682
x42 = 0.125032109690
x43 = 0.124982761950
x44 = 0.124998733895
x45 = 0.125013583591
x46 = 0.124984222410
x47 = 0.125009867832
x48 = 0.124998911447
x49 = 0.124994452650
x50 = 0.125007553103
x51 = 0.124994643745
x52 = 0.125001280596
x53 = 0.125002159325
x54 = 0.124996497314
x55 = 0.125002732188
x56 = 0.124999136052
x57 = 0.124999159324
x58 = 0.125001562962
x59 = 0.124998784148
x60 = 0.125000301168
x61 = 0.125000491374
x62 = 0.124999305590
x63 = 0.125000284379
x64 = 0.125000361480
x65 = 0.124999280122
x66 = 0.125000447690
x67 = 0.125000385643
x68 = 0.124998714759
x69 = 0.125001570478
x70 = 0.124999220377
x71 = 0.124999044921
x72 = 0.125002794116
x73 = 0.124996506330
x74 = 0.125002082721
x75 = 0.125001377485
x76 = 0.124994588335
x77 = 0.125007530068
x78 = 0.124994527652
x79 = 0.124998824174
x80 = 0.125009913805
x81 = 0.124984248180
x82 = 0.125013498730
x83 = 0.124998828368
x84 = 0.124982714825
x85 = 0.125032079743
x86 = 0.124968347493
x87 = 0.125009708804
x88 = 0.125028288914
x89 = 0.124936351228
x90 = 0.125071380468

```
x91 = 0.124965638166
x92 = 0.124958098410
x93 = 0.125122867283
x94 = 0.124844082450
x95 = 0.125098321003
x96 = 0.125050783992
x97 = 0.124769977848
x98 = 0.125331157945
x99 = 0.124746152896
x100 = 0.124970493785
x101 = 0.125415297794
x102 = 0.124315103869
x103 = 0.125615469051
x104 = 0.124905764516
x105 = 0.124283218952
x106 = 0.126377703190
x107 = 0.123571056211
x108 = 0.125507783772
x109 = 0.126168368391
x110 = 0.122319773860
x111 = 0.128214856955
x112 = 0.123323655134
x113 = 0.123215744559
x114 = 0.129960000943
x115 = 0.117926058396
x116 = 0.129767010886
x117 = 0.127684999186
x118 = 0.116698403211
x119 = 0.140353917045
x120 = 0.111997231780
x121 = 0.119578844670
x122 = 0.135207479020
x123 = 0.091962627321
x124 = 0.162311307093
x125 = 0.146794910818
x126 = 0.130930204793
x127 = 0.194276791972
```

```
x91 = 0.124965538910
x92 = 0.124958147283
x93 = 0.125122896169
x94 = 0.124843993972
x95 = 0.125098417087
x96 = 0.125050735008
x97 = 0.124769953871
x98 = 0.125331238295
x99 = 0.124746063762
x100 = 0.124970541729
x101 = 0.125415315047
x102 = 0.124315035216
x103 = 0.125615547841
x104 = 0.124905719266
x105 = 0.124283208997
x106 = 0.126377757954
x107 = 0.123570990391
x108 = 0.125507824368
x109 = 0.126168371747
x110 = 0.122319733580
x111 = 0.128214908273
x112 = 0.123323621125
x113 = 0.123215746070
x114 = 0.129960027706
x115 = 0.117926021811
x116 = 0.129767036788
x117 = 0.127684995141
x118 = 0.116698387716
x119 = 0.140353939990
x120 = 0.111997214768
x121 = 0.119578848862
x122 = 0.135207486300
x123 = 0.091962615745
x124 = 0.162311315286
x125 = 0.146794908343
x126 = 0.130930202478
x127 = 0.194276795444
```

Efektywność obliczeniowa dla rozkładu Choleskyego wynosi $O(5n^2)$.
Dla metody Gaussa-Seidela wynosi ona O(m*5n). Tak samo jest w przypadku metody gradientow sprzężonych.