

Enhancing 3D reconstruction using Mobile Sensors Data

LATEX

Krzysztof Wrbel

CollegeOrDepartment

University

A thesis submitted for the degree of

Philosophiae Doctor (PhD), DPhil,..

year month

1. Reviewer: Name

2. Reviewer:

Day of the defense:

Signature from head of PhD committee:

Abstract

Put your abstract or summary here, if your university requires it.

To ...

Acknowledgements

I would like to acknowledge the thousands of individuals who have coded for the LaTeX project for free. It is due to their efforts that we can generate professionally typeset PDFs now.

Contents

List of Figures	vii
List of Tables	ix
1 Introduction	1
1.1 Purpose of this thesis	1
1.2 Scope	1
1.3 Initial assumptions	2
1.4 Thesis Outline	2
2 Fundamentals	3
2.1 3-D reconstruction in general	3
2.1.1 Feature extraction and correspondence matching	4
2.1.2 Fundamental & Essential Matrices	4
2.1.3 Triangulation	4
2.1.4 Common problems	4
2.2 Structure from Motion	4
2.2.1 Relative Pose Estimation	4
2.2.2 Homography estimation	4
2.2.3 Projective Factorization	4
2.2.4 Bundle Adjustment	4
2.2.5 Common problems	4
2.3 Mobile Sensors overview	4
2.3.1 Accelerometer	4
2.3.2 Gyroscope	4
2.3.3 Magnetometer	4

CONTENTS

2.3.4	Sensor Fusion	4
3	Related Work	5
4	Concept	7
4.1	Requirements	7
4.2	Reconstruction process strategy	8
4.3	Enhancing epipolar geometry equation	9
4.3.1	Rotation enhancements	9
4.3.2	Alternative 3-point algorithm for translation finding	10
4.3.3	Translation enhancements	11
4.4	Pose estimation	11
4.4.1	Known rotations & translations	12
4.4.2	Rotation enhancements	12
4.4.3	Rotation & translation enhancements	12
5	Implementation	13
5.1	Choosing Environment	13
5.2	Project Structure	13
5.3	”Sensor Enhanced Images Camera” - Android Gradle based project . . .	14
5.3.1	Installation	14
5.3.2	User Interface	14
5.3.3	Important Implementation Aspects	14
5.3.3.1	Rotation calculation	14
5.3.3.2	Custom heuristic for move estimation	15
5.3.3.3	Custom Sensor Data File format	16
5.4	”Enhanced 3D Reconstructor” - OSX CMake based project	18
5.4.1	User Interface	18
5.4.1.1	Test Efficiency	18
5.4.1.2	Test reconstruction	19
5.4.2	Important Implementation Aspects	19
5.4.2.1	Rotation matrix generation	20
5.4.2.2	Enhancing epipolar equations	20
5.4.2.3	3-point translation estimation, between cameras	21

CONTENTS

5.4.2.4	Enhancing pose estimation	23
6	Evaluation	25
6.1	Acquiring datasets	25
6.2	Test Environment	26
6.3	Testing two-view reconstruction methods	26
6.3.1	Accuracy - Epipolar lines correspondence	26
6.3.2	Time comparison	33
6.4	Testing reconstruction strategies	34
6.4.1	Accuracy	34
6.4.2	Execution time	36
6.5	Effectiveness	39
6.5.1	3D cloud reconstructed models	39
7	Conclusion	41
7.1	Summary	41
7.2	Dissemination	41
7.3	Problems Encountered	41
7.4	Future work	41
8	Materials & methods	43
References		47

CONTENTS

List of Figures

6.1	Plot of total Sampson Error in picture(1024x768pixels) in comparison to initial Sift feature number	27
6.2	Plot of per point Sampson Error in picture(1024x768pixels) in comparison to initial Sift feature number	28
6.3	Results of drawing estimated Epipolar lines on Warsaw Univeristy Dataset for 300 Sift points. 1) Standard Fundamental 8-point(upper pair), 2) Rotation Enhanced Fundamental 8-point(middle), 3) Alternative 3-point algorithm(bottom)	29
6.4	Results of drawing estimated Epipolar lines on Warsaw Univeristy Dataset for 300 Sift points. 1) Fundamental matrix created from rotation and translation(upper pair), 2) Standard Essential matrix 5-point(middle), 3)Rotation Enhanced Essential 5-point(bottom)	30
6.5	Results of drawing estimated Epipolar lines on Warsaw Univeristy Dataset for 1000 Sift points. 1) Standard Fundamental 8-point(upper pair), 2) Rotation Enhanced Fundamental 8-point(middle), 3) Alternative 3-point algorithm(bottom)	31
6.6	Results of drawing estimated Epipolar lines on Warsaw Univeristy Dataset for 1000 Sift points. 1) Fundamental matrix created from rotation and translation(upper pair), 2) Standard Essential matrix 5-point(middle), 3)Rotation Enhanced Essential 5-point(bottom)	32
6.7	Execution time of proposed algorithms(1024x768pixels) in comparison to initial Sift feature number	33
6.8	Comparison of different reconstruction strategies influence on Bundle Adjustment	35

LIST OF FIGURES

6.9 Total reconstruction execution time (4 images with resolution 1024x768pixels)
in comparison to initial Sift feature number 37
6.10 Total execution time of reconstruction with Bundle Adjustment(4 images
with resolution 1024x768pixels) in comparison to initial Sift feature number 38

List of Tables

8.1	Efficeincy table of proposed methods for 100 SIFT features in Warsaw Univeristy of technology dataset. Columns: Total Sampson Error, Avarage Sampson error per point, Amount of points left after outliers removal, Execution time	45
8.2	Efficeincy table of proposed methods for 500 SIFT features in Warsaw Univeristy of technology dataset. Columns: Total Sampson Error, Avarage Sampson error per point, Amount of points left after outliers removal, Execution time	45
8.3	Efficeincy table of proposed methods for 1000 SIFT features in Warsaw Univeristy of technology dataset. Columns: Total Sampson Error, Avarage Sampson error per point, Amount of points left after outliers removal, Execution time	45
8.4	Efficeincy table of proposed methods for 5000 SIFT features in Warsaw Univeristy of technology dataset. Columns: Total Sampson Error, Avarage Sampson error per point, Amount of points left after outliers removal, Execution time	46

GLOSSARY

1

Introduction

Mobile and wearable devices are becoming more and more popular. Modern smart-phones despite having extremely good camera's also use advanced sensor's, like Accelerometers, Gyroscope, Magnetometer, Barometer etc.. There is also a big need and growing market of Augmented Reality (AR) and Virtual Reality(VR). That's why image analysis and recognition, as well as 3-D reconstruction techniques are really hot topic. Unfortunately algorithms that support these techniques are very time and memory consuming, that's why it's really hard to run them on mobile devices, which have many limitations in terms of CPU speed and RAM memory capacity.

1.1 Purpose of this thesis

Author of this document will present the reader with an overview of the idea of 3D reconstruction. This thesis also inculdes brief description of related research in this area. After short analysis of efficiency, accuracy and common problems of few chosen algorithms this thesis will propose their enhacment with data acquired with sensors, which can be found in smartphones. At the end author presents evaluation and discuss test results. TODO finish

1.2 Scope

The author researched, how Accelerometer, Gyroscope and Magnetometer can be used in order to improve Fundamental, Essential matrix and also relative Pose Estimation.

1. INTRODUCTION

Unfortunately raw data sensors are really noisy and it's really hard to use them individually to enhance reconstruction. However there is a way to combine these data together in order to compensate error of each individual sensor. The term describing this process is called "Sensor Fusion". This data fusion allows to estimates in real time a relative or global(in term of earth magnetic field) rotation and translation of the device. TODO finish

1.3 Initial assumptions

The general process of 3-D reconstruction is quite broad, that's why the author of the thesis focus only on certain aspects of this topic. That's why author didn't write algorithms from the scratch, but built his algorithms on top of OpenCV library and "Relative Pose Estimation" Open-source project set up by In terms of sensor fusion, currently state of art approach is used by most of big Mobile Operating Systems(Android, iOS, Windows Phone). That's why author used Sensor Fusion API from API and only wrote what's needed in terms of getting rotation and translation of the smartphone camera, when acquiring images for his research. TODO finish

1.4 Thesis Outline

In Chapter 2 something something and so on

In Chapter 3

In Chapter 4

In Chapter 5

In Chapter 6

In Chapter 7

In Chapter 8

2

Fundamentals

In order to help user understand topics mentioned in this thesis, small theoretical background is needed.

2.1 3-D reconstruction in general

Today we have many devices, which are capable of 3D reconstruction. Most popular Kinect(?) is capable of real-time 3D cloud point generation, but that's very special case, because it uses 2 camera: RGB camera and IR depth-finding camera.

2. FUNDAMENTALS

2.1.1 Feature extraction and correspondence matching

2.1.2 Fundamental & Essential Matrices

2.1.3 Triangulation

2.1.4 Common problems

2.2 Structure from Motion

2.2.1 Relative Pose Estimation

2.2.2 Homography estimation

2.2.3 Projective Factorization

2.2.4 Bundle Adjustment

2.2.5 Common problems

2.3 Mobile Sensors overview

2.3.1 Accelerometer

2.3.2 Gyroscope

2.3.3 Magnetometer

2.3.4 Sensor Fusion

3

Related Work

There are many approaches to the problems, from raw one by one pixel analysis to high level abstraction of objects, light and shadows estimation[some references to each]. However this thesis does not focus on high-level abstraction reconstruction, but focuses on refining relative poses estimation steps. In order to estimates especially first two relative positions of cameras essential matrix must be decomposed. Since basic epipolar geometry equation many scientist introduced a way to solve this linear problems, where the main differences were in terms of accuracy and speed. One of the first was 8-point algorithm[reference], which can be used to compute a fundamental matrix. This is done without any prior knowledge of the scene, as well as camera parameters. Still to find relative position knowledge of internal camera parameters is needed in order to calculate and decompose Essential Matrix. Later on 5-point algorithm approaches were introduced[references], which needed prior knowledge of internal camera parameters. David Nister in his paper shows that 5-point outperforms almost all similar algorithms in terms of accuracy and speed. Only 8-point algorithm can be competitive, when it comes to forward image sequences. One of the state-of-art real-time and robust approaches is iterative 5-pt Algorithm created by Vincent Lui and Tom Drummond[].

Most of algorithms are very sensitive to presence of outliers. One of the most common approach is to use of RANSAC modelling[refining estimates], where iteratively subset of data is chosen to find a solution and then other points are checked, if they also satisfy equation with calculated solution.

3. RELATED WORK

Research group from Technische Universitt Berlin made an comparison and evaluation of methods, which were published at that point. It turned out that estimation of camera rotation is much more stable than translation. Also there are a lot of ambiguities in terms of choosing the correct solution of epipolar geometry equation.

In certain situation where external camera parameters as rotation and translation can be measured more accurate algorithms were proposed. In 2011 D. Scaramuzza from Zurich proposed a 1-point algorithm[reference], which shows how to describe and use model of camera mounted on a car to enhance 3D reconstruction. Introduced in 2013 4- point algorithm, which uses information of rotation angle in certain axis from additional sensor as show in paper[reference] can outperform even some versions 5-point algorithm. Lately scientists are creating more complex models to estimates relative stereometry. For instance group from Zurich proposed a way to enhance reconstruction with additional 6DOF sensor [Robust Real-Time Visual Odometry with a Single Camera and an IMU].

There are also different approaches like [Line-Based Relative Pose Estimation], where it's shown how to estimates the relative pose from 3 lines with two of the lines parallel and orthogonal to the third. Very accurate estimations also can be achieved when there is no camera rotation[Epipole Estimation under Pure Camera Translation*]. All these references shows that enhanced models help to achieve often faster more accurate solution.

Accuracy and speed are very important, when it comes to create systems capable of augmenting our reality. One of first successful systems for such situations were proposed by research group[PTAM]. They showed how two simultaneously working threads can be used to both create model of environment and use this knowledge to apply graphical effects to objects presented on stream camera video. Also some of these concepts where applied already even to robotic vision. Authors showed efficiency of proposed system for robot walking in cluttered indoor workspaces[MonoSLAM: Real-Time Single Camera SLAM].

The most important things, which can be concluded are rotation estimation is more stable than translation estimation and the more well described model of setup.

4

Concept

Here general concept will be described without details about descriptors used and so on... As indicated in similar research it's very attractive to use additional data to enhance reconstruction and reduce ambiguity in finding correct solution of 3D reconstruction. It also helps to achieve faster, more stable and robust algorithms. This thesis will show how prior knowledge of rotation or translation can be used to faster process 3D reconstruction of series of images. However there are many algorithms, which rely on accuracy of additional rotation and translation data. In reality especially, when it comes to hand-held smartphones, collected data are very noisy. That's why this thesis also proposes enhancements of most popular algorithmic approaches, when noisy data are used.

4.1 Requirements

Proposed methodology needs as the input series of images with additional information about position of the camera - euclidean rotation and optionally translation. Usage of smartphone is actually not necessary. Any camera with SensorFusioned accelerometer and gyroscope(magnetometer is optional and as discussed in 2.5??? has its up and downsides) capable of storing pictures and sensor data can be used. During algorithm runtime either both rotation and translation informations are used or just rotation, which as indicated in??? is less noisy than translation estimation. Internal camera parameters need to be calculated before reconstruction process is began. Additional sensor data can be unaccurate and noisy.

4. CONCEPT

4.2 Reconstruction process strategy

Both Epipolar equations and Pose Estimation improvements can be used in different configurations. It's expected that some of them are more accurate and some are faster. It was necessary to evaluate this approaches both in term of speed and accuracy. Author of this thesis proposes environment, where user can decide what type of stargy she/he wants to use. In terms of initialization of 3D cloud point reconstruction can be made using:

1. Known rotatations and translations - relative poses are calculated from sensor data - euclidian reconstruction
2. Known rotations - Alternative 3-point algorithm for translation finding or enhanced fundamental/essential
3. Noisy rotation - enhanced fundamental/essential for dR and translation
4. No known extrisinc parameters - standard fundamental/essential for R and Translation

Later one new images are analized in comparison to previous one to enrich initial cloud point with new points. It's only necessary to keep track of each 3D cloud point corresponding 2D positions in images. In terms of Pose Estimation following methodologies can be used:

1. Known rotatation and translations - no additional calculations, just triangulation - euclidian reconstruction
2. Known rotation - looking for relative translation by backProjection optimisations
3. Noisy rotation - looking for dR and translation by backProjection optimisations
4. No known extrisinc parameters - standard pose estimation

Of course in all of this steps it's really important to have as minimum outliers as possible. All of this methods are pretty good in terms of removing outliers, espiecially when connected with RANSAC algorithm.

4.3 Enhancing epipolar geometry equation

4.3.1 Rotation enhancements

Taking standard fundamental geometry equation and relative camera based system ($P = [I|0]$, $P' = [R|t]$) we can note that:

$$x^T * K^{-T} * [T]_x * R * K^{-1} * x = 0 \quad (4.1)$$

It's also good to note that:

$$[T]_x = \begin{bmatrix} 0 & -t_z & t_y \\ t_z & 0 & -t_x \\ -t_y & t_x & 0 \end{bmatrix} \text{ where } T = [t_x, t_y, t_z] \quad (4.2)$$

As we were discussing both rotation and translation can be distorted with noise. This can be written as:

$$R = R_{error} * R_{init} \quad (4.3)$$

where R_{init} is rotation matrix from measured angles and R_{error} is rotation matrix of angles errors. Looking at this from different point of view 4.3 can be interpreted as multiplying two rotations matrix: One estimated, but close to local optimum initial rotation matrix and second one correcting noise error rotation matrix. Basic idea of algorithm proposed in this thesis is instead of R calculation, which as described in [reference] can be acquired from Essential matrix SVD decomposition, R_{error} will be estimated. In the end 4.1 can be rewritten in form:

$$x^T * K^{-T} * [T]_x * R_{error} * R_{init} * K^{-1} * x = 0 \quad (4.4)$$

Having:

$$\begin{aligned} h^T &= x^T * K^{-T} \\ h &= R_{init} * K^{-1} * x \\ G &= [T]_x * R_{error} \end{aligned} \quad (4.5)$$

With such notation one can notice that

$$h^T * G * h = 0 \quad (4.6)$$

quite resembles both standard fundamental and essential equation [reference]. Of course h' and h are both homogenous. From analysis it's known that G has 6DOF: 3 due to unknown translation and 3 due to unknown correction angles. From theory such

4. CONCEPT

matrix can be resolved for instance by both 5 and 8-point algorithms. So basicly standard fundamental and essential equation solvers can be used in order to retrieve both $[T]_x$ and R_{error} in order to resolve some common problems in retrieving correct solution and improve accuracy. In the end estimated R_{error} and calculated R_{init} can be multiplied to retrieve new rotation R (4.3). Also to reduce error estimation using Rodrigues parametrization, when the angles are small(and they indeed are because only small error is present in sensor data) we can note that R_{error} in fact is more or less equals to:

$$R_{error} \cong \begin{bmatrix} 1 & -w_z & w_y \\ w_z & 1 & -w_x \\ -w_y & w_x & 1 \end{bmatrix} \quad (4.7)$$

[Refernece to Hartley]. It can be used when decomposing G to ensure proper decomposition. What's more in normal situation in case of both these algorithms we have to decompose recovered matrix to both relative rotation and translation. However we normally have to deal with small ambiguity and check for instance by initial triangulation, which R and T use. Using this Rodriguez representation, we can reduce 4 solution test cases to 2 possibly solutions test-case.

4.3.2 Alternative 3-point algorithm for translation finding

Starting 4.6 it can be written that:

$$x'_r^T * K^{-T} * \begin{bmatrix} 0 & -t_z & t_y \\ t_z & 0 & -t_x \\ -t_y & t_x & 0 \end{bmatrix} * R * K^{-1} * x = 0 \quad (4.8)$$

Having:

$$\begin{aligned} h'_r^T &= x'_r^T * K^{-T} \\ h &= K^{-1} * x \end{aligned} \quad (4.9)$$

$$[h'_{11} \ h'_{12} \ h'_{13}] * \begin{bmatrix} 0 & -t_z & t_y \\ t_z & 0 & -t_x \\ -t_y & t_x & 0 \end{bmatrix} * \begin{bmatrix} h_1 \\ h_2 \\ h_3 \end{bmatrix} = 0 \quad (4.10)$$

and multiplying it we will end up with

$$h_1 * h'_{12} * t_z - h_1 * h'_{13} * t_y - h_2 * h'_{11} * t_z + h_2 * h'_{13} * t_x + h_3 * h'_{11} * t_y - h_3 * h'_{12} * t_x = 0 \quad (4.11)$$

what can be grouped:

$$t_x * (h_2 * h'_{13} - h_3 * h'_{12}) + t_y * (h_3 * h'_{11} - h_1 * h'_{13}) + t_z * (h_1 * h'_{12} - h_2 * h'_{11}) = 0 \quad (4.12)$$

rewritten as:

$$\begin{bmatrix} t_x & t_y & t_z \end{bmatrix} * \begin{bmatrix} (h_2 * h_{\prime 3} - h_3 * h_{\prime 2}) \\ (h_3 * h_{\prime 1} - h_1 * h_{\prime 3}) \\ (h_1 * h_{\prime 2} - h_2 * h_{\prime 1}) \end{bmatrix} = 0 \quad (4.13)$$

and solved for instance with SVD with only 3 points. This is very attractive way of reconstructing images from only 3 points especially in terms of speed. Overall accuracy strictly relies on precise measurements of camera orientation.

4.3.3 Translation enhancements

It's known that without any additional informations about photographed scene or exact translation of camera scale cannot be retrieved and only affine reconstruction can be done. As described in [ref] using SensorFusion linear acceleration of the capable camera can be calculated. Combining it with certain robust heuristic for movement estimation and low-pass filter relative/global translation of the camera can also be estimated. This information can be used to perform Euclidian reconstruction. Calculated T from G decomposition(??) can be combined with T_{global} acquired by double integration of linear acceleration. Due to double integration error can be big, but in general it's almost the same in every direction. It may not be perfect, but still it can help to estimate range of euclidian reconstruction.

4.4 Pose estimation

Different approaches to continuous multiview 3D reconstruction were discussed. This research main goal was to make it more accurate and faster. That is why it focuses on pose estimation instead of homographies merging. This is also good in terms of keeping scale in between next image analysis. For any point in image following condition is kept:

$$x = P * X \quad (4.14)$$

where x is homogenous image point (x , y , 1) and X homogenous 3D point (X , Y , Z , 1). Of course

$$P = K * [R | t] \quad (4.15)$$

4. CONCEPT

4.4.1 Known rotations & translations

In situation were rotations and translations of cameras are known no additional calculations are needed. Both rotation and translation of the camera can be estimated from sensors. Such situation is interesting, because there is already everything needed for triangulation of points. To resolve inaccuracy of especially translation measurements standard Bundle Adjustment methods can be used in order to refine reconstruction results.

4.4.2 Rotation enhancements

Using similar thinking as in previous section[ref] we can note that:

$$\begin{aligned} x &= K * [Rinit + dR | t] * X \\ x &= K * [Rinit | 0] * X + K * [dR | t] * X \\ x - K * [Rinit | 0] &= K * [dR | t] * X \end{aligned} \quad (4.16)$$

Substituting $x_m = x - K * [Rinit | 0]$ we get:

$$x_m = K * [dR | t] * X \quad (4.17)$$

This can be solved using normal PNP calculating algorithms. It's known that orientation estimation is more accurate than translation estimation using SensorFusion and this approach allows very accurate calculation of rotation error matrix dR and translation t , which keeps the scale of initially reconstructed points cloud.

4.4.3 Rotation & translation enhancements

Similar to 4.16:

$$\begin{aligned} x &= K * [Rinit + dR | Tinit + dt] * X \\ x &= K * [Rinit | Tinit] * X + K * [dR | dt] * X \\ x - K * [Rinit | Tinit] &= K * [dR | dt] * X \end{aligned} \quad (4.18)$$

end in the end by Substituting $x_n = x - K * [Rinit | Tinit]$ we get:

$$x_n = K * [dR | dt] * X \quad (4.19)$$

We can note that when initial solution is already known, the problems begins to focus on refining pose estimation instead of searching for it.

5

Implementation

In order to perform some tests with proposed methodology there was a need to prepare environment for it.

5.1 Choosing Environment

One thing was to prepare application, which would be capable of taking both pictures with additional SensorFusioned data. Currently Android has one of the best APIs which allows user to get both raw and fusioned sensor data. In order to avoid coding from scratch all sterometry algorithms there was need to choose library, which is fast and has most of discussed algorithms implemented. This is where OpenCV performs really good. However it's really hard to get it running on Android, due to long time compiling, problematic error debugging and speed performance. This is why author decided to separate process of acquiring images from processing them. In order to enrich images with sensor data Android app was created and standalone C++ desktop app to perform processing and evaluation.

5.2 Project Structure

Both applications source can be found on attached CD and under the Github web-page: <https://github.com/KrzysztofWrobel/MasterThesisSource.git>. In general project was separated to different subprojects: Android and Desktop. In addition some sample datasets were added to Dataset folder.

5. IMPLEMENTATION

5.3 "Sensor Enhanced Images Camera" - Android Gradle based project

In order to capture images and associate them with Sensor data custom photo capture app called "... were created. User can track in real time parameters euclidian angles of smartphone in global earth coordinate system. When taking picture current rotation data as well relative translation from last capture are stored in custom JSON file, which is later saved along taken picture in separate folder. All of captured pictures and sensor data can be compressed and sent through internet to the user. By default they are saved on internal SD card in folder, which is automatically created timestamp folder.

5.3.1 Installation

Gradle based build system was used, which is currently recommended way to handle Android based projects ref. google. Currently this app supports devices with Android 4.0 and above. In order to compile this project it's recommended to install Android Studio. It already contains Android SDK and also has built-in Gradle support. More informations about configuration, compilation and install steps can be found in README.md in main catalog.

5.3.2 User Interface

ScreenShot. Apps allows to track camera angles in real time, so user can precisely decide angles of capture. Also heuristical movement and translation estimation can be seen. In order to capture photo, user only has to click in the screen center.

5.3.3 Important Implementation Aspects

Only master thesis specific code is described in detail.

5.3.3.1 Rotation calculation

Android SDK has already API, which can be used to access both raw and "sensor fused" data. In particular for rotation estimation *Sensor.TYPE_ROTATION_VECTOR* was used. It returns 9DOF quaternion in reference to geomagnetic north. In order to decompose it to euler angles helper method were used:

5.3 "Sensor Enhanced Images Camera" - Android Gradle based project

```
private float[] euclidianAnglesFromQuaternion(float[] quaternion) {
    ...
    //Converts quaternion to 4x4 rotation matrix
    SensorManager.getRotationMatrixFromVector(rotMat, quaternion);
    ...
    //Extracts euclidian Angles in radians
    SensorManager.getOrientation(rotMat, orientation);
    ...
    return orientation;
}
```

5.3.3.2 Custom heuristic for move estimation

Unfortunately using only accessible sensor data it's hard to estimate relative translation of the device. Accelerometer, even compensated Android *Sensor.TYPE_LINEAR_ACCELERATION* measures only linear acceleration of the device. These measures, which are very noisy itself, not only due to for instance hands shaking, need to be double integrated in time in order to get move distance. As proposed system is supposed to be used for hand-held cameras on order to minimise noise influence following enhanced heuristic for people walk model was proposed:

1. When new linear acceleration sensor data is ready, first apply lowPass filtering in order to reduce some high frequency noise.
2. Change sensor datda vector from local camera coordinates to global reference system(multiply with inverted rotation matrix)
3. Decide depending on current state, if deviceMovmentState has changed:
 - (a) If device was previously IDLE and incoming Acceleration value is bigger than $0.5 \frac{m}{s^2}$ change device state to MOVING and reset current velocity to $0 \frac{m}{s}$
 - (b) If device was previously MOVING and incoming Acceleration value is smaller than $0.1 \frac{m}{s^2}$ change device state to IDLE
4. Only if device is currently moving:
 - (a) Update device velocity

5. IMPLEMENTATION

- (b) Check current speed with walk constraint(People walk with average speed $1.5 \frac{m}{s}$) and eventually scale it down to maximum value
- (c) Update device position

Described algorithm implementation snippet can be found in listing 5.1. Human walking model was introduced in order to constraint the velocity. Without it integrating small noise over time, would eventually result in high unrealistic movements. Maximum walking speed can be adjusted but by default it should be around $1.5 \frac{m}{s}$ http://en.wikipedia.org/wiki/Preferred_walking_speed. In fact the most important factor of good position estimation is vector angle, fortunately noise equally influence each axes, so it should be statistically correct.

5.3.3.3 Custom Sensor Data File format

As mentioned each photo capture stores additional sensor information. These informations are:

- id - indicates order of photos
- relative path to image file
- Euler Angles - pitch, roll, azimuth
- Position coordinates in geomagnetic north system(relative to previous image)
- Android rotation quaternion

All of this information are stored in a list and when the user is done with taking pictures all informations are saved into JSON file named sensor.txt. Sample file can be found in attachments.

5.3 "Sensor Enhanced Images Camera" - Android Gradle based project

```
1  public void onSensorChanged(SensorEvent event) {
2      ...
3      } else if (event.sensor == mLinearAcceleration) {
4          ...
5          //Filtering out some noise
6          newGlobalAcceleration = lowPass(newGlobalAcceleration,
7              currentGlobalAcceleration);
8          //Switch linear acceleration from phone local coordinates to
9          //global coordinates
10         Matrix.multiplyMV(newGlobalAcceleration, 0,
11             invertedRotationMatrix.clone(), 0, newGlobalAcceleration,
12             0);
13
14         double distance = getLength(currentGlobalAcceleration);
15         long currentTimeMillis = System.currentTimeMillis();
16         //Decide state of the device. Distance is in m/s^2
17         if (distance > 0.5 && deviceState == State.IDLE) {
18             if (currentTimeMillis - movingEndTime > 300) {
19                 deviceState = State.MOVING;
20                 currentGlobalVelocity = {0,0,0};
21             }
22         }
23
24         if (deviceState == State.MOVING) {
25             //Update current device velocity
26             currentGlobalVelocity += currentGlobalAcceleration * dT;
27
28             double velocity = getLength(currentGlobalVelocity);
29             //Check and adjust current velocity. People walk with
30             //avarage speed 1.5\frac{m}{s}
31             if (velocity > WALKING_MAX_VELOCITY) {
32                 currentGlobalVelocity /= velocity /
33                     WALKING_MAX_VELOCITY;
34             }
35
36             //Update device relative position, s = v0 * t + a * t
37             //^2/2;
38             currentRelativePosition += currentGlobalVelocity * dT +
39                 currentGlobalAcceleration * dT * dT / 2;
40         }
41         ...
42     }
```

Listing 5.1: Snippet from Android source code position estimation heuristic

5. IMPLEMENTATION

5.4 "Enhanced 3D Reconstructor" - OSX CMake based project

In order to evaluate algorithms there was need to prepare project environment suitable for this task. Discussion of choosing motivations, where done in 5.2. Author choosed CMake in order to make simpler build and compilation process. Whole project, where developed and tested on OSX 10.9 Mavericks. In order to compile this project following things need to be installed first:

- CMake 2.8
- OpenCV 2.4.10
- Point Cloud Library (PCL) 1.7
- Boost 1.55
- cvsba (<http://www.uco.es/investiga/grupos/ava/node/39>)

5.4.1 User Interface

There two targets defined in CMake file:

1. Test efficiency - used to evaluate pair reconstruction methods, draw epipolar lines in images and calculate samson error distances
2. Test reconstruction - used to evaluate proposed initialization reconstruction with different pose estimation methods

5.4.1.1 Test Efficiency

There is no graphical interface for reconstruction parameters configuration. However at the beginning there are few command-line inputs required to continue reconstruction. User needs to configure:

1. Enhanced Photo Data folder path
2. SIFT features number

Calculated parameters are printed to Console Window. TODO What can be seen there? Screenshot from console output.

5.4 "Enhanced 3D Reconstructor" - OSX CMake based project

5.4.1.2 Test reconstruction

There is no graphical interface for reconstruction parameters configuration. However at the beginning there are few command-line inputs required to continue reconstruction. User needs to configure:

1. Enhanced Photo Data folder path
2. SIFT features number
3. Init pair reconstruct method:
 - Standard Fundamental equation based
 - Enhanced Fundamental equation based
 - Standard essential equation based
 - Enhanced essential equation based
 - 3-point Translation estimation
 - None - use existing rotations and translations
4. Pose estimation method:
 - Standard 3d-2d perspective estimation
 - Enhanced 3d-2d perspective estimation with noisy rotation
 - Enhanced 3d-2d perspective estimation with noisy rotation and translation
 - None - use existing rotations and translations
5. Whether drop outliers or not
6. Whether use Bundla Adjustment or not

As output user gets reconstructed *.asc files with suffix depending on used methods and choosed features. TODO write more about it

5.4.2 Important Implementation Aspects

Write about how you modified different libraries and how you tricked OpenCV to do what you need to get

5. IMPLEMENTATION

5.4.2.1 Rotation matrix generation

To parse Android generated Sensor data file Boost JsonParser was used. As mentioned earlier Android saves decomposed Euler Angles. In order to properly multiply these angles to acquire proper rotation matrix following code inspired on MathWorld Wolfram <http://mathworld.wolfram.com/EulerAngles.html>

```
Mat getRotation3DMatrix(double pitch, double azimuth, double roll) {
    Mat D = (Mat_<T>(3, 3) <<
        cos(roll), -sin(roll), 0,
        sin(roll), cos(roll), 0,
        0, 0, 1);

    Mat C = (Mat_<T>(3, 3) <<
        cos(azimuth), 0, -sin(azimuth),
        0, 1, 0,
        sin(azimuth), 0, cos(azimuth));
    Mat B = (Mat_<T>(3, 3) <<
        1, 0, 0,
        0, cos(pitch), -sin(pitch),
        0, sin(pitch), cos(pitch));
    // Important
    return B * C * D;
}
```

5.4.2.2 Enhancing epipolar equations

As we could observe in ?? in order to enhance initial pair reconstruction we can use the same algorithms as standard ones, for example 8-point and 5-point algorithms. The only thing to do is to change input data from local image coordinates into camera coordinates. In OpenCV it can be done with:

```
...
undistortPoints(points1Exp, points1Exp, K, distCoeffs, rotDiffGlobal
);
undistortPoints(points2Exp, points2Exp, K, distCoeffs);
...
```

where `rotDiffGlobal` is rotation between 2 cameras. These lines automatically allow us to calculate h and h' from 4.4. In order to choose proper matrix decomposition we can do as follows:

5.4 "Enhanced 3D Reconstructor" - OSX CMake based project

```
void chooseProperMatrixFromEnhanced(Mat &dRx, Mat &dR1x, Mat &TdRExp,
    Mat &dR, Mat &T) {
    dR = dRx;
    if (decideProperMatrix(dRx, 0.05)) {
        dR = constraintMatrix(dRx);
    } else if (decideProperMatrix(dR1x, 0.05)) {
        dR = constraintMatrix(dR1x);
    } else if (decideProperMatrix(-dRx, 0.05)) {
        dR = constraintMatrix(-dRx);
    } else if (decideProperMatrix(-dR1x, 0.05)) {
        dR = constraintMatrix(-dR1x);
    }

    Mat skewT = TdRExp * dR.inv();
    cout << "skewT" << skewT << endl;

    Mat tdecx = Mat(3,1, CV_64FC1);
    tdecx.at<double>(0) = (skewT.at<double>(2,1) - skewT.at<double>(1,2)
        )/2;
    tdecx.at<double>(1) = (skewT.at<double>(0,2) - skewT.at<double>(2,0)
        )/2;
    tdecx.at<double>(2) = (skewT.at<double>(1,0) - skewT.at<double>(0,1)
        )/2;
    T = tdecx;
}

bool decideProperMatrix(Mat dRot, double tolerance){
    double a00 = abs(dRot.at<double>(0,0) - 1);
    double a11 = abs(dRot.at<double>(1,1) - 1);
    double a22 = abs(dRot.at<double>(2,2) - 1);
    if((a00 + a11 + a22)/3 < tolerance) {
        return true;
    } else {
        return false;
    }
}
```

5.4.2.3 3-point translation estimation, between cameras

When we do have rotation data, which are more or less accuratre, we can focus on estimating only translation between images. Proposed in 4.11 and 4.13 were implemented.

5. IMPLEMENTATION

As similar to other Epipolar estimations methods implemented in OpenCV, this one also has ability to filter out outliers with RANSAC schema.

```
...
for (iterationNumber = 0; iterationNumber < niters; iterationNumber
++) {

    getSubsety(prev_points_raw, next_points_raw, point1s, point2s,
              300, modelPoints);
    Mat t = findTranslation(point1s, point2s, rotDiffGlobal, Kinv);
    Mat F1 = constructFundamentalMatrix(rotDiffGlobal, t, Kinv);

    int goodCount = findInliersy(prev_points_raw, next_points_raw,
                                  F1, errors, statuses, reprojThreshold);
    if (goodCount > maxGoodCount) {
        swap(statuses, goodStatuses);
        FEnhanced = F1;
        tEnhanced = t / t.at<double>(2);
        maxGoodCount = goodCount;
        niters = cvRANSACUpdateNumIters(confidence,
                                         (double) (count - maxGoodCount) / count, modelPoints
                                         , niters);
    }

}

...
.

Mat findTranslation(std::vector<cv::Point2d> &points1, std::vector<
cv::Point2d> &points2, Mat &rotDiff, Mat &Kinv) {

    Mat hg1 = Mat::zeros(points1.size(), 3, CV_64FC1);
    Mat hg2 = Mat::zeros(points2.size(), 3, CV_64FC1);
    for (int i = 0; i < points1.size(); i++) {
        hg1.at<double>(i, 0) = points1[i].x;
        hg1.at<double>(i, 1) = points1[i].y;
        hg1.at<double>(i, 2) = 1;
        hg2.at<double>(i, 0) = points2[i].x;
        hg2.at<double>(i, 1) = points2[i].y;
        hg2.at<double>(i, 2) = 1;
    }

    hg1 = hg1 * (rotDiff * Kinv).t();
    hg2 = hg2 * (Kinv).t();
}
```

5.4 "Enhanced 3D Reconstructor" - OSX CMake based project

```
Mat A = Mat::zeros(hg1.rows, 3, CV_64FC1);
for (int i = 0; i < hg1.rows; i++) {
    A.at<double>(i, 0) = (hg2.at<double>(i, 2) * hg1.at<double>(i,
        1) - hg2.at<double>(i, 1) * hg1.at<double>(i, 2));
    A.at<double>(i, 1) = (hg2.at<double>(i, 0) * hg1.at<double>(i,
        2) - hg2.at<double>(i, 2) * hg1.at<double>(i, 0));
    A.at<double>(i, 2) = (hg2.at<double>(i, 1) * hg1.at<double>(i,
        0) - hg2.at<double>(i, 0) * hg1.at<double>(i, 1));
}

SVD svd1(A);
Mat tCalc = svd1.vt.row(2);

//Translation between cameras estimated and Fundamental Matrix from
//that as well
Mat T = (tCalc.t());

return T;
```

5.4.2.4 Enhancing pose estimation

There was nothing special to implement regarding enhanced pose estimation. OpenCv has option to use initially estimated rotation and translation values(reference)

5. IMPLEMENTATION

6

Evaluation

All implemented algorithms were tested in terms speed, accuracy and effectiveness. For speed test normal processor execution time were measured. For accuracy Sampson Error was used(point distance to corresponding epipolar line in image). For effectivness visual comparison of reconstructed 3D cloud points was used.

6.1 Acquiering datasets

Following datasets were captured with implemented "Sensor Enhanced Images Camera" and Nexus 5 camera:

1. Warsaw University of technology main building(4 images 1024x768pixels)
2. Advertisment Pole ???
3. Warsaw Buisness School Gate and Entrance ??
4. Warsaw Shopping Center Back???
5. Warsaw Shopping Center Front???

As most of proposed algorithms require that Intersic Camera Parametrs are known, also used camera was calibrated and its parameters stored in "*out_camera_data.yml*" file. All of these datasets can be found on attached CD or Github repository.

6. EVALUATION

6.2 Test Environment

All test were performed on MacBook Air with 1.7GHz dual-core Intel Core i7 processor and 8GB 1600MHz DDR3 RAM using implemented "Enhanced 3D Reconstructor". Numerical tests, which allowed to measure Total Errors and execution time were run on "Waraw University of Technology" dataset. Also reconstruction ability of each proposed methods was measured and different reconstruction strategies as well. Finally for each dataset most promising Enhanced 8-point method was used to reconstruct sparse models.

6.3 Testing two-view reconstruction methods

The most important thing to determine was to evaluate, whether proposed sensor enhanced improvements scored better than normal algorithms. Following methods were tested: TODO methods should be already described in Concept and implementation

1. **Standard 8-point** - based on [] Fundamental matrix decomposition, implemented in OpenCV
2. **Enhanced 8-point** - proposed camera rotation enhanced version of above 8-point algorithm
3. **Alternative 3-point** - proposed 3-point algorithm to translation estimation.
4. **Known rotations and translations** - calculation from known cameras rotations and translations
5. **Standard essential 5-point** - based on [] Essential matrix decomposition, implemented in []
6. **Enhanced essential 5-point** - similar to 2. improvements rotation enhanced version of above 5-point algorithm

6.3.1 Accuracy - Epipolar lines correspondence

In terms of two pair images one of the most important factors is the epipolar constraint. With properly estimated Fundamental matrix we can draw in both images corresponding epipolar lines. What's more points that lie on two matching epipolars line can

6.3 Testing two-view reconstruction methods

be easily matched. Simply speaking epipolar line crosses exactly the same points in both images. The more accurate it is the more corresponding pairs can be later found for instance to perform dense reconstruction. Sampson Error[reference] is one of metrics, that can be used in order to estimate, how accurate epipolars line are. It basically measures sum of all points distances to their corresponding epipolar lines. However each of proposed methods has different outliers removal capabilities. That's why also

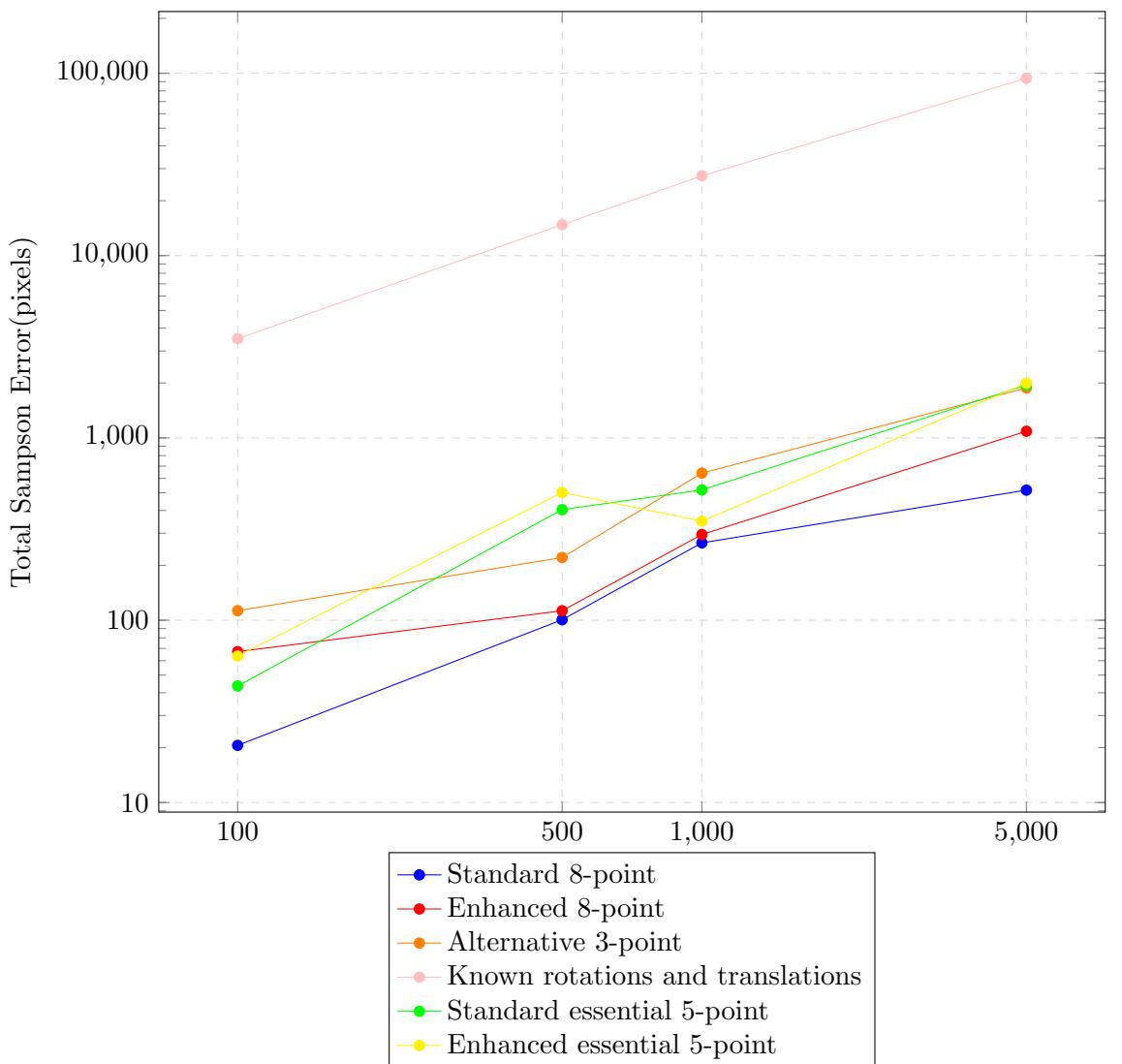


Figure 6.1: Plot of total Sampson Error in picture(1024x768pixels) in comparison to initial Sift feature number

6. EVALUATION

Samson Error Per Corresponding Pair was used. On plot 6.1 were visualized calculated total sampson errors for different initial SIFT features sets. Knowing that Total Sampson Error were calculated for different number of final inliers the only thing that can be noted here that most of the algorithms properly filter out outliers. Obviously drawing epipolar lines from heuristically estimated movement and noisy rotation gives extremly large error in comparison to others. Taking a look at Per Pair Sampson Error

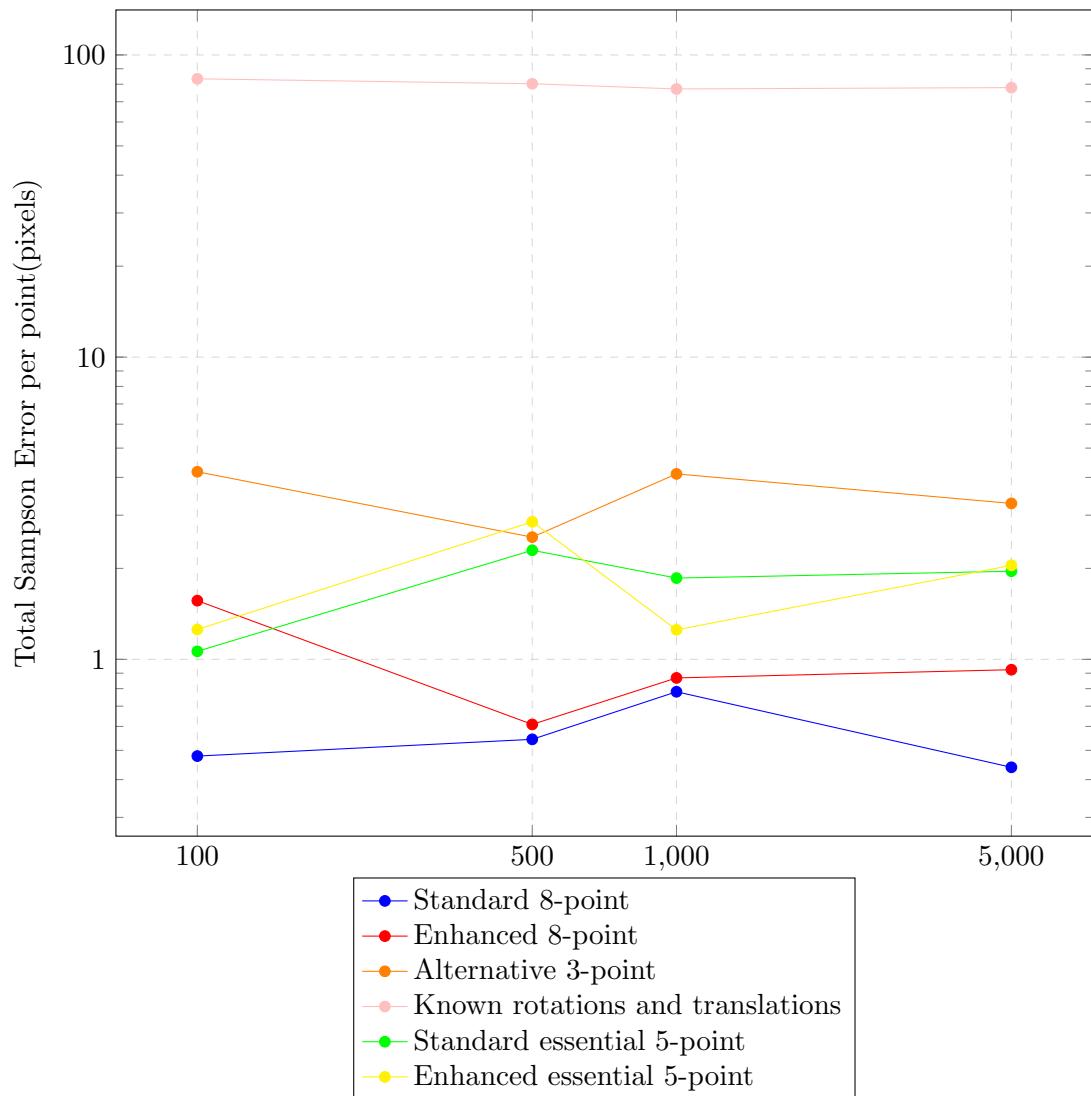


Figure 6.2: Plot of per point Sampson Error in picture(1024x768pixels) in comparison to initial Sift feature number

6.3 Testing two-view reconstruction methods

6.2 one can note that proposed sensor enhanced versions neither had improved 8-point nor 5-point algorithm. However proposed 3-point algorithm, which was much faster than 8-point algorithm turned out to be quite accurate. To present the reader, of what errors are we talking about on figures 6.3 - 6.4 estimated epipolar lines for 300 initial SIFT features were drawn. It can be seen that both Standard 8-point algorithm and proposed Rotation Enhanced version give very good results in term of epipolar lines. Alternative 3-point algorithm gives slightly worse results having good direction of lines, but due to uncompensated mobile sensors noise slightly incorrect. In these particular



Figure 6.3: Results of drawing estimated Epipolar lines on Warsaw University Dataset for 300 Sift points. 1) Standard Fundamental 8-point(upper pair), 2) Rotation Enhanced Fundamental 8-point(middle), 3) Alternative 3-point algorithm(bottom)

6. EVALUATION



Figure 6.4: Results of drawing estimated Epipolar lines on Warsaw University Dataset for 300 Sift points. 1) Fundamental matrix created from rotation and translation(upper pair), 2) Standard Essential matrix 5-point(middle), 3)Rotation Enhanced Essential 5-point(bottom)

dataset Essential 5-point method in really sparse datasets had some problems in Essential matrix estimation, but our proposed improved 5-point version found pretty good corresponding sets. To check if number of SIFT features influence these visualization epipolar calculation was also presented on 1000 SIFT features(6.5 - 6.6). Generally proposed improvements versions aren't better in terms of accuracy due to noise in data sensors, however they are always close to optimal solutions, when standard versions can fail sometimes.

6.3 Testing two-view reconstruction methods



Figure 6.5: Results of drawing estimated Epipolar lines on Warsaw University Dataset for 1000 Sift points. 1) Standard Fundamental 8-point(upper pair), 2) Rotation Enhanced Fundamental 8-point(middle), 3) Alternative 3-point algorithm(bottom)

6. EVALUATION



Figure 6.6: Results of drawing estimated Epipolar lines on Warsaw University Dataset for 1000 Sift points. 1) Fundamental matrix created from rotation and translation(upper pair), 2) Standard Essential matrix 5-point(middle), 3)Rotation Enhanced Essential 5-point(bottom)

6.3.2 Time comparison

As was mentioned in previous chapter we expect some of these methods to be faster than the others. On plot 6.7 averaged execution time for 100 attempts was presented. As

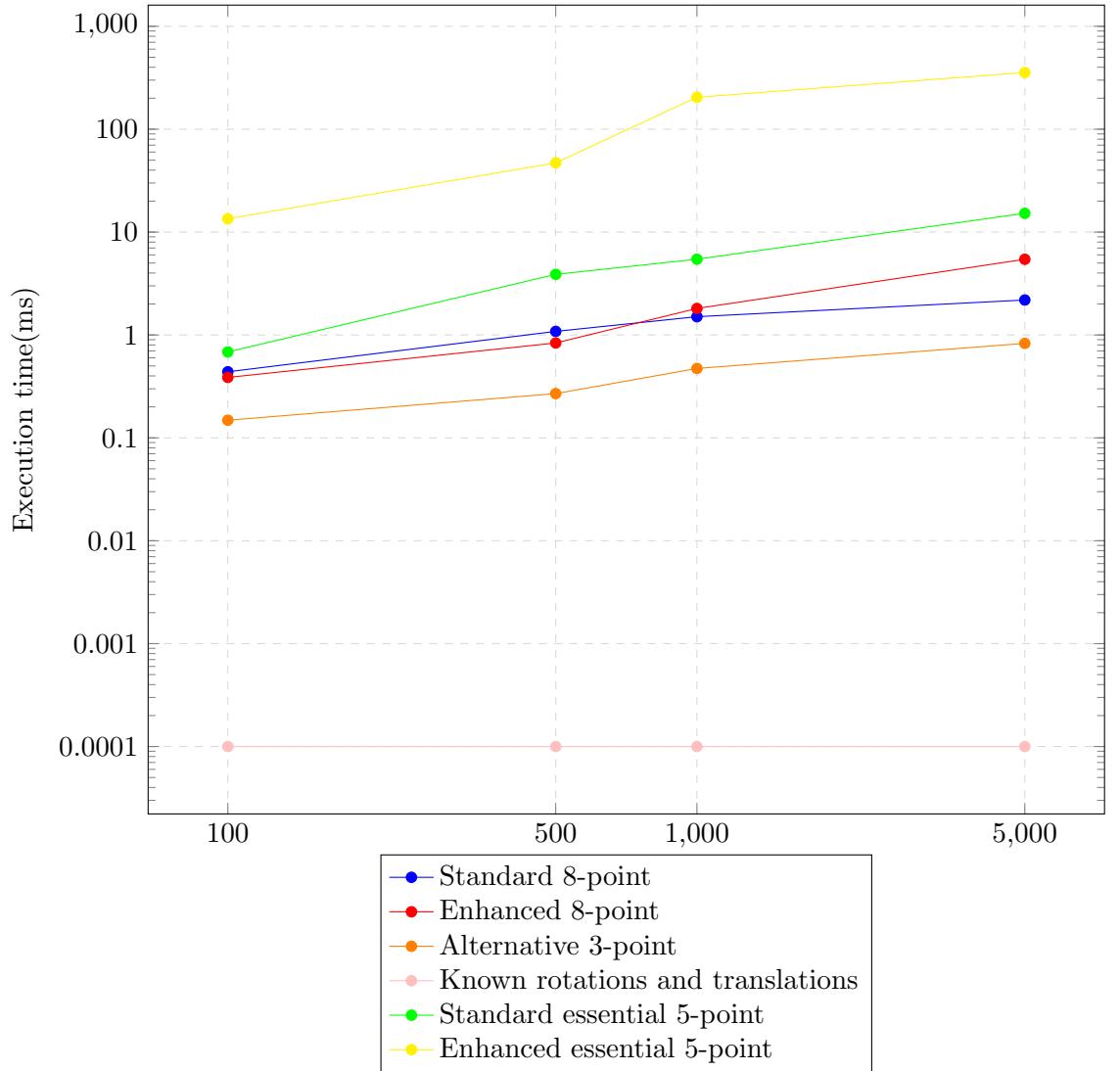


Figure 6.7: Execution time of proposed algorithms(1024x768pixels) in comparison to initial Sift feature number

expected reconstructing using known rotations and translations is few orders smaller than rest algorithms. Also 3-point algorithm execution time is few times smaller than 8-point algorithms. Execution time of 8-point versions are very similar, but 5-point

6. EVALUATION

versions differ much. Either finding optimal solution with initial rotation is much harder or implementation differences in memory allocation of enhanced versions takes a lot of additional time.

6.4 Testing reconstruction strategies

As was seen in 6.3 not every initial reconstruction gives good results. To keep clearness of this document only most promising and interesting strategies were used: TODO methods should be already described in Concept and implementation

1. Standard 8-point + OpenCV Pose Estimation
2. Enhanced 8-point + OpenCV Pose Estimation
3. Enhanced 8-point + Initial Rotation and Translation OpenCV Pose Estimation
4. Alternative 3-point + OpenCV Pose Estimation
5. Alternative 3-point + Initial Rotation and Translation OpenCV Pose Estimation

First method gives us basic reference to normal 3D reconstruction pipeline. 2nd and 3rd were used in order to check how Pose Estimation enhancement influence final results. 4th and 5th one were compared with 2nd-3rd strategies. Finally 6th one was proposed in order to check, how well reconstruction can be performed with only sensor data.

6.4.1 Accuracy

Accuracy of 3D reconstruction were measured using Bundle Adjustment process from SBA library[ref]. At the beginning initial error of whole point cloud is calculated. What's more to better understand, how well models were reconstructed it's interesting to take a look at both model error reduction and BA execution time. For "Warsaw Univeristy" dataset performed performance tests were plotted on 6.8. Big differences in Initial Error mainly lay in number of reconstructed points and scale of models, which turned out to be more very different due to differences in outlier removals. What's interesting is impact of enhancing reconstruction with initial rotations and translation on Bundle Adjustments.

6.4 Testing reconstruction strategies

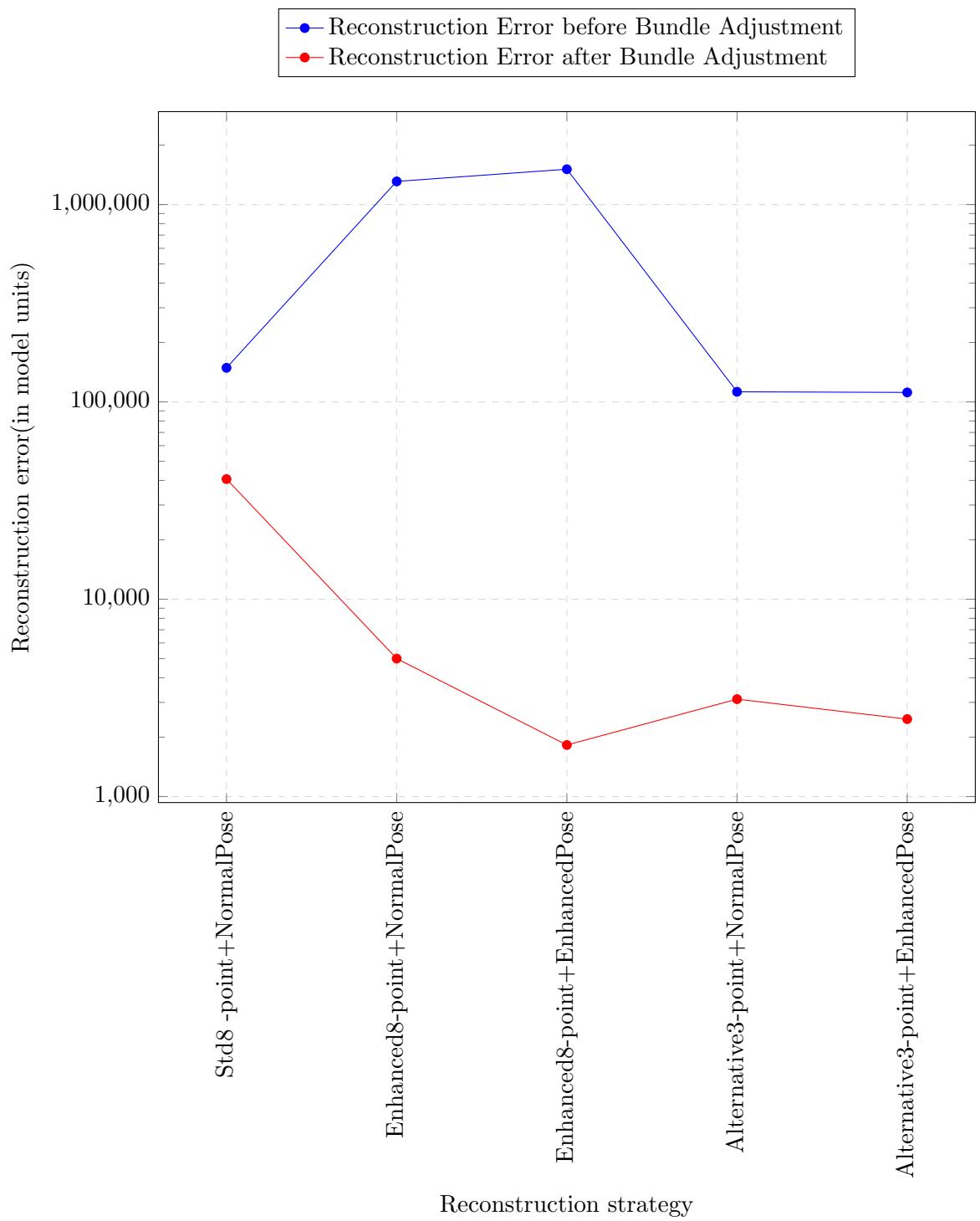


Figure 6.8: Comparison of different reconstruction strategies influence on Bundle Adjustment

6. EVALUATION

Bundle Adjustmet process allows to rearrange both estimated 3D points positions and positions of the cameras. When camera positions are close to their true,optimal positions it allows algorithms to focus on 3D points movement refinments. What's more Rotation and Translation enhanced position estimation has further influence in reduction of final BA error in comparison to Normal Pose Estimation.

6.4.2 Execution time

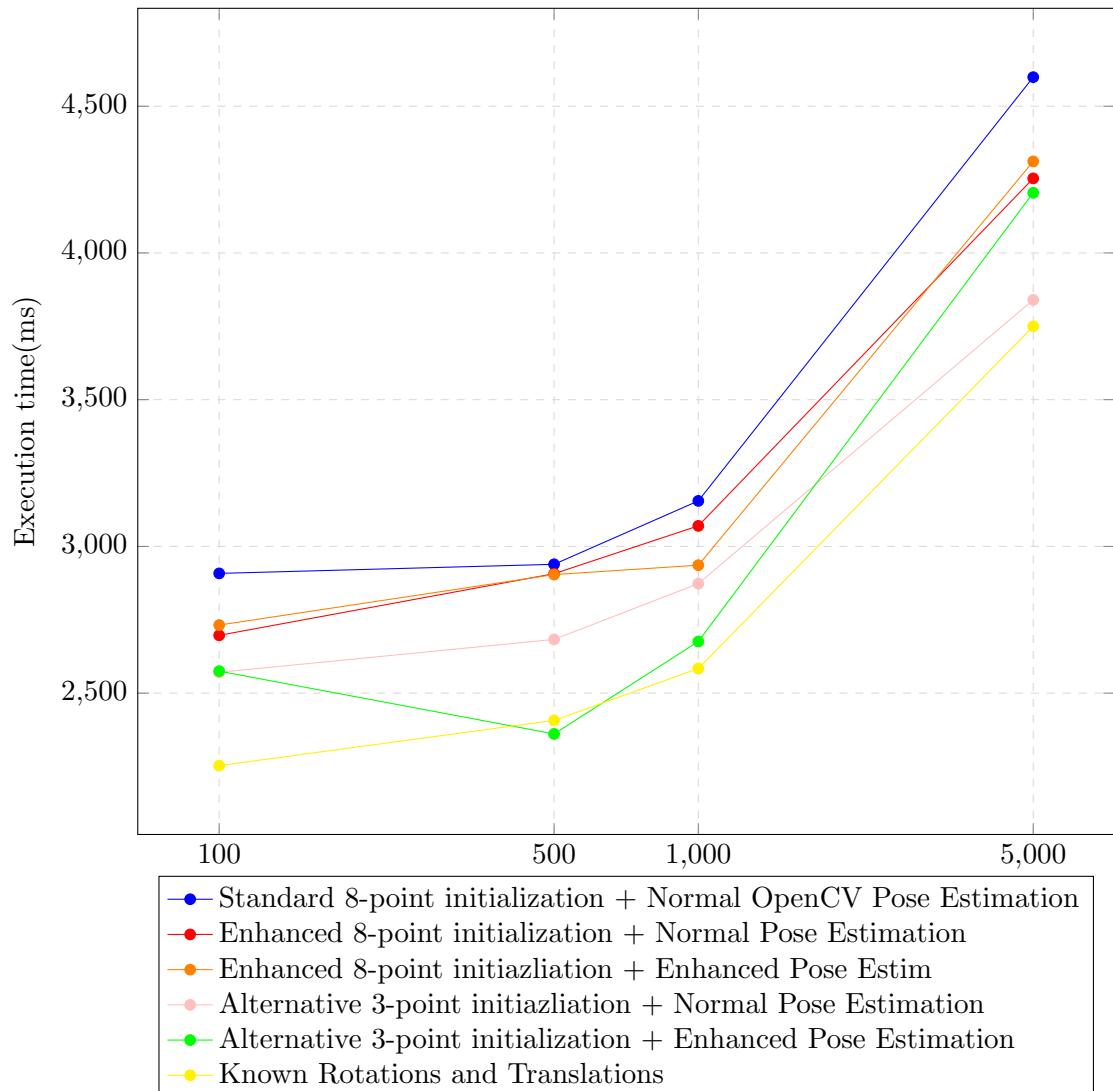


Figure 6.9: Total reconstruction execution time (4 images with resolution 1024x768pixels) in comparison to initial Sift feature number

6. EVALUATION

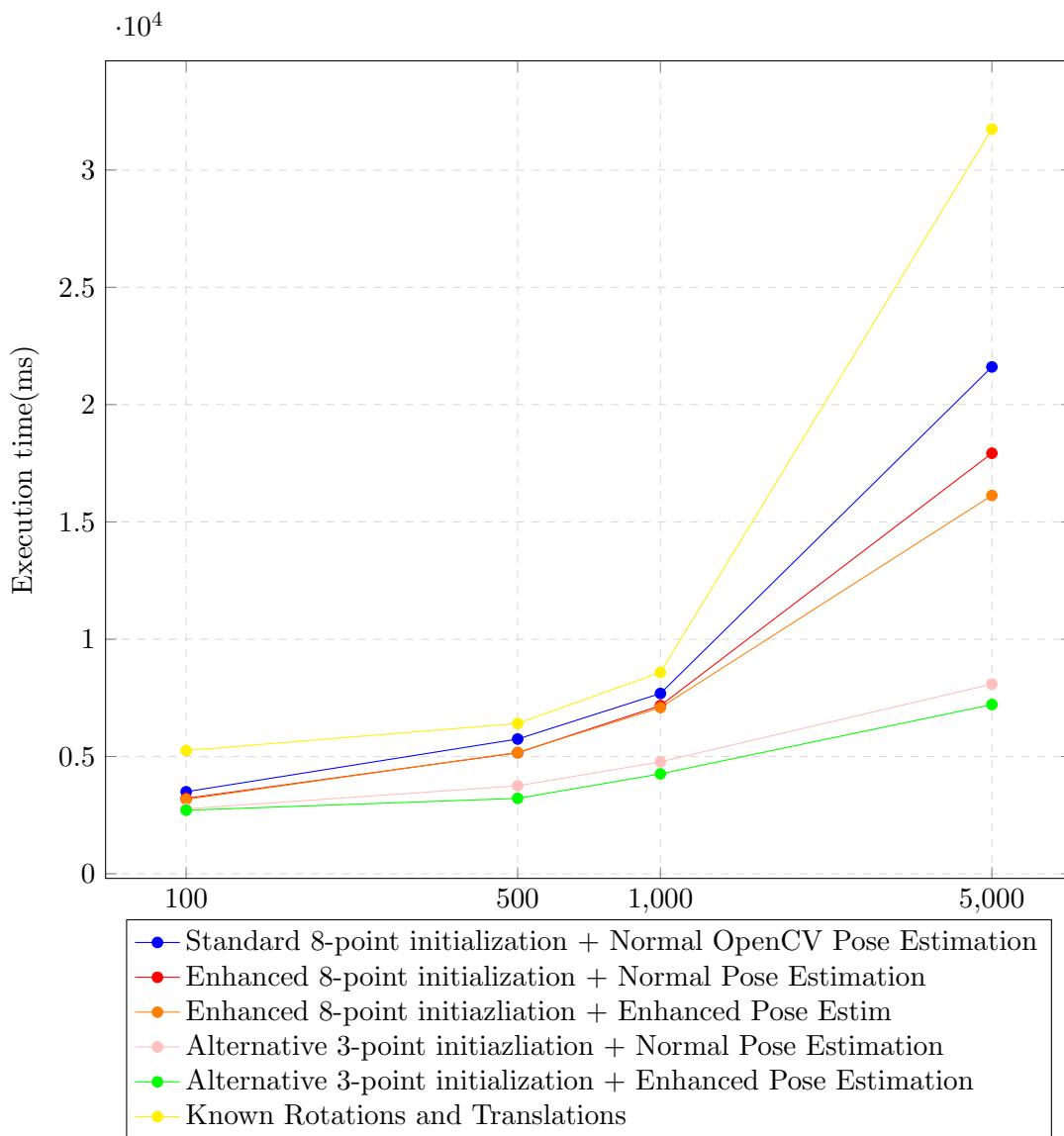


Figure 6.10: Total execution time of reconstruction with Bundle Adjustment(4 images with resolution 1024x768pixels) in comparison to initial Sift feature number

6.5 Effectivness

6.5.1 3D cloud reconstructed models

Reconstructed models were injected into normal images

6. EVALUATION

7

Conclusion

7.1 Summary

7.2 Dissemination

Who uses your component or who will use it? Industry projects, EU projects, open source...? Is it integrated into a larger environment? Did you publish any papers?

7.3 Problems Encountered

7.4 Future work

7. CONCLUSION

8

Materials & methods

8. MATERIALS & METHODS

```
1 [  
2 {  
3     "photoPath": "20141210_145643/0.jpg",  
4     "rotationMatrix": [],  
5     "azimuth": 121.88075,  
6     "posX": -1.7521392107009888,  
7     "posY": -1.4345977306365967,  
8     "posZ": 0.9248641133308411,  
9     "photoId": 1,  
10    "pitch": 13.867888,  
11    "roll": 178.16968  
12 },  
13 {  
14     "photoPath": "20141210_145643/1.jpg",  
15     "rotationMatrix": [],  
16     ],  
17     "azimuth": 110.66925,  
18     "posX": -4.244707942008972,  
19     "posY": -1.1443554759025574,  
20     "posZ": 0.9647054933011532,  
21     "photoId": 2,  
22     "pitch": 11.625216,  
23     "roll": 179.73383  
24 }  
25 . . .  
26 ]
```

100 SIFT Features	Total Sampson Error	Sampson Error per Point	Points left	Execution time(ms)
8-point OpenCV	20.5793	0.478588	43	0.4387
Alternative 3-point	112.749	4.17588	27	0.1484
8-point enhanced	67.2559	1.56409	43	0.3867
Known rot and trans	3501.23	83.3625	42	0.0001
Essential 5-point	43.5866	1.06309	41	0.684
5-point enhanced	1863.66	45.4552	41	13.4643

Table 8.1: Efficiency table of proposed methods for 100 SIFT features in Warsaw University of technology dataset. Columns: Total Sampson Error, Average Sampson error per point, Amount of points left after outliers removal, Execution time

500 SIFT features	Total Sampson Error	Sampson Error per Point	Points left & Execution time(ms)
8-point OpenCV	100.584	0.543697	185 1.0833
Alternative 3-point	220.722	2.53704	87 0.2692
8-point enhanced	112.7	0.609189	185 0.8362
Known rot and trans	14770.7	80.2756	184 0.0001
Essential 5-point	404.098	2.29601	176 3.8827
5-point enhanced	501.987	2.8522	176 47.0683

Table 8.2: Efficiency table of proposed methods for 500 SIFT features in Warsaw University of technology dataset. Columns: Total Sampson Error, Average Sampson error per point, Amount of points left after outliers removal, Execution time

1000 SIFT features	Total Sampson Error	Sampson Error per Point	Points left	Execution time(ms)
8-point OpenCV	265.637	0.781287	340	1.5055
Alternative 3-point	640.895	4.1083	156	0.4725
8-point enhanced	295.152	0.868093	340	1.8099
Known rot and trans	27394.4	77.1673	355	0.0001
Essential 5-point	518.293	1.85768	279	5.4482
5-point enhanced	349.393	1.2523	279	204.2998

Table 8.3: Efficiency table of proposed methods for 1000 SIFT features in Warsaw University of technology dataset. Columns: Total Sampson Error, Average Sampson error per point, Amount of points left after outliers removal, Execution time

8. MATERIALS & METHODS

5000 SIFT features	Total Sampson Error	Sampson Error per Point	Points left	Execution time(ms)
8-point OpenCV	517.189	0.439413	1177	2.187
Alternative 3-point	1879.98	3.28094	573	0.8286
8-point enhanced	1087.78	0.924199	1177	5.4395
Known rot and trans	93951.1	77.9677	1205	0.0001
Essential 5-point	1949.53	1.95736	996	15.2223
5-point enhanced	19966.6	20.0468	996	355.464

Table 8.4: Efficiency table of proposed methods for 5000 SIFT features in Warsaw University of technology dataset. Columns: Total Sampson Error, Average Sampson error per point, Amount of points left after outliers removal, Execution time

References

Declaration

I herewith declare that I have produced this paper without the prohibited assistance of third parties and without making use of aids other than those specified; notions taken over directly or indirectly from other sources have been identified as such. This paper has not previously been presented in identical or similar form to any other German or foreign examination board. The thesis work was conducted from XXX to YYY under the supervision of PI at ZZZ.

CITY,