

# K-Nearest Neighbour (KNN)

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\* KNN is Instance Base Learning

\* Instance Base Learning

- 1) When we get the training example we don't process them and learn a model instead we just store example.
- 2) Algorithm not train rather when it gets the test instance, it uses the stored instance in memory in order to find possible  $y$ .
- 3) In space we have instance with  $x$  &  $y$  value if new instance is given find out close  $x_i$  & that  $x_i \Rightarrow y_i$   
Find similar instance or find same neighboring instance, most nearest instances.

KNN:- Algorithm.

- 1) Training Phase - Save training example. Store the example in structure so that searching through this example become faster.
- 2) Predication :- Get test instance -  $x_t$ . Find training example  $(x_1, y_1)$  ie closest to  $x_t$ , & Predict  $y_1$  as the output  $y_t$ .
- 3) Instead find one ~~example~~ training example. find  $K$  - No of training example.

## \* Classification

Predict majority class from  $\{y_1, y_2, \dots, y_K\}$

\* Regression :- we will get different values of  $y_1, y_2, y_3, \dots, y_K$  Predict the average.

1) Regression take average of  $K$  values for averaging under circumstances where there are.

- 1) Noise in Attributes.
- 2) Noise in class labels.
- 3) Classes may partially overlap.

\* How to decide  $K$  value.

1) Small  $K$  capture fine structure of problem for small training set.

2) Large  $K$  :-

- 1) Use large  $K$ , use weighted distance function.
- 2) Less sensitive to noise (particularly class noise).
- 3) Better probability estimate for discrete classes.
- 4) Large training set allows use large  $K$  value.

\* Weighted Euclidian Distance.

$$D(x_i, x_j) = \sqrt{\sum_{m=1}^N w_m (x_{im} - x_{jm})^2}$$



## \* Why Feature Reduction is important in KNN

(3)

- 1) If we have instance based large features it pose a problem, because some features may be more important than other and some features may be irreterent.

This specially impacts K-nearest neighbor instance based learning algorithm.

- 2) So it is important to remove extra features because for high dimensional phase two items which are similar may still differ in some unimportant attributes & the difference in distance may similar.
- 3) So it is important to find good representative training example for given test example.  
So feature reduction is important.

## \* Distance weighted KNN

- 1) There is treadoff between small & large K can be difficult.
- 2) Use large K, but more emphasis on near neighbor
- 3) Predication test = 
$$\frac{\sum_{i=1}^K w_i * \text{classes}}{\sum_{i=1}^K w_i}$$



KNN: - K Nearest Neighbors.  
 \* Instances Based Learning (lazy learning)  
 distance function

- 1) KNN is based on features similarity, we can do classification using KNN classifier.
- 2) KNN - K Nearest Neighbors is one of the simplest Supervised Machine Learning algorithm. It classifies a data point based on how its neighbors are classified.
- 3) KNN algorithm is based on feature similarity. Choosing the right value of  $k$  is a process called parameter tuning & important for better accuracy.

\* A very Simple Classification & Regression

- a) In case of classification new data points gets classified in a particular class.
- b) In case of regression, new data gets labeled based on the avg. value of  $k$ -nearest neighbour.

\* It is a lazy learner because it doesn't learn much from training data, learn from live data.

\* Default method is Euclidean distance.

\* Requirement for K-NN

- 1) Generally  $k$  gets decided based on the square root of data points ( $k$  is generally odd)  
 for ex - if 1000 data points then  $k=100$  with class
- 2) Data Normalization
- 3) Installation of "class" library.



breast cancer.

\* A case is classified by a majority vote of its neighbors with the case being assigned to the class most common amongst its  $K$  Nearest neighbors measured by a distance function.

### Distance measure

Euclidean  $\sqrt{\sum_{i=1}^K (x_i - y_i)^2}$

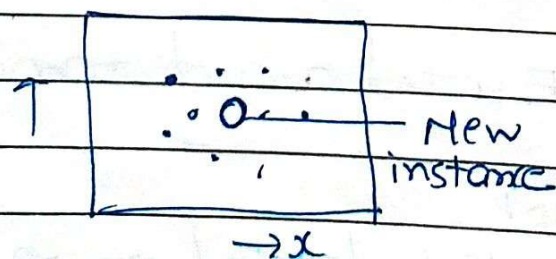
Manhattan  $\sum_{i=1}^K |x_i - y_i|$

Minkowski  $\left( \sum_{i=1}^K (|x_i - y_i|)^q \right)^{1/q}$

Hamming Distance  $D_H = \sum_{i=1}^K |x_i - y_i|$

$x = y \Rightarrow D = 0$	$x$	$y$	
	male	male	0
$x \neq y \Rightarrow D = 1$	male	female	1

\* Instance Based Learning (Lazy Learning)  
In this it won't learn the model it stores the value & used it.



find closest instance to  $(x, y)$   
ie. of that  $x$  find  $y$ .

1) Find most similar instance (similarity) distance function.



\* Training Phase - Save the example (store example) in such way that it will be helpful later

\* Prediction time - Get the test instance  $x_t$   
Find the training example  $(x_1, y_1)$  is closest to  $x_t$  & then predict  $y_t$  as the output

Instead of finding single training example we find  $K$ -training example

$\{(x_1, y_1), (x_2, y_2), \dots, (x_K, y_K)\}$  which are closest to  $x_t$  & predict as output  $y_t$  we  $y_1, y_2, \dots, y_K$  in

classification: - predict majority of class as O/P (most frequent class) from  $(y_1, y_2, \dots, y_K)$

Regression: -

i) Predict  $y_1, y_2, \dots, y_K$  & take average of it & predict it as  $y_t$  (estimate)

\* Voronoi Diagram

\* Improvements

- Weighting examples from the distance
- measuring "closeness"
- Finding "close" examples in a large training set quickly

$$x_i = (x_{i1}, x_{i2}, \dots, x_{iN}) \quad x_j = (x_{j1}, x_{j2}, \dots, x_{jN})$$

$$\text{Distance Euclidean} = \sqrt{\sum_{k=1}^N (x_{ik} - x_{jk})^2}$$

Find Euclidean distance from a test point to all the points of training & select the smallest distance point.



Noise in attributes.  
 Noise in class labels.  
 classes may partially overlap.

Small  $k$ : - Capture fine structure of pattern space better. may be necessary for small training set.

Large  $k$ : - Less sensitive noise (class noise) better probability <sup>estimate</sup> for discrete classes

For larger training set allows use to large  $k$ .

$X(P_1=3 \text{ \& } P_2=7)$			$K=3$ nearest neighbour
	$P_1$	$P_2$	class
i	7	7	False
ii	7	4	False
iii	3	4	True
iv	1	4	True

Euclidean Distance =

$$\sqrt{(\underset{\substack{\uparrow \\ \text{Actual}}}{x_H - H_1})^2 + (\underset{\substack{\uparrow \\ \text{observed}}}{x_N - w})^2 + \dots}$$

observed Actual.

Here observed is 3 & 7

$$D(X, i) = \sqrt{(3-7)^2 + (7-7)^2} = 4 \leftarrow N_4 \text{ False}$$

$$D(X, ii) = \sqrt{(3-7)^2 + (7-4)^2} = 5$$

$$D(X, iii) = \sqrt{(3-3)^2 + (7-4)^2} = 3 \leftarrow N_1 \text{ True}$$

$$D(X, iv) = \sqrt{(3-1)^2 + (7-4)^2} = 3.6 \leftarrow N_2 \text{ True}$$

$\therefore K\text{-NN} = N_1 \quad 2 \text{ True} > 1 \text{ False}$

$\therefore$  Answer is  $X(P_1=3, P_2=7)$  belong to ~~False~~ True



Predict the type of fruit or food type  
tomato (Sweet = 6, Crunch = 4) belongs.

Ingredient	Sweet	Crunch	Food Type
Grape	8	5	Fruit
Greenbean	3	7	Vegetable
Nuts	3	6	Protein
Orange	7	3	Fruit

$D(\text{Tomato, Grape})$

$$D(X, i) = \sqrt{(6-8)^2 + (4-5)^2} = 2.2 \text{ F}$$

$$D(X, ii) = \sqrt{(6-3)^2 + (4-7)^2} = 3.6 \text{ V}$$

$$D(X, iii) = \sqrt{(6-3)^2 + (4-6)^2} = 3.6 \text{ P}$$

$$D(X, iv) = \sqrt{(6-7)^2 + (4-3)^2} = 1.4 \text{ Fruit}$$

Since distance of tomato from Orange is minimum  
∴ tomato will belong to Fruit.

Eager Vs Lazy learner.

1) Eager

a) Generalized model from training data set is constructed

b) using the model the class of test data set is predicted

c) Decision Tree

ex -

a) Training datasets stored

b) on querying similarity between test data & training set records is calculated to predict the class of test data

ex - KNN



## K-NN

- 1) Non-parametric method used for classification
- 2) Prediction for test data is done on the basis of its neighbor

3)  $K$  is an integer (small)  $K=1$  is assigned to class of single nearest neighbor

	Acid Durability	Strength	Class
1	7	7	Bad
2	7	4	Bad
3	3	4	Good
4	1	4	Good

Test data  $\rightarrow$  acid durability = 3 & strength = 7 Class

$$D = \sqrt{(3-7)^2 + (7-7)^2} = 4$$

$$D = \sqrt{(3-7)^2 + (7-4)^2} = 5$$

$$D = \sqrt{(3-3)^2 + (7-4)^2} = 3 \leftarrow \min^m$$

$$D = \sqrt{(3-1)^2 + (7-4)^2} = 3.6$$

$\therefore$  (Durability = 3, Strength = 7 - Good)

- \* Instance based Learning includes nearest neighbor & locally weighted regression ~~space~~ methods that assume instances can be represented as point in a Euclidean space.

- \* Instance based methods are sometimes referred to as "lazy" learning method because the delay processing until a new instance must be classified.

A key advantage of this kind of ~~delay~~ or lazy learning is that instead of estimating the target function once for the entire instance space these methods can estimate it locally & differently for each new instance to be classified.