

# DAA Lab-3

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**Q1)** Write a program to sort a given set of elements using the insertion sort. Additionally, determine the time required (in terms of steps) to sort the elements.

(Note: assume cost of any basic operation is 1, i.e.,  $c_1 = c_2 = \dots = c_8 = 1$ ).

1) Repeat the experiment for different values of  $n = 500, 1000, 5000, 10000$

2) For each of aforementioned case, consider arrays as sorted, random, and reverse-sorted. Provide the complexity in terms of step count

Program:

/\*

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Question:

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Ideal of the Solution:

First I will define a insertion sort function and then I will generate random array of different size and then I will check for all the three cases.

\*/

```
#include<bits/stdc++.h>
```

```
#include<stdio.h>
```

```
#include<time.h>
```

```
#include<stdlib.h>
```

```
using namespace std;
```

```
int insertionSort(int a[],int n)    //Insertion sort function taking an array and its size as parameter
```

```
{
```

```
    int i,j,temp,c=0;                //c is the step counter
```

```
    for(i=1;i<n;i++)
```

```
    {
```

```
        temp=a[i];                  //storing the element into a temporary variable for finding it position
```

```
        c++;
```

```
        j=i-1;
```

```
        c++;
```

```
        while(temp<a[j])            //loop for finding the position
```

```
        {
```

```
            c++;
```

```
            if(j== -1)
```

```
            {
```

```
                c++;
```

```
                break;
```

```
            }
```

```
            a[j+1]=a[j];            //swaping for creating position
```

```

        c++;
        j--;
        c++;
    }
    a[j+1]=temp;                //Inserting the element at the position
    c++;
}
return c;                      //returning the total step count
}

int main()
{
    int n,i,j,k,c1,c2,c3;        //Variables for keeping different step counts
    clock_t start, end;         //Variables for keeping start and end time
    double cpu_time_used;       //Variable for keeping cpu time used
    for(i=0;i<4;i++)
    {
        cout<<endl;
        cout<<"Enter the size of the array : ";
        cin>>n;
        int a[n];
        srand(time(0));
        for(j=0;j<n;j++)
            a[j]=rand()%1000000;    //generating the random array
        cout<<"For n= "<<n<<endl;
        start=clock();              //keeping start time of the clock for random array
        c1=insertationSort(a,n);    //sorting
        end=clock();                //keeping end time of the clock for random array
        cpu_time_used=((double)(end-start))/CLOCKS_PER_SEC; //calculating cpu time used for random array
        cout<<"Step count for random : "<<c1<<endl;
        //cout<<"time taken : "<<cpu_time_used<<endl;
        printf("Time taken for random : %fsec \n",cpu_time_used);
        sort(a,a+n);

        start=clock();              //keeping start time of the clock for sorted array
        c2=insertationSort(a,n);    //sorting
        end=clock();                //keeping end time of the clock for sorted array
        cpu_time_used=((double)(end-start))/CLOCKS_PER_SEC; //calculating cpu time used for sorted array
        cout<<"Step count for sorted : "<<c2<<endl;
        //cout<<"time taken : "<<cpu_time_used<<endl;
        printf("Time taken for sorted : %fsec \n",cpu_time_used);

        sort(a,a+n,greater<int>());
        start=clock();              //keeping start time of the clock for reverse sorted array
        c3=insertationSort(a,n);    //sorting
        end=clock();                //keeping end time of the clock for reverse sorted array
        cpu_time_used=((double)(end-start))/CLOCKS_PER_SEC; //calculating cpu time used for reverse
sorted array
        cout<<"Step count for reverse sorted : "<<c3<<endl;
        //cout<<"time taken : "<<cpu_time_used<<endl;
        printf("Time taken for reverse sorted : %fsec \n",cpu_time_used);
    }
}

```

}

}

Output:

```
kshiti@kshiti: ~/Documents/DAA/lab3
kshiti@kshiti:~/Documents/DAA/lab3$ g++ 1_insertion_sort.cpp
kshiti@kshiti:~/Documents/DAA/lab3$ ./a.out

Enter the size of the array : 500
For n= 500
Step count for random : 196527
Time taken for random : 0.000337sec
Step count for sorted : 1497
Time taken for sorted : 0.000003sec
Step count for reverse sorted : 375777
Time taken for reverse sorted : 0.000631sec

Enter the size of the array : 1000
For n= 1000
Step count for random : 739899
Time taken for random : 0.001145sec
Step count for sorted : 2997
Time taken for sorted : 0.000006sec
Step count for reverse sorted : 1501529
Time taken for reverse sorted : 0.002310sec

Enter the size of the array : 1500
For n= 1500
Step count for random : 1699980
Time taken for random : 0.002650sec
Step count for sorted : 4497
Time taken for sorted : 0.000008sec
Step count for reverse sorted : 3377307
Time taken for reverse sorted : 0.005147sec

Enter the size of the array : 2000
For n= 2000
Step count for random : 3046909
Time taken for random : 0.004646sec
Step count for sorted : 5997
Time taken for sorted : 0.000011sec
Step count for reverse sorted : 6003074
Time taken for reverse sorted : 0.009352sec
kshiti@kshiti:~/Documents/DAA/lab3$
```

**Q2)** Write a program to compute the nth Magic number (recursively) defined as below and find its time complexity (in terms of number of recursions).nth magic number  $MN(n) = MN(n-1) + MN(n-2)$ , whereas  $MN(0) = 0$ , and  $MN(1) = 1$ .

Program:

/\*

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Write a program to compute the nth Magic number (recursively) defined as below and find its time complexity (in terms of number of recursions).nth magic number  $MN(n) = MN(n-1) + MN(n-2)$ , whereas  $MN(0) = 0$ , and  $MN(1) = 1$ .

Idea of the solution:

I am defining a fibo function for calculating the n th fibonacci series number recursively, and then applying the divide and conquer approach for finding the n th number.

\*/

#include<bits/stdc++.h>

using namespace std;

int t=0;

//Variable for keeping no. of recursions

int fibo(int n,int a,int b,int c)

//function for calculating the n<sup>th</sup> fibonacci number.

```

{
t++;
if(n==0)
    return a;
if(n==1)
    return b;
if(n==2)                                //break condition of the recursion
    return c;
a=b;
b=c;
c=a+b;
n--;
fibo(n,a,b,c);                          //recursively calling the fibo function with the updated value
}

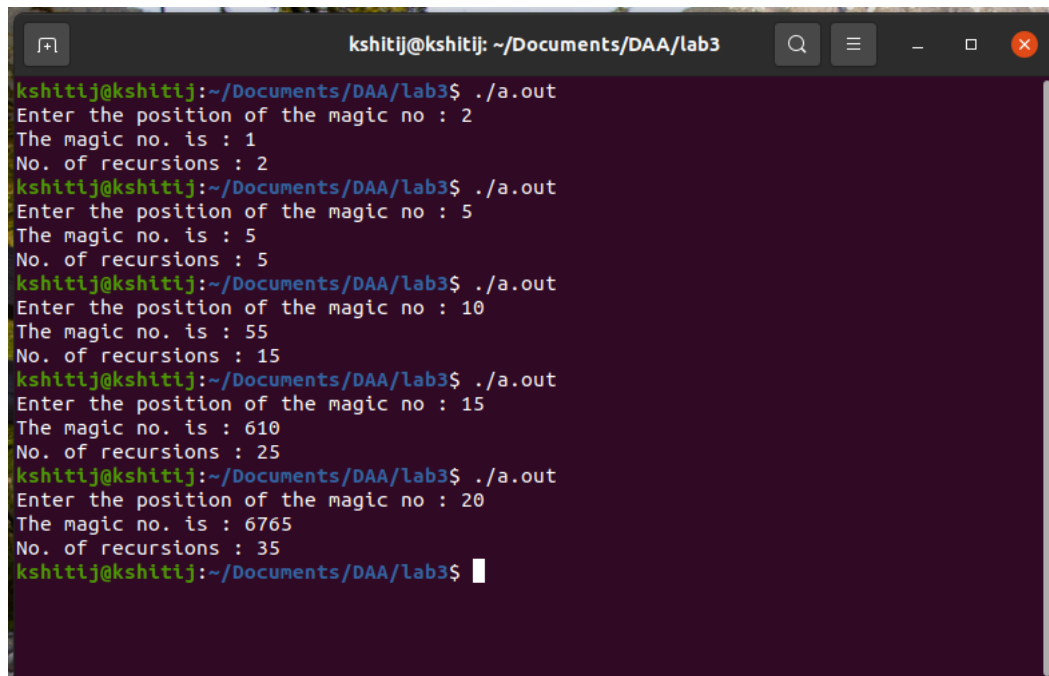
```

```

int main()
{
    int n,mn;
    cout<<"Enter the position of the magic no : ";
    cin>>n;
    //taking the n th number from user
    if(n>=2)
        mn=fibo(n-1,0,1,1)+fibo(n-2,0,1,1);    //applying divide and conquer
    cout<<"The magic no. is : "<<mn<<endl;
    cout<<"No. of recursions : "<<t<<endl;
}

```

Output:



```

kshiti@kshiti: ~/Documents/DAA/lab3$ ./a.out
Enter the position of the magic no : 2
The magic no. is : 1
No. of recursions : 2
kshiti@kshiti: ~/Documents/DAA/lab3$ ./a.out
Enter the position of the magic no : 5
The magic no. is : 5
No. of recursions : 5
kshiti@kshiti: ~/Documents/DAA/lab3$ ./a.out
Enter the position of the magic no : 10
The magic no. is : 55
No. of recursions : 15
kshiti@kshiti: ~/Documents/DAA/lab3$ ./a.out
Enter the position of the magic no : 15
The magic no. is : 610
No. of recursions : 25
kshiti@kshiti: ~/Documents/DAA/lab3$ ./a.out
Enter the position of the magic no : 20
The magic no. is : 6765
No. of recursions : 35
kshiti@kshiti: ~/Documents/DAA/lab3$

```