Lab 3.1

- **3.1**. Write a program to sort a given set of elements using the insertion sort. Additionally, determine the time required (in terms of steps) to sort the elements. (Note: assume cost of any basic operation is 1, i.e., $c_1 = c_2 = \ldots = c_8 = 1$).
 - 1) Repeat the experiment for different values of n = 500, 1000, 5000, 10000
 - 2) For each of aforementioned case, consider arrays as sorted, random, and reverse-sorted. Provide the complexity in terms of step count

Note: No keyboard input. Use

Random number generator.

n	Sorted	Random	Reverse Sorted
500			
1000			
5000			
10000			

Help: Insertion Sort

Insertion-Sort (A)		cost	$\#\ times$
1: f	or $j=2$ to n	c_1	n
2:	key = A[j]	c_2	n-1
3:	// Insert $A[j]$ to the sorted	0	n-1
	sequence $A[1j-1]$		
4:	i = j - 1	c_4	n-1
5:	while $i > 0$ and $A[i] > key$	c_5	$\sum_{j=2}^{n} t_j$
6:	A[i+1] = A[i]	c_6	$\sum_{j=2}^{n} (t_j - 1)$
7:	i = i - 1	c_7	$\sum_{j=2}^{n} (t_j - 1)$
8:	A[i+1] = key	c_8	n-1

Help: Random Number Generator

Random Number Generation

```
#include <stdlib.h>
#include <time.h>

srand(time(NULL)); //once

rand()%30; //everytime
```

Generating in sorted order

```
arr[0] = rand()%100;
//for sorted order
for(int i = 1; i < arr_size; i++){
    arr[i] = arr[i - 1] + rand()%30;
}</pre>
```

Lab 3.2

3.2. Write a program to compute the nth Magic number (recursively) defined as below and find its time complexity (in terms of number of recursions).

 n^{th} magic number MN(n) = MN(n-1) + MN(n-2), whereas MN(0) = 0, and MN(1) = 1

Lab 3.2

3.2. Write a program to compute the $n^{\rm th}$ Magic number (recursively) defined as below and find its time complexity (in terms of number of recursions).

```
n^{th} magic number MN(n) = MN(n-1) + MN(n-2), whereas MN(0) = 0, and MN(1) = 1
```

[Divide and conquer approach]

Homework

HW 3.1. Write an program for counting inversions in an array. Inversion is a pair such that for an array $A = \{a1, a2, a3,...., an\}$, and ai > aj and i < j.

- HW 3.2. Write a program to implement GCD (greatest common divisor) using the following three algorithms.
- a) Euclid's algorithm
- b) Consecutive integer checking algorithm.
- c) Middle school procedure which makes use of common prime factors. Study the time complexity. Present some results to show which is more effective.
- HW 3.3 Write a program to implement binary search on an array which may has two subsequences: first consists of numbers in ascending order and second in descending order.





