

forward  
the result.  
the step, return

Project Title :- Create a Knowledgebase consisting of FOL  
logic statements and prove the given query using  
forward reasoning.

Forward Reasoning Algorithm :-

function FOL-FC-TSK (KB,  $\alpha$ ) returns a substitution or  
false

inputs: KB, knowledge base, a set of ~~rule~~ first or definite  
clauses,  $\alpha$ , the query, an atomic sentence.

local variables: new, the new sentence inferred on each  
iteration

repeat until new is empty

new  $\leftarrow \alpha$

for each rule in KB do

$(p_1 \wedge \dots \wedge p_n \Rightarrow q) \in \text{STANDARDIZE-VARIABLES (rules)}$

for each  $\theta$  such that  $\text{SUBST}(\theta, p_1 \wedge \dots \wedge p_n)$   
 $= \text{SUBST}(\theta, p_1' \wedge \dots \wedge p_n')$

for some  $p_1', \dots, p_n'$  in KB

$q' \leftarrow \text{SUBST}(\theta, q)$

if  $q'$  does not unify with some sentence already in KB or  
new then

add  $q'$  to new

$\phi \leftarrow \text{UNIFY}(q', \alpha)$

if  $\phi$  is not fail then return  $\phi$

add new to KB

return false.



## # Given case study:-

As per the law, it is a crime for an American to sell weapon to hostile nations. Country A, an enemy of America, has some missiles, and all the missiles are sold to it by Robert who is an American citizen. Prove that Robert is Criminal!

### Representation in FOL

1. It is a crime for an American to sell weapon to hostile nation.

Let say  $p, q$ , and  $x$  are variables.

$$\text{American}(p) \wedge \text{Weapon}(q) \wedge \text{Sells}(p, q, x) \wedge \text{Hostile}(x) \Rightarrow \text{Criminal}(p)$$

2. Country A has some missile.

$$\exists x \text{ owns}(A, x) \wedge \text{Missile}(x).$$

Existential instantiation, introducing a new variable  $T_i$ ,  
 $\text{owns}(A, T_i)$   
 $\text{Missile}(T_i)$

3. All of the missiles were sold to country A by Robert  
 $\forall x \text{ Missile}(x) \wedge \text{owns}(A, x) \Rightarrow \text{Sells}(\text{Robert}, x, A)$

4. Missiles are weapons  
 $\text{Missile}(x) \Rightarrow \text{Weapon}(x)$

5. Enemy of America is known as hostile  
 $\forall x \text{ Enemy}(x, \text{America}) \Rightarrow \text{Hostile}(x)$

6. Robert is an American  
 $\text{American}(\text{Robert})$

7. The country A, an enemy of America  
 $\text{Enemy}(A, \text{America})$

## # output:-

9. 'Criminal'

## # forward ch

American

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an American to  
country A, an enemy of  
all the missiles were  
real citizen.

to sell weapon to

Hostile(x)  $\Rightarrow$   
criminal(x)

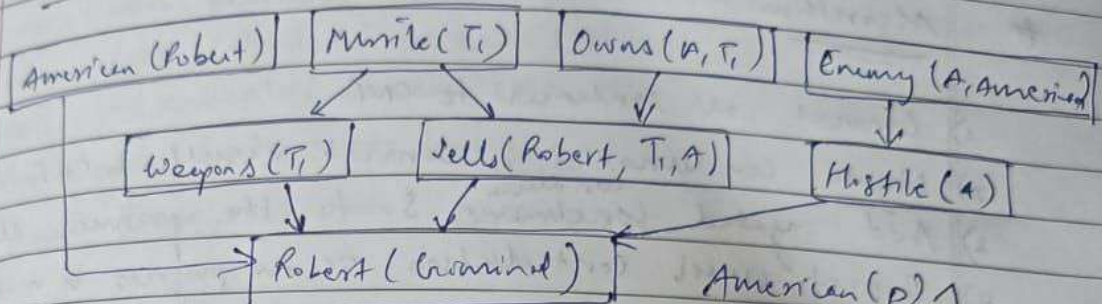
variable T,

try A by Robert  
Robert, T, A)

# output:

q: 'Criminal(Robert)' provable? True.

# forward chaining proof



American(p)  $\wedge$   
Weapon(q)  $\wedge$  Sells(p, q, A)  
 $\wedge$  Hostile(A)  $\Rightarrow$  Criminal(p)

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# Project title :- Create a knowledge base of first order logic and solve query using resolution.

# Algorithm :-

- 1) Convert all sentences to CNF
- 2) Negate conclusion <sup>condition</sup> & convert result to CNF
- 3) Add negated conclusion <sup>condition</sup> to the premise clauses
- 4) Repeat until contradiction or no progress is made
  - a) Select 2 clauses (call them parent clauses)
  - b) Release them together, performing all required unification
  - c) If resolvent is the empty clause, a contradiction has been found.
  - d) If not, add resolvent to the premises. If we succeed in step 4, we have proved the ~~conclusion~~ condition.

# Proof by Resolution :-

Given the KB or Premise

- a) John likes all kind of food
- b) Apple & vegetables are food
- c) Anything anyone eats and not killed is food
- d) Anil eats peanuts and still alive
- e) Harry eats anything that Anil eats.
- f) Anyone who is alive implies not killed
- g) Anyone who is alive implies not killed
- h) John likes peanuts

⇒ Rep

- a)  $\forall x$
- b) food
- c)  $\forall x$
- d) co
- e)  $\forall x$
- f)  $\forall x$
- g)  $\forall x$
- h) like

# Elim

- a)  $\forall x$
- c)  $\forall x$
- e)  $\forall x$
- f)  $\forall x$
- g)  $\forall x$

→ M

- c)  $\forall x$
- f)  $\forall x$

→ s

- c)  $\forall y$
- e)  $\forall w$
- f)  $\forall g$
- g)  $\forall k$

→ Dr

- a)  $\neg$  fo
- b) food
- c) food



## Representation in FOL

- $\forall x: \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$
- $\text{food}(\text{apple}) \wedge \text{food}(\text{vegetables})$
- $\forall x \forall y: \text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \text{alive}(\text{Anil})$
- $\forall x: \text{eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Merry}, x)$
- $\forall x: \neg \text{killed}(x) \rightarrow \text{alive}(x)$
- $\forall x: \text{alive}(x) \rightarrow \neg \text{killed}(x)$
- $\text{likes}(\text{John}, \text{Peanuts})$

## # Eliminate Implications

- $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- $\forall x \forall y \neg [\text{eats}(x, y) \wedge \neg \text{killed}(x)] \vee \text{food}(y)$
- $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Merry}, x)$
- $\forall x \neg [\neg \text{killed}(x)] \vee \text{alive}(x)$
- $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$

→ Move negation ( $\neg$ ) inwards

- $\forall y \neg \text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}(y)$
- $\forall x \text{killed}(x) \vee \text{alive}(x)$

→ Standardize variables

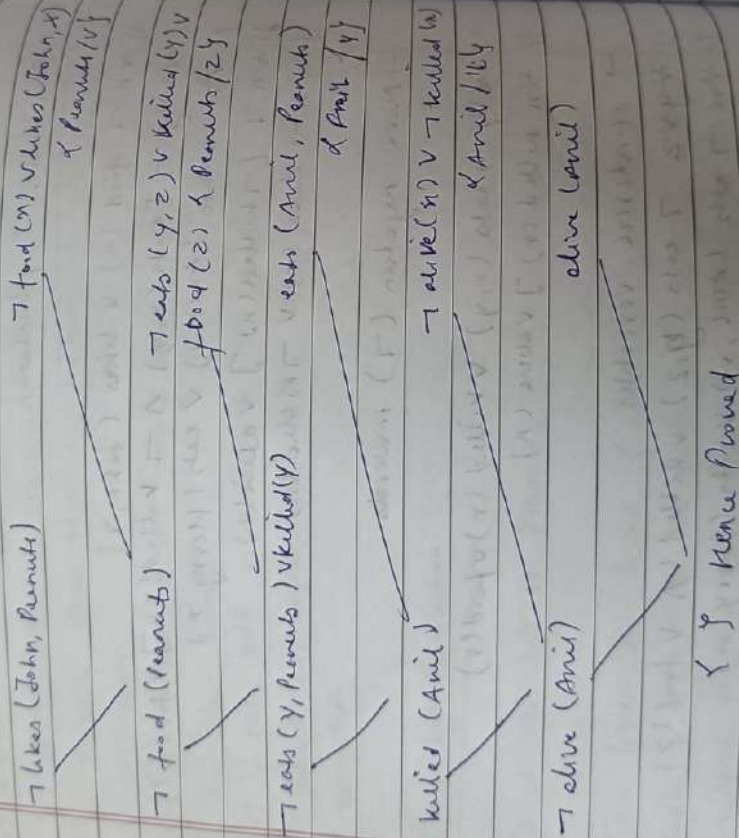
- $\forall y \forall z \neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
- $\forall w \neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Merry}, w)$
- $\forall g \text{killed}(g) \vee \text{alive}(g)$
- $\forall k \neg \text{alive}(k) \vee \neg \text{killed}(k)$

→ Drop universal

- $\neg \text{food}(n) \vee \text{likes}(\text{John}, n)$
- $\text{food}(\text{Apple})$
- $\text{food}(\text{Vegetables})$

- c) food (vegetables)  
 d)  $\neg$  eats (xz)  $\vee$  killed (y)  $\vee$  food (z)  
 e) eats (Anil, Peanuts)  
 f) alive (Anil)  
 g)  $\neg$  eats (Anil, w)  $\vee$  eats (Harry, w)  
 h) killed (y)  $\vee$  alive (y)  
 i)  $\neg$  alive (x)  $\vee$   $\neg$  killed (x)

# Proof :-



# Project #1  
 # Algorithm  
 $\hookrightarrow$  Alpha (2)  
 path with  
 Max w  
 $\hookrightarrow$  blind de  
 $\hookrightarrow$  in Both  
 while co  
 $\hookrightarrow$  Both ne  
 same p  
 $\hookrightarrow$  Alpha (x  
 even more  
 # Problem.  
 Apply  
 mode (H

