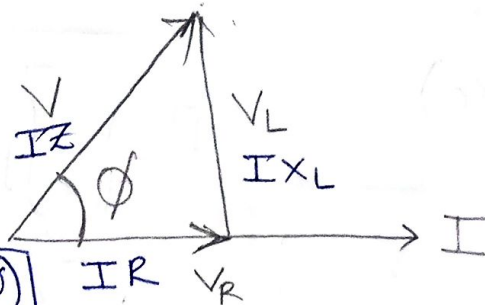


→ For pure resistance; V & I are at 0°
i.e. V & I are in phase.

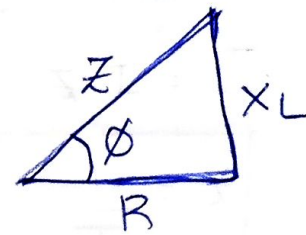
⇒ Phasor :

$$V = V_m \sin \omega t$$

$$i = I_m \sin(\omega t - \phi)$$



$$\phi = 0 \text{ to } 90^\circ$$



Impedance Δ^e .

Clockwise \rightarrow ve \rightarrow lagging angle

$$P = \frac{1}{\pi} \int_0^\pi p \, d\theta$$

$$= \frac{1}{\pi} \int_0^\pi V_m I_m \sin \theta \sin(\theta - \phi) \, d\theta$$

$$= \frac{V_m I_m}{\pi} \int_0^\pi \left[\frac{\cos(\phi)}{2} - \frac{\cos(2\theta - \phi)}{2} \right] d\theta.$$

$$= \frac{V_m I_m}{\pi} \int_0^\pi \left[\frac{\cos \phi}{2} - \frac{\cos(2\theta - \phi)}{2} \right] d\theta$$

$$= \frac{V_m I_m}{2\pi} \cdot \cos \phi \cdot \pi$$

$\cos \phi = \text{Power factor}$

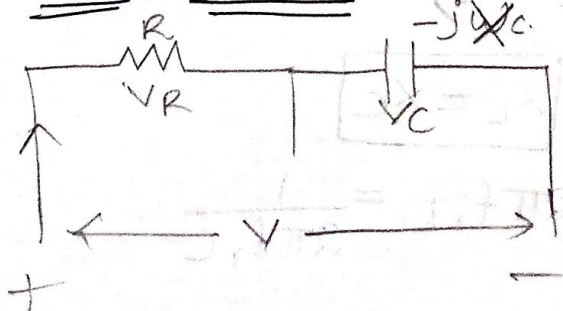
$$P = \frac{V_m I_m}{2} \cos \phi$$

$$P = V_{rms} I_{rms} \cos \phi$$

$$P = VI \cos \phi$$

* ϕ should be close to 0° so as to get max. power.

* SERIES RC CIRCUIT:



$$j\omega RC = jX$$

$$\frac{1}{j\omega C} = -jX$$

$$\bar{V} = \bar{V}_R + \bar{V}_C$$

$$= IR + I(-jX_C)$$

$$\boxed{Z = R - jX_C}$$

$$= I(R - jX_C)$$

$$\bar{V} = IZ$$

$$\boxed{Z = \frac{V}{I}}$$

$$\boxed{P = VI}$$

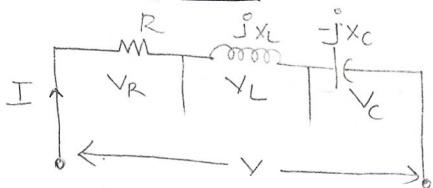
$$P = \frac{1}{T} \int_0^T p d\theta$$

$$= \frac{1}{T} \int_0^T V_m \sin \theta \cdot I_m \sin(\theta - \phi) d\theta$$

$$I = \frac{V_m I_m}{T} \int_0^T \sin \theta \cdot \sin(\theta - \phi) d\theta$$

$$\boxed{P = \frac{V_m I_m}{2} \cos \phi}$$

* SERIES LCR CIRCUIT:



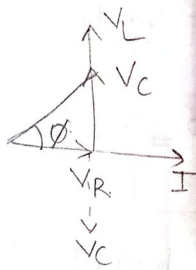
$$V = V_R + V_L + V_C$$

$$= IR + IjX_L - IjX_C$$

$$= IR + Ij(X_L - X_C)$$

$$V = I(R + j(X_L - X_C))$$

$$Z = R + j(X_L - X_C)$$



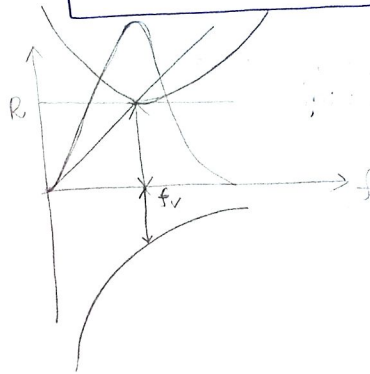
$$\left. \begin{array}{l} X_L = 2\pi fL \\ X_C = \frac{1}{2\pi fC} \end{array} \right\} \begin{array}{l} \boxed{X_L = X_C} \\ 2\pi f_r L = \frac{1}{2\pi f_r C} \end{array}$$

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$$f_r^2 = \frac{1}{4\pi^2 LC} \Rightarrow \boxed{f_r = \frac{1}{2\pi\sqrt{LC}}}$$

$$\text{at } Z=R \quad \text{i.e. } X_L = X_C = 0$$

$$\Rightarrow \boxed{I_{\max} = \frac{V}{Z} = \frac{V}{R}}$$



$$* f = 50 \text{ Hz} \quad R = 10 \Omega \quad L = 10 \text{ mH} ; C = 10 \mu\text{F} \quad V = 250 \text{ V}$$

$$X_L = 2\pi fL$$

$$= 314 \times 10 \times 10^{-3}$$

$$\boxed{X_L = 3.14 \Omega}$$

$$X_C = \frac{1}{2\pi fC}$$

$$= \frac{1}{314 \times 10^{-5}}$$

$$= \frac{10^5}{314}$$

$$\boxed{X_C = 318.47 \Omega}$$

$$\omega = \frac{1}{2\pi\sqrt{LC}}$$

$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

$$= 80.10 \text{ Hz} \quad 503.54 \text{ Hz}$$

$$I = \frac{250}{10} = 25 \text{ A}$$

$$(X_L)_r = 31.629 \Omega \quad (X_C)_r = \frac{1}{2\pi f_r C}$$

$$V_L = 25 \times 31.219 = 780.47 \text{ V} \quad V_C = 790.57 \text{ V}$$

$$* R = 7 \Omega; L = 31.8 \text{ mH}; V = 230 \text{ V}; f = 50 \text{ Hz}$$

$$X_L = 2 \times 3.14 \times 50 \times 31.8 \times 10^{-3}$$

$$= 9.98 \Omega$$

$$jX_L = 9.98j$$

$$= 10j$$

$$Z = R + jX_L$$

$$= \sqrt{7^2 + 10^2} = \sqrt{149} = 12.2 \Omega$$

$$I = \frac{230}{7 + 10j} = \frac{230}{12.2} = 18.85 \text{ A}$$

$$\tan \phi = \frac{X_L}{R} = \frac{10}{7}$$

$$\phi = 55^\circ$$

$$\cos \phi = 0.57$$

$$P = VI \cos \phi = 2471.23 \text{ W}$$

$$\text{Voltage across } R = IR = 18.85 \times 7 = 131.95 \text{ V}$$

$$\text{across } L = IX_L = 188.5 \text{ V}$$

$$* V = 250 \text{ V}; f = 50 \text{ Hz}; I = 5 \text{ A}; P = 750 \text{ W}$$

$$\cos \phi = \frac{P}{VI} = \frac{750}{250 \times 5} = \frac{3}{5} = 0.6 \text{ lag}$$

$$Z = \frac{V}{I} = 50 \Omega$$

$$I^2 R = 750$$

$$R = \frac{750}{25} = 30 \Omega$$

no power through L

$$Z^2 = R^2 + X_L^2$$

$$R^2 = 2500$$

$$X_L^2 = 2500 - 900 = 1600$$

$$X_L = 40 \Omega$$

$$2\pi fL = 40$$

$$L = \frac{40}{2 \times 3.14 \times 50}$$

$$L = 0.127 \text{ H}$$

$$* i(t) = 5 \sin(314t + 2\pi/3)$$

$$v(t) = 15 \sin(314t + \pi/6)$$

- (i) Impedance
(ii) Resistance (iii) Inductance (iv) average Power
(v) Power factor ($\cos \phi$)

$$\phi = \frac{5\pi}{6} - \frac{2\pi}{3} = \frac{\pi}{6} = 30^\circ$$

Current lags the voltage applied by 30° .

$$Z = \frac{V_m}{I_m} = \frac{15}{5} = 3 \Omega$$

$$\cos \phi = \frac{\sqrt{3}}{2} = \frac{R}{Z}$$

$$R = \frac{3\sqrt{3}}{2} \Omega$$

$$L = \frac{3}{2} \times \frac{1}{314}$$

$$= 4.7 \times 10^{-3}$$

$$= 4.7 \text{ mH}$$

$$Z^2 = X_L^2 + R^2$$

$$X_L^2 = 9 - \frac{9 \times 3}{4}$$

$$X_L^2 = \frac{36 - 27}{4}$$

$$X_L = \frac{3}{2}$$

$$\omega = 314 = 2\pi f$$

$$P = I^2 R = VI \cos \phi = \frac{15}{\sqrt{2}} \cdot \frac{5}{\sqrt{2}} \cos 30^\circ = \frac{75 \times \sqrt{3}}{2}$$

$$P = 75\sqrt{3}/4$$

* $C = 79.5 \mu F$ $R = 30 \Omega$ $V = 100 V$

$f = 50 Hz$
 $Z = \sqrt{R^2 + X_C^2} = \sqrt{30^2 + X_C^2}$

$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C} = 40 \Omega$

$Z = \sqrt{900 + 1600} = 50 \Omega$

$I = \frac{V}{Z} = 2 A$

$\cos \phi = \frac{R}{Z} \Rightarrow \phi = \cos^{-1}\left(\frac{R}{Z}\right)$
 $= \cos^{-1}\left(\frac{30}{50}\right) = 53^\circ \text{ lead}$

$I_m = 2\sqrt{2} A$

$\omega = 2\pi f = 314 \text{ rad/sec}$

$I = 2.428 \sin(314t + 53)$

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* COMPLEX POWER(S): \Rightarrow Apparent Power.

$S = VI^* \rightarrow \text{conjugate}$

$V = V \angle 0^\circ$

$I = I \angle -\phi$

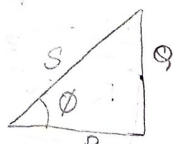
$S = VI \angle -\phi$

$S = VI^* = VI \angle \phi = VI \cos \phi + j VI \sin \phi$
 (P) (Q)

$VI \cos \phi = \text{Active Power (P)}$

$VI \sin \phi = \text{Reactive Power (Q)}$

$VI = \text{Apparent Power (S)}$



* $V = 100 \sin 500t$
 $I = 25 \sin(500t - 30^\circ)$

Determine circuit elements & their values,
 Determine P, Q, S.

$V_{rms} = \frac{100}{\sqrt{2}} \angle 0^\circ$

$I_{rms} = \frac{25}{\sqrt{2}} \angle -30^\circ$

$2\pi f L = 2 \Omega$

$L = \frac{2}{500} = 4 \times 10^{-3} H$

$Z = \frac{V}{I} = 4 \angle 30^\circ$
 $= 3.46 + j2$
 $\underbrace{\quad}_R \quad \underbrace{\quad}_{X_L}$

$R = 3.46 \Omega$
 $X_L = 2 \Omega$

$P = VI \cos \phi = \frac{2500}{2} \angle -30^\circ \cos \phi \cdot \frac{\sqrt{3}}{2}$
 $= 1082.53 + 625j$

$S = VI^* = \frac{2500}{2} \angle 30^\circ = 1082.53 + 625j$

$VI \cos \phi = P = 1082.53 W$

$VI \sin \phi = Q = 625$

$VI = S = 1250$

* $V(t) = 100 \sin 314t$ $R = 10 \Omega$; $L = 0.0318 H$;

$C = 63.6 \mu F$

$i(t)$, ϕ , power factor, active power, peak value of pulsating power.

$X_L = \omega L = 314 \times 0.0318 = 9.98 \approx 10$

$X_C = \frac{1}{\omega C} = \frac{1}{314 \times 63.6} = 5 \times 10^{-5} \times 10^6$
 $= 50$

$X = X_L - X_C = -40$

$$Z = \sqrt{R^2 + X^2} = \sqrt{(10)^2 + (-40)^2} = \sqrt{100 + 1600}$$

$$\boxed{Z = \underline{\underline{41.2 \Omega}}}$$

$$I = \frac{V}{Z}$$

$$= \frac{100/\sqrt{2}}{41.2} = \underline{\underline{1.716 A}}$$

$$I_m = \sqrt{2} I = 1.414 \times 1.716 = \underline{\underline{2.426 A}}$$

$$\phi = \tan^{-1}(-40/10) = \tan^{-1}(-4) = 76^\circ \text{ lead}$$

$$i = I_m \sin(314t + \phi)$$

$$= 2.43 \sin(314t + 76^\circ)$$

$$\cos \phi = \cos 76^\circ = \underline{\underline{0.24}}$$

$$VI = 100 \sin 314t \cdot 2.43 \sin(314t + 76^\circ)$$

$$= 243 [\cos(76^\circ) - \cos(628t + 76^\circ)]$$

$$= [58.78 - 243 \cos(628t + 76^\circ)]$$

$$= 58.78 - 243 \sin(90 - 628t - 76^\circ)$$

$$= \frac{58.78}{2} + \frac{243}{2} \sin(628t - 14^\circ)$$

$$= \underline{\underline{29.39 + 121.5 \sin(628t - 14^\circ)}}$$