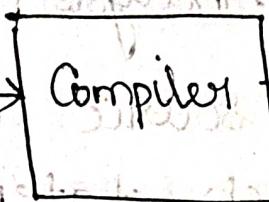


05/02/2024

→ Compiler converts high-level language to low language.

Source code

(source language)



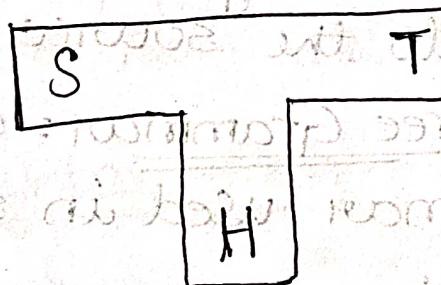
Target code

→ High-level language: human readable.

→ Low-level language: machine understandable.

→ Opcode: combination of 0's & 1's.

→ Represented as:



S → Source Code

T → target code

H → host

language.

→ Compilers (C): TurboC, gcc

→ Host language for C compiler is C language.

→ Using the same host language as the programming language for a compiler is called Bootstrapping.

→ Most of compilers are implemented using C.

→ Pass: group of phases.

→ Phase: consists of a specified functionality which takes a I/P and gives a O/P.

→ O/P of final phase is the target code.

* Basic phases of a compiler:

Phase-1 → Lexical Analysis (Lexer / Scanner)

- reads the source code statement by statement
- converts each statement into a token forming a sequence.
- removes all the extra spaces and new line characters.
- removes the comments.

token:
 $\langle \text{name}, \text{loc} \rangle$

Phase-2: → Syntax Analysis (Parser) mandatory

- checks if the program is correct according to the source language.
- Context Free Grammar: specifies the grammar used in source language.

O/P of this phase is a syntax tree.

Phase-1: Lexical Analysis

If it is a reserved word then token consists only $\langle \text{name} \rangle$.

If it is not a reserved word then token consists $\langle \text{name}, \text{loc} \rangle$.

Eg: variables / identifiers.

Eg: int a; $\langle \text{int}, 1 \rangle \langle ; \rangle$

→ symbol table is the data structure where we store the pre-defined symbols.

* We store all symbols, reserved words, special characters etc.

| Name | Type | Description |
|------|---------|-------------|
| int | keyword | integer |

→ If the symbol is not present in the symbol table we create a token and update the symbol table. No repetition is allowed.

Phase-2: Syntax Analysis (Parser)

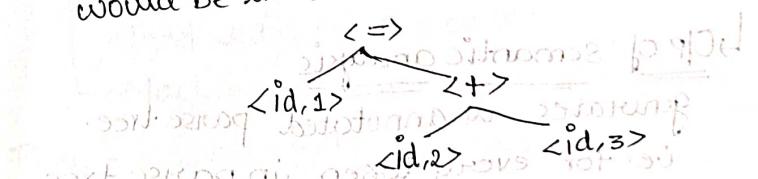
Ex: $a = b + c$ * all terminal symbols are given by operators

Phase-1: $\langle \text{id}, 1 \rangle \Rightarrow \langle \text{id}, 2 \rangle + \langle \text{id}, 3 \rangle \langle ; \rangle$

→ We draw the parse tree to these tokens.

→ Types: bottom-up, top-down

→ Leaf nodes: are variables and operators would be the internal nodes.



Phase-3: Semantic Analysis:

- Meaning of the statement.
- Checks if the given tokens generate meaningful statements.
- for this it checks the types of identifiers and verifies if further operations are meaningful (or) not.
- performs type conversion for the required types to be modified.

Interview questions

Strongly typed languages: The type of the variable is explicitly declared.

Eg: C, C++, Java.

Weakly typed languages: Type of the variable is known while usage in the code.

Eg: Python.

Explicit type conversion: C, C++.

↳ O/P of semantic analysis generates unannotated parse tree. i.e. for every token in parse tree

we add a "type" tag.

Phase-4: Intermediate Code Generation

↳ Eg: source code ; target code
 ⇒ high-level language ⇒ low-level language.

⇒ intermediate code ⇒ 3-address code

$c = a + b * d;$ to the right side of the assignment operator; we have atmost 1 operator and atmost 2 operands.

⇒ 3-address code:

| | |
|-----------------|------------|
| $t_1 = b * d$ | LD R0, b |
| $t_2 = a + t_1$ | LD R1, d |
| $c = t_1 + t_2$ | MUL R1R0 |
| | LD R2, a |
| | ADD R1, R2 |
| | ST C, R2 |

3-address code helps in generating the assembly language code easily.

Phase-5: Code Generation : Target Code:

Phase-6: Code Optimization (Optional)

↳ checks to reduce the size or time of execution of the code.

↳ Machine dependent code optimization.

Phase - 1, 2, 3 : Analysis Phases

Phase - 4, 5 : Synthesis Phases

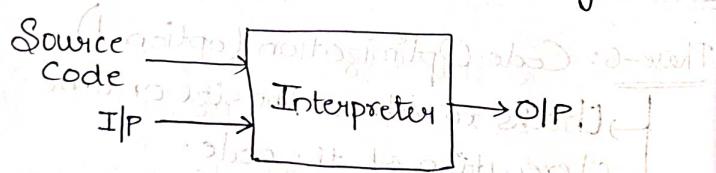
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UNIT - 1

* Language Processors:
→ Compiler:
Source Code → Compiler → Target Code.

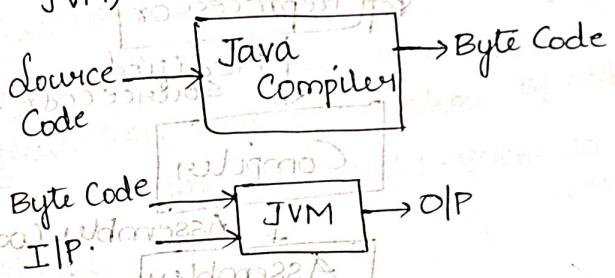
* Target Code is I/P → Target Code → O/P
executable.
→ Compiler is machine dependent: we must execute the executable code on the same machine.

→ Interpreter:
* Converts each statement of the code one at a time, to target code:

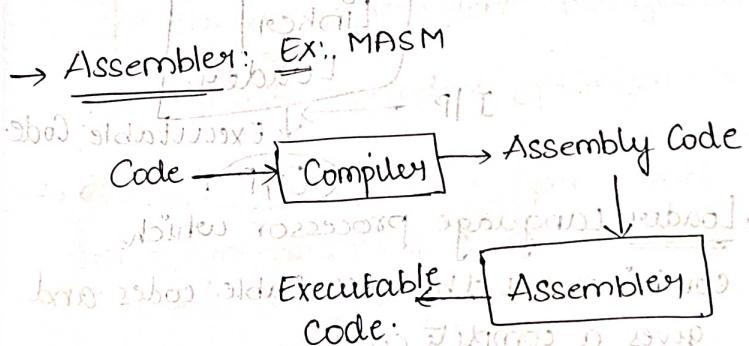


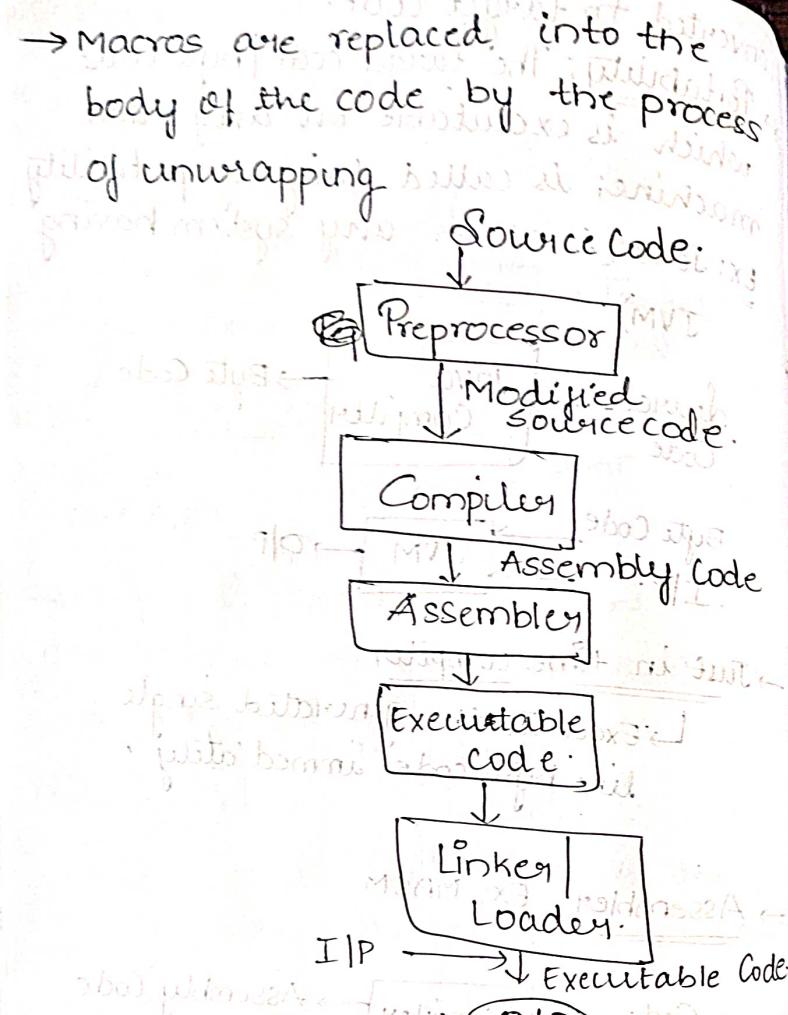
* Compiler is faster than interpreter due to source code being complete and well written.

converted to target code.
* Portability: The target code / byte code which is executable on any other machine, is called language portability.
Ex: Java (runs on any system having JVM).



→ Just in time compiler:
↳ Executes the generated single line byte code immediately.





- Loader: Language processor which combines all the executable codes and gives a complete code.
- Linker: used to link executable codes which are ... + ... n/p.

* Structure of the compiler:

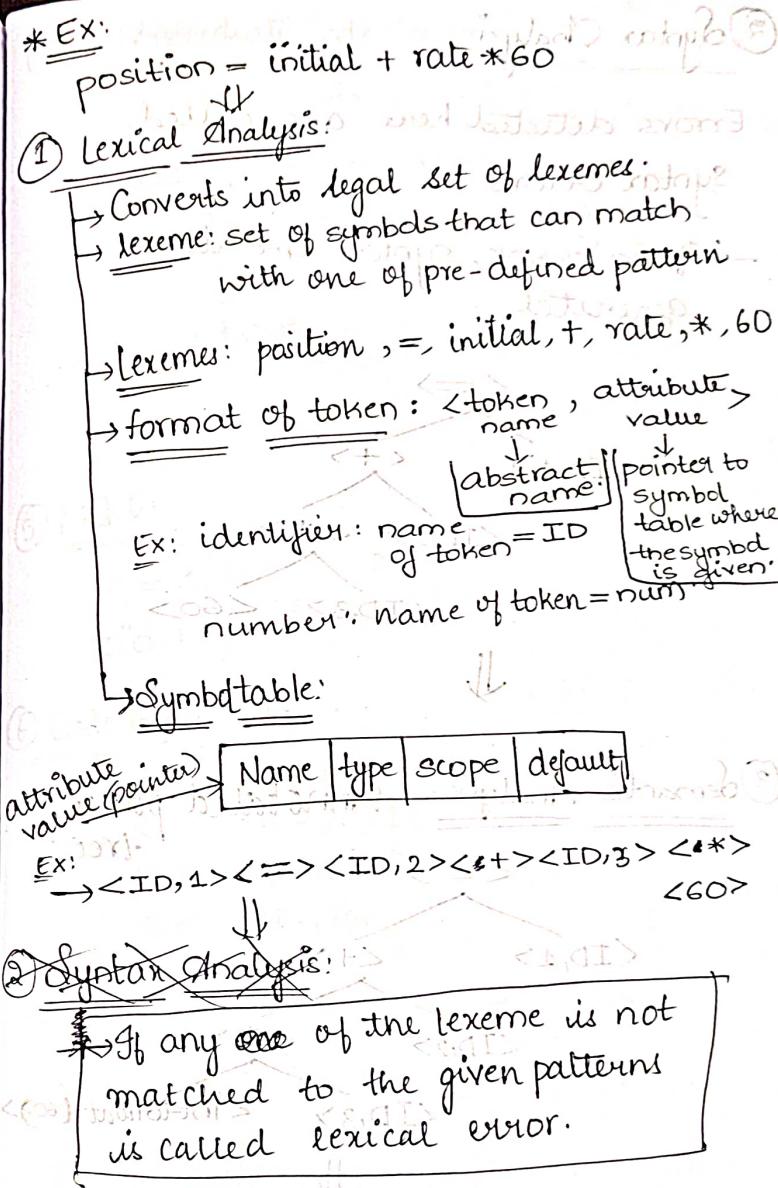
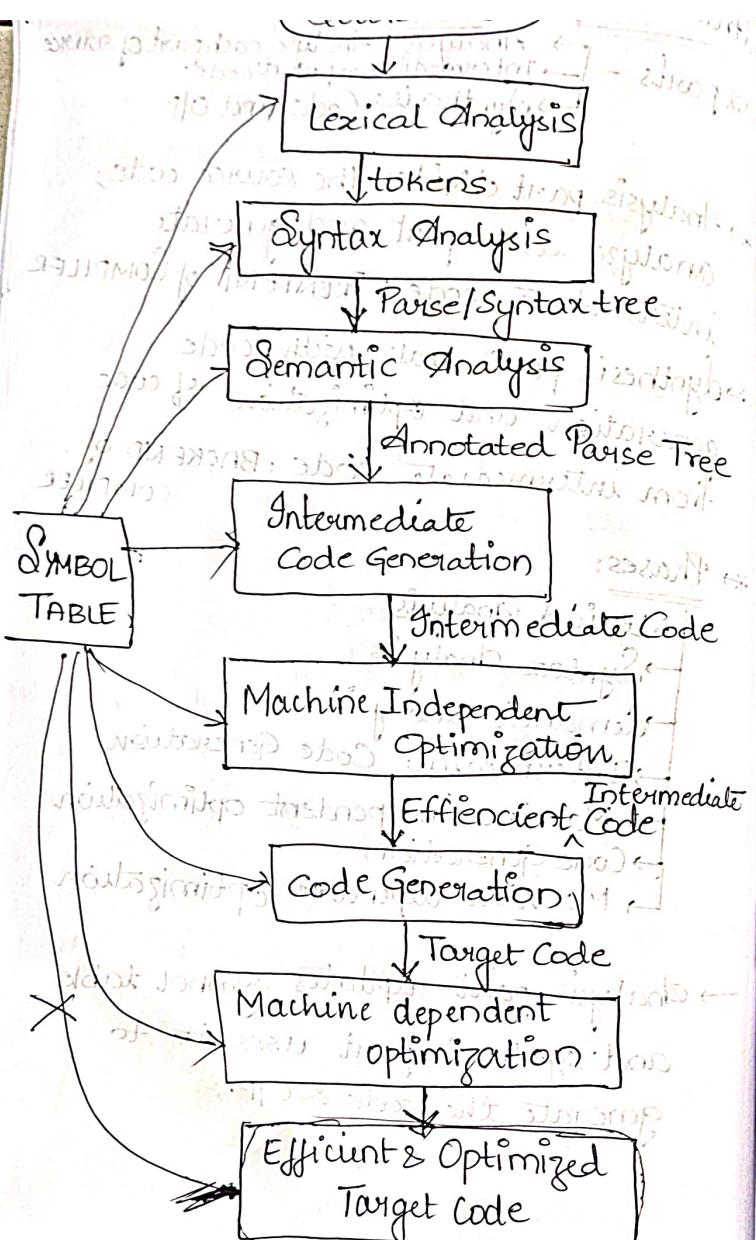
→ 2 parts →
 Analysis: Analyse each part of source code.
 Intermediate representation code.
 Synthesis: Code and O/P

- Analysis part divides the source code, analyze each part and generate intermediate code : FRONTEND of COMPILER
- synthesis part deals with code generation and optimization of code from intermediate code : BACKEND of COMPILER

* Phases:

- Lexical analysis
- Syntax analysis
- Semantic analysis
- Intermediate Code Generation
- Machine independent optimization
- Code Generation
- Machine dependent optimization

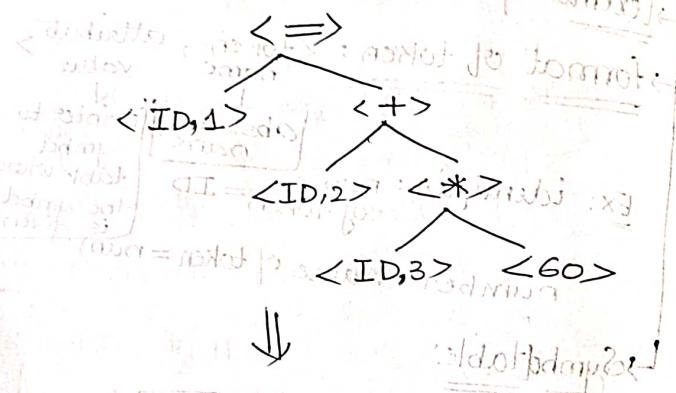
- Analysis part updates symbol table and synthesis part uses it to generate the code & O/P.



② Syntax Analysis:

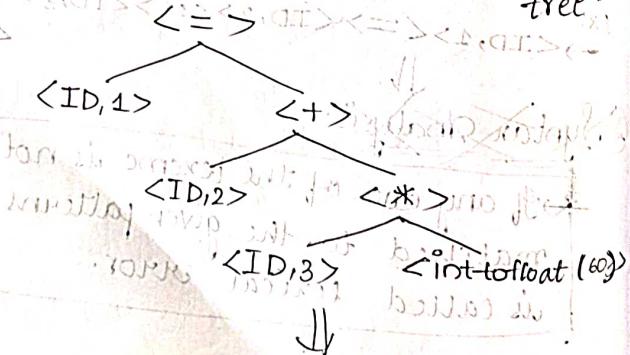
Errors detected here are called syntax errors.

If no error, syntax tree is generated:



③ Semantic Analysis:

Annotated parse tree



④ Intermediate Code Generation:

3-address code: ($a = b + c$)

$t_1 = \text{int-to-float}(60)$

$t_2 = \text{rate} * t_1$ | $t_2 = <\text{id}, 3> * t_1$

$t_3 = \text{initial} + t_2$ | $t_3 = <\text{id}, 2> + t_2$

$t_4 = <\text{id}, 1> = t_3$

⑤ M10:

MOV R0, #60.0

MULF R0, R0, ID3

ADDF R0, R0, ID2

STF ID1, R0

⑥ Code Generation:

MOV R0, #60.0

MULF R0, R0, ID3

ADDF R0, R0, ID2

STF ID1, R0

12/02/

- Target Code is machine dependent & we convert intermediary code (machine independent, as they are just repetition of source code) to target code which is a set of micro instructions. As micro instructions contains register and unique instructions set that depends on your machine (risk/cisk). Hence target code is machine dependent.

* SYMBOL TABLE:

We store info regarding constants & identifiers.

* Compiler design tools:

- Compiler is a software
- Lex: It is a tool that automatically generates/implements lexical analyser.
- YACC/ parser generator: automatic

parse tree generation with taking input as grammar

YACC: Yet Another Compiler Compiler

→ syntax directed translation engine

Annotated parse tree generation

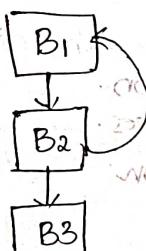
→ Data flow analysis engine: Tracks flow of

data in 3-address code

data flow

control flow

→ 3-address code is divided into blocks where each block has statements that executes only sequentially.



→ code generator: helps to efficiently use register

* Applications of Compiler Technology: 13/02/24

- register variable is allocated to the register.
- Implementation of High-level programming languages:

- Improve the efficiency of generated code:
 - * using registers
- Optimization of computer architectures.

Parallelism

- Instructor level
 - Processor level

Program Translation:

- Compiled simulation.
- Hardware synthesis.
- Binary Translation.

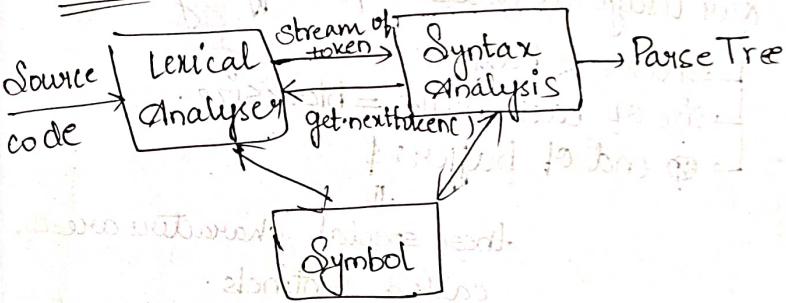
Programming language basics

→ Static/dynamic distinction:

- Aliasing
- Parameter passing
- Dynamic Scope
- Explicit Access Control
- Static scope and block structure
- Environment & states:

13/02/24

→ Lexical Analysis:



* Lexical error:

- If the lexeme is not matched with any one of the pattern, such error is called lexical error.

- Error recovery takes place in a compiler whenever an error is occurred; then it overcomes the error and compiles other statements.

Panic Mode Error Recovery:

- 1) Skip the symbols unless the lexeme is matched with any one of the pattern.
- 2) Transpose the symbols.

* The process of moving the data from main memory to the buffer and scanning for our usage is called input buffering.

- uses 2 buffers.
- size of each buffer = blocksize.
- end of buffer: \$

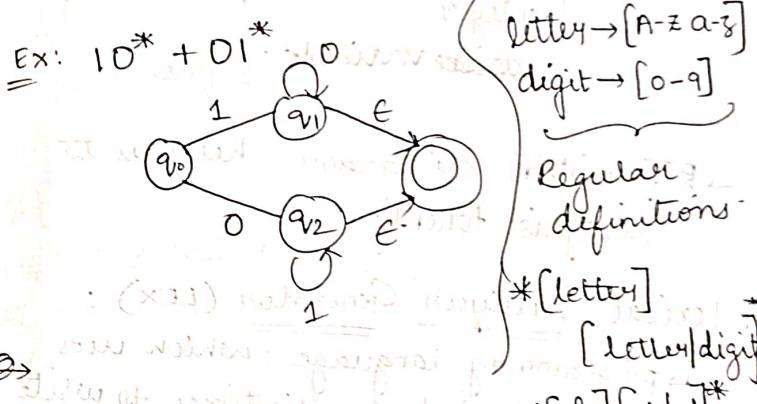
these special characters are called sentinels.

Specification of patterns/tokens

- Regular Expressions model text files.
- Representation of regular languages.
- Operations:
 - Union $L_1 \cup L_2$
 - Intersection $L_1 \cap L_2$
 - Concatenation $L_1 L_2$

closure: L^* ; L^+
 complement \bar{L}
 reverse L^R

Ex: 1000110
 0110 → substring
 0010 → subsequence



$(\times 3)$ letter and digit

new states - occupied by letter or digit

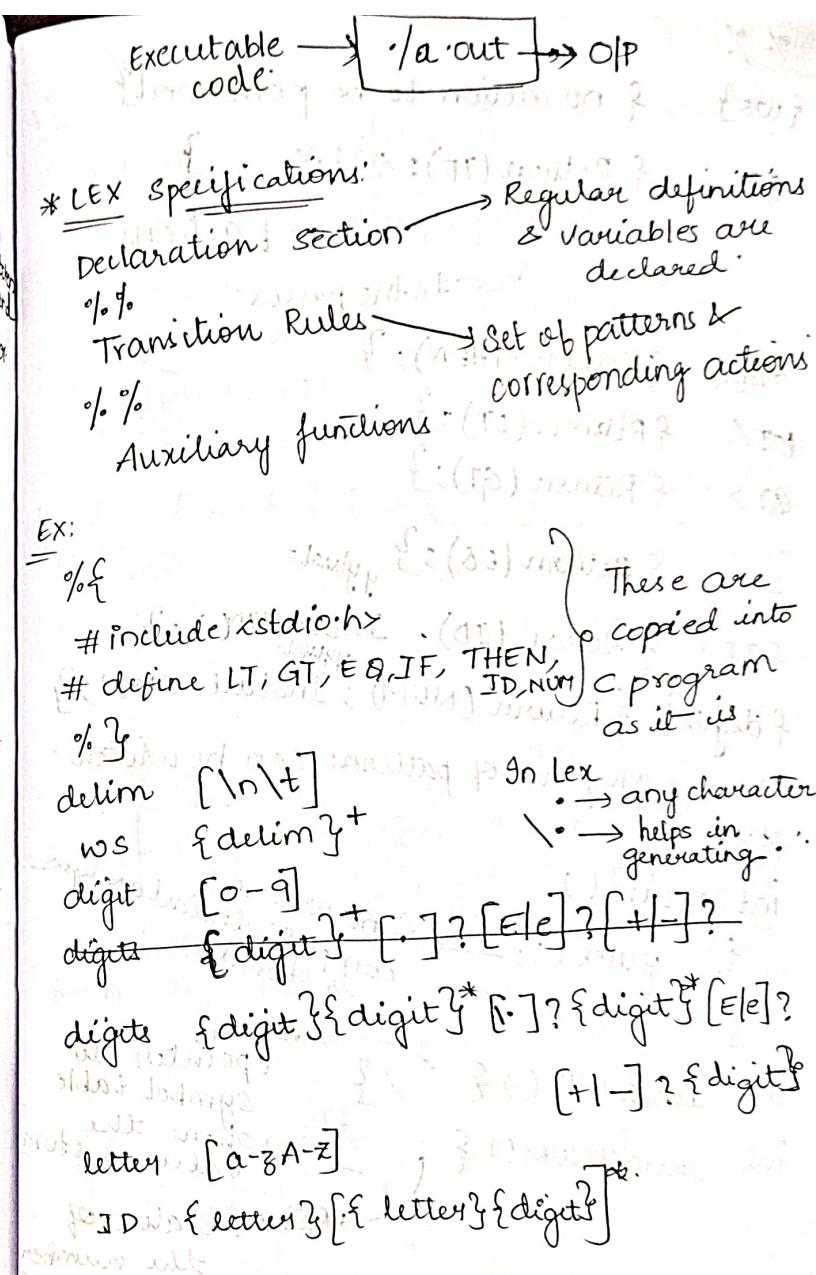
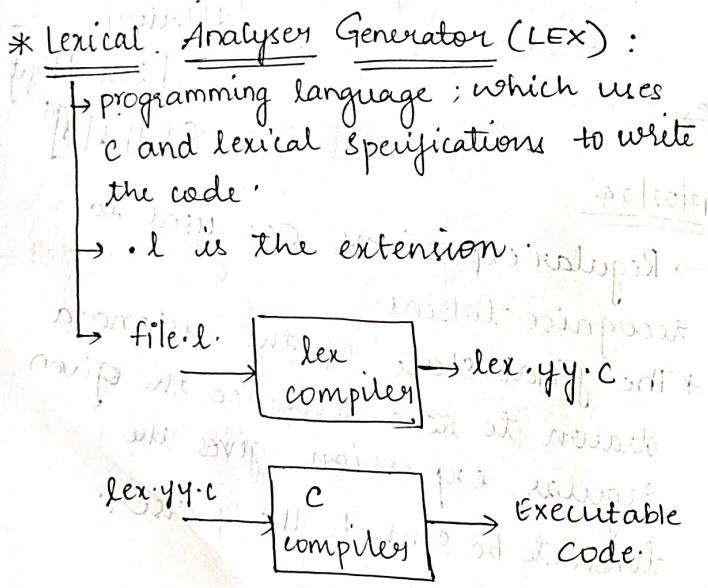
state of writing sqd dataset $\Rightarrow [l][ld]^*$

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→ Regular expressions are used to recognise tokens.

* The final state of the automata drawn to ~~rec~~ recognise the given regular expression; gives the token to be sent to the parser.

- Predefined Variables
 - yytext: current lexeme scanned by the lexical analyser.
 - character variable: holds the character scanned by the lexical analyser.
 - yyval: holds the attribute value which is passed to parser.
 - integer variable: holds integer values.
- * → Transition diagrams helps us to recognise tokens.



$\{ws\}$ { no action to be performed }
 { Return(IF); A2; A3 ... }
 ↗ min. no. of actions
 ↗ to the parser.
 THEN { Return(THEN); }
 < L { Return(LT); }
 > R { Return(GT); }
 == { Return(EQ); } yyval =
 { ID } { Return(ID); InstallID(); } yyval =
 { digits } { Return(NUM); InstallNUM(); }
 } any no. of patterns can be written.
 %%
 int main().
 { yylex(); → func where complete lexical analysis is stored.
 }
 int InstallID() { } → Return (pointer to symbol table where the value is stored)
 int InstallNUM() { } → Return (value of number)

17/02/2021
 * Syntax Analysis: (Parser)
 → stream of tokens & grammar are the I/P.
 CFG is used $G = (V, T, P, S)$ ($N+T$)
 $P \rightarrow E$ $E \rightarrow E + T | T$ body of the production
 $T \rightarrow T * F | F$
 $F \rightarrow (E) | id$
 head of the production (only one variable)
 total no. of productions = 6
 order of production:
 $S = E$
 → Issues in CFG:
 i) Left recursion: $A \rightarrow A\alpha | \beta | \gamma$
 ii) Left factoring: $A \rightarrow \alpha B_1 | \alpha B_2 | \alpha B_3$
 Ambiguous: $(A \rightarrow \alpha A)^n$, $A^* \rightarrow B_1 | B_2 | \dots | B_n$.
 * Few algorithms do not produce efficient parsers.
 Given productions have left recursions:
 $E \rightarrow TE'$
 $E' \rightarrow +TE'| E$
 $T \rightarrow FT'$
 $T' \rightarrow *FT'| E$
 $F \rightarrow (E)| id$

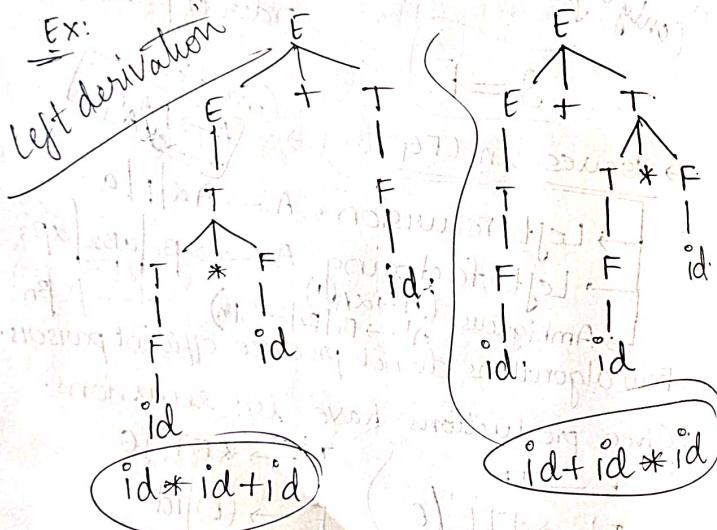
$\rightarrow \Sigma^*$

Ex: $S \rightarrow iE\$$ | $iE + S e S | a.$
 $S \rightarrow i E \$\$ | a.$
 $\$ \rightarrow e\$ | e:$

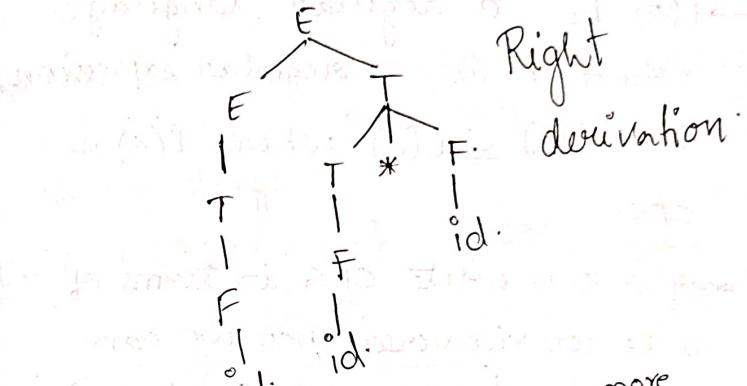
* Derivation → Left most derivation
→ Right most derivation
↳ deriving strings from the given productions

→ In any step, the replacing variable is called handle.

Parse Tree



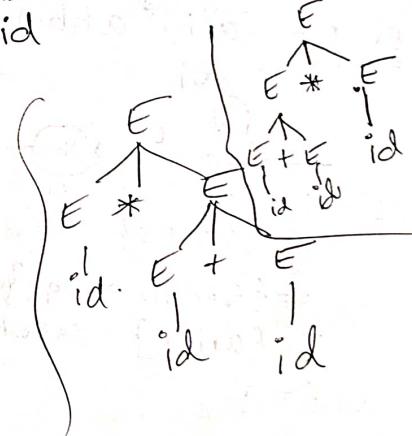
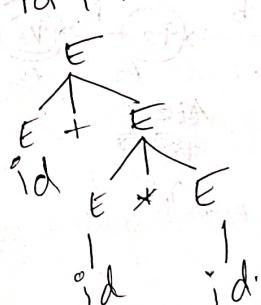
$$\begin{aligned} E = E + T &\Rightarrow E = E + T * F \Rightarrow E + F * id \\ &\Rightarrow E = E + id * id \Rightarrow E = T + id * id \\ &\Rightarrow E = F + id * id \Rightarrow E = id + id * id \end{aligned}$$



* Ambiguity: for any string, there are more than one parse trees.

$$E \rightarrow E + E | E * E | id$$

id + id * id.



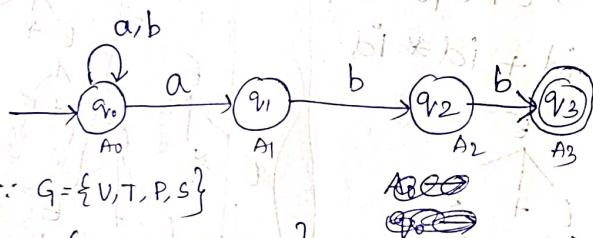
19/05/2024

* Context Free Grammar:

→ Let $L(R)$ be a regular language where R is a regular expression. Then $L(R) \subseteq L(G)$ where $L(G)$ is CFG.

* If we can write CFG in terms of a RE (or) vice versa then we can say that $L(G) = L(R)$ (Equivalent)

Ex: $R = (a/b)^* abb$



$$G = \{V, T, P, S\}$$

$$V = \{q_0, q_1, q_2, q_3\}$$

$$T = \{a, b, \epsilon\} = \{A_0, A_1, A_2, A_3\}$$

$$S = q_0$$

Productions:

$$\begin{aligned} A_0 &\rightarrow aA_0 \mid bA_0 \mid aA_1 \\ A_1 &\rightarrow bA_2 \\ A_2 &\rightarrow bA_3 \\ A_3 &\rightarrow \epsilon \end{aligned}$$

→ $L(G)$ and $L(R)$ are said to be equivalent if and only if they consist of similar strings.

Ex: $L = \{a^n b^n \mid n \geq 0\}$

~~$A_0 \rightarrow aA_0 \mid bA_1$~~
 ~~$A_1 \rightarrow bA_2$~~
 $A_0 \rightarrow aA_0 \mid b \mid \epsilon$



* We use CFG in syntax analysis to specify the syntax of the programming language.

* Parsing is the process where we can derive the string from the start symbol (or) to check if the given set of strings are generated from the given grammar.

→ To get a proper string; we must keep on back track the parse tree to get a correct NIP.

Ex:

$$\begin{array}{l}
 E \rightarrow E + T \mid T \\
 T \rightarrow T * F \mid F \\
 F \rightarrow (E) \mid id
 \end{array}
 \quad \Rightarrow \quad
 \begin{array}{l}
 E' \rightarrow TE' \\
 T \rightarrow FT' \\
 F \rightarrow (E) \mid id
 \end{array}$$

RDP:

```

char input[10];
for(j=0; j<=n; j++) {
    if(input[j] == '$')
        printf("Success");
}

```

\Rightarrow

```

char input[10];
for(j=0; j<=n; j++)
{
    E();
    if(input[j] == '$')
        printf("Success");
}

E()
{
    T();
    E();
}

T()
{
    F();
    T();
}

F()
{
    if(input[j] == '*')
        j++; T(); F();
}

```

FC)

```

if(input[j] == '(') { j++;
    E();
    if(input[j] == ')') {
        j++;
    }
    else if(input[j] == 'i') {
        j++;
    }
}

```

→ LL(1) parser: (Predictive Non-backtracking parser)

↑ 1 symbol is parsed at a time
↑ left most derivation is used

Scanning of the string
is from left
to right

* for any G (CFG) if we can construct LL(1) parser; such G is called LL(1) grammar.

→ The grammar G must ~~not~~ have left recursion and ambiguity.

* Ex: $A \rightarrow \alpha | \beta \Rightarrow$ LL(1) grammar (Checking)

$A \xrightarrow{\alpha} \epsilon$ i) $\text{First}(\alpha) \cap \text{First}(\beta) = \emptyset$
 $\qquad\qquad\qquad$ ii) $\alpha \xrightarrow{*} \epsilon \Rightarrow \text{Follow}(A) \cap \text{First}(\beta) = \emptyset$
 $\qquad\qquad\qquad$ iii) $\alpha \xrightarrow{*} C \Rightarrow \text{Follow}(A) \cap \text{First}(C) = \emptyset$

* FIRST SET and FOLLOW SET:

$\alpha \rightarrow$ terminal : First set : Only

$\alpha \rightarrow$ Non-terminal : Both first set & follow set

$\alpha \rightarrow$ grammar symbol

$\text{First}(\alpha) = \{\text{set of terminal symbols}\}$ are derived from $\{\alpha\}$

$\text{First}(\alpha) = \alpha : \alpha \Rightarrow \alpha^*$

$\text{Follow}(A) =$ symbol that is following A in $A \Rightarrow A^*$ the body of production.

if $\alpha \rightarrow$ non-terminal : find a terminal

First Set: \Rightarrow ~~First set of current IIP symbol~~

\hookrightarrow if current IIP symbol is in First set (α) ; Such a α is substituted

Follow Set: used when non-terminal produces ϵ .

* First Set:

Let X be grammar symbol.

1. $\text{First}(X) = \{X\}$ if X is terminal.

2. If X is non-terminal

$X \Rightarrow Y_1, Y_2, Y_3, \dots, Y_k$

if Y_i is terminal symbol

$$\text{First}(X) = \{Y_i\}$$

If Y_i is non-terminal having ϵ

$$\text{First}(X) = \text{First}(Y_1) \cup \text{First}(Y_2) \cup \dots \cup \text{First}(Y_k)$$

if $X \Rightarrow \epsilon$ $\text{First}(X) = \{\epsilon\}$ $\text{First}(Y_k)$

$$\begin{aligned} \text{EX: } E &\rightarrow TE' \\ E' &\rightarrow +TE' \mid \epsilon \\ T &\rightarrow FT' \\ T' &\rightarrow *FT' \mid \epsilon \\ F &\rightarrow (E) \\ F &\rightarrow \text{id} \end{aligned} \quad \left. \begin{aligned} \text{First}(E) &= \text{First}(T) = \text{First}(F) \\ &= \{\$, \text{id}\} \\ \text{First}(F) &= \{\$, \text{id}\} \\ \text{First}(E') &= \{+, *\} \\ \text{First}(T') &= \{*, \epsilon\} \end{aligned} \right\} \text{First}(E) = \text{First}(T) = \text{First}(F) = \{\$, \text{id}\}$$

$$\begin{aligned} \Rightarrow E &\rightarrow ETT \mid T \\ T &\rightarrow T*F \mid F \\ F &\rightarrow (E) \mid \text{id} \end{aligned} \quad \left. \begin{aligned} \text{First}(F) &= \{\$, \text{id}\} \\ \text{First}(E) &= \{\$, \text{id}\} \\ \text{First}(T) &= \{\$, \text{id}\} \end{aligned} \right\} \text{First}(E) = \text{First}(T) = \text{First}(F) = \{\$, \text{id}\}$$

$$\begin{aligned} \Rightarrow S &\rightarrow iESS' \\ S' &\rightarrow eS \mid \epsilon \\ E &\rightarrow b \end{aligned} \quad \left. \begin{aligned} \text{First}(S) &= i \\ \text{First}(S') &= \{e, \epsilon\} \\ \text{First}(E) &= \{b\} \end{aligned} \right\} \text{First}(S) = i$$

* $S \rightarrow (L) | a$ } Left recursion $A \rightarrow PA$
 $L \rightarrow L_1, S | S$ } Recursion $A' \rightarrow \alpha A' | \epsilon$
 $S \rightarrow (L) | a$ $\text{First}(S) = \{(, a\}$
 $L \rightarrow \emptyset | L'$ $\text{First}(L) = \text{First}(S) = \{(,$
 $L' \rightarrow , S | \epsilon$ $\text{First}(L') = \{\, , \epsilon\}$

* $\text{First}(+EE') = \{+\}$
* $\text{First}(ET') = \text{First}(E)$
 if E is having ϵ
 $\text{First}(E) \cup \text{First}(T') \cup \{\epsilon\}$
 if T' is having ϵ

* Follow Set

for non-terminals

① If 'S' is start symbol; then $\text{Follow}(S) = \{\$\}$

② Let A be any non-terminal except start symbol; $X \rightarrow \alpha A \beta B$

if B is terminal

then $\text{Follow}(A) = \{B\}$

if B is non-terminal
 then $\text{Follow}(A) = \text{First}(B) - \{\epsilon\}$

③ $X \rightarrow \alpha AB$ (or) $X \rightarrow \alpha A$
 if $B \rightarrow \epsilon$ $\text{Follow}(A) = \text{Follow}(X)$
 then $\text{Follow}(A) = \text{Follow}(X)$

$\Rightarrow E \text{Ex: } E \rightarrow TE'$ $\text{Follow}(E) = \{\$, \}\}$
 $E' \rightarrow +TE' | G$ $\text{Follow}(E') = \{\$, \}\}$
 $T \rightarrow FT'$ $\text{Follow}(T) = (\text{First}(E) - \text{Follow}(E)) \cup \text{Follow}(E')$
 $T' \rightarrow *FT' | G$
 $F \rightarrow (E)$
 $F \rightarrow id$ $= \{+, \$, \}\}$

$\text{Follow}(T') = \text{Follow}(T)$

$(A) \text{Follow} = \{+, \$, \}\}$

$\text{Follow}(F) = (\text{First}(T') - \{\epsilon\}) \cup \text{Follow}(T)$
 $= \{*, +, \$, \}\}$

$A \rightarrow \alpha | \beta$

$\text{First}(\alpha) \cap \text{First}(\beta) = \emptyset$

$A \rightarrow \alpha | \epsilon$

$\text{First}(\alpha) \cap \text{Follow}(A) = \emptyset$

Check if these conditions are satisfied for LL(1) grammar

* 28/02/2024

* Parsing Table:

- 1) Find first set and follow set
 - 2) LL(1) parsing table.
- rows: non-terminal.
columns: terminals including \$

| | a | b | c | d | \$ |
|---|---|---|---|---|----|
| A | | | | | |
| B | | | | | |
| C | | | | | |
| D | | | | | |
| E | | | | | |

M.

* LL(1) table filling algorithm:

- $A \rightarrow \alpha$
 $\alpha \in (VUT)^+$
- $(M[A, a]) \leftarrow A \rightarrow \alpha$
- $+ a \in \text{First}(\alpha)$
- $* E \rightarrow TE'$
 $E' \rightarrow +TE'/\epsilon$
- $T \rightarrow FT'$
 $T' \rightarrow *FT'/\epsilon$
- $F \rightarrow (E)$
 $F \rightarrow id$
- $A \rightarrow \epsilon$
 $M[A, b] \leftarrow A \rightarrow \epsilon$
- $+ b \in \text{Follow}(A)$
- $\text{First}(\alpha) = \{ \epsilon \}$

$$\text{Follow}(E) = \{ \$, \} \quad \text{Follow}(E') = \{ \$, \}$$

$$\text{Follow}(T) = \{ +, \$, \} \quad \text{Follow}(T') = \{ +, \$, \}$$

$$\text{Follow}(F) = \{ *, +, \$, \} \quad \text{Follow}(F') = \{ *, +, \$, \}$$

| | $E \rightarrow TE'$ | | $E \rightarrow TE'$ | | |
|------|---------------------|-----------------------|---------------------------|---------------------------|--|
| E' | $E' \rightarrow +T$ | | $E' \rightarrow \epsilon$ | $E' \rightarrow \epsilon$ | |
| T | $T \rightarrow FT'$ | | $T \rightarrow FT'$ | | |
| T' | $T' \rightarrow E$ | $T' \rightarrow *FT'$ | $T' \rightarrow \epsilon$ | $T' \rightarrow \epsilon$ | |
| F | $F \rightarrow id$ | | $F \rightarrow (E)$ | | |

$$① E \rightarrow TE' \quad A \rightarrow \alpha$$

$$\text{First}(\alpha) = \text{First}(T) = \{ (, id) \}$$

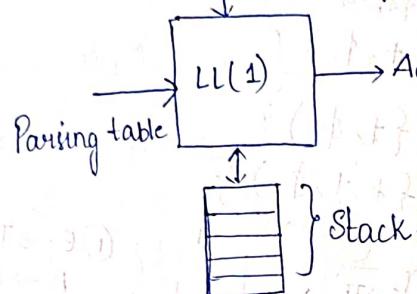
$$M[E, ()], M[E, id]$$

| LL(1) parsing table. | | | | | |
|----------------------------------|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------|
| ② $E' \rightarrow +TE'$ | $E' \rightarrow \epsilon$ |
| $A \rightarrow \alpha$ | $M[A, b]$ | | | | |
| $\alpha = +TE'$ | | $M[E', \$]$ | | | |
| $\text{First}(\alpha) = \{ + \}$ | | | $M[E', \$]$, $M[E', ()]$ | | |

| | | | |
|--|------------------------|-------------------------|---------------------|
| ③ $T \rightarrow FT'$ | $A \rightarrow \alpha$ | $M[T, ()]$, $M[T, id]$ | $M[T, *, FT']$ |
| $\alpha \in M[A, a]$ | | | $M[T, \epsilon]$ |
| $a \in \text{First}(F) = \{ (, id) \}$ | | | $M[T, Follow(F)]$ |
| | | | $M[T, +], M[T, \$]$ |

| | | |
|-----------------------|------------|------------|
| ⑤ $F \rightarrow (E)$ | $M[F, ()]$ | $M[T, ()]$ |
|-----------------------|------------|------------|

$* \underline{id + id * id}$



| Matched symbol | Stack | Input | Action |
|----------------|----------|-----------------|--|
| id | \$E | id + id * id \$ | $M[E, id] \leftarrow E \rightarrow id$ |
| | \$E'T' | id + id * id \$ | $M[T, id] \leftarrow T \rightarrow id$ |
| | \$E'T'F | id + id * id \$ | $M[F, id] \leftarrow F \rightarrow id$ |
| | \$E'T'id | id + id * id \$ | POP |
| | \$E'T' | + id * id \$ | $M[T, +] \leftarrow T \rightarrow +$ |
| | \$E' | + id * id \$ | $M[E, +] \leftarrow E \rightarrow +$ |
| id + | \$E'T'+ | + id * id \$ | POP |
| | \$E'T | id * id \$ | $M[T, id] \leftarrow T \rightarrow id$ |
| | \$E'T'F | id * id \$ | $M[F, id] \leftarrow F \rightarrow id$ |
| id + id | \$E'T'id | id * id \$ | POP |
| | \$E'T' | * id \$ | $M[T, *] \leftarrow T \rightarrow *$ |
| id + id * | \$E'T'F* | * id \$ | POP |

| | | | |
|----------------------------|----------|-------|--|
| $\underline{id + id * id}$ | \$E'T'F | id \$ | $M[F, id] \leftarrow F \rightarrow id$ |
| | \$E'T'id | \$ | POP |
| | \$E'T' | \$ | $M[T, \$] \leftarrow T \rightarrow \$$ |
| | \$E' | \$ | $M[E, \$] \leftarrow E \rightarrow \$$ |
| | \$ | \$ | Accepted |

$* S \rightarrow (L) | a$

$L \rightarrow L, S | S$

$Follow(S) = \{ \$, a,) \}$

$Follow(L) = \{ \} \}$

$Follow(L') = \{ \} \}$

$$\begin{aligned} First(S) &= \{ \}, a \} \\ First(L) &= First(S) \\ &= \{ \}, a \} \end{aligned}$$

$$First(L') = \{ \} \}$$

11/03/2024

* Bottom-Up Parsing:

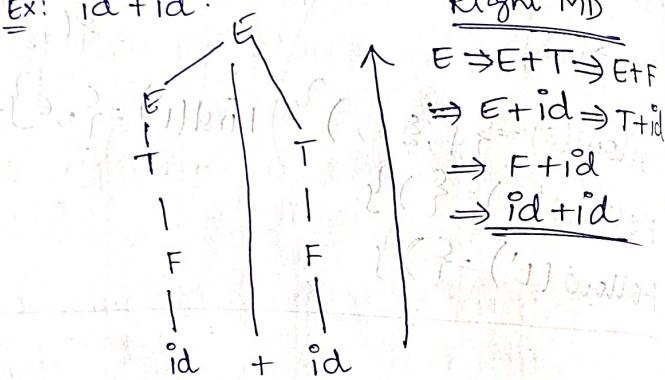
→ Leaves to the root node.

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

Ex: id + id



→ Bottom-up parsing uses right most derivation in reverse direction.

* Types:

Shift-Reduce Parser.

LR parsers.

Simple LR (SLR)

Canonical LR (CLR)

LALR (LookAhead)

→ YACC: uses LALR parser
↳ covers many grammars.

* Shift-Reduce Parser:

* operations: → Moving IP symbol on to stack: SHIFT

→ Shift

→ Reduce

→ Accept

→ Error

* Backtracking is possible.

→ When we reach the start symbol as top of stack: ACCEPT.

| <u>Stack</u> | <u>IP</u> | <u>Input</u> | <u>Action</u> |
|--------------|-----------|--------------|---------------|
| \$ | | id * id \$ | shift |
| \$ id | | * id \$ | F → id reduce |
| \$ F | | * id \$ | shift |
| \$ F * | | * id \$ | shift |
| \$ T * | | * id \$ | T → F reduce |
| \$ id | | id \$ | shift |
| \$ T * id | | \$ () id | shift |
| \$ T * F | | \$ () id F | F → id reduce |

| | | |
|------|----|--------------------------|
| \$ T | \$ | $I \rightarrow T * F$ |
| \$ E | \$ | $E \rightarrow T$ reduce |
| \$ E | \$ | Accept. |

* Conflicts in Shift-Reduce Parser:

→ Reduce-Reduce problem where we have 2 chances to reduce particular symbol.

→ Shift-Reduce problem where we must choose b/w shifting (or) reducing.

→ These problems are raised due to Brute force method.

→ Parsing a lengthy string using shift-reduce parser is costly as backtracking is difficult and takes long time.

* LR Parsers:
 ↗ $\kappa = 0/1$ → how many symbols parser can predict after a step.
 ↗ Right most derivation in reverse.
 ↗ Parsing is from left to right.
 ↗ SLR \rightarrow LR(0) parser.
 ↗ CLR \rightarrow LR(1) parser.

→ ∵ \cdot placed in any productions. Specifies to use reduce or shift operations.

$A \rightarrow \cdot XYZ$ } Shift operation

$A \rightarrow X \cdot YZ$

$A \rightarrow XY \cdot Z$ → reduce operation

→ LR parsers are powerful and we need LR grammar to implement this parser.

* LR is the superset of LL grammar.

* SIMPLE LR (SLR)

→ LR(K) item sets

→ LR parsing table

→ Parse string

* LR(0) item sets:

Let $G \rightarrow$ grammar.

$S \rightarrow$ start symbol.

* Convert grammar G to Augmented grammar G' .

→ We add $S \rightarrow S$ to G .

E → E + T
E → T
T → T * F
T → F
F → (E)
F → id.
E' → E

Original Grammar (G)
Augmented Grammar (G')

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* Given grammar:

$$G : \begin{array}{l} 1. E \rightarrow E + T \\ 2. E \rightarrow T \\ 3. T \rightarrow T * F \\ 4. T \rightarrow F \\ 5. F \rightarrow (E) \\ 6. F \rightarrow \text{id.} \end{array} \quad \left\{ \begin{array}{l} G : E \rightarrow E \\ G : T \rightarrow E \end{array} \right.$$

* Operations required for $LR(0)$ itemsets:

→ Closure

→ Goto: → used to move dot one symbol from #.

* Closure: checks if the `.` is placed before

and if it is before a non-terminal

and if it is before a non-terminal $T \rightarrow T$.
 i.e., in $\dots \vdash \text{production into the item sets.}$

Ex: Closure(I)

$$A \rightarrow x \cdot B \quad B$$

$$B \rightarrow \cdot y$$

~~for the grammar: $G = \{S \mid S \rightarrow \cdot x \cdot y\}$~~

Item Sets exists; it need not be included:

I₀

$$E' \rightarrow \cdot E$$

$$E \rightarrow \cdot E + T$$

$$E \rightarrow \cdot T$$

$$T \rightarrow \cdot T * F$$

$$T \rightarrow \cdot F$$

$$F \rightarrow \cdot (E)$$

$$F \rightarrow \cdot id$$

Adding the productions if the ' \cdot ' is before non-terminal and this process continues till no new item set is added.

$\overline{I_1} : \text{goto } (I_0, E)$ { Items from I_0 , where \therefore is before E
 $E \rightarrow E \cdot$
 $E \rightarrow E \cdot + T$
 $I_2 : \text{goto } (I_0, T)$ {
 $E \rightarrow T \cdot$
 $T \rightarrow T \cdot * F$
 $I_3 : \text{goto } (I_0, F)$
 $T \rightarrow F; F \rightarrow F \cdot$

$$\begin{aligned}
 I_4 &= \text{goto}(I_0, l) \quad | \quad I_5 : \text{goto}(I_0, \text{id}), \\
 &\quad F \rightarrow (\cdot E) \\
 &\quad E \rightarrow \cdot E + T \\
 &\quad E \rightarrow \cdot T \\
 &\quad T \rightarrow \cdot T * F \\
 &\quad T \rightarrow \cdot F \\
 &\quad F \rightarrow (\cdot E) \\
 &\quad F \rightarrow \cdot \text{id} \\
 &\quad F \rightarrow (\cdot \text{id}) \quad | \quad F \rightarrow \cdot \text{id}
 \end{aligned}$$

$$\begin{aligned}
 I_7 &= \text{goto}(I_2, *) \quad | \quad I_8 : \text{goto}(I_4, E) \\
 &\quad T \rightarrow T * \cdot F \\
 &\quad F \rightarrow (\cdot E) \\
 &\quad F \rightarrow \cdot \text{id}
 \end{aligned}$$

$$\begin{aligned}
 \text{goto}(I_4, T) &= I_2 \quad | \quad \text{goto}(I_4, \text{id}) = I_5 \\
 \text{goto}(I_4, F) &= I_3 \\
 \text{goto}(I_4, l) &= I_4
 \end{aligned}$$

** & items are equal iff all the items are equal.*

$$\begin{aligned}
 I_9 &= \text{goto}(I_6, T) \\
 E &\rightarrow E + T \\
 T &\rightarrow T * F
 \end{aligned}$$

$\text{goto}(I_6, F) = I_3$ Not to be written
 $\text{goto}(I_6, l) = I_4$
 $\text{goto}(I_6, \text{id}) = I_5$

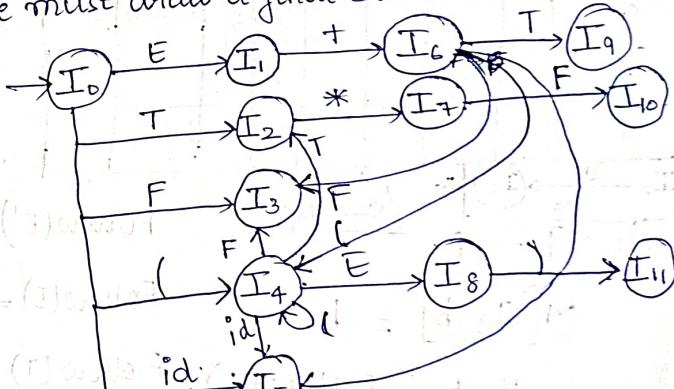
$$\begin{aligned}
 I_{10} &= \text{goto}(I_7, F) \quad | \quad I_{11} : \text{goto}(I_8, l) \\
 &\quad T \rightarrow T * F \\
 &\quad \text{goto}(I_7, l) = I_4 \\
 &\quad \text{goto}(I_7, \text{id}) = I_5
 \end{aligned}$$

$\text{goto}(I_8, 4) = I_6$
 $\text{goto}(I_9, *) = I_7$

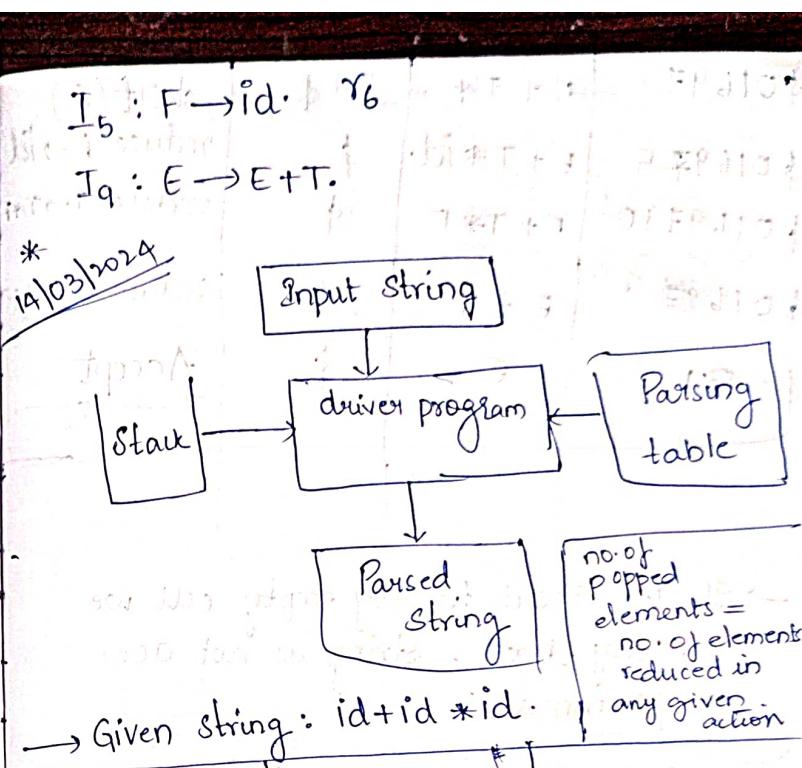
→ To check if the given productions are correct; we must check all the items contain each & every production with '•' at its right end.

$$\boxed{E \rightarrow E + T \cdot}$$

→ We must draw a finite state machine



| | | Action | | | | | | gotos | |
|----------------|----------------|----------------|----------------|----------------|-----------------|----------------|---|-------|----|
| Item acts | id | * | (|) | ? | \$ | E | T | F |
| 0 | S ₅ | | | S ₄ | | | 1 | 2 | |
| 1 | | S ₆ | | | | ACC | | | 3 |
| 2 | | S ₂ | S ₇ | | R ₂ | R ₂ | | | |
| 3 | | R ₄ | R ₄ | | R ₄ | R ₄ | | | |
| 4 | S ₅ | | | S ₄ | | | 8 | 2 | 3 |
| 5 | | R ₆ | R ₆ | | R ₆ | R ₆ | | | |
| 6 | S ₅ | | | S ₄ | | | | 9 | 3 |
| 7 | S ₅ | | | S ₄ | | | | | 10 |
| 8 | | S ₆ | | | S ₁₁ | | | | |
| 9 | | R ₁ | S ₇ | | R ₁ | R ₁ | | | |
| 10 | | R ₃ | R ₃ | | R ₃ | R ₃ | | | |
| 11 | | R ₅ | R ₅ | | R ₅ | R ₅ | | | |
| I ₀ | id | T | 1 | | | | | | |



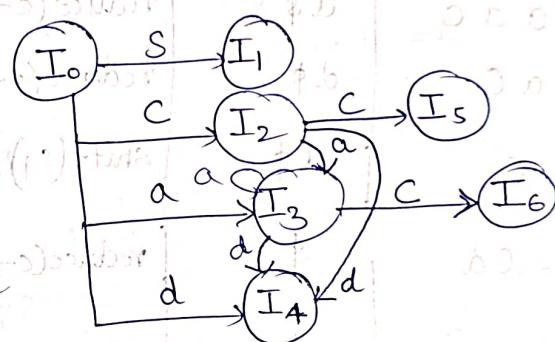
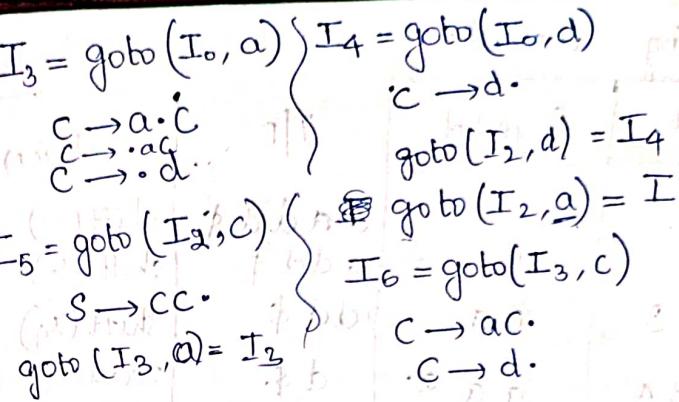
→ Given string: id + id * id

| Stack | Symbol | Input | Action |
|---------|--------|-----------------|---------------|
| \$ 0 | | id + id * id \$ | Shift (S5) |
| \$ 05 | id | + id * id \$ | reduce F → id |
| \$ 03 | F | + id * id \$ | reduce T → F |
| \$ 02 | T | + id * id \$ | reduce E → T |
| \$ 01 | E | + id * id \$ | shift (S6) |
| \$ 016 | E + | id * id \$ | shift (S5) |
| \$ 0165 | E + id | * id \$ | reduce F → id |
| \$ 0163 | E + F | * id \$ | reduce T → F |
| \$ 0169 | E + T | * id \$ | shift (S7) |

| | | | |
|------------|-----------------|-----------|---------------|
| \$01697 | E + T* | id \$: 61 | shift (S) |
| \$016975 | E + T* id. | \$ | reduce F |
| \$0169710) | E + <u>T* F</u> | \$ | reducer |
| \$016979 | E + T | \$ | reduce E |
| \$0169710 | E | \$ | <u>Accept</u> |

→ If we reach to any empty cell we can say that ; string is not acc. to grammar.

* $s \rightarrow cc$ }
 $c \rightarrow ac$ }
 $b \rightarrow c \rightarrow d$ }
 Agumented Grammar
 $G1 \rightarrow \underline{s} \rightarrow s$
 $\quad \quad \quad s \rightarrow cc$
 $\quad \quad \quad c \rightarrow ac$



| | a | d | \$ | S | C |
|---|-------|-------|-------|----|----|
| 0 | s_3 | s_4 | | 13 | 2 |
| 1 | | | Acc. | | |
| 2 | s_3 | s_4 | | | 5. |
| 3 | s_3 | s_4 | | 3 | 6 |
| 4 | r_3 | r_3 | r_3 | | |
| 5 | | | r_1 | | |

String (a add)

| Stack | Symbol | I/P | Action |
|------------|--------|----------|-------------------------------|
| \$ 0 | | a add \$ | shift (s_3) |
| \$ 0 3 | a | add \$ | shift (s_3) |
| \$ 0 3 . 3 | aa | dd \$ | shift (s_4) |
| \$ 0 3 3 4 | aa d. | d \$. | reduce ($C \rightarrow d$) |
| \$ 0 3 3 6 | aac | d \$ | reduce ($C \rightarrow a$) |
| \$ 0 3 6 | ac | d \$ | reduce ($C \rightarrow a$) |
| \$ 0 2 | c | d \$ | shift (s_4) |
| \$ 0 2 4 | cd | \$ | reduce ($C \rightarrow d$) |
| \$ 0 2 5 | cc | \$ | reduce ($S \rightarrow cc$) |
| \$ 0 1 | s | \$ | Accept Reduce |

$$1 S \rightarrow L = R$$

$$2 S \rightarrow R$$

$$3 L \rightarrow *R$$

$$4 L \rightarrow id$$

$$5 R \rightarrow L$$

Augmented Grammar

$$S' \rightarrow S$$

$$S \rightarrow L = R$$

$$L \rightarrow *R$$

$$L \rightarrow id$$

$$R \rightarrow L$$

$$S \rightarrow R$$

$$\text{First}(S) = \text{First}(L) = \{\ast, id\}$$

$$\text{First}(R) = \text{First}(L) = \{\ast, id\}$$

$$\text{Follow}(S) = \{\$\}$$

$$\text{Follow}(L) = \{=\}$$

$$\text{Follow}(R) = \{\ast, \$, =, id\}$$

$$I_0 =$$

$$S' \rightarrow S.$$

$$S \rightarrow \cdot R$$

$$S \rightarrow \cdot L = R$$

$$L \rightarrow \cdot \ast R$$

$$L \rightarrow \cdot id$$

$$R \rightarrow \cdot L$$

$$R \rightarrow \cdot$$

$$I_1 = \text{goto}(I_0, S)$$

$$S' \rightarrow S.$$

$$S \rightarrow \cdot$$

$$I_2 = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot = R$$

$$R \rightarrow L \cdot$$

$$I_3 = \text{goto}(I_0, \ast)$$

$$S \rightarrow \cdot R$$

$$R \rightarrow \cdot$$

$$I_4 = \text{goto}(I_0, id)$$

$$L \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_5 = \text{goto}(I_0, =)$$

$$S \rightarrow L = R \cdot$$

$$R \rightarrow \cdot$$

$$I_6 = \text{goto}(I_2, =)$$

$$S \rightarrow L = \cdot R$$

$$R \rightarrow \cdot$$

$$I_7 = \text{goto}(I_5, L)$$

$$S \rightarrow L \cdot = R$$

$$R \rightarrow L \cdot$$

$$I_8 = \text{goto}(I_3, R)$$

$$S \rightarrow \cdot R$$

$$R \rightarrow \cdot$$

$$I_9 = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{10} = \text{goto}(I_0, L)$$

$$S \rightarrow \cdot L$$

$$L \rightarrow \cdot$$

$$I_{11} = \text{goto}(I_0, id)$$

$$L \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_{12} = \text{goto}(I_0, \$)$$

$$S \rightarrow \cdot \$$$

$$\$ \rightarrow \cdot$$

$$I_{13} = \text{goto}(I_0, =)$$

$$S \rightarrow \cdot =$$

$$= \rightarrow \cdot$$

$$I_{14} = \text{goto}(I_0, *)$$

$$S \rightarrow \cdot *$$

$$* \rightarrow \cdot$$

$$I_{15} = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{16} = \text{goto}(I_0, S)$$

$$S \rightarrow S \cdot$$

$$S \rightarrow \cdot$$

$$I_{17} = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot$$

$$L \rightarrow \cdot$$

$$I_{18} = \text{goto}(I_0, id)$$

$$S \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_{19} = \text{goto}(I_0, *)$$

$$S \rightarrow * \cdot$$

$$* \rightarrow \cdot$$

$$I_{20} = \text{goto}(I_0, =)$$

$$S \rightarrow = \cdot$$

$$= \rightarrow \cdot$$

$$I_{21} = \text{goto}(I_0, \$)$$

$$S \rightarrow \$ \cdot$$

$$\$ \rightarrow \cdot$$

$$I_{22} = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{23} = \text{goto}(I_0, S)$$

$$S \rightarrow S \cdot$$

$$S \rightarrow \cdot$$

$$I_{24} = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot$$

$$L \rightarrow \cdot$$

$$I_{25} = \text{goto}(I_0, id)$$

$$S \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_{26} = \text{goto}(I_0, *)$$

$$S \rightarrow * \cdot$$

$$* \rightarrow \cdot$$

$$I_{27} = \text{goto}(I_0, =)$$

$$S \rightarrow = \cdot$$

$$= \rightarrow \cdot$$

$$I_{28} = \text{goto}(I_0, \$)$$

$$S \rightarrow \$ \cdot$$

$$\$ \rightarrow \cdot$$

$$I_{29} = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{30} = \text{goto}(I_0, S)$$

$$S \rightarrow S \cdot$$

$$S \rightarrow \cdot$$

$$I_{31} = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot$$

$$L \rightarrow \cdot$$

$$I_{32} = \text{goto}(I_0, id)$$

$$S \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_{33} = \text{goto}(I_0, *)$$

$$S \rightarrow * \cdot$$

$$* \rightarrow \cdot$$

$$I_{34} = \text{goto}(I_0, =)$$

$$S \rightarrow = \cdot$$

$$= \rightarrow \cdot$$

$$I_{35} = \text{goto}(I_0, \$)$$

$$S \rightarrow \$ \cdot$$

$$\$ \rightarrow \cdot$$

$$I_{36} = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{37} = \text{goto}(I_0, S)$$

$$S \rightarrow S \cdot$$

$$S \rightarrow \cdot$$

$$I_{38} = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot$$

$$L \rightarrow \cdot$$

$$I_{39} = \text{goto}(I_0, id)$$

$$S \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_{40} = \text{goto}(I_0, *)$$

$$S \rightarrow * \cdot$$

$$* \rightarrow \cdot$$

$$I_{41} = \text{goto}(I_0, =)$$

$$S \rightarrow = \cdot$$

$$= \rightarrow \cdot$$

$$I_{42} = \text{goto}(I_0, \$)$$

$$S \rightarrow \$ \cdot$$

$$\$ \rightarrow \cdot$$

$$I_{43} = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{44} = \text{goto}(I_0, S)$$

$$S \rightarrow S \cdot$$

$$S \rightarrow \cdot$$

$$I_{45} = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot$$

$$L \rightarrow \cdot$$

$$I_{46} = \text{goto}(I_0, id)$$

$$S \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_{47} = \text{goto}(I_0, *)$$

$$S \rightarrow * \cdot$$

$$* \rightarrow \cdot$$

$$I_{48} = \text{goto}(I_0, =)$$

$$S \rightarrow = \cdot$$

$$= \rightarrow \cdot$$

$$I_{49} = \text{goto}(I_0, \$)$$

$$S \rightarrow \$ \cdot$$

$$\$ \rightarrow \cdot$$

$$I_{50} = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{51} = \text{goto}(I_0, S)$$

$$S \rightarrow S \cdot$$

$$S \rightarrow \cdot$$

$$I_{52} = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot$$

$$L \rightarrow \cdot$$

$$I_{53} = \text{goto}(I_0, id)$$

$$S \rightarrow id \cdot$$

$$id \rightarrow \cdot$$

$$I_{54} = \text{goto}(I_0, *)$$

$$S \rightarrow * \cdot$$

$$* \rightarrow \cdot$$

$$I_{55} = \text{goto}(I_0, =)$$

$$S \rightarrow = \cdot$$

$$= \rightarrow \cdot$$

$$I_{56} = \text{goto}(I_0, \$)$$

$$S \rightarrow \$ \cdot$$

$$\$ \rightarrow \cdot$$

$$I_{57} = \text{goto}(I_0, R)$$

$$S \rightarrow R \cdot$$

$$R \rightarrow \cdot$$

$$I_{58} = \text{goto}(I_0, S)$$

$$S \rightarrow S \cdot$$

$$S \rightarrow \cdot$$

$$I_{59} = \text{goto}(I_0, L)$$

$$S \rightarrow L \cdot$$

$$L \rightarrow \cdot$$

$$I_{60} = \text{goto}(I_0, id)$$

$$S \rightarrow id \cdot$$

| | = | * | id | \$ | S | RL | R | L |
|---|---|---|----|----|---|----|----|---|
| 0 | | | | | 1 | 2 | 3 | |
| 1 | | | | | | | | |
| 2 | | | | | | | | |
| 3 | | | | | | 8 | 07 | |
| 4 | | | | | | | | |
| 5 | | | | | | 8 | 89 | |
| 6 | | | | | | | | |
| 7 | | | | | | | | |
| 8 | | | | | | | | |

∴ there is an ambiguity to choose between shift | reduce operation in cell (2, =)

* The demerits with SLR grammar are

- * is that, we expect next input using follow set which raises ambiguity in few cases.

* Checking for LL(1) grammar:

- * Not left recursive if debt recursive; remove left recursion.
- * if any production $A \rightarrow \alpha | \beta$

- * $\text{First}(\alpha) \cap \text{First}(\beta) = \emptyset$
- * if $A \rightarrow \alpha | \epsilon$
- * $\text{First}(\alpha) \cap \text{Follow}(A) = \emptyset$



→ The demerits in SLR is due to LR(0) item sets; which can be avoided using LR(1) item sets.

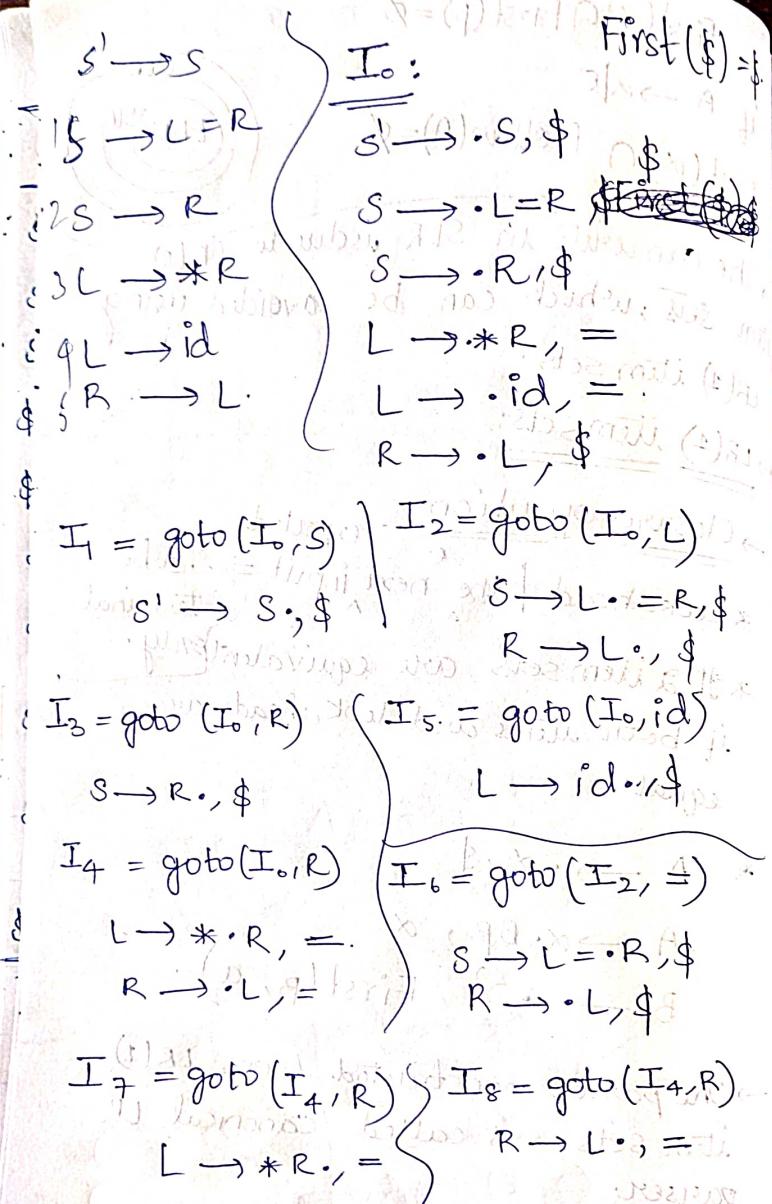
* LR(1) item sets:

→ Closure operation: expected

- * Lookahead | the next input \Rightarrow shd be a terminal
- * If 2 item sets are equivalent only if both items and lookahead are equal.

- * $(A \xrightarrow{\cdot} \cdot \alpha, \$)$, $(A \xrightarrow{\cdot} \cdot \alpha, B\beta, a)$
- * $A \xrightarrow{\cdot} \alpha \cdot B\beta, \alpha$
- * $B \xrightarrow{\cdot} \cdot \gamma, \text{First}(B, a)$

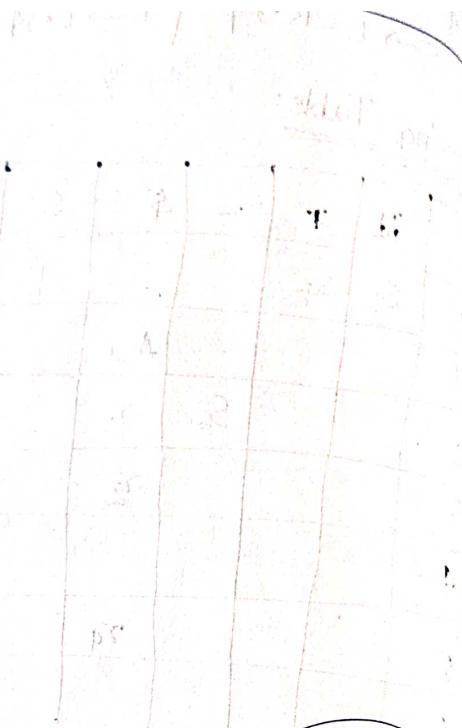
→ The parser constructed from LR(1) item sets is called canonical LR parser.



$$I_q = \text{goto}(I_b, R) \quad | \quad I_{10} = \text{goto}(I_a, L) \\ S \rightarrow L = R \cup \$ \quad | \quad R \rightarrow L \cup \$$$

* Parsing Table:

| | id | * | = | \$ | S | L | R |
|----|----------------|----------------|----------------|----------------|---|----|---|
| 0 | S ₅ | S ₄ | | | J | 2 | 3 |
| 1 | | | | Acc | | | |
| 2 | | | S ₆ | r ₅ | | | |
| 3 | | | | r ₂ | | | |
| 4 | | | | | | 8 | 7 |
| 5 | | | | r ₄ | | | |
| 6 | | | | | | 10 | 9 |
| 7 | | | r ₃ | | | | |
| 8 | | | r ₅ | | | | |
| 9 | | | | r ₁ | | | |
| 10 | | | | r ₅ | | | |



$$I_0: \begin{cases} S' \rightarrow \cdot S, \$ \\ S \rightarrow \cdot CC, \$ \\ S \rightarrow \cdot AC, ald \\ S \rightarrow \cdot d, ald \end{cases}$$

$$I_1: \text{goto}(I_0, S): \quad S' \rightarrow S \cdot, \$$$

$$I_2: \text{goto}(I_0, C): \quad S \rightarrow C \cdot C, \$$$

$$C \rightarrow \cdot d, \$$$

$$I_3: \text{goto}(I_0, a): \quad I_4: \text{goto}(I_0, d)$$

$$C \rightarrow a \cdot C, ald$$

$$C \rightarrow \cdot d, ald$$

$$C \rightarrow \cdot AC, ald$$

$$I_5: \text{goto}(I_2, C): \quad I_6: \text{goto}(I_2, a)$$

$$S \rightarrow CC \cdot \$$$

$$I_7: \text{goto}(I_2, d): \quad I_8: \text{goto}(I_3, C)$$

$$C \rightarrow d \cdot, \$$$

$$C \rightarrow \cdot AC, ald$$

$$I_9: \text{goto}(I_3, C): \quad C \rightarrow a \cdot C, \$$$

→ For LALR; if the item sets have same items; but having different look aheads; can be merged.

$$I_0: \begin{cases} S' \rightarrow \cdot S, \$ \\ S \rightarrow \cdot CC, \$ \\ S \rightarrow \cdot AC, ald \\ S \rightarrow \cdot d, ald \end{cases}$$

$$I_1: \text{goto}(I_0, S): \quad I_2: \text{goto}(I_0, C)$$

$$S' \rightarrow S \cdot, \$$$

$$S \rightarrow C \cdot C, \$$$

$$C \rightarrow \cdot AC, \$$$

$$C \rightarrow \cdot d, \$$$

$$I_{3G}: \begin{cases} C \rightarrow a \cdot C, ald, \$ \\ C \rightarrow \cdot AC, ald, \$ \\ C \rightarrow \cdot d, ald, \$ \end{cases}$$

$$I_{47}: \begin{cases} C \rightarrow d \cdot, ald, \$ \end{cases}$$

$$I_5: \quad S \rightarrow CC \cdot \$$$

$$I_{89}: \quad C \rightarrow AC \cdot, ald, \$$$

| | a | d | \$ | s | c | l |
|----|-----|-----|-----|---|----|--------------|
| 0 | S36 | S47 | | 1 | 2 | |
| 1 | | | ACC | | -5 | J (not diff) |
| 2 | S36 | S47 | | | 5 | |
| 36 | S36 | S47 | | | 89 | |
| 47 | r3 | r3 | r3 | | | |
| 5 | | | r1 | | | |
| 89 | r2 | r2 | r2 | | | |

Some word derivatives in : तेज़ रोके
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