

Data Preprocessing:-

→ The process of transforming raw data into an understandable format. eg:- Marks of students.
60 dm rank (a, b, c ---- 2) } The data is different
(90, 91, 92 ---- 100) } here.

→ Databases have noisy, missing and inconsistent data due to their huge size

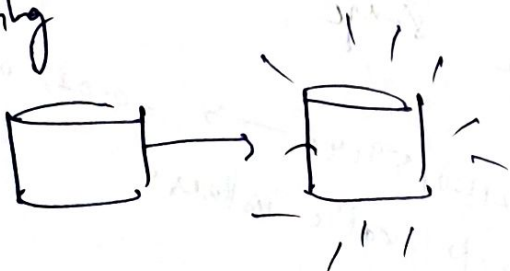
→ Low Quality data leads to low quality data-mining

→ Data pre-processing is used to improve the quality of data and Mining results.

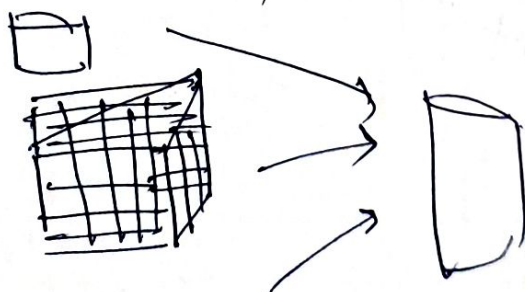
→ Various techniques like, data cleaning, data integration, data reduction, and data transformation are used in data pre-processing.

→ Steps in data pre-processing

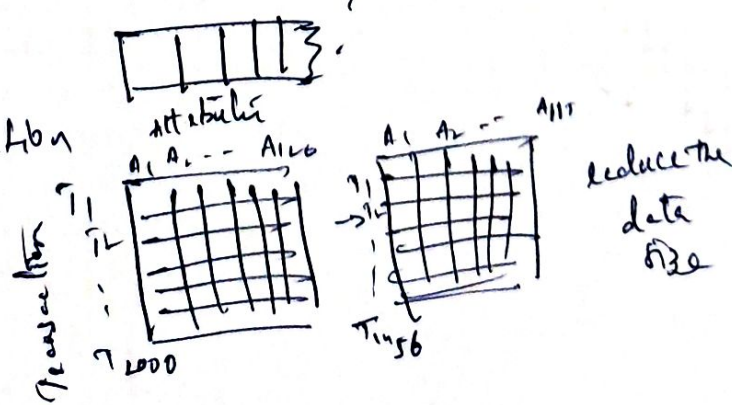
Data cleaning



Data Integration



Data reduction



1) Data cleaning :- is applied to remove noise and correct data. It fills missing values, smooths out noise while identifying outliers. Outliers :- "data points" if the data is not fitting into the main group. Other than type of data is called outliers.

2) Data Integration :- merges data from multiple sources into a single data source such as data warehouse which helps to reduce the redundant data. [Here reduce the redundancy data]

3) Data Reduction :- The size of data by using aggregation, clustering methods or by eliminating redundant data.

4) Data Transformation :- Data is scaled to fall within a smaller range like $1.0 \rightarrow 0.0$

Eg: $-2, 32, 100, 59, 48 \rightarrow -0.02, 0.32, 1.00, 0.59, 0.48$
Convert into smaller values.

②

Data cleaning :-
 Data cleaning (or data cleansing) routines attempt to fill in missing values, smooth out noise while identifying outliers, and correct inconsistencies in the data.

⇒ Approaches in data cleaning :-

1. Missing values.
2. Noisy data.

1. Missing values :-

- i) Ignore the tuple.
- ii) Fill in the missing values manually.
- iii) Use a global constant to fill in the missing values eg (NA)
- iv) Use a measure of central tendency for the attribute (e.g. the mean or median) to fill in the missing value.
- v) Use the most probable value to fill in the missing value (e.g. using a decision tree)

2) Noisy data :-

Noise is a random error or variance in a measured variable.

Approaches in Noisy data :-

- i) Binning
- ii) Regression
- iii) Outlier analysis.

Ex:- 6, 10, 17, 22, 22, 25, 27, 30, 36 [9 values numeric]
partition into equal frequency bins :-

Bin 1: 6, 10, 17
 Bin 2: 22, 22, 25
 Bin 3: 27, 30, 36.
Smoothing by bin Mean's

Bin 1: 11, 11, 11
 Bin 2: 23, 23, 23
 Bin 3: 31, 31, 31.
Smoothing by bin boundaries

Bin 1: 6, 17
 Bin 2: 22, 25
 Bin 3: 27, 36.

$$\frac{6+10+17}{3} = \frac{33}{3} = 11$$

$$\frac{22+22+25}{3} = \frac{69}{3} = 23$$

$$\frac{27+30+36}{3} = \frac{93}{3} = 31$$

ii) Regression :-

⇒ Linear Regression involves finding the "best" line to fit two attributes (variables) so that one attribute can be used to predict the other.
⇒ Multiple Linear Regression :- is an extension of linear regression, where more than two attributes are involved and the data are fit to a multidimensional surface.

iii) Outlier analysis :-

Outliers may be detected by clustering,
for eg:- where similar values are organized into groups, or "clusters".
Intuitively, values that fall outside of the set of clusters may be considered outliers.

Data Integration in data pre-processing
 → Merging of data collected from multiple sources. Careful integration can help reduce redundancies and inconsistencies in the resulting dataset.

Approaches in Data Integration:

1. Entity Identification and Correlation analysis.
2. Redundancy and Tuple Duplication.
3. Data value conflict Detection and Resolution.
4. Entity Identification problem

⇒ 1. Correlation coefficient is for the Numeric data.

How two attributes are strongly related each other with the availability of attribute

$$r_{A,B} = \frac{\sum_{i=1}^n (a_i - \bar{A})(b_i - \bar{B})}{(n-1) \sigma_A \sigma_B}$$

$$= \frac{\sum_{i=1}^n (a_i b_i) - n \bar{A} \bar{B}}{(n-1) \sigma_A \sigma_B}$$

1) $r_{A,B} > 0$; A, B are positively "correlated".

2) $r_{A,B} = 0$ independent

3) $r_{A,B} < 0$; both are negatively correlated.

A ↑ increase B ↓ like vice versa

→ Avoiding the eliminating the redundancy.

2. Correlation Analysis (Nominal Data)

- * For the nominal data, a relationship between the two attributes "A" and "B" can be discovered by χ^2 .
- $A \rightarrow c$ distinct values, a_1, a_2, \dots, a_c .
- $B \rightarrow r$ distinct values, b_1, b_2, \dots, b_r .
- $\Rightarrow A$ & B are values are shown as "Contingency table".
- \Rightarrow With the c values of A making up the columns and the r values of B making up "the rows".
- \Rightarrow Let (A_i, B_j) denote the joint event that attribute 'A' takes on value a_i and attribute B takes on value b_j .

Where $(A = a_i, B = b_j)$

$$\chi^2 (\text{chi-square}) = \sum_{i=1}^c \sum_{j=1}^r \frac{(\text{observed} - \text{expected})^2}{\text{expected}}$$

$$\chi^2 = \sum_{i=1}^c \sum_{j=1}^r \frac{(o_{ij} - e_{ij})^2}{e_{ij}}$$

Contingency table

	Male	Female	Sum (row)
Like Science fiction	250 (90)	200 (360)	450
Not like it	50 (210)	1000 (240)	1050
Sum	300	1200	1500

using Eq (3.2) we can verify the expected frequency for each cell

eg:- expected frequency for the cell (male fiction) is

$$E_{11} = \frac{\text{Count (male)} \times \text{Count (fiction)}}{n}$$

$$= \frac{300 \times 450}{1500} = 90$$

4 cells values

$$\chi^2 = \frac{(250-90)^2}{90} + \frac{(50-210)^2}{210} + \frac{(200-360)^2}{360} + \frac{(1000-840)^2}{840} = 507.91$$

degree of freedom are $(2-1)(2-1) = 1$

⇒ Covariance of Numeric data :

* Measures how much two numeric attributes A & B change together

* For n observations $(a_1, b_1), (a_2, b_2) \dots (a_n, b_n)$ the

Covariance between A & B is $(-1 \text{ to } +)$
 Where \bar{A} & \bar{B} are the mean values of A & B.

$$\begin{aligned} \text{Cov}(A, B) &= E(A - \bar{A})(B - \bar{B}) \\ &= \frac{\sum_{i=1}^n (a_i - \bar{A})(b_i - \bar{B})}{n} = \sigma_A \sigma_B \end{aligned}$$

⇒ The correlation coefficient $r_{A, B}$ is related to covariance by

$$r_{A, B} = \frac{\text{Cov}(A, B)}{\sigma_A \sigma_B}$$

→ Positive Covariance :- If A & B tend to change together in the same direction (both increase or decrease) (their covariance is positive)

→ Negative Covariance :- If A & B tends to change in opposite direction (one ↑ while the other decreases).
 Their covariance is negative.

→ Zero Covariance :- If A & B are independent, their covariance is zero.

All electronics $\rightarrow 6, 7, 4, 3, 2$

High Tech $\rightarrow 20, 10, 14, 5, 7$

Mean value = $\bar{A} = \frac{6+7+4+3+2}{5} = 4$

Mean value $\bar{B} = \frac{20+10+14+7+7}{5} = 10.8$

Covariance: $\text{Cov}(A, B) = \sum_{i=1}^n (a_i - \bar{A})(b_i - \bar{B})$

$$= \frac{(6-4)(20-10.8) + (7-4)(10-10.8) + (4-4)(14-10.8) + (3-4)(5-10.8) + (2-4)(7-10.8)}{5}$$

p. of covary. (-1 to 1)

The positive co-variance indicator that the stock prices for both companies tend to increase together.

⇒ Data Reduction in preprocessing ^{data} :

* Data reduction techniques can be applied to obtain a reduced representation of the data set that is much smaller in volume.

⇒ Mining on the reduced data set should be more efficient yet produce the same (or almost the same) analytical results.

⇒ Methods of data Reduction :

1. Dimensionality reduction
2. Numerosity reduction
3. Data Compression.

1. "Dimensionality reduction" :

⇒ DR is the process of reducing the number of random variables or attributes under consideration.

⇒ "It eliminates the redundant attributes" which are

weakly important across the data .

eg:

① DOB	② age
└──┬──┘	

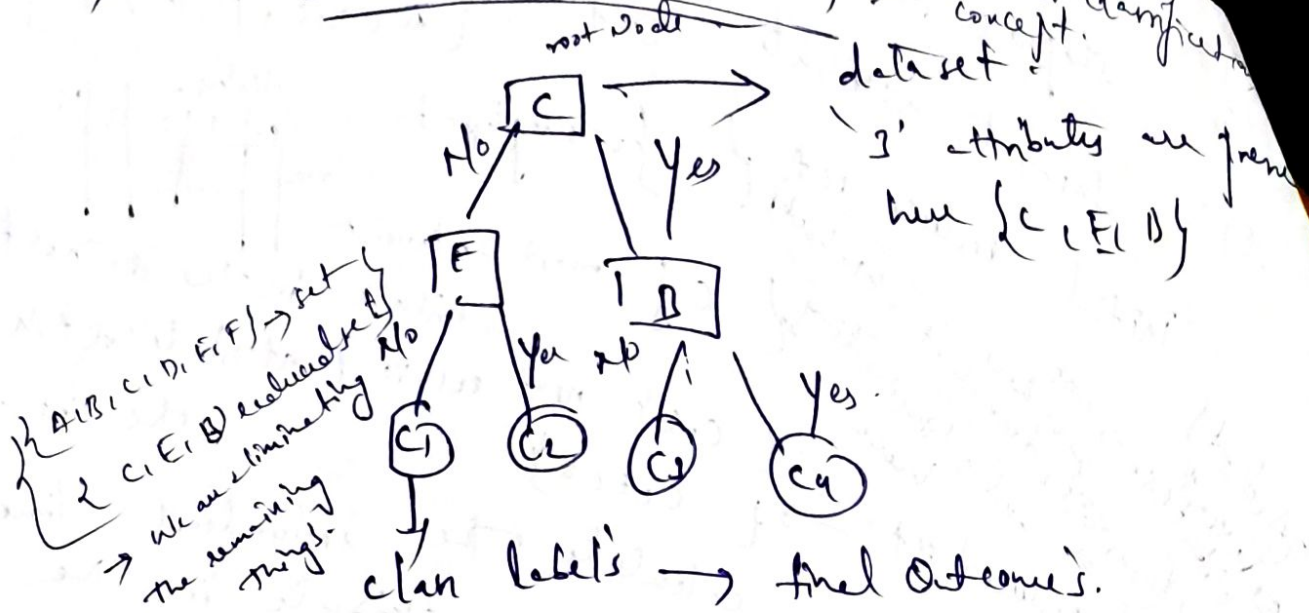
└──┬──┘ present is hard to say.
└──┬──┘ redundant attribute here age

↓
like we are storing the age here so it is called as redundant attribute.

- ① Stepwise forward selection.
- ② Stepwise backward elimination.
- ③ Decision tree induction.

iii)

Decision tree Inductivity :- This is classification concept.



2. 'Numerosity Reduction'

=> Replaces the original data with small form of data representation. There are two methods

Parametric and non-parametric reduction.

1. parametric method: Used to estimate the data, so that only parameters of data are required to be stored, instead of actual data.

a) Regression: Simple linear regression (to fit in a straight line)

multiple linear regression [with 2 or more predictor variables]
 $(y = ax + b)$
 by Long

Long - Linear model

Used to estimate the probability of each data point in a multidimensional space for a set of discretized attributes, based on a smaller subset of dimensional combinations.

$$\log(g) = \text{int} b$$

→ This allows a higher-dimensional data space to be constructed from lower-dimensional attribute.

2. ~~Parametric~~ Non-Parametric Method
Used to store reduced representation of the data. It includes.

- Histograms.
- Clustering.
- Sampling
- Data cube aggregation.

3. Data Compression

Reduce the size of the files using different "encoding mechanisms". There are 2 types.

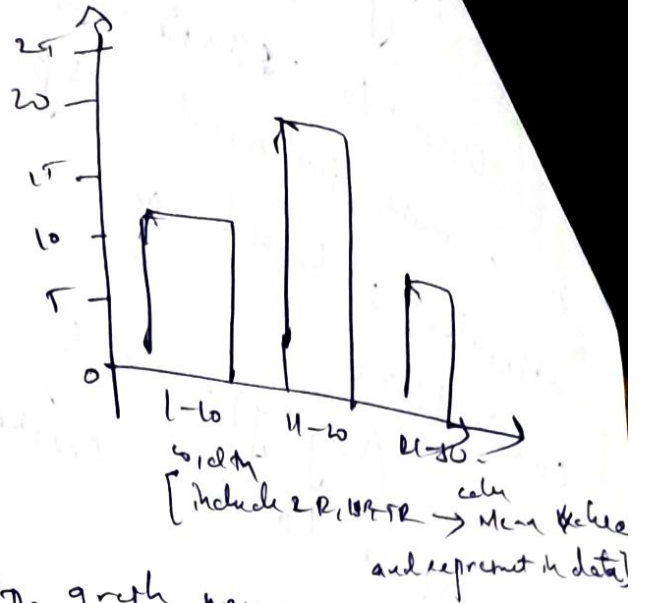
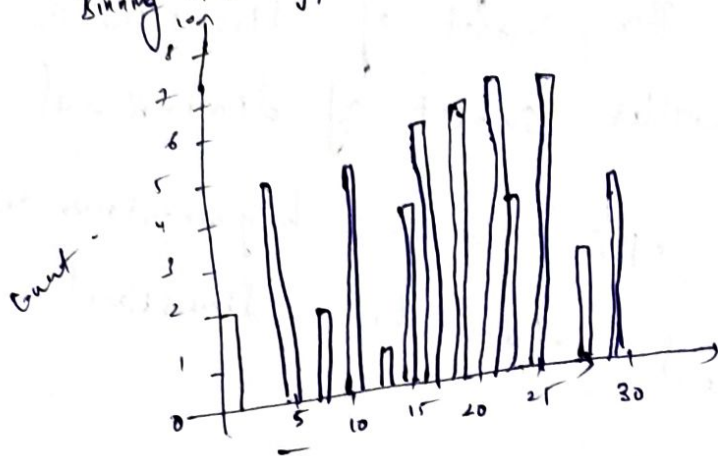
i) Lossless compression :- without loss after compression.

ii) Lossy compression :- The decompressed data may differ to the original data, but are useful enough to retrieve information from them. They are.

- Discrete Wavelet Transforms.
- Principal Component Analysis.

⇒ a) Histograms :-

Binning to approximate data distributions.



⇒ Band on the data we have display in the graph manner.

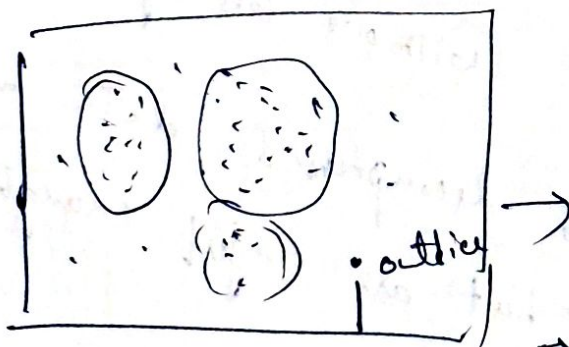
⇒ before we construct the Equal width in the above histogram.

⇒ {0, 5, 10, 15, 20, 25, 30} → we have equal unit price [0-10]
 unit price → equal width we have to dividing the data into
 equal frequency

⇒ Equal frequency is three, 1st price item, 2nd price item, 3rd price item } frequency based.

b) Clustering :-

partitions the whole data into different clusters. Centroid distance is an alternative measure of cluster quality and is defined as the average distance of each cluster object from the cluster centroid.



When we clustering the object some data is missing here at that time (ignoring the unimportant data).
 (group) → outlier eliminated by cluster
 value data reduce variance