

22/09/2022

* STEPPER MOTORS:

→ Rotor moves in discrete steps.

Types of motors:

1) Variable Resistance type (VR)

2) Permanent magnet type (PM)

3) Hybrid type, a combination of VR & PM

⇒ VARIABLE RELUCTANCE(VR) TYPE STEPPER MOTOR

• property of flux lines to occupy low reluctance path.

• Therefore, stator and rotor should be aligned such that magnetic reluctance is minimum.

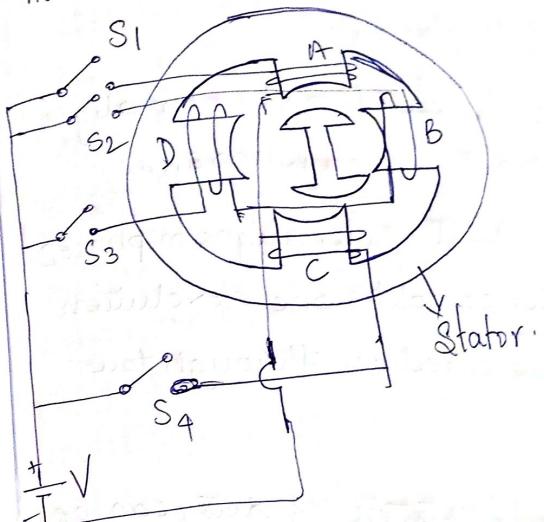
• Stator has connected windings placed over the stator poles.

• Rotor carries no windings.

• Stator and Rotor are made up of high quality magnetic materials that have high permeability.

• Stator phases are excited in a proper sequence from a DC source using semi-conductor switches; there is a magnetic field generated.

• Rotor occupies the position which presents minimum reluctance to the stator field.



→ It is 4 phase 4/2 pole (4 poles in stator & 2 poles in rotor)
single stack variable reluctance stepper motor.

→ Four phases A, B, C, D are connected to DC source with the help of semi conductor switches S_A, S_B, S_C, S_D.

→ Phase windings are energised in sequence.

$$A \rightarrow B \rightarrow C \rightarrow D \rightarrow A$$

* A is excited; rotor aligns its position to the axis of phase A and cannot move until phase A is de-energised.

* Switch off S_A and on S_B; where rotor moves 90° in clockwise and aligns itself to phase B.

* Further C is excited and rotor aligns itself to phase C and when S_D is on and S_C is off; rotor aligns to phase D.
* In this rotor completes one revolution in clockwise direction through four steps -

* The direction of rotation of rotor can be reversed by reversing the sequence of switches i.e. A D B B A

* Direction of rotation depends only on sequence of switching the phase & independent of direction of current.

magnitude of step angle

$$\alpha = \frac{360^\circ}{m_s N_r}$$

$\alpha \rightarrow$ step angle

$m_s \rightarrow$ no. of stator phases

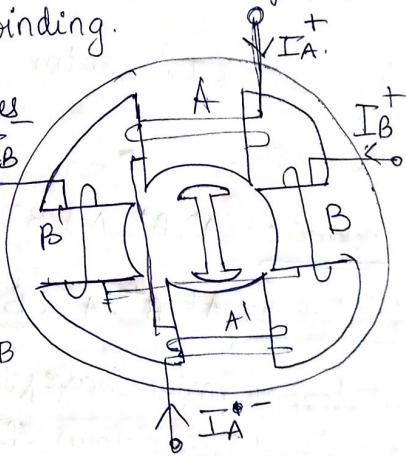
$N_r \rightarrow$ no. of rotor teeth poles

PERMANENT MAGNET (PM) STEPPER MOTOR:

- Rotor is cylindrical and consists of permanent magnet poles made of high retentivity steel.
- The concentrated winding on diametrically opposite poles are connected in series to form 2 phase winding on stator poles
- Rotor poles align with stator, depending on excitation of phase winding.

A-A' connected in series to form phase A winding.

B-B' connected in series to form phase B winding.



When I_A⁺ passes through phase A winding, South pole of rotor is attracted by the stator so that magnetic axes of the stator & rotor coincide $\alpha = 0^\circ$.

$$\alpha = 0^\circ$$

If current flows only in phase B winding
rotor poles are attracted by stator &
rotor moves by 90° & in clockwise direction
 $\alpha = 90^\circ \Rightarrow I_B^+$

If current is I_A^- ; rotor moves further
by 90° i.e. $\alpha = 180^\circ$

If current is I_B^- ; rotor moves further by
 90° i.e. $\alpha = 270^\circ$

If current is I_A^+ rotor moves by 90° &
 $\alpha = 360^\circ$

Clockwise: $A^+, B^+, A^-, B^-, A^+ \dots$

Anticlockwise: $A^+, B^-, A^-, B^+, A^+ \dots$

PM stepper motor have higher inertia
& low acceleration than VR stepper motors.

* Brushless DC Motor:

- runs on DC source but don't have brushes
and commutator.

- Superior efficiency, long life, smooth torque
delivery and high speed operation.

DC motor have excessive sparking and brush
wear.

∴ No brushes in BLDC: no sparking &
no brush wear and no need of
replacement of brushes.

* Components of BLDC:

- 1) permanent magnet rotor
- 2) Stator with 3-4 phase windings
- 3) rotor position sensor.
- 4) electric circuit to control phase of rotor windings

* Working of BLDC:

- A BLDC motor functions by energizing one stator
coil at a time using const. DC voltage.

- When coil is turned on it produces a stator
magnetic field (B_s) and torque $T = k B_r \times B_s$

- aligns rotor with stator magnetic field.

$B_r \rightarrow$ stator magnetic field points up producing
a counter clockwise torque on rotor.

- Therefore, rotor turns left.

* The key to the operation of a BLDC motor
is that, it includes a position sensor.
So that control will know when rotor is

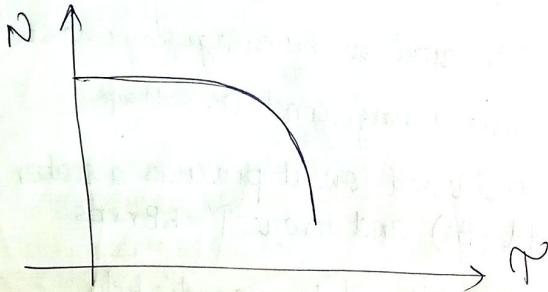
almost aligned with stator magnetic field.

* position sensor is used to switch the energized stator coil, when rotor is almost aligned; keeping the rotor rotating & speed set by control electronics.

→ Salient pole rotors: / projected pole:

application with speeds from 100 to 1500 rpm.

→ Non salient pole rotors → application at higher speeds: $1500 \text{ rpm}^{\text{tab}}$



* 3 phase induction Motor:

Components:

Frame

Stator

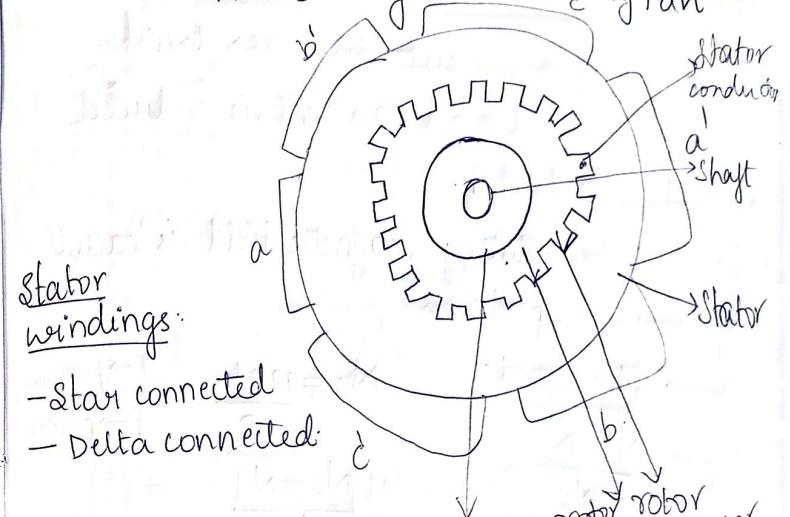
Stator winding

Rotor

Rotor winding

Cooling fan
Bearings

- Frame → mechanical support to both stator & rotor.
- Stator → stationary part of induction motor.
- Rotor →
 - Driving end → mechanical load
 - Non-Driving end → cooling fan.



Rotor Windings:

wound as rotor bars &
short circuited at both ends.

Types:

Squirrel Cage:

- Laminated cylindrical core and consists of parallel slots joined at each end using end rings.

Slip-Ring:

{ Laminated cylindrical core and carries a 3-phase winding.
- star connected rotor windings whose open ends are brought together using slip rings.

Working:

* A Rotating Magnetic field is set up in the stator when a 3-phase supply is given.

* Stationary rotor cuts the revolving magnetic field and an emf is induced in rotor conductor.

* Speed of the rotating magnetic field is called synchronous speed (N_s)

$N \rightarrow$ rotor speed.

$$N_s = \frac{120f}{P} \quad f \rightarrow \text{frequency}$$

P → poles.

$$\text{slip} = \frac{N_s - N}{N_s}$$

$$\therefore N_s = N$$

$$\phi_R = \phi_m \sin \omega t$$

$$\phi_B = \phi_m \sin(\omega t - 120^\circ)$$

$$\phi_Y = \phi_m \sin(\omega t - 240^\circ)$$

$$\phi_X = \phi_R - \phi_B \cos 60^\circ$$

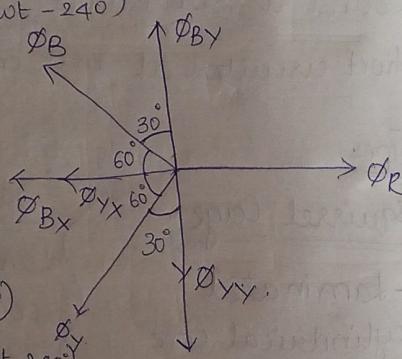
$$- \phi_Y \cos 60^\circ$$

$$\phi_Y = \phi_B \cos 30^\circ$$

$$- \phi_Y \cos 30^\circ$$

$$\phi_X = \phi_R - \frac{\phi_m}{2} \left[\sin(\omega t - 120^\circ) + \sin(\omega t - 240^\circ) \right]$$

$$\phi_X = \phi_m \left[\sin \omega t - \frac{1}{2} \left[\sin \omega t \left(-\frac{1}{2} \right) - \cos \omega t \frac{\sqrt{3}}{2} \right] + \sin \omega t \left(-\frac{1}{2} \right) - \cos \omega t \left(-\frac{\sqrt{3}}{2} \right) \right]$$



$$\phi_X = \phi_m \left[\sin \omega t + \frac{1}{2} [\sin \omega t] \right] = \frac{3}{2} \phi_m \sin \omega t$$

$$\boxed{\phi_X = \frac{3}{2} \phi_m \sin \omega t}$$

$$\phi_Y = \frac{\sqrt{3}}{2} [\phi_m \sin(\omega t - 120^\circ) - \phi_m \sin(\omega t - 240^\circ)]$$

$$= \frac{\sqrt{3}}{2} \phi_m \left[\sin \omega t \left(-\frac{1}{2} \right) - \cos \omega t \left(\frac{\sqrt{3}}{2} \right) + \sin \omega t \left(\frac{1}{2} \right) + \cos \omega t \left(-\frac{\sqrt{3}}{2} \right) \right]$$

$$= \frac{\sqrt{3}}{2} \phi_m (+\sqrt{3} \cos \omega t) = \frac{3}{2} \phi_m \cos \omega t$$

$$\boxed{\phi_Y = \frac{3}{2} \phi_m \cos \omega t}$$

$$\phi_R = \frac{3}{2} \phi_m$$

$$\tan \theta = \frac{E_2 r}{R_2} =$$

$$\phi_R = \frac{\pi}{2} - \theta$$

* Effect of slip on various rotor parameters:

- rotor frequency

$$f_{2r} = S f_2$$

- rotor induced emf

$$E_{2r} = S E_2$$

$$Z_{2r} = \sqrt{R_2^2 + (Sx_2)^2}$$

- rotor reactance

$$X_{2r} = S X_2$$

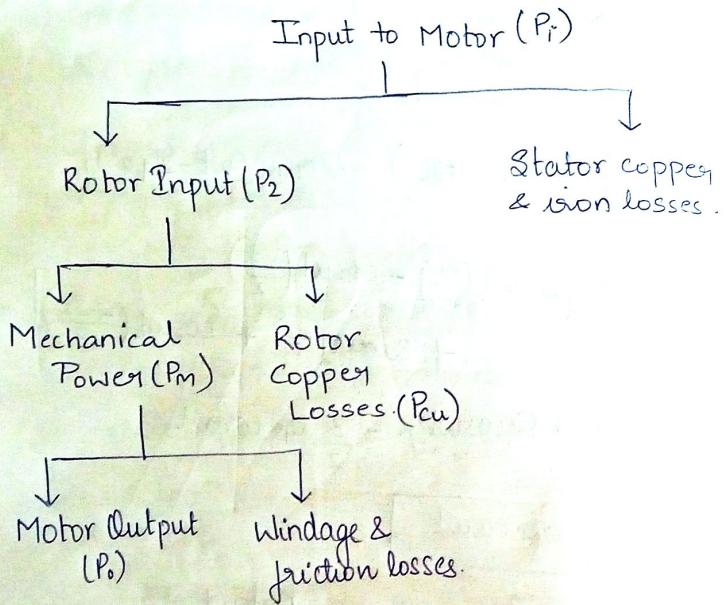
- Rotor power factor

$$\cos \phi_{2r} = \frac{R_2}{\sqrt{R_2^2 + (Sx_2)^2}}$$

- Rotor current

$$I_{2r} = S E_2 / \sqrt{R_2^2 + (Sx_2)^2}$$

* Power Stages:



* Relation b/w rotor copper loss & rotor power:

$$P_2 = \omega_s T_d \quad | \quad P_{in} = \omega_r T_d = P_m \\ = \frac{2\pi N_s}{60} T_d \quad | \quad = \frac{2\pi N}{60} T_d.$$

$$P_{cu} = P_2 - P_m.$$

$$P_{cu} = \frac{2\pi}{60} T_d (N_s - N)$$

$$\frac{P_m}{P_2} = \frac{N}{N_s}$$

$$\frac{P_{cu}}{P_2} = \frac{N_s - N}{N_s} = \frac{sN}{N}$$

$$\frac{P_{cu}}{P_m} = \frac{N_s - N}{N} = \frac{sN}{N}$$

$$\left(\frac{P_m}{P_{cu}} = \frac{1-s}{s} \right)$$

$$P_2 : P_m : P_{cu} = 1 : (1-s) : s$$

* Torque in an induction motor:

$$P = 3E_2 r I_2 r \cos \phi / 2\pi$$

$$= 3E_2 r \cdot \frac{E_2 r}{Z_2 r} \cdot \frac{R_2}{\sqrt{R_2^2 + (S \times Z_2)^2}}$$

$$P = \frac{3 E_2^2 R_2 S^2}{R_2^2 + (S \times Z_2)^2}$$

$I^2 R$ losses:

$$\text{input power to rotor} = \frac{2\pi N_s T_d}{60}$$

$S \times \text{rotor input} = \text{rotor copper loss.}$

$$S \times \frac{2\pi N_s T_d}{60} = 3 \left(\frac{E_2^2 S^2}{R_2^2 + S^2 \times Z_2^2} \right) R_2$$

$$T_d = \frac{K S E_2^2 R_2}{R_2^2 + S^2 \times Z_2^2}$$

* Torque Slip characteristics:

$$T_d = \frac{S R_2}{R_2^2 + (S \times Z_2)^2}$$

Low slip region:

$$R_2^2 \gg (s \times 2)^2$$

$$R_2^2 + (s \times 2)^2 = R_2^2$$

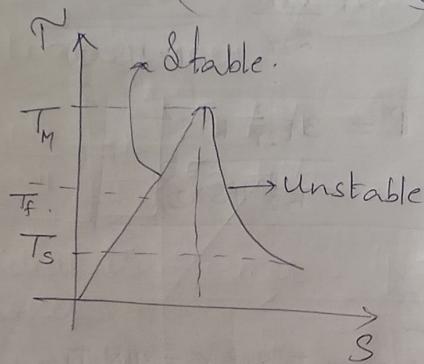
$$T_d \propto s$$

High slip region:

$$(s \times 2)^2 \gg R_2^2$$

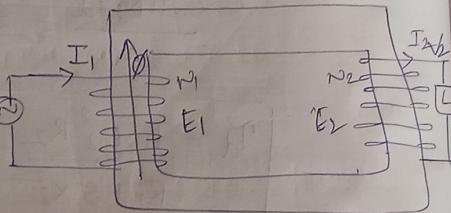
$$R_2^2 + (s \times 2)^2 \approx (s \times 2)^2$$

$$T_d \propto \frac{1}{s}$$



* TRANSFORMERS :

winding connected to load \rightarrow secondary winding connected to AC source \rightarrow primary.



$V_2 > V_1 \rightarrow$ step-up transformer

$V_1 > V_2 \rightarrow$ step-down transformer

When an alternating emf V_1 is applied to transformer to the primary winding and flux is developed in the coil.

This flux links both the windings & induces emfs E_1 & E_2

where $E_1 = -N_1 \frac{d\phi}{dt}$

$$E_2 = -N_2 \frac{d\phi}{dt}$$

$$\frac{E_1}{E_2} = \frac{N_1}{N_2}$$

- Electromagnetic Induction : flux remains constant in both windings
- Losses in transformer:
 - core losses \Rightarrow eddy current & hysteresis loss
 - copper losses \Rightarrow resistance of windings.

* Ideal Transformer:

- (i) no winding resistance.
- (ii) no leakage flux.
- (iii) no iron losses in the core.

* EMF Equation of a transformer:

$$\phi = \phi_M \sin \omega t$$

$$e_1 = -N_1 \frac{d\phi}{dt} = -N_1 \frac{d}{dt} (\phi_M \sin \omega t)$$

$$= -N_1 \phi_M \omega \cos \omega t$$

$$= 2\pi f N_1 \phi_M \sin(\omega t - 90^\circ)$$

$$E_{M1} = 2\pi f N_1 \phi_M$$

$$E_1 = \frac{E_{M1}}{r_2} = \frac{2\pi f N_1 \phi_M}{r_2}$$

$$E_2 = 4.44 f N_2 \phi_M$$

$$E_1 = 4.44 f N_1 \phi_M$$

* Voltage Transformation Ratio (K)

$$K = \frac{V_2}{V_1} = \frac{E_2}{E_1} = \frac{N_2}{N_1} \Rightarrow \text{Ideal Transformer}$$

$E_1 = V_1, E_2 = V_2$

for any transformer

$$\left[\frac{E_2}{E_1} = \frac{N_2}{N_1} = K \right] \begin{matrix} : E_1 \neq V_1 \\ E_2 \neq V_2 \end{matrix}$$

In an ideal transformer - if there are no losses

$$V_1 I_1 = V_2 I_2$$

$$\left[\frac{V_1}{V_2} = \frac{I_2}{I_1} = \frac{1}{K} \right]$$

* Practical Transformer and its losses:

(i) Iron losses:

Alternating flux in iron core; where eddy current & hysteresis loss occur.

Iron losses depend on magnetic flux density, supply frequency etc.

(ii) Winding Resistances:

Being made up of copper, the windings

too generate a ~~loss~~ power loss ($I^2 R$)

(iii) Leakage Reactances:

The flux generated in the coil is called a mutual flux since it joins both primary & secondary coils.

- primary current produces flux ϕ_1

- secondary current produces flux ϕ_2

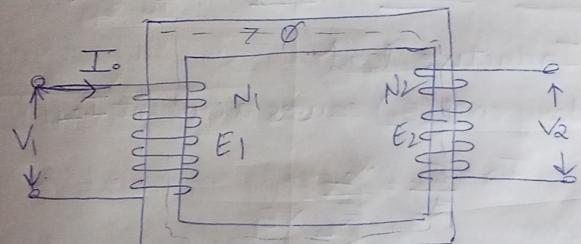
where these ϕ_1/ϕ_2 link only one winding; either primary or secondary ~~coil~~ respectively.

These flux ϕ_1 and ϕ_2 are called leakage flux.

: primary leakage flux ϕ_1 introduces inductive reactance X_1 and secondary leakage flux ϕ_2 , introduces inductive reactance X_2 .

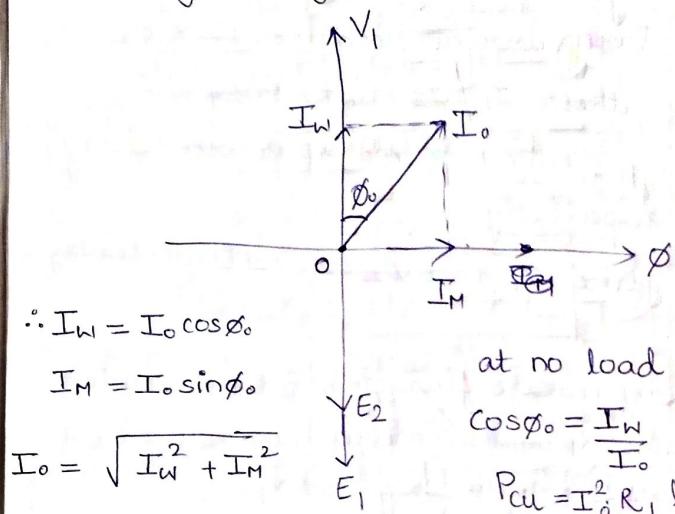
* Practical Transformer on no load:

No load \Rightarrow Secondary is open circuited.



Only a current I_o flows in primary circuit where this I_o is divided among I_w (iron loss component) & I_M (magnetising component).

$\therefore I_o$ lags V_1 by angle $\phi_o < 90^\circ$



* Ideal Transformer On load:

$Z_L \rightarrow$ Inductive load.

Secondary emf (E_2) causes a current I_2

$$I_2 = \frac{E_2}{Z_L} = \frac{V_2}{Z_L}$$

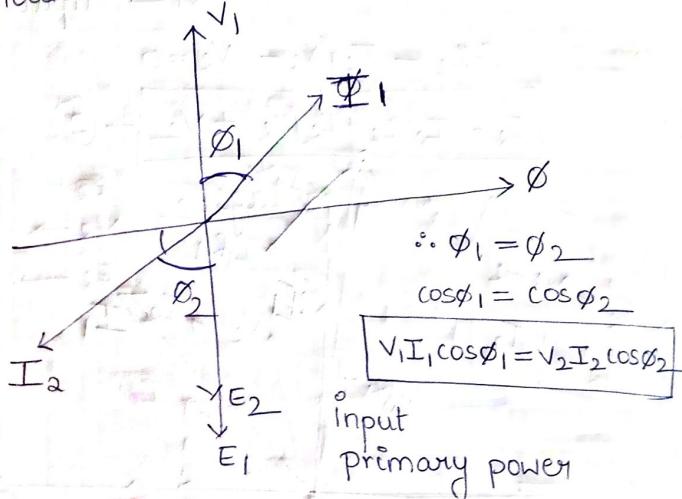
\therefore Inductive load I_2 lags V_2

\therefore flux in the coil should remain constant
 \therefore current I_1 in primary should be:

$$N_1 I_1 = N_2 I_2$$

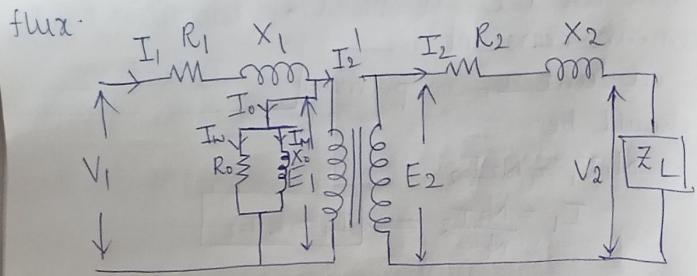
$$I_1 = \frac{N_2}{N_1} I_2 \Rightarrow I_1 = K I_2$$

\Rightarrow Primary must draw enough current to neutralise the demagnetising effect of secondary current so that mutual flux remains constant.



* Practical Transformer on ~~no~~ load power with resistance & leakage reactance.

Primary current I_1 being divided as
 $I_o \rightarrow$ for iron loss & magnetising loss
 $I_1' \rightarrow$ demagnetise the effect of secondary



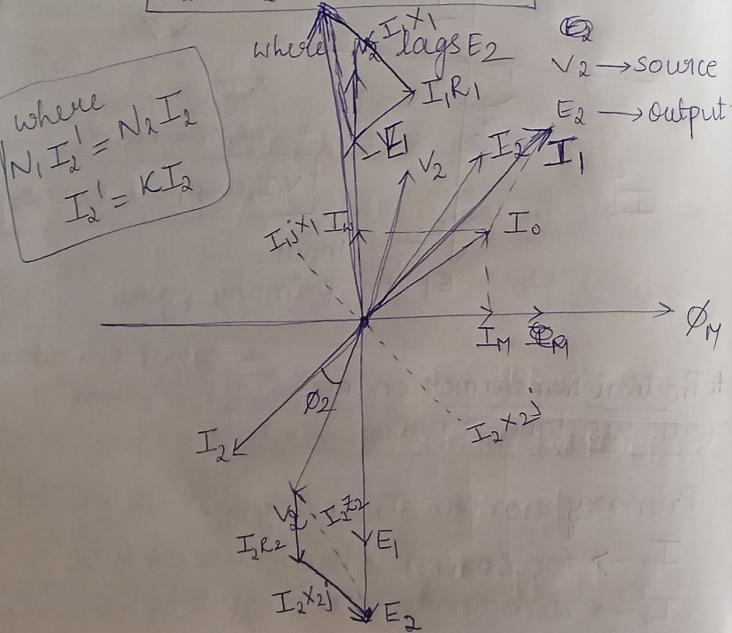
$$V_1 - I_1 R_1 - I_1 j X_1 - E_1 = 0$$

$$V_1 = I_1 R_1 + I_1 j X_1 + E_1 \quad \text{--- (1)}$$

where E_1 lags V_1 $E_1 \rightarrow$ source
 $v_1 \rightarrow$ output

$$E_2 - I_2 R_2 - I_2 j X_2 - V_2 = 0$$

$$E_2 = I_2 R_2 + I_2 j X_2 + V_2 \quad \text{--- (2)}$$



Impedance ratio:

$$Z_2 = \frac{V_2}{I_2} \quad Z_1 = \frac{V_1}{I_1}$$

$$\frac{Z_2}{Z_1} = \frac{V_2}{I_2} \times \frac{I_1}{V_1} = K \cdot K = K^2$$

* Shifting Impedances in transformer:

* Primary to secondary reference:

∴ primary has high resistance & reactance.

∴ when these are referred to secondary

$$R_1 = \cancel{R_1} \quad R_{02} = R_2 + \cancel{R_1} \\ = R_2 + K^2 R_1$$

$$X_{02} = \cancel{X_2} + X_1 \quad X_{02} = X_2 + \cancel{X_1} \\ = X_2 + X_1 K^2$$

* Secondary to primary reference:

$$\therefore R_{01} = R_1 + \cancel{R_2} \\ = R_1 + R_2 / K^2$$

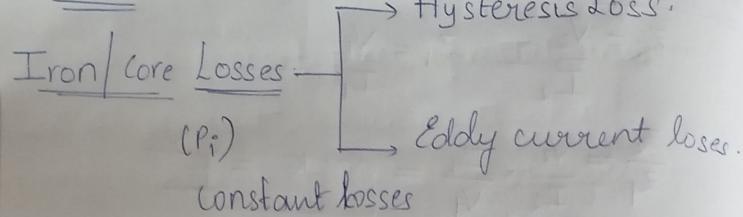
$$X_{01} = X_1 + \cancel{X_2} \\ = X_1 + X_2 / K^2$$

$$Z_{01} = \sqrt{R_{01}^2 + X_{01}^2}$$

If we shift all impedances to one winding:

we can eliminate transformer and solve as equivalent electrical circuit.

* Losses:



Hysteresis loss can be minimised using steel of high silicon content.

Eddy current losses can be reduced using core of thin laminations.

Copper Losses:

Losses in both the windings due to their ohmic resistances.

$$P_{Cu} = I^2 R$$

$$P_{Cu} = I_1^2 R_1 + I_2^2 R_2$$

↳ 90% of total transformer losses.

* Efficiency:

$$\eta = \frac{\text{Output Power}}{\text{Input Power}} = \frac{\alpha(\text{Full load VA}) \times Pf}{(\alpha \times \text{Full load VA} \cdot Pf) + P_i + \alpha^2 P_c}$$

where P_i = Full load iron loss

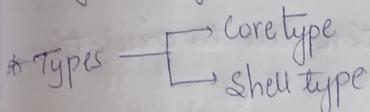
P_c = Full load copper loss.

α → type of load

* Construction:

- core is made of silicon steel which has low hysteresis loss and high permeability.
- core is laminated to reduce eddy current loss.
- winding one half of each limb on winding on one limb: This ensures tight coupling and reduces leakage flux.

- R_1 & R_2 → reduced; rise in temp & high efficiency.



* Power Factor Improvement:

∴ Most of the electronic devices used are LR circuits. ∴ To improve the power factor lags due to which there is less power output in the device.

To improve the power factor and power output we should add a capacitor.

$$\text{Active Power} = VI \cos\phi = P$$

$$\text{Reactive Power} = VI \sin\phi = Q$$

$$\text{Apparent Power} = V \cdot I = S$$

for Resistive load $\cos\phi = 1$

Inductive load $\cos\phi = \text{Lagging}$
capacitive load $\cos\phi = \text{Leading}$

* Fuse:

A fuse is a short piece of metal inserted in the circuit which melts when excessive current flows in the circuit and thus breaks the circuit.

Characteristics:

- Low melting point
- High conductivity
- Free from deterioration due to oxidation
- Low cost.

Materials used: tin, lead, tinned copper, Ag

Types:

(i) Re-wireable / Kit-kat fuse:

- low values of fault current can be interrupted.
- simple, cheap; available upto current of 200A.
- Erratic in operation & performance deteriorates with time.

ii) High Rupturing capacity cartridge Fuse:

- Consists of heat resisting ceramic body

having metal end caps to which a silver current carrying element is welded. The space b/w surrounding elements is filled with chalk, POP etc.

- carries normal current without overheating
- Fault ^{occurs} current increases and the fuse element melts and heat produced; vaporizes the melted silver element.
- Reaction b/w silver vapours and filling powder results in the formation of high resistance which is used in quenching the arc.

* Circuit Breaker:

Switching device which can be operated manually / automatically for controlling and protection of electrical system.

- consists of fixed and moving contacts called electrodes.
- These contacts remain closed until and unless a fault occurs.
- When a fault occurs; the trip coils of the breaker get energized and moving contacts are pulled apart; thus opening circuit.

Types:

- Miniature CB
- Residual current CB
- Air Blast CB.
- Vacuum CB.

* Miniature Circuit Breaker:

→ Switching function: On/Off.

Protection from overloads & short circuits.

- Electromechanical device to protect an electrical circuit from overcurrent which may lead to short circuits / overload.

- MCB is better than fuse; since it need not be replaced once overcurrent is detected.

- A switch which turns off automatically when the current flowing in the circuit is more than rated value.

- When current exceeds the limit ; the solenoidal forces the moveable contact to open & MCB turns off breaking the circuit

* Advantages:

- Simple to resume supply
- Better interface
- Electrically safer
- Reusable
- less maintenance & replacement cost.

* Applications:

- Home electrical panels
- lights
- Heaters

* Earthing:

Process of connecting metallic bodies of all electrical equipment to a huge mass of earth by a wire of negligible resistance is called earthing.

- Discharge of electrical energy takes place smoothly without any danger.

Purpose:

- To avoid electrical shock / death.

- To protect buildings & machinery from fault conditions.

- To provide safe path to dissipate lightning or short circuit currents.

Methods of Earthing

- Maintenance Free Earthing
- Conventional Earthing

Maintenance Free Earthing:

- No need to pour water at regular interval
- Maintain stable & consistent earth resistance.
- More surface area for peak current dissipation.

Conventional Earthing:

Digging a large pit which a GI pipe or copper plate positioned in middle layers of charcoal & salt.

- Requires maintenance & regular pouring of water.

* Methods of conventional Earthing:

1) Plate Earthing:

- Copper or GI plate is embedded in alternative layer of coke & salts for min. thickness.
- Earth wire is securely bolted to an earth plate with bolt nut & washer.

2) Rod Earthing:

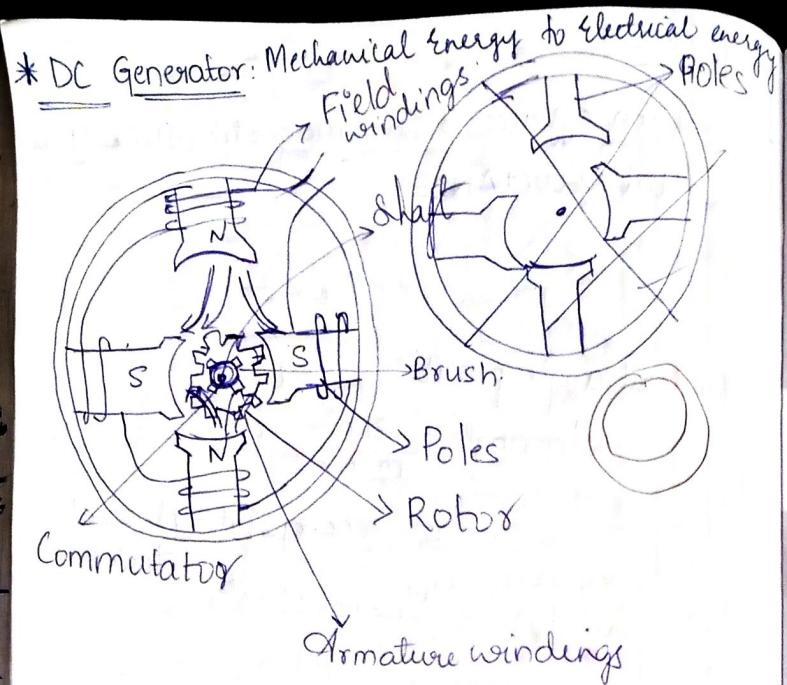
- Copper/GI/ steel rods are driven vertically into earth.
- We need to ↑se the embedded length of electrode under the ground which is necessary to reduce the earth resistance.
- Very cheap.

3) Pipe Earthing:

- Earthing a GI pipe vertically in ground to work as earth electrode & depth depends upon soil conditions.
- Wire is embedded upto wet soil.
- Can take heavy leakage current compared to Plate earthing.

* Applications:

- Telecommunication
- Transmission
- Power Generations
- Residential Building
- Water Treatment plants.



When current starts flowing; magnetic field is produced.

In all rotating machines; dynamically induced emf is seen.

When the rotor starts rotating ; there is an emf induced.

• Supply is given \rightarrow current starts flowing

• Magnetic field is produced \rightarrow Relative motion in b/w

• emf is induced in rotor conductor

• Current starts flowing.

* A DC emf is induced in the circuit due to an AC source.

Principle: Whenever there is a change in flux linkage; an emf is induced in the circuit.

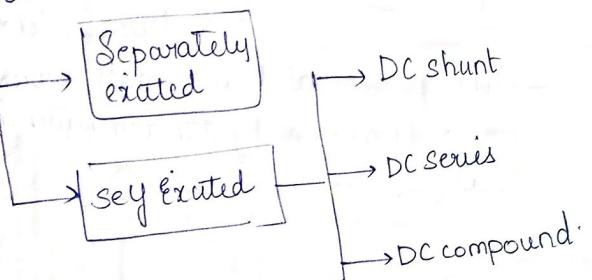
Stator:

- Magnetic frame
- Pole cores & pole shoes
- field windings
- Brushes & Brush holders
- End covers

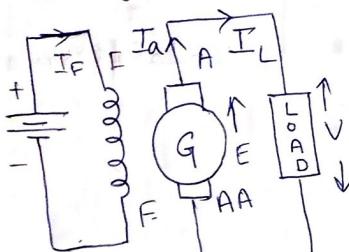
Rotor:

- Armature Core
- Armature winding
- Commutator
- Shaft

TYPES



Separately excited DC Generator:



\therefore field is supplied from external DC source.

and the excitation to the field & armature are separate

• Field winding consists of large no. of turns.

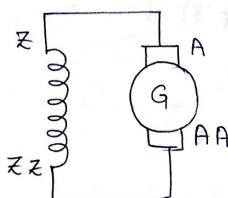
resistance of field is high, in order to limit the field current.

$$I_a = I_L \quad E = \frac{\Phi N Z \Phi}{60 A}$$

$$E = V + I_a R_a + V_{brush}$$

↳ Brush contact drop

* Say excited DC generator:

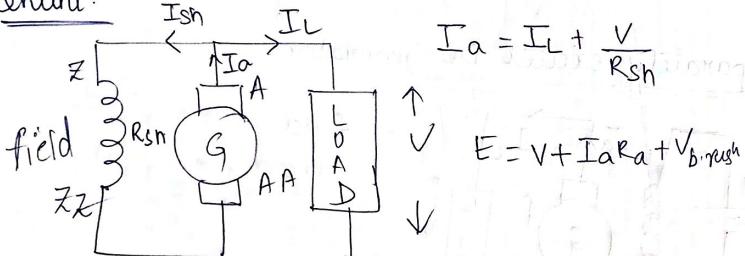


Residual Magnetism

When the generator is started; the field poles possess some procedural flux.

- flux is generated and small currents are produced by the armature in field winding

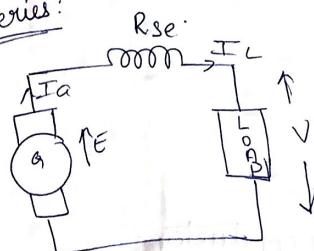
Shunt:



$$I_a = I_L + \frac{V}{R_{sh}}$$

$$E = V + I_a R_a + V_{brush}$$

Series:



resistance of series field winding is very small with less no. of turns & thick cross section area.

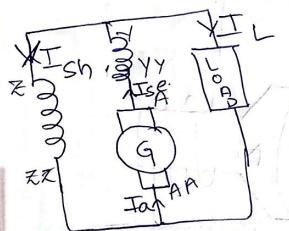
$$I_a = I_L = I_{se}$$

$$E = V + I_a R_a + I_{se} R_{se} + V_{brush}$$

↓ series field resistance drop

Compound:

Long Shunt:



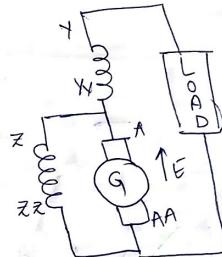
$$I_a = I_{se}$$

$$I_a = I_{sh} + I_L$$

$$I_{sh} = \frac{V}{R_{sh}}$$

$$E = V + I_a R_a + I_{se} R_{se} + V_{brush}$$

Short Shunt:



$$I_L = I_{se}$$

$$I_a = I_L + I_{sh}$$

$$I_{sh} = \frac{E - I_a R_a}{R_{sh}}$$

EMF equation

$$e = \frac{d\phi}{dt} = \frac{P\phi N}{60} \times \frac{z}{A}$$

where ϕ = flux.

P = No. of poles

z = total no. of conductors

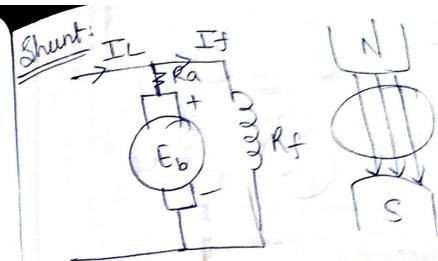
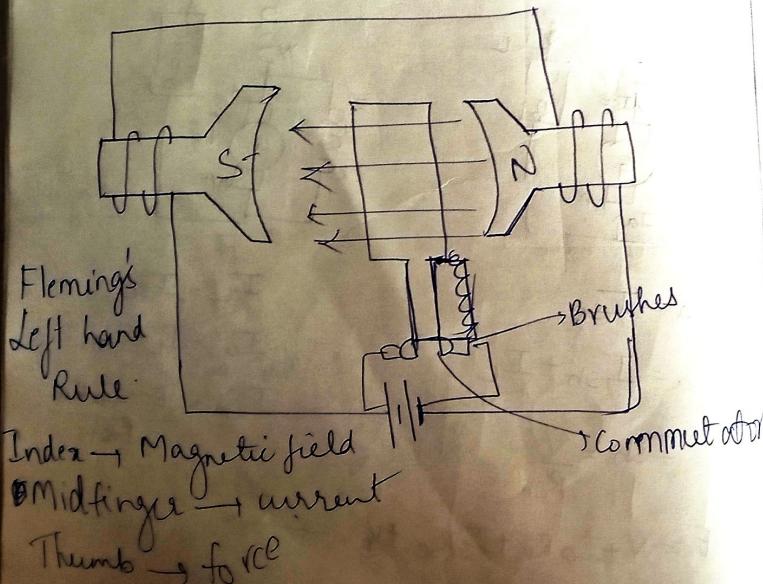
N = speed of armature

A = No. of parallel paths \propto current

Lap windings: A = P

Wave windings: A = 2 \Rightarrow constant

* DC Motors: Electrical to Mechanical



$$I_L = I_a + I_f$$

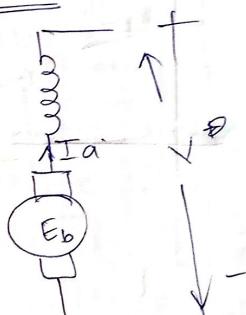
$$V = I_a R_a + E_b \rightarrow \text{back emf} \rightarrow \text{opposes the source voltage}$$

E_b controls the current I_a

Starter is used to limit the starting current (I_a); we need to limit the starting current to avoid damage to the circuit

$$I_a = \frac{V - E_b}{R_a}$$

Series:



$$I_L = I_{Sc} = I_a$$

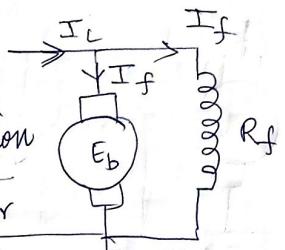
$$E_b - V = I_a R_a$$

$$I_a = \frac{E_b - V}{R_a}$$

* Torque in DC Motor:

$$P_m = E_b I_a$$

Power = Work done / Revolution
time taken for one revolution



$$= \frac{F \times 2\pi \gamma}{60/N} = F \times \left(\frac{2\pi N}{60} \right) = F_r (2\pi f) = F_r w$$

$$\boxed{P = T w}$$

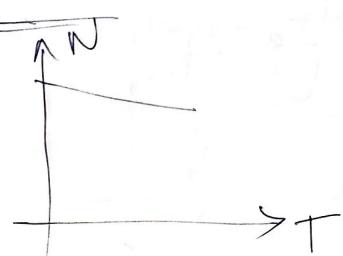
$$E_b I_a = T w$$

$$\frac{\phi Z A}{60 A} \cdot P \cdot I_a = T \cdot \frac{2\pi N}{60}$$

$$T = P \frac{\phi Z}{2\pi A} I_a$$

$$\boxed{T \propto I_a}$$

N vs T



$$E_b = \frac{\phi Z N P}{60 A}$$

$$N \propto \frac{E_b}{\phi}$$

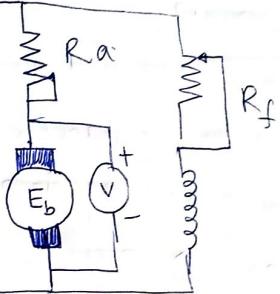
$$N \propto V - I_a R_a$$



* Speed control of DC shunt motor:

Speed shd be minimum at beginning

$$N \propto \frac{E_b}{\phi}$$



~~V_a~~ → armature
~~V_a~~ → Ra
V_a can be varied with Ra at max and R_f at min. to start the circuit.

→ Varying flux per pole: Flux control method

→ Varying armature resistance: armature control method.

* Flux control:

variable resistance is placed in series with field winding.

shostat reduces shunt field current I_{sh} & hence the ~~core~~ flux ϕ .

- raise the speed of motor above rated speed.

Only above rated speeds are obtained;
Shunt field winding resistance cannot be below R_{sh}

- * Armature Control:
 - Vary voltage across armature: hence back emf and ~~and~~ speed are changed.
 - & Controller resistance in series with armature
∴ there is a voltage drop; back emf is ↓ sed
 $\therefore N \propto E_b \Rightarrow$ speed also decreases.

* AC CIRCUITS :

$$e = I_m \sin \omega t$$

$$E_{max} =$$

$$E = E_m \sin \omega t$$

$$E_{max} =$$

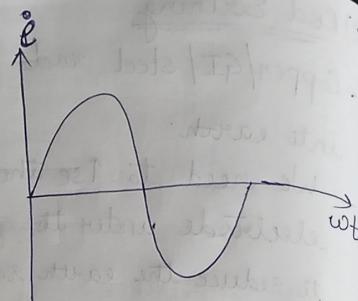
flux linkage of coil = no. of turns \times flux linking
 $= n \phi_{max} \cos \omega t$

$$e = - \frac{d\phi}{dt}$$

$$= -n\phi_m \sin \omega t \cdot \omega$$

$$e = +n\phi_m \omega \sin \omega t$$

$$E_{max} = n\phi_m \omega$$



$$T = \frac{1}{f}$$

$$\omega = \frac{2\pi}{T}$$

$$f = \frac{PN}{120}$$

$N \rightarrow$ speed
 $P \rightarrow$ poles.

* Average Value of Sinusoidal Current:

$$I = I_m \sin \omega t$$

$$I_{av} = \frac{\text{Area of half cycle}}{\text{Base length}} = \frac{\int_0^{\pi} I_m \sin \omega t d\omega}{\pi}$$

$$= I_m \left[-\cos \omega t \right]_0^{\pi}$$

$$= -\frac{I_m}{\pi} (-2) = \frac{2I_m}{\pi}$$

$$I_{av} = \frac{2I_m}{\pi}$$

$$E_{av} = \frac{2E_m}{\pi}$$

* RMS Value of Sinusoidal Current:

$$I = I_m \sin \omega t$$

$$I_{rms} = \sqrt{\frac{\text{Area of half-cycle squared wave}}{\text{Half-cycle base}}}$$

$$= \sqrt{\frac{\int_0^{\pi} I_m^2 \sin^2 \omega t d\omega}{\pi}}$$

$$= \sqrt{\frac{I_m^2}{\pi} \int_0^{\pi} \frac{1 - \cos 2\omega t}{2} d\omega}$$

$$= \frac{I_m}{\sqrt{\pi}} \int_0^{\pi} \left[\frac{1}{2} \cos \theta - \right] \frac{\cos 2\theta}{2} d\theta$$

$$= \frac{I_m}{\sqrt{\pi}} \int_0^{\pi} \left[\frac{1}{2} - \frac{1}{2} \cdot \frac{1}{2} [\sin 2\theta] \right] d\theta$$

$$= \frac{I_m}{\sqrt{\pi}} \cdot \frac{\pi}{2} = \frac{I_m}{\sqrt{2}}$$

$$I_{rms} = \frac{I_m}{\sqrt{2}}$$

$$E_{rms} = \frac{E_m}{\sqrt{2}}$$

* Form Factor: $\frac{\text{RMS value}}{\text{Avg value}} = \frac{\frac{E_m}{\sqrt{2}}}{\frac{E_m}{2}} = \frac{\frac{I_m}{\sqrt{2}}}{\frac{I_m}{2}} = 1.11$

* Peak Factor: $\frac{\text{Max Value}}{\text{RMS value}} = \frac{\frac{I_m \times \sqrt{2}}{I_m}}{\frac{E_m \times \sqrt{2}}{E_m}} = 1.414$

* Capacitor:  (passive)
- 2 metallic plates separated by a dielectric which stores energy in the form of charge / electric field.

$$\begin{aligned} q \propto v &\Rightarrow q = Cv \\ i = C \frac{dv}{dt} & \\ W = \int P dt & \end{aligned}$$

$$W = \int VI dt = \int V C \frac{dv}{dt} dt$$

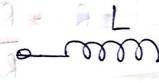
$$W = \frac{C V^2}{2}$$

$$V = V_0 + \int_0^t i dt$$

* When we apply DC, capacitor acts as open circuit.

→ Capacitor do not allow sudden changes in voltage.

→ Capacitor acts as voltage source initially and act as open circuit at the end.

* Inductor:  (passive)

→ Faraday's law: Rate of change of flux will generate an emf.

→ Stores energy in the form of flux or magnetic field.

$$L = \frac{N^2 \mu A}{l}$$

• Active elements provide energy for infinite time

N → turns

A → area

l → length

• Passive elements provide energy for short interval of time.

$L = \text{Flux linkage}$
Ampere.

$$L \frac{di}{dt} = v$$

$$v = \frac{d\phi}{dt} N$$

$$i = I_0 + \int_{t_0}^t v dt$$

* Inductor acts as a current source initially and acts as short circuit at the final conditions.

Inductor do not allow sudden changes in current

$$L = L_1 + L_2$$

$$C = \frac{C_1 C_2}{C_1 + C_2}$$

$$R = R_1 + R_2$$

Series Parallel

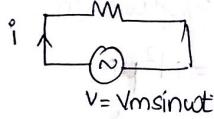
$$L = \frac{L_1 L_2}{L_1 + L_2}$$

$$C = C_1 + C_2$$

$$R = \frac{R_1 R_2}{R_1 + R_2}$$

* Rotating vector is called a phasor.

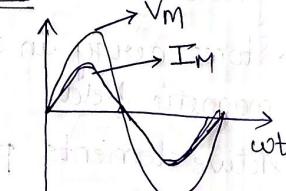
* AC through pure resistance



$$i = I_m \sin wt$$

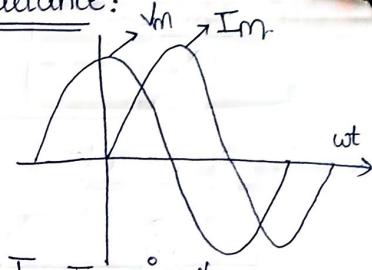
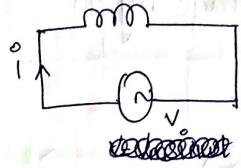
$$P_{av} = \frac{V_m I_m}{\pi} \int_0^\pi \sin^2 \theta d\theta$$

$$= \frac{V_m I_m}{2\pi} [\pi - 0] = \frac{V_m I_m}{2}$$



$$P = V_{rms} \times I_{rms}$$

* AC through pure inductance:



$$v = L \frac{di}{dt}$$

~~$$\frac{v}{L} dt = di$$~~

$$v = L I_m \omega \cos wt$$

$$v = V_m \sin(wt + 90^\circ)$$

$P_{av} = 0 \rightarrow$ Inductor will not consume any power.

$$i = I_m \sin wt$$

$$X_L = \omega L 2\pi$$

$$v = I_m \omega L e^{jwt}$$

$$v = j X_L I_m e^{jwt}$$

current lags voltage by 90° .

* AC through pure capacitance:

$$i = C \frac{dv}{dt}$$

$$= C V_m \cos wt \cdot \omega$$

$$i = I_m \cos wt$$

$$i = I_m \sin(wt + 90^\circ)$$

$$X_C = \frac{1}{2\pi f C}$$

$$v = V_m e^{jwt}$$

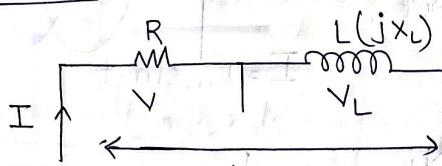
$$i = -V_m j \omega e^{-jwt}$$

$$i = -j X_C V_m e^{-jwt}$$

$$i = \frac{V_m}{jX_c} e^{-j\omega t}$$

current leads voltage by 90°

* Series RL circuit:



$$\bar{V} = \bar{V}_R + \bar{V}_L$$

$$Z = R + jX_L$$

$$V = IR + IjX_L$$

$$I = \frac{V}{R+jX_L}$$

Phasor $V = V_m \sin \omega t$

$$I = \frac{I_m}{\pi} \sin(\omega t - \phi)$$

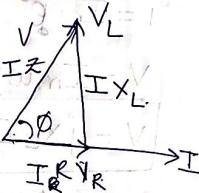
$$P = \int_{0}^{\pi} \frac{P}{\pi} d\theta$$

$$P = \frac{1}{\pi} \int_{0}^{\pi} V_m I_m \sin \theta \cdot \sin(\theta - \phi) d\theta$$

$$= \frac{V_m I_m}{\pi} \int_{0}^{\pi} \sin \theta [\sin \theta \cos \phi - \cos \theta \sin \phi] d\theta$$

$$= \frac{V_m I_m}{\pi} \int_{0}^{\pi} [\sin^2 \theta \cos \phi - \frac{1}{2} \sin 2\theta \sin \phi] d\theta$$

$$= \frac{V_m I_m}{\pi} \left[\frac{\cos \phi}{2} (\pi) + \frac{\sin \phi}{2} \cdot \frac{1}{2} (1-1) \right]$$

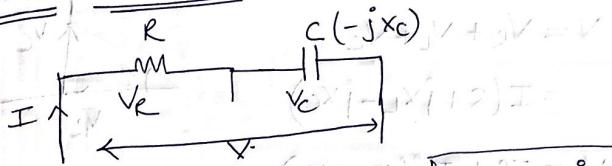


$$P = \frac{V_m I_m}{\pi} \cdot \frac{\pi \cos \phi}{2}$$

$$P = \frac{V_m I_m \cos \phi}{2}$$

$$P = V_{rms} I_{rms} \cos \phi$$

* Series RC circuit:



$$\bar{V} = \bar{V}_R + \bar{V}_C$$

$$Z = R - jX_C$$

$$V = I(R - jX_C)$$

$$I = \frac{V}{R - jX_C}$$

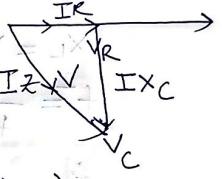
Phasor

$$V = V_m \sin(\omega t)$$

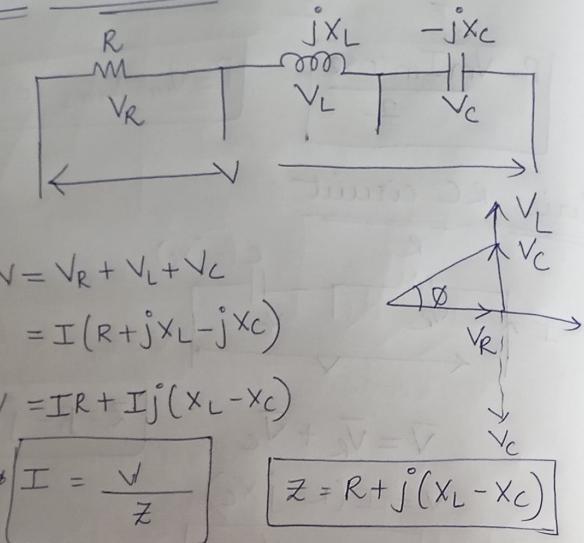
$$I = \frac{I_m}{\pi} \sin(\omega t + \phi)$$

$$P = \frac{1}{\pi} \int_{0}^{\pi} V_m I_m \sin \omega t \sin(\omega t + \phi) d\theta$$

$$P = \frac{V_m I_m}{\pi} \cos \phi$$



* Series LCR circuit:

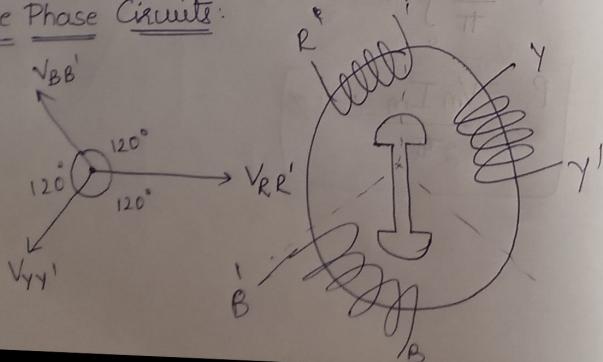


$$X_L = 2\pi f L \quad X_C = \frac{1}{2\pi f C}$$

at resonance condition

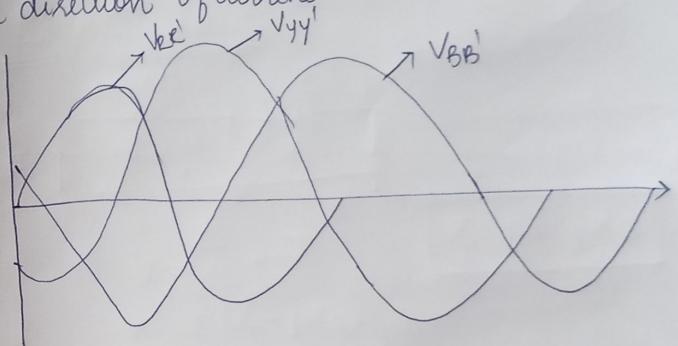
$$X_L = X_C \quad f^2 = \frac{1}{4\pi^2 LC} \Rightarrow f = \frac{1}{2\pi\sqrt{LC}}$$

* Three Phase Circuits:



The order in which the phases attain their maximum/reference value is called phase sequence.

By changing the phase sequence; we can change the direction of current.



$$V_{R'R'} = V_m \sin \omega t$$

$$V_{Y'Y} = V_m \sin(\omega t - 120^\circ)$$

$$V_{B'B} = V_m \sin(\omega t - 240^\circ)$$

* STAR AND DELTA CONNECTIONS: