

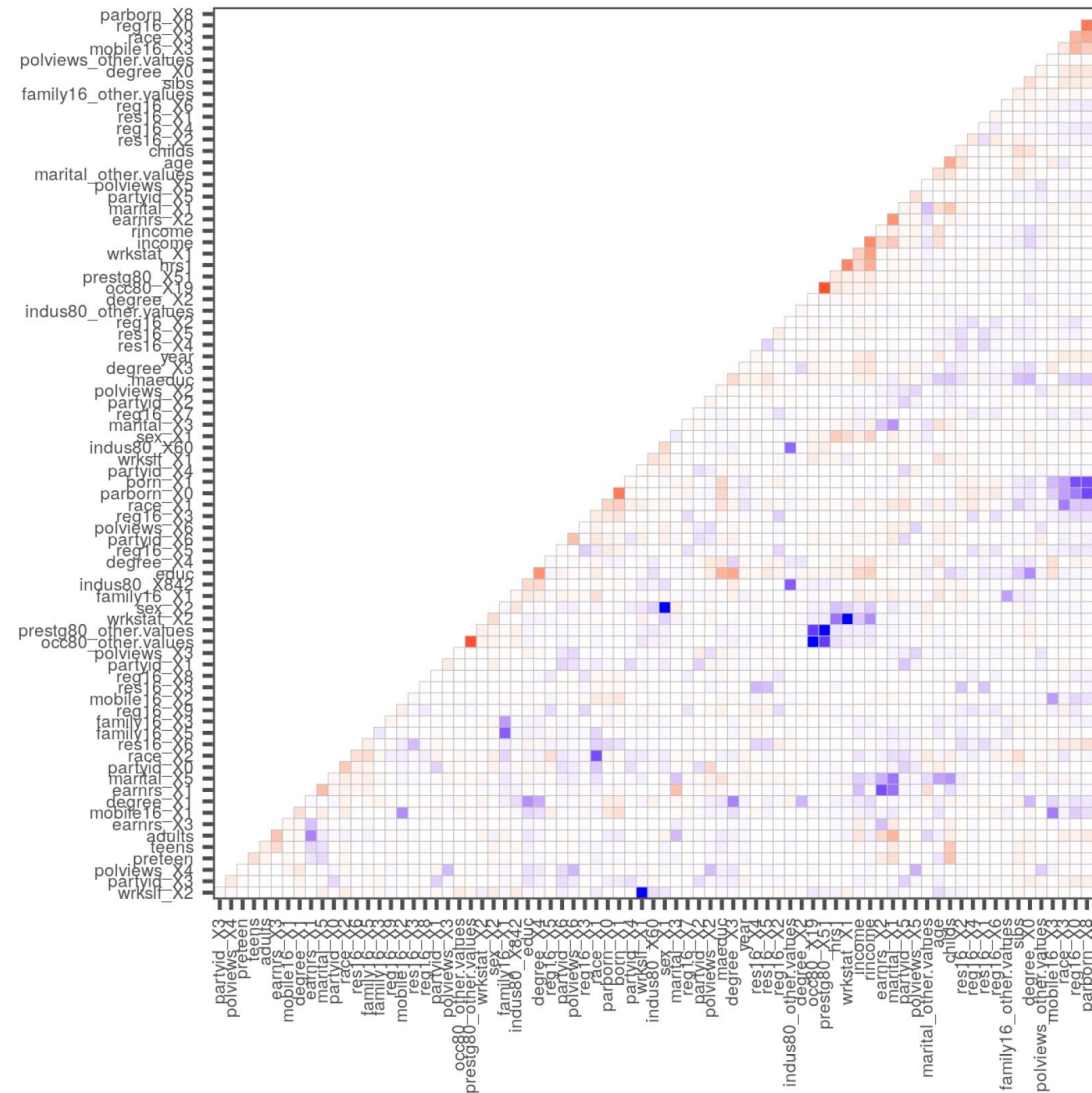
# Causal Tree Algorithm

- Divide data into tree-building  $\mathcal{S}^{tr}$  and estimation  $\mathcal{S}^{est}$  samples
- Use a greedy algorithm to recursively partition covariate space  $\mathcal{X}$  into a deep partition  $\Pi$ 
  - At each node the split is selected as the one that minimizes our estimate of EMSE over all possible binary splits
  - Preserve minimum number of treated and control units in each child leaf
- Use cross-validation to select the depth  $d^*$  of the partition that minimizes an estimate of MSE of treatment effects, using left-out folds as proxies for the test set
- Select partition  $\Pi^*$  by pruning  $\Pi$  to depth  $d^*$ , pruning leaves that provide the smallest improvement in goodness of fit
- Estimate the treatment effects in each leaf of  $\Pi^*$  using the estimation sample  $\mathcal{S}$

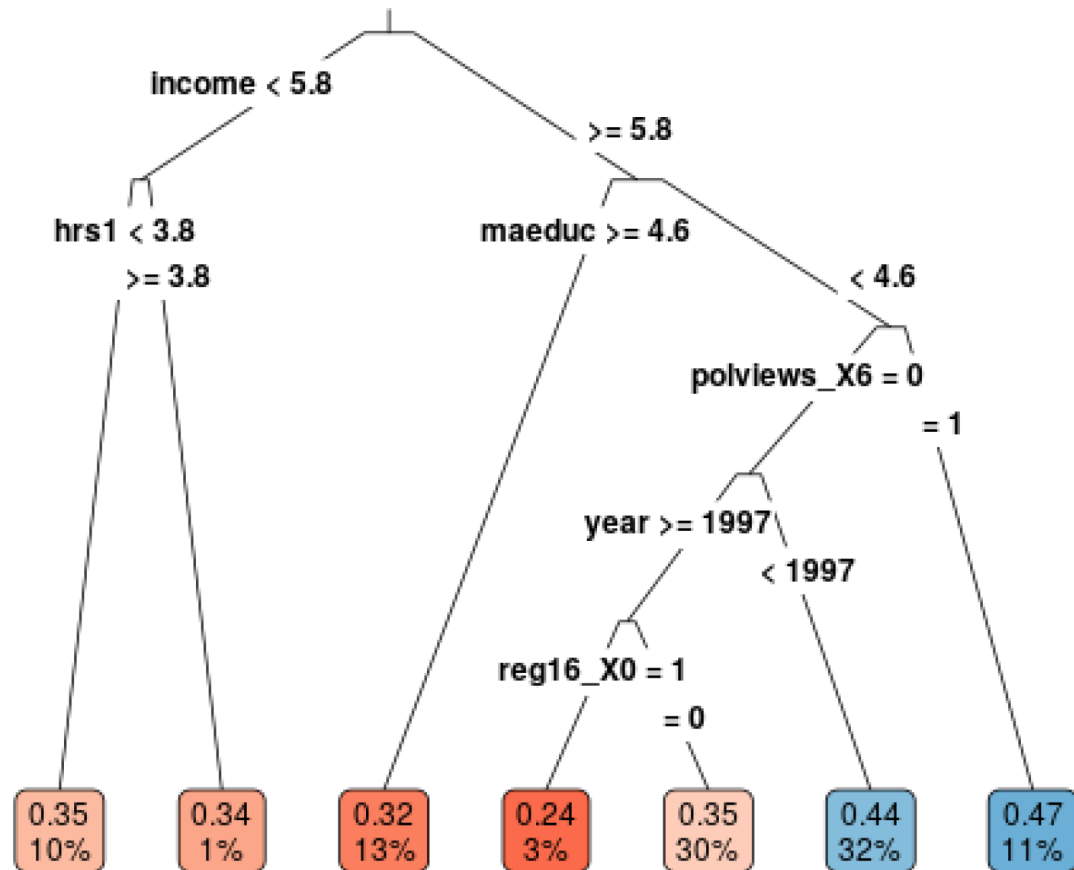
# Causal Trees: GSS Survey Experiment

- Survey experiment in the General Social Survey conducted between 1986 and 2010 (Green and Kern, 2012)
- Respondents randomly assigned to one of two questions about public spending
- Experimental condition respondents were asked about “welfare” and in the other they were asked about “assistance to the poor”
- Outcome of interest: expressed support for government spending in this domain

# GSS Survey Experiment, 88 covariate correlation matrix



# Causal Tree: Visualize the Tree



Linear hypothesis test

Hypothesis:

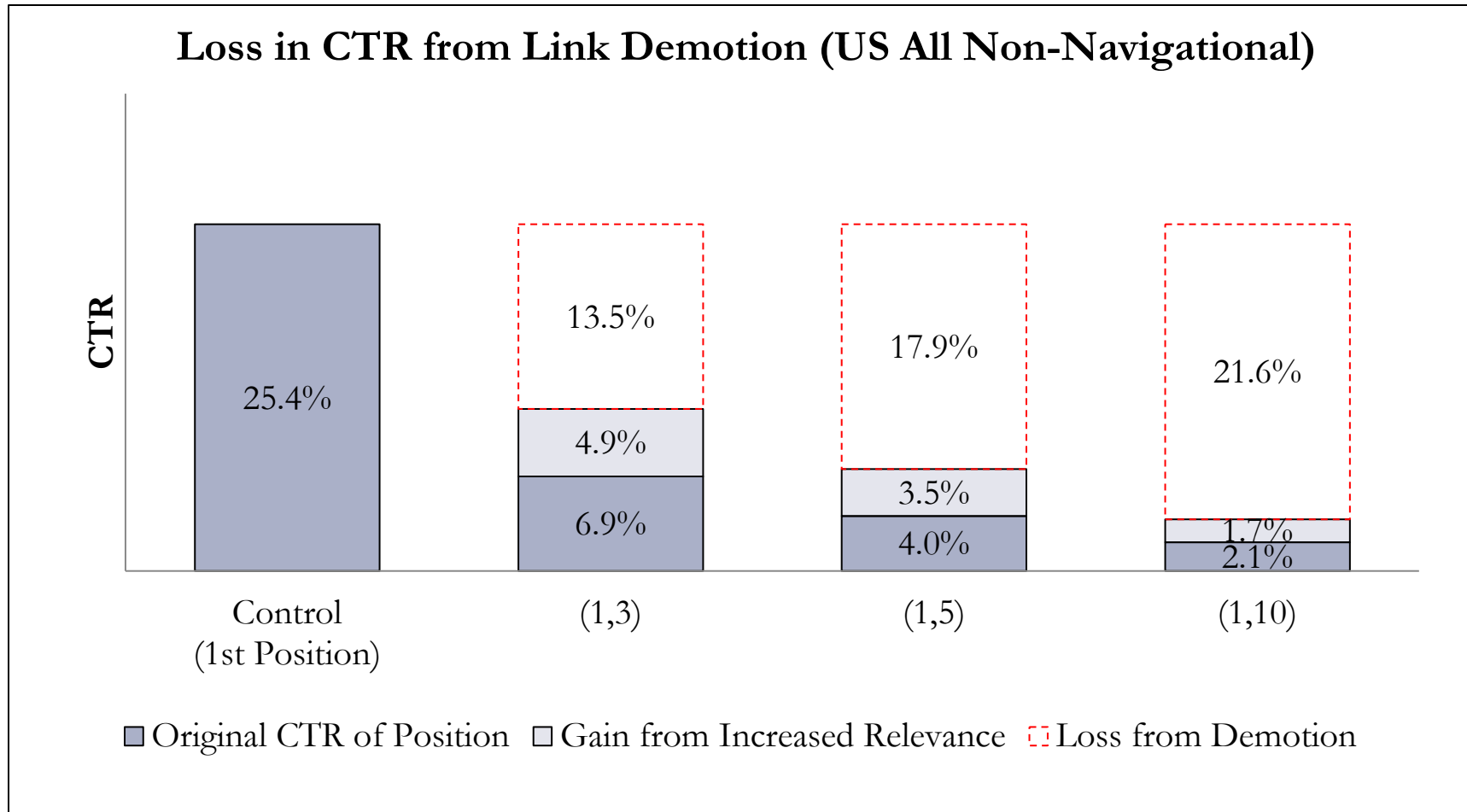
leaf1:W - leaf2:W = 0  
leaf1:W - leaf3:W = 0  
leaf1:W - leaf4:W = 0  
leaf1:W - leaf5:W = 0  
leaf1:W - leaf6:W = 0  
leaf1:W - leaf7:W = 0

Model 1: restricted model  
Model 2:  $Y \sim \text{leaf} + W:\text{leaf}$

	Res.Df	Df	F	Pr(>F)
1	5272			
2	5266	6	4.4771	0.0001575 ***

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

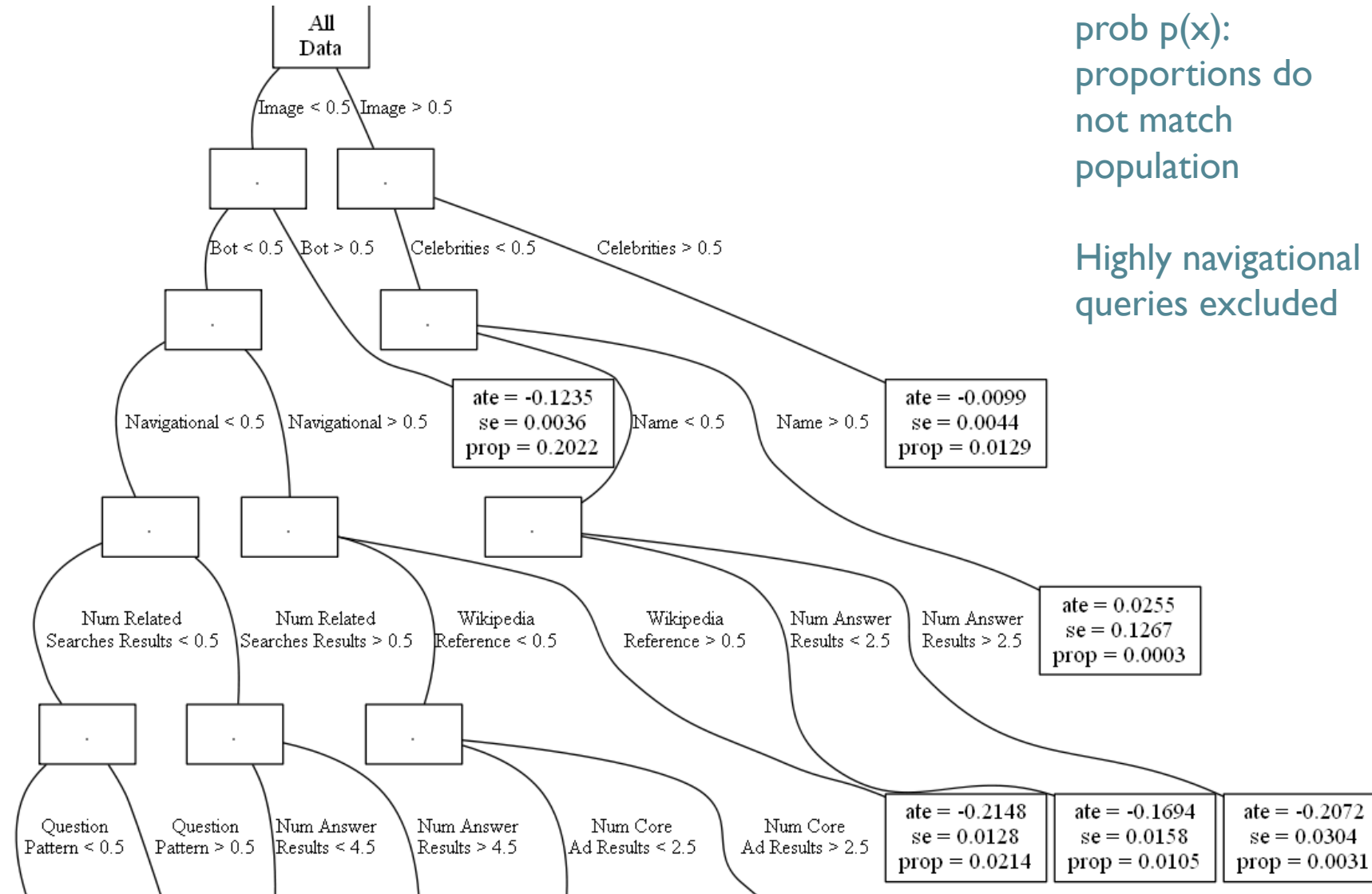
# Relevance v. Position

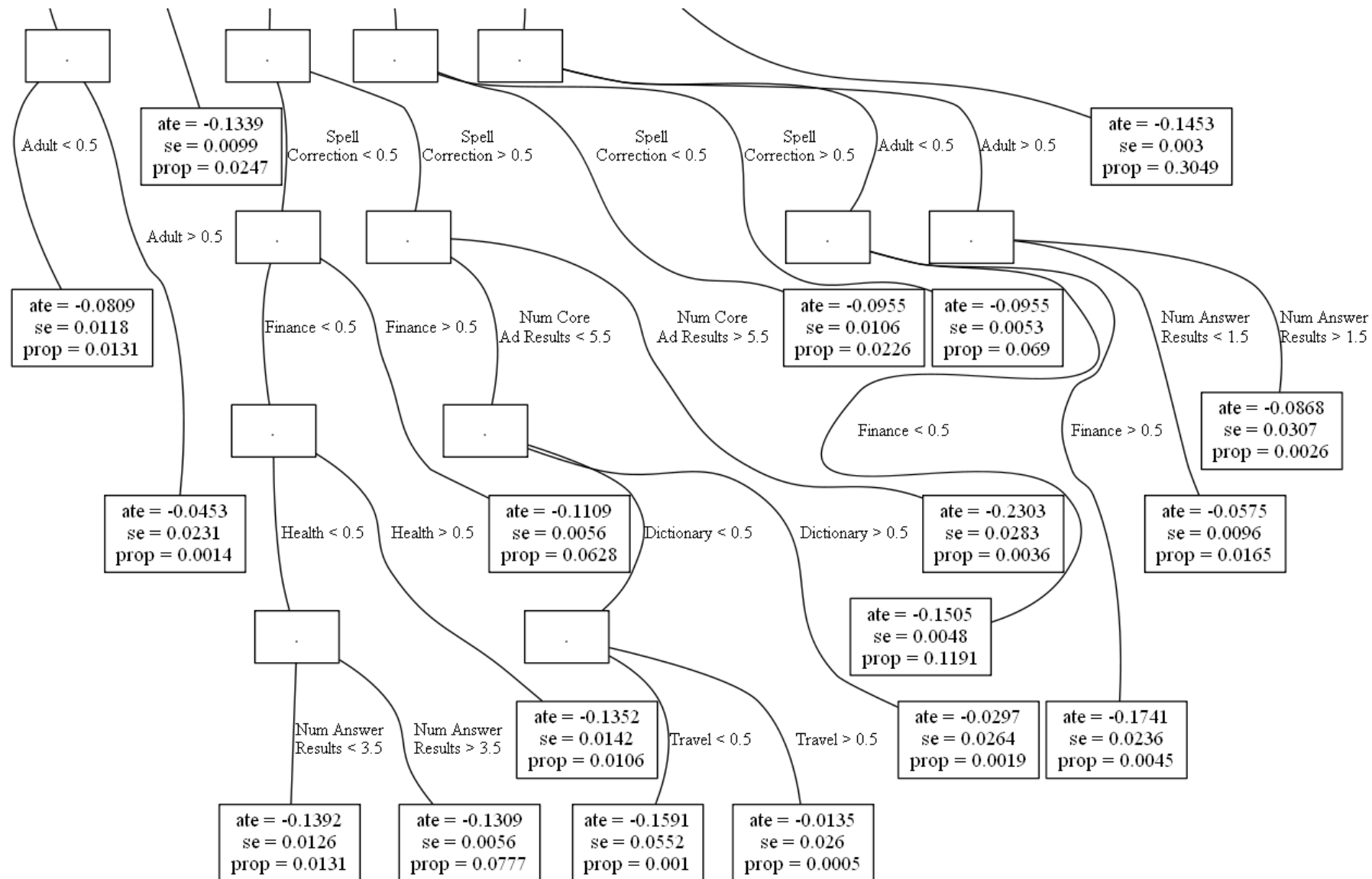


# Search Experiment Tree: Effect of Demoting Top Link (Test Sample Effects)

Some data  
excluded with  
prob  $p(x)$ :  
proportions do  
not match  
population

Highly navigational  
queries excluded





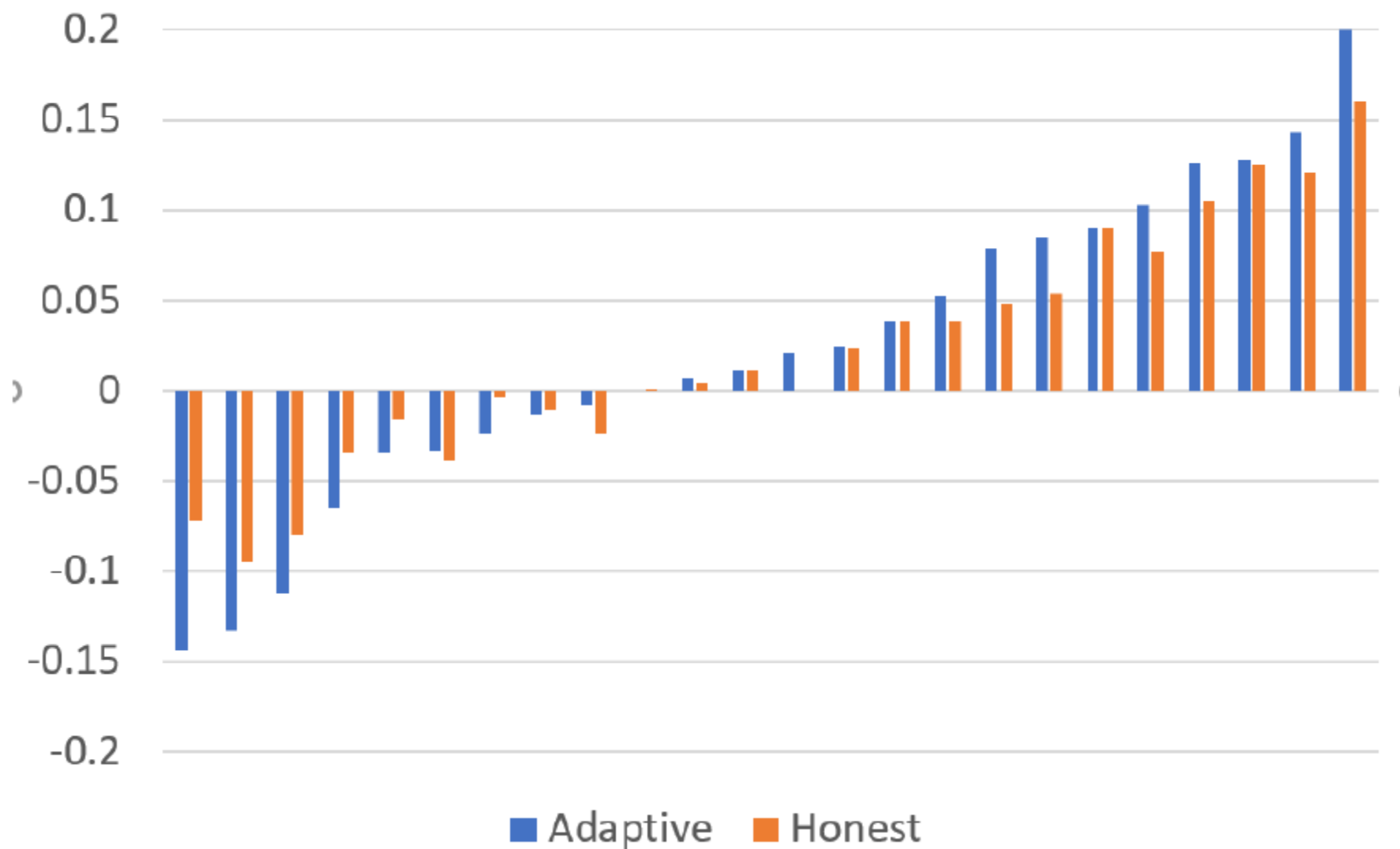
	Honest Estimates			Adaptive Estimates		
	Treatment	Standard	Proportion	Treatment	Standard	Proportion
	Effect	Error		Effect	Error	
Use Test Sample for Segment Means & Std Errors to Avoid Bias	-0.124	0.004	0.202	-0.124	0.004	0.202
	-0.134	0.010	0.025	-0.135	0.010	0.024
	-0.010	0.004	0.013	-0.007	0.004	0.013
	-0.215	0.013	0.021	-0.247	0.013	0.022
	-0.145	0.003	0.305	-0.148	0.003	0.304
	-0.111	0.006	0.063	-0.110	0.006	0.064
	-0.230	0.028	0.004	-0.268	0.028	0.004
	-0.058	0.010	0.017	-0.032	0.010	0.017
	-0.087	0.031	0.003	-0.056	0.029	0.003
	-0.151	0.005	0.119	-0.169	0.005	0.119
Variance of estimated treatment effects in training sample 2.5 times that in test sample (adaptive estimates biased)	-0.174	0.024	0.005	-0.168	0.024	0.005
	0.026	0.127	0.000	0.286	0.124	0.000
	-0.030	0.026	0.002	-0.009	0.025	0.002
	-0.135	0.014	0.011	-0.114	0.015	0.010
	-0.159	0.055	0.001	-0.143	0.053	0.001
	-0.014	0.026	0.001	0.008	0.050	0.000
	-0.081	0.012	0.013	-0.050	0.012	0.013
	-0.045	0.023	0.001	-0.045	0.021	0.001
	-0.169	0.016	0.011	-0.200	0.016	0.011
	-0.207	0.030	0.003	-0.279	0.031	0.003
	-0.096	0.011	0.023	-0.083	0.011	0.022
	-0.096	0.005	0.069	-0.096	0.005	0.070
	-0.139	0.013	0.013	-0.159	0.013	0.013
	-0.131	0.006	0.078	-0.128	0.006	0.078





Devia

Deviation from ATE: Adaptive v. Honest Estimates



# Low-Dimensional Representations v. Fully Nonparametric Estimation

## Causal Trees

- Move the goalpost, but get guaranteed coverage
- Easy to interpret, easy to mis-interpret
- Can be many trees
- Leaves differ in many ways if covariates correlated; describe leaves by means in all covariates

## Causal Forests

- Attempt to estimate  $\tau(x)$
- Can estimate partial effects
- In high dimensions, still can have omitted variable issues
- Confidence intervals lose coverage in high dimensions (bias)