作品二、Python 迴圈、矩陣與外部檔案的練習

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本作品藉由繪圖和製作卡方表練習(1)迴圈與矩陣的運算、(2)繪製散佈圖、(3)線性代數的矩陣運算處理重複性計算、(4)利用 Pandas 與 Scipy 套件, 處裡資料、(5)將矩陣儲存到 EXCEL 檔案

1.繪製下圖 (線條顏色、符號與數量都可以由程式輕易變更)

繪製6圈的同心圓, 半徑分別為10、12、14、16、18和20, 並在各圈的圓上均勻畫上12個方框。

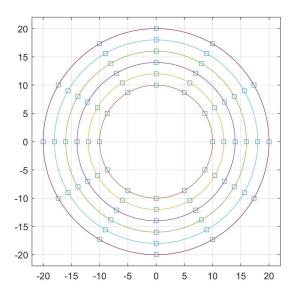
注意事項:

將數量的決定放在 code 第一條,譬如,n = 6

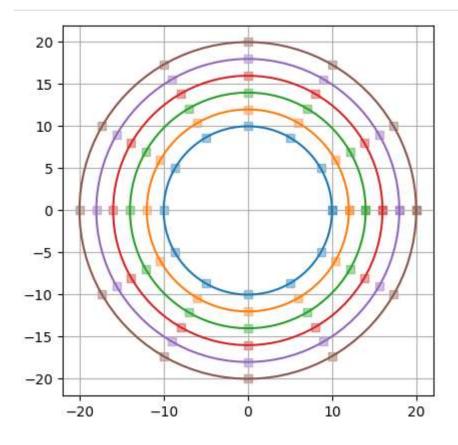
將符號的決定放在 code 第二條,譬如,marker = 's'

不論畫同心圓或圓上方塊符號,可以採用迴圈方式或非迴圈的矩陣計算方式。最好兩者都試試看(從自己最有把握的方法先做),才知道 python 的長處(可以先不論顏色)。

上述方式可以迅速變更設定,看到結果。



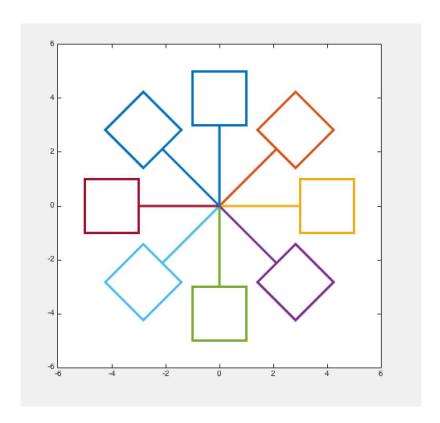
```
In [ ]: from cmath import sqrt
        import numpy as np
        import matplotlib.pyplot as plt
        import turtle
        figure, ax = plt.subplots()
        r=np.linspace(10, 20, 6)
        theta=np.linspace(0, 2*np.pi, 100)
        theta1=np.linspace(0, 2*np.pi, 13)
        for i in r:
            x=i*np.cos(theta)
            y=i*np.sin(theta)
            plt.plot(x, y)
        for i in r:
            x=i*np.cos(theta1)
            y=i*np.sin(theta1)
            plt.scatter(x, y, marker='s', alpha=0.4)
        ax.set_aspect(1)
        ax.set_xlim([-22, 22])
        ax.set_ylim([-22, 22])
        ax.grid(True)
```

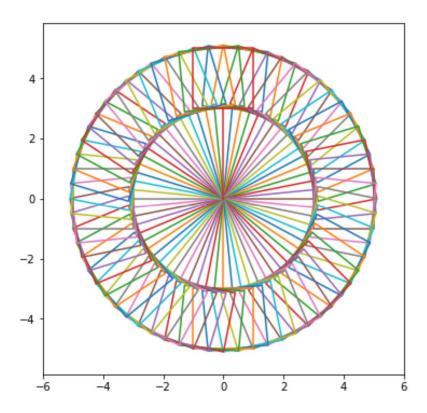


2. 繪製下圖 (線條顏色與數量都可以由程式輕易決定)

注意事項:

將方框數量的決定放在 code 第一條,譬如,n=8,改變 n 值,便能看到結果的改變,譬如,n=128 得到右圖。





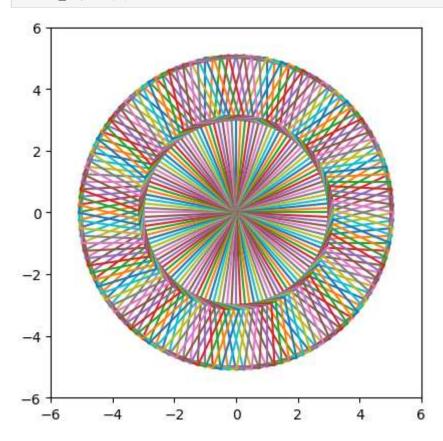
```
In [ ]: import numpy as np
    import matplotlib.pyplot as plt

figure, ax = plt.subplots()

x=[0, 0, -1, -1, 1, 1, 0]
y=[0, 3, 3, 5, 5, 3, 3]
ax.set_xlim([-6, 6])
ax.set_ylim([-6, 6])
S=np.array([[0, 0, -1, -1, 1, 1, 0], [0, 3, 3, 5, 5, 3, 3]])

#n=8
n=128

for i in range(n):
    A=np.array([[np.cos(i*np.pi/(n/2)), np.sin(i*np.pi/(n/2))], [-np.sin(i*np.pi/(n/2)), np.cos(i*np.pi/(n/2))]]).dot(S
B=A[0, ]
C=A[1, ]
plt.plot(B, C)
```



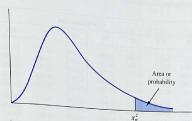
3.計算如下右圖的卡方右尾面積與自由度對照表,並輸出到 EXCEL 檔,檔名為:Chi2Table.xlsx,含欄與列的名稱,如下左圖。

注意事項:

提示的套件與程式碼如下方 code 區所示。

利用 pandas 將矩陣內容儲存到 EXCEL 檔,製作方式請參考 pandas 手冊。

| | A | В | С | D | Е | F | G | Н | I | J | K |
|----|----|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 1 | | 0.995 | 0.99 | 0.975 | 0.95 | 0.9 | 0.1 | 0.05 | 0.025 | 0.01 | 0.005 |
| 2 | 1 | 3.93E-05 | 0.000157 | 0.000982 | 0.003932 | 0.015791 | 2.705543 | 3.841459 | 5.023886 | 6.634897 | 7.879439 |
| 3 | 2 | 0.010025 | 0.020101 | 0.050636 | 0.102587 | 0.210721 | 4.60517 | 5.991465 | 7.377759 | 9.21034 | 10.59663 |
| 4 | 3 | 0.071722 | 0.114832 | 0.215795 | 0.351846 | 0.584374 | 6.251389 | 7.814728 | 9.348404 | 11.34487 | 12.83816 |
| 5 | 4 | 0.206989 | 0.297109 | 0.484419 | 0.710723 | 1.063623 | 7.77944 | 9.487729 | 11.14329 | 13.2767 | 14.86026 |
| 6 | 5 | 0.411742 | 0.554298 | 0.831212 | 1.145476 | 1.610308 | 9.236357 | 11.0705 | 12.8325 | 15.08627 | 16.7496 |
| 7 | 6 | 0.675727 | 0.87209 | 1.237344 | 1.635383 | 2.204131 | 10.64464 | 12.59159 | 14.44938 | 16.81189 | 18.54758 |
| 8 | 7 | 0.989256 | 1.239042 | 1.689869 | 2.16735 | 2.833107 | 12.01704 | 14.06714 | 16.01276 | 18.47531 | 20.27774 |
| 9 | 8 | 1.344413 | 1.646497 | 2.179731 | 2.732637 | 3.489539 | 13.36157 | 15.50731 | 17.53455 | 20.09024 | 21.95495 |
| 10 | 9 | 1.734933 | 2.087901 | 2.700389 | 3.325113 | 4.168159 | 14.68366 | 16.91898 | 19.02277 | 21.66599 | 23.58935 |
| 11 | 10 | 2.155856 | 2.558212 | 3.246973 | 3.940299 | 4.865182 | 15.98718 | 18.30704 | 20.48318 | 23.20925 | 25.18818 |
| 12 | 11 | 2.603222 | 3.053484 | 3.815748 | 4.574813 | 5.577785 | 17.27501 | 19.67514 | 21.92005 | 24.72497 | 26.75685 |
| 13 | 12 | 3.073824 | 3.570569 | 4.403789 | 5.226029 | 6.303796 | 18.54935 | 21.02607 | 23.33666 | 26.21697 | 28.29952 |
| 14 | 13 | 3.565035 | 4.106915 | 5.008751 | 5.891864 | 7.041505 | 19.81193 | 22.36203 | 24.7356 | 27.68825 | 29.81947 |
| 15 | 14 | 4.074675 | 4.660425 | 5.628726 | 6.570631 | 7.789534 | 21.06414 | 23.68479 | 26.11895 | 29.14124 | 31.31935 |
| 16 | 15 | 4.600916 | 5.229349 | 6.262138 | 7.260944 | 8.546756 | 22.30713 | 24.99579 | 27.48839 | 30.57791 | 32.80132 |



Entries in the table give χ^2_α values, where α is the area or probability in the upper tail of the chi-square distribution. For example, with 10 degrees of freedom and a .01 area in the upper tail, $\chi^2_{01}=23.209$.

| Degrees | | | | | | | | | | | |
|------------|--------|--------|--------|--------|----------------|----------------|------------------|------------------|------------------|--------|--|
| of Freedom | .995 | .99 | .975 | .95 | .90 | .10 | .05 | .025 | .01 | .005 | |
| 1 | .000 | .000 | .001 | .004 | .016 | | | | | 7.879 | |
| 2 | .010 | .020 | .051 | .103 | .211 | 2.706 | 3.841 | 5.024 | 6.635 | 10.597 | |
| 3 | .072 | .115 | .216 | .352 | | 4.605 | 5.991 | 7.378 | 9.210 | 12.838 | |
| 4 | .207 | .297 | .484 | .711 | .584 | 6.251 | 7.815 | 9.348 | 11.345 | 14.860 | |
| 5 | .412 | .554 | .831 | 1.145 | 1.064 1.610 | 7.779 9.236 | 9.488 11.070 | 11.143 12.832 | 13.277 15.086 | 16.750 | |
| 6 | .676 | .872 | 1.237 | 1.635 | 2.204 | 10.645 | 12.592 | 14.449 | 16.812 | 18.548 | |
| 7 | .989 | 1.239 | 1.690 | 2.167 | 2.833 | 12.017 | 14.067 | 16,013 | 18,475 | 20.278 | |
| 8 | 1.344 | 1.647 | 2.180 | 2.733 | 3.490 | 13.362 | 15.507 | 17.535 | 20.090 | 21.955 | |
| 9 | 1.735 | 2.088 | 2.700 | 3.325 | 4.168 | 14.684 | 16.919 | 19.023 | 21.666 | 23.589 | |
| 10 | 2.156 | 2.558 | 3.247 | 3.940 | 4.865 | 15.987 | 18.307 | 20.483 | 23.209 | 25.188 | |
| 11 | 2.603 | 3.053 | 3.816 | 4.575 | 5.578 | 17.275 | 19.675 | 21.920 | 24.725 | 26.75 | |
| 12 | 3.074 | 3.571 | 4.404 | 5.226 | 6.304 | 18.549 | 21.026 | 23.337 | 26.217 | 28.30 | |
| 13 | 3.565 | 4.107 | 5.009 | 5.892 | 7.041 | 19.812 | 22.362 | 24.736 | 27.688 | 29.81 | |
| 14 | 4.075 | 4.660 | 5.629 | 6.571 | 7.790 | 21.064 | 23.685 | 26.119 | 29.141 | 31.31 | |
| 15 | 4.601 | 5.229 | 6.262 | 7.261 | 8.547 | 22.307 | 24.996 | 27.488 | 30.578 | 32.80 | |
| 16 | 5.142 | 5.812 | 6.908 | 7.962 | 9.312 | 23.542 | 26.296 | 28.845 | 32.000 | 34.26 | |
| 17 | 5.697 | 6.408 | 7.564 | 8.672 | 10.085 | 24.769 | 27.587 | 30.191 | 33.409 | 35.71 | |
| 18 | 6.265 | 7.015 | 8.231 | 9.390 | 10.865 | 25.989 | 28.869 | 31.526 | 34.805 | 37.15 | |
| 19 | 6.844 | 7.633 | 8.907 | 10.117 | 11.651 | 27.204 | 30.144 | 32.852 | 36.191 | 38.58 | |
| 20 | 7.434 | 8.260 | 9.591 | 10.851 | 12.443 | 28.412 | 31.410 | 34.170 | 37.566 | 39.99 | |
| 21 | 8.034 | 8.897 | 10.283 | 11.591 | 13.240 | 29.615 | 32.671 | 35.479 | 38.932 | 41.40 | |
| 22 | 8.643 | 9.542 | 10.982 | 12.338 | 14.041 | 30.813 | 33.924 | 36.781 | 40.289 | 42.79 | |
| 23 | 9.260 | 10.196 | 11.689 | 13.091 | 14.848 | 32.007 | 35.172 | 38.076 | 41.638 | 44.18 | |
| 24 | 9.886 | 10.856 | 12.401 | 13,848 | 15.659 | 33.196 | 36.415 | 39.364 | 42.980 | 45.55 | |
| 25 | 10.520 | 11.524 | 13.120 | 14.611 | 16.473 | 34.382 | 37.652 | 40.646 | 44.314 | 46.92 | |
| 26 | 11.160 | 12.198 | 13.844 | 15.379 | 17.292 | 35.563 | 38.885 | 41.923 | 45.642 | 48.29 | |
| 27 | 11.808 | 12.878 | 14.573 | 16.151 | 18.114 | 36.741 | 40.113 | 43.195 | 46.963 | 49.64 | |
| 28 | 12.461 | 13.565 | 15.308 | 16.928 | 18.939 | 37.916 | 41.337 42.557 | 44.461 45.722 | 48.278 49.588 | 50.99 | |
| 29 | 13.121 | 14.256 | 16.047 | 17.708 | 19.768 | 39.087 | 42.55/ | 45./22 | 47.588 | 52.33 | |

```
In [ ]: from scipy.stats import chi2
        import pandas as pd
        import numpy as np
        import math
        #F = 0.995 # cumulative to 1
        \#df = 1
        \#x = chi2.ppf(F, df) \# inverse of CDF
        #print(x)
        df=np.linspace(1, 29, 29)
        F=np.array([[0.995], [0.99], [0.975], [0.95], [0.9], [0.1], [0.05], [0.025], [0.01], [0.005]])
        x = chi2.ppf(1-F, df)
        A = pd.DataFrame(x)
        B=A.T
        B.columns=["0.995", "0.99", "0.975", "0.95", "0.9", "0.1", "0.05", "0.025", "0.01", "0.005"]
        B.index=[np.linspace(1, 29, 29)]
        file name = 'Chi2Table.xlsx'
        B.to_excel(file_name)
        #for i in F:
         # for j in df:
          \# x=chi2.ppf(1-i, j)
           # print(x)
```