## Labor Economics Homework 3 Due:

## 1. Estimation of McCall's Job Search Model

Recall our settings from homework 1. An unemployed worker solves the following Bellman equation:

$$v(w) = \max_{s} sw + (1-s) \left[\underline{c} + \rho \int v(w')F(dw')\right],$$

where *F* is the CDF of the wage offer distribution  $Beta(\alpha, \beta)$ .

- 1. Use the parameters in homework 1.3 to simulate the data for one period, i.e.,  $\{(w_i, s_i)\}_{i=1}^{1000}$ . Note that we do not observe the wage if  $s_i = 0$ .
- 2. Compute the mean wage among those who are employed. Is the mean wage you computed close with the mean wage in the distribution of wage offers? (Hint:  $X \stackrel{iid}{\sim} Beta(\alpha, \beta)$  implies  $\mathbb{E}[X] = \frac{\alpha}{\alpha + \beta}$ .)
- 3. Estimate the wage distribution parameters  $\alpha$  and  $\beta$  by MLE. (Hint: The observed wage follows a truncated beta distribution.)
- 4. We do know  $\underline{c} = 0.1$  since it is the unemployment benefit. Estimate  $\rho$ .

Solution. 1.1, 1.2, 1.4.

See the Julia code file.

Solution. 1.3.

Notice that the reservation wage  $\bar{w}$  is the threshold. The MLE estimator is

$$\underset{\alpha,\beta,\bar{w}}{\arg\max} \sum_{i=1}^{1000} s_i \log \frac{f(w_i;\alpha,\beta)}{1 - F(\bar{w};\alpha,\beta)} + (1 - s_i) \log F(\bar{w};\alpha,\beta),$$

where f is the PDF of the beta distribution and F is the CDF. Implementation is in the Julia code file.

## 2. Estimation of Crusoe's Coconuts Model

Recall our settings from homework 2. Crusoe solves the following Bellman equation:

$$v(y) = \max_{c} u(c) + \beta \int v(y') F(dy' \mid y, c),$$

where  $F(dy' \mid y, c)$  is the transition probability from y to y' given c, with the law of motion y' = zf(y-c),  $f(k) = k^{\alpha}$  and  $\log z \stackrel{iid}{\sim} N(0, \sigma^2)$ .

- 1. Use the parameters in homework 2.3 to simulate the time series data  $\{(y_t, k_t, c_t)\}_{t=1}^{200}$ .
- 2. Estimate the production process parameters  $\alpha$ ,  $\mu$  and  $\sigma$ .
- 3. Estimate  $\beta$  and  $\gamma$  by SMM. What moment conditions would you use?

Solution. 1.1, 1.2.

See the Julia code file.

Solution. 1.3.

I would use

$$\mathbb{E}[c_t - \hat{c}_t | y_t] = 0,$$

but you may use other moment conditions.