

## Phase Rule

1

- Rule given by J. Willard Gibbs.
- Iss rule ke help se hum predict kr skte hain effect of temp., pressure and conc. for a heterogeneous system.
- lekin ek aisa equillm jiske external effect nahi padta hain hi property ka jaise electrical forces, gravity, magnetic forces etc:- but that equillm is influenced by temp., pressure, and concentration. tab iss tarah ke jo bhi equillm honge woh phase rule follow krenge.

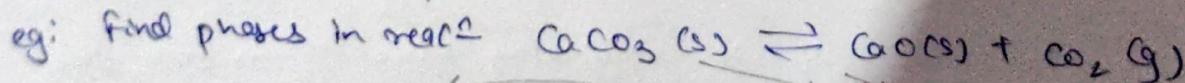
$$\text{i.e. } F + P = C + 2$$

where,  
 $F$  = no. of Degree of freedom  
 $P$  = no. of phase  
 $C$  = no. of component

### \* Phase (P) :-

- phase may be define as physically distinct, mechanically separable by such parts of system.

- eg:- ~~Ice (s)~~  $\rightleftharpoons$  water (l)  $\rightleftharpoons$  vapour (g)  
 isme 3 phases jo physically distinct hain, aur mechanically separable hain
- Solids:- Solid jiske baar batte hain separate phase banati hain. eg. Salt & sand  $\rightarrow$  dono solid hain aur physically distinct hain to 2 phase count hogा.
  - liquids:- liquids mein depend krega means agar dono liquid immiscible hain toh woh 1 phase form krenge aur if both liq. are immiscible then they form 2 phase.  
 eg. water & alcohol  $\rightarrow$  mix krenge to 1 phase banayenge
  - Gases:- gases nemasta 1 phase banati hain because atmospheric mein bahot sare gases ke molecules hote hain they are homogeneous unhe alog se identify nahi kr skte,  $\therefore$  gases always forms 1 phase.  $\hookrightarrow$  means they are not physically distinct
  - Solutions:- Solution separate phase banayenge. eg. agar sugar ko water mein dissolve krenge jab tak soln unsaturated hain tab tak sugar dissolve hogi aur humko 1 phase millega prajaise hi soln saturated hua  $\rightarrow$  then sugar dissolve hone band hoga degi aur sugar and ~~sugar~~ alog dikrege aur humko fir 2 phase millega.

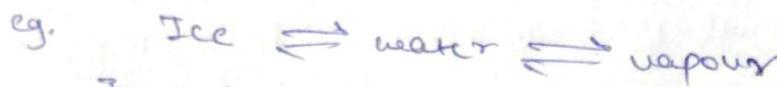


Ans) 3 phases  $\rightarrow$  solid, solid, gas.

Solid hamesha separate phase banata hain  $\therefore$  2 baat liye

### \* Component (c) :-

- Isi bhi system mein jithi bhi phase present hai unke chemical composition ko represent represent karne wali smallest no. is called component.



Isme ice, water & vapour ko  $H_2O$  se represent krsakte hai  
Ag. 3 phase ko represent karne k liye 1 chemical composition  
alga hai i.e.  $H_2O$  therefore it's 1 component system.

### \* Degree of freedom :-

- no' of intensive variable i.e temp., pressure & conc. jinko hum independently change kr skte, hamare equill<sup>m</sup> mein jo bhi phase hai usko bina disturb kiye, iss no' ko kہte hai degree of freedom.  
If  $f=0$ , the system is nonvariant  
 $f=1$ , then system is Unvariant  
 $f=2$ , then system is bivariant

### \* Advantages of phase rule :-

- 1) Phase rule helps in classifying various equill<sup>m</sup> in terms of no' of phase, no' of components & no' of degree of freedom.
- 2) we can predict the behaviour of any system with changes in the variable such as temp., pressure & conc.
- 3) Applicable to both physical & chemical equilibria.
- 4) The different system, which are having same value of degree of freedom, they would behave similarly.
- 5) It have extensive use in study of heterogeneous system, this rule is useful in metallurgy and provide useful info. about complex formation.

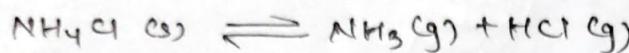
### \* Disadvantages of phase rule :-

1. Not easy to identify no' of phases, no' of components and no' of degree of freedom.
2. This rule apply only on simple equill<sup>m</sup> state and does not tell us about the no' of other possible equilibria present in system.
3. Phase rule deals with macroscopic study and it does not tell anything about molecular structure.
4. Phase rule does not give any info. regarding time taken for the system to attain equill<sup>m</sup>.

Q:- calculate no. of phases in given equill<sup>m</sup> !-

1.  $\text{CaCO}_3(s) \rightleftharpoons \text{CaO}(s) + \text{CO}_2(g)$   
3 phases - Solid, Solid, gas Solid homestha separate phase banate hai
2.  $\text{PCl}_5(s) \rightleftharpoons \text{PCl}_3(l) + \text{Cl}_2(g)$   
3 phases - 1 (solid), 1 (liq.), 1 (gas) gas homest single phase banate hai
3.  $2\text{CaSO}_4(s) \rightleftharpoons 2\text{CaO}(s) + 2\text{SO}_2(g) + \text{O}_2(g)$   
3 phases - solid, solid, gas.

\* calculate phase by component



phases - 2, (Solid, Gas) NH<sub>3</sub> aur HCl ka proportion same  
hi kota hai as NH<sub>4</sub> Cl so yeh equill<sup>m</sup>  
component - 1 (NH<sub>4</sub> Cl) hai taki is one component system.

If NH<sub>3</sub> or HCl present in excess - 2 component.

→ also system jiske component 1 ho

### \* Application of phase rule G-

- one component system - water system

we know that

$$F + P = C + 2$$

↗ F = no. of degree of freedom      C = no. of component

P = No. of phase

e.g. water system i.e.  $\text{Ice}(s) \rightleftharpoons \text{water}(l) \rightleftharpoons \text{Vapour}(g)$

In teeno system ko represent karne ke liye ek component

i.e.  $\text{H}_2\text{O}$  req. hai. ∴ it is one component system.

### phase diagrams-

- equill<sup>m</sup> mein jo bhi phases present hei unke behaviour ka complete description is called phase diagram.

eg: for one component system : toh yeh '1' ho jayega.

$$F + P = C + 2$$

$$F + P = 1 + 2$$

$$F = 3 - P$$

that will depend on system ki hamare.

↗ system mein kitni phase hai? usse hamari<sup>o</sup> degree of freedom calculate hogi.  
yahi calculate kerenge from phase diagram of water

If P=1, then F=2 → called Bivariant → mtlb humhe iss system ko completely describe karne ke liye 2 variables change

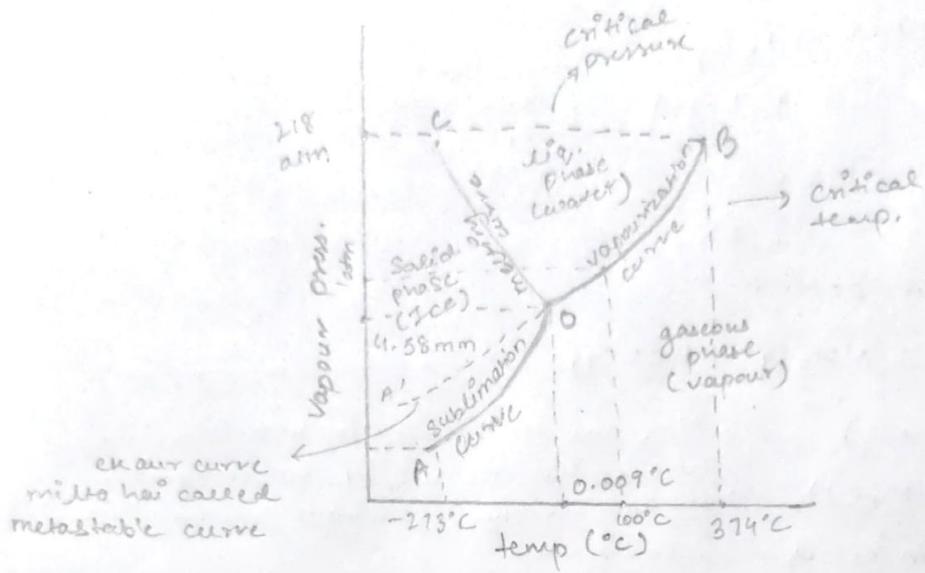
P=2, then F=1 → called univariant

↗ ek variable change woh temp., pressure ya concentration kuch bhi ho skta hai

P=3, then F=0 → called non variant

↓  
variables must be specified and fixed

# \* phase diagram of water system (4)



- phase rule apply kernege har area pr.

so, • Area

AOC - 1 phase i.e. Solid phase hai

AOB - 1 phase i.e. liq. gas. phase hai

BOC - 1 phase i.e. liq. phase hai

Now, w.k.t for one component system

$$f = 3-p \quad \text{yen } f = AOC, AOB \text{ aur } BOC$$

$$f = 2-1 \rightarrow f = 1 \rightarrow \text{ke liye 2 hi aye ga.}$$

that mean har area bivariant hai

mean har area mein jo bhi phase present hai usko maintain karna  
ke liye 2 variable req. honge i.e. temp. as well as pressure

Sublimation  
curve

- Curve :- total 3 curve hai  
curve OA - 2 (S, G) i.e. ice & gas.

$$OC - 2 (S, L)$$

$$OB - 2 (L, G) \quad \text{2 phase hai on}$$

w.k.t  $f = 3-p \rightarrow$  every curve  
 $= 3-2 \rightarrow f = 1 \rightarrow$

means every curve is  
univariant means hamare  
system ko describe kerne ke  
liye ek variable either press.  
or temp. seq. hai

- Point 'O' :- Yaha pe teeno curve aake mil rhe hai means  
teeno equilibrium methe hai. this pt. also called  
triple point. Yeh pt. humhe  $0.0098^{\circ}\text{C}$  aur  
 $4.58 \text{ mm}$  pressure pe milta hai

3 phase in equillibrium  $\rightarrow 3 (S, L, G)$

so,  $f = 3-p^3 \rightarrow f = 0$   $\rightarrow$  nonvariant hai mtlb agar hum kisi bhi  
ek variant ko const. karte hain to equillibrium  
mein se ek phase disappear ho jayegi

- metastable curve  $\xrightarrow{\text{solid}}$  vapour  
 Yaha pr ~~sol.~~ aur ~~solid~~ equill  $\rightleftharpoons$  mein hote hain  
 i.e. ~~solid~~  $\rightleftharpoons$  vapour

agar hum water ke freezing pt. i.e.  $0^{\circ}\text{C}$  se niche uss paani ko cool kerte rhe toh woh ice mein convert nhii hogi isko hum super cooled water bolte hain.

- metastable curve is also known as vapour pressure curve of super cooled water.  $\quad$  2 phase mai i.e. liq. & water

- Degree of freedom  $F = 3 - P$   
 $= 3 - 2$   
 $\boxed{F = 1}$

### • Tabular form :-

Curve / area / point	no. of phases	no. of phases	phases in equilibrium	Degree of freedom	System
Areas	AOC	1	Solid	$F = 3 - P$ $= 3 - 1$ $= 2$	Bivariant
	BOC	1	liq.		
	AOB	1	gaseous		
Curves	OA	2 (Sublimation)	Solid $\rightleftharpoons$ vapour	$F = 3 - P$ $= 3 - 2$ $= 1$	Univariant
	OB	2 (melting)	liq $\rightleftharpoons$ solid		
	OC	2 (Vapourisation)	vapour $\rightleftharpoons$ liq.		
Triple point	O	3	<del>S</del> $\rightleftharpoons$ l $\rightleftharpoons$ g	$F = 3 - 3$ $= 0$	Invariant
metastable curve	OA'	2	S $\rightleftharpoons$ g	$F = 3 - 2$ $= 1$	Univariant

\* Determine no. of phases and components in saturated and unsaturated salt / sugar soln :-

1. unsaturated salt / sugar soln :-

Salt soln :-



phase  $\rightarrow$  1 (soln)

component  $\rightarrow$  2 component system (NaCl & H<sub>2</sub>O)

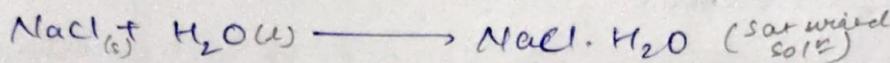
similarly for sugar soln

BS NaCl ke jagah sabse C<sub>6</sub>H<sub>12</sub>O<sub>6</sub> aa jayega.

Since yeh unsaturated soln he tohisme 1 phase present hogi.

2. Saturated Salt / sugar sol<sup>12</sup> :-

a) Saturated sol<sup>12</sup> at room temp. :-



Phase - 2 phases (sol<sup>12</sup>, solid)

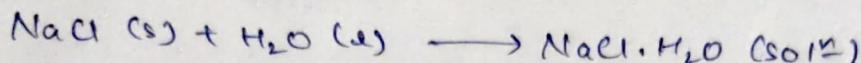
Component - 2 component (NaCl, H<sub>2</sub>O)

Since yeh saturated sol<sup>12</sup> hui toh yaha pr 2 phase show hogi.

Sugar ke case mein

NaCl ni jagah C<sub>6</sub>H<sub>12</sub>O<sub>6</sub> mil jati dete

b) Saturated sol<sup>12</sup> at boiling point :-



phases - 3 phases (solid, solution, vapour) water jab boil hogi toh obviously vapour mil jati.

component - 2 component (NaCl, H<sub>2</sub>O)

### \* One component system - Sulphur System

- Iske 4 phases system mein present hain

1. Rhombic sulphur (S<sub>R</sub>) also system jisme 2 or more solid state exist krti hain in equillm then it is called Polymorphic system

2. Monoclinic sulphur (S<sub>M</sub>)

3. liq. sulphur (S<sub>L</sub>) Inn chaaro phase ko represent karne ke liye ch chemical 'S' ki zarurat nahi. It is one component system.

4. Vapour sulphur (S<sub>V</sub>)

w.k.t

$$F + P = 2 + 1$$

$$F = 3 - P$$

4 phase no  
skhi hui

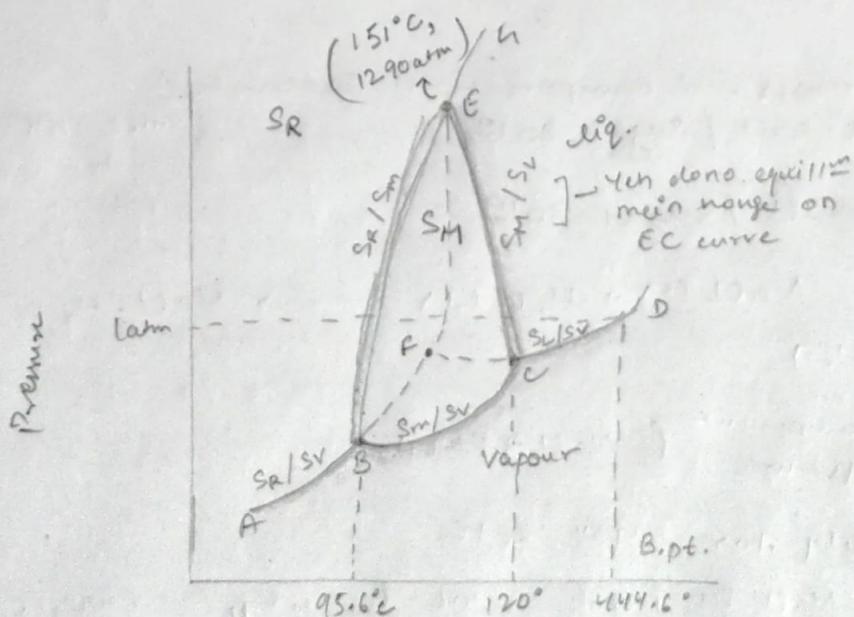
If P=1, then F=2  $\rightarrow$  Bivariant

P=2, then F=1  $\rightarrow$  univariant

P=3, then F=0  $\rightarrow$  Invariant

If P=4, then F=-1  $\rightarrow$  Not possible

kisi bhi system ke liye F = 3 - P  
nhii ho skta so not possible  
so kabhi bhi Sulphur system ke case mein chaaro phase equillm mein exist nhii ker skii only 3 phases can exist at a time in Sulphur system.



temp (°C)  $\rightarrow$

- Applying phase rule on every area.

so, area ABC (Rhombic Sulphur)	] - hara area mein ek phase present hai
BECB (monoclinic sulphur)	
GECD (liq. sulphur)	
ABCD (vapour phase)	

W.L.K.T  $F + P = C + 2$  means every area is bivariant and 2 variables i.e. temp & pressure required to locate any point.

$$\begin{aligned} F &= 3 - P \\ &= 3 - 1 = 2 \end{aligned}$$

- Curve :- total 6 curves

Curve AB - Vapour pressure curve of  $S_R$ ,  $S_R \rightleftharpoons S_v$

BC - " " " of  $S_M$ ,  $S_M \rightleftharpoons S_v$

CD - " " " of  $S_L$ ,  $S_L \rightleftharpoons S_v$

yeh humne effect

of press. on transition temp. ke liye

BE - Transition curve of  $S_R$  to  $S_M$ ,  $S_R \rightleftharpoons S_M$

LE - fusion curve of  $S_M$ ,  $S_M \rightleftharpoons S_L$

boare mein batata hai fab  $S_R$  curve

nota hai  $S_M$  mein transition curve :- curve BE mein  $S_R$  aur  $S_M$  2<sup>nd</sup> phase equilibrium

methe hai aur yeh transition curve hai of  $S_R$  to  $S_M$ .

also curve BE slopes away from pressure axis with transition temp. can be raise in increase in pressure.

- fusion curve :- curve LE mein monoclinic aur liq. sulphur exist kerti hai. It represent effect of pressure on melting point of S.M. melting point increases with increase in pressure. yaha pe yeh curve point E

se kuchh nota hai jiska with monoclinic sulphur its point se aage exist nhi kerti hai.

W.L.K.T  $F = 3 - P$

$\boxed{F = 1}$  (univariant)

means system ko describe karne ke liye ek variable req. hoi.

- points !-

Point B  $\rightarrow (95.6^\circ\text{C}, 0.006 \text{ mm}) \rightarrow S_R, S_M, S_v$

C  $\rightarrow (120^\circ\text{C}, 0.04 \text{ mm}) \rightarrow S_M, S_L, S_v$

E  $\rightarrow (151^\circ\text{C}, 1290 \text{ atm}) \rightarrow S_R, S_M, S_L$

yeh teeno equilibrium pr miliye on that pts.

W.L.K.T  $F = 3 - P$

$= 3 - 3 = 0 \rightarrow$  Invariant, means agar

temp. aur pressure mein chota sa bhi disturbance hote hai to ek phase disappear ho jayegi

• metastable curve G-

(i) Dashed curve BF - Vapour pressure curve of metastable  $s_R$ ;  $s_R \rightleftharpoons s_V$

(ii) Dashed curve CF - Vapour pressure curve of metastable supercooled liq. S.;  $s_L \rightleftharpoons s_V$

(iii) Dashed curve FE - Fusion curve of metastable  $s_R$ ; ( $s_R \rightleftharpoons s_L$ )

univariant  
 $f = 3 - P = 3 - 2$   
 $f = 1 \rightarrow$  univariant

• metastable triple point 'F'

$s_R \rightleftharpoons s_L \rightleftharpoons s_V$

• Tabular form G-

curve / Area /

Point

no. of phases

phase in equil $\infty$

Degree of freedom

System

Area

ABG

$s_R$

1

$f = 3 - P$

$= 3 - 1$

Bivariant

BECB

$s_M$

1

$= 2$

GECO

$s_L$

1

ABCD

$s_V$

1

curve

AB

$s_R \rightleftharpoons s_V$

2

BC

$s_M \rightleftharpoons s_V$

2

CD

$s_L \rightleftharpoons s_V$

2

$f = 3 - P$

$= 3 - 2$

Univariant

BE

$s_R \rightleftharpoons s_M$

2

$= 1$

CE

$s_M \rightleftharpoons s_L$

2

EG

$s_R \rightleftharpoons s_L$

2

metastable curve

BF

$s_R \rightleftharpoons s_V$

2

$f = 3 - P$

$= 3 - 2$

Univariant

CF

$s_L \rightleftharpoons s_V$

2

$= 1$

FE

$s_R \rightleftharpoons s_V$

2

$f = 3 - P$

$= 3 - 3$

Invariant

B

$s_R \rightleftharpoons s_M \rightleftharpoons s_V$

3

C

$s_M, s_L, s_V$

3

$f = 3 - P$

$= 3 - 3$

Triple point

E

$s_R, s_M, s_L$

3

$f = 3 - P$

$= 3 - 3$

metastable triple pt.  $\leftarrow F$

F

$s_R, s_L, s_V$

3

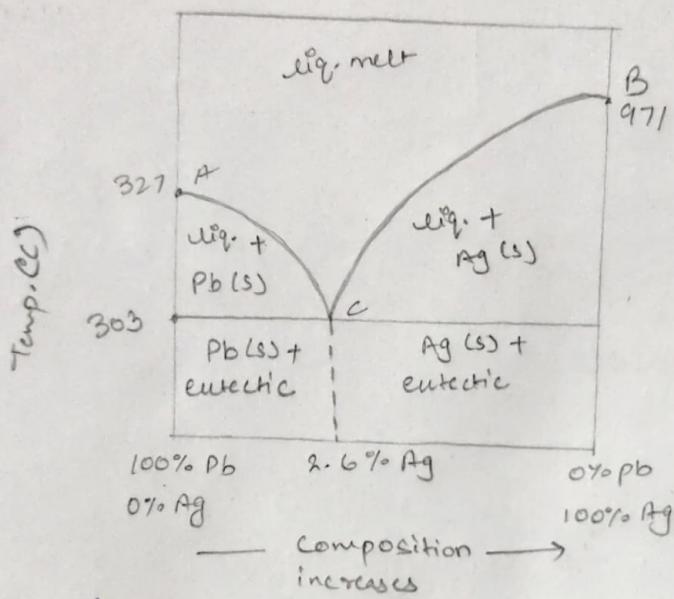
$f = 3 - P$

$= 3 - 3$

$= 20$

\* 2 component system - Pb & Ag

- 2 solids haiisme i.e. Pb, Ag
- Agar alone i.e. Pb aur Ag ko melt kare toh alone mix ho jaae na ache se i.e. they are miscible.
- But solid phase mein yeh alone immiscible hote hai. mtlb total 3 phases banenge  $\rightarrow$  solid + solid + melt
- melting point of Pb, Ag is different.
- Aisa system jism yeh above saari properties hoti hei wo eutectic system kehte hai.



• at const. pressure

AC - freezing pt. curve of Pb  $\rightarrow$  2phase  $\rightarrow$  so,  $F = 3 - P = 1$  (univariant)

BC - freezing " " " Ag  $\rightarrow$  2phase  $\rightarrow$  so,  $F = 1$  (monovariant)

pt. C - Eutectic point  $\rightarrow$  yaha pe teeno phase co-exist kerte hai  $\rightarrow$  3phases, so,  $F = 0$  (invariant)