

AC FUNDAMENTAL

AC :- Magnitude & direction changes wrt time.

(a)

IMPORTANCE OF AC

#

Power system :-

(a)

Generation \rightarrow 11 kV

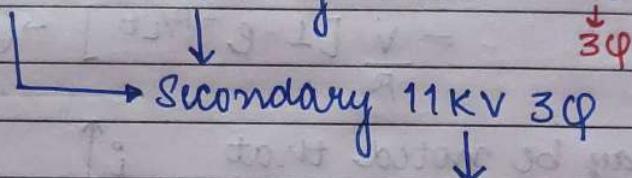
(b)

Transmission \rightarrow 132 kV, 66 kV

(c)

Distribution \rightarrow Primary (11 kV \downarrow 440 V) $\xrightarrow{\text{step down}}$ output

(d)



3φ

#

Secondary 11 kV 3φ

(a)

220 V 1φ / 440 V 3φ

(b)

$$(a) P = VI \cos \theta$$

\downarrow
 \downarrow
Const
vary

 $I \propto$ load

$$P = \text{const} \Rightarrow V \propto \frac{1}{I}$$

$V \uparrow \rightarrow I \downarrow \rightarrow \text{LOSSES} \downarrow$

(b) less cost & wt of wire bcs these quantities $\propto \frac{1}{I}$

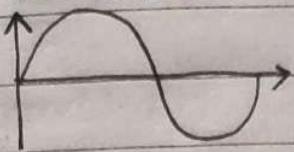
wt of wire \propto tower size \propto ckt breaker $\propto \frac{1}{I}$

Rating of appliances.

$I \downarrow$ hence these things are less

(c) Induction motor works on AC as DC motors cannot do heavy work. Induction motors are robust (no heating on heavy work)

(d) Natural zero break :- Shock prevention.



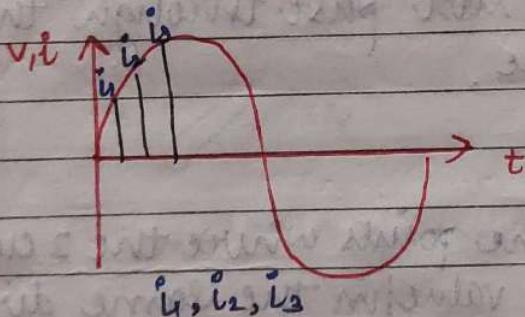
Adv of choosing sinusoidal wave form over other

- (a) produces less losses
- (b) ↓ Harmonics :- less Freq (undesirable)
- (c) ↓ Interferences with communication ckt.
- (d) ↓ noise

Important Terms.

(a) Waveform :- shape of the curve (V or I) when plotted against time.

(b) Instantaneous value :- value of quantity at any particular instant is called Instantaneous value



all instantaneous values are written in small letters

(c) Frequency (Hz) :- No. of cycles in 1 sec.

$$f = \frac{1}{T}$$

(d) Time Period (sec) :-

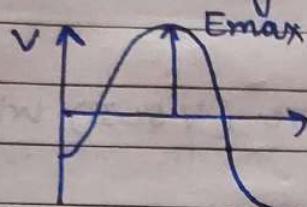
time taken to complete one cycle

(e) Cycle :- Set of all +ve & -ve instantaneous value is 1 cycle.

(f) Half cycle / Alternation :- Set of all +ve values \rightarrow +ve half cycle
Set of all -ve values \rightarrow -ve half cycle.

(g) Amplitude / Peak value / crest value / max value :-

The max mag (+ve / -ve) which an alternating qty attains during one cycle.

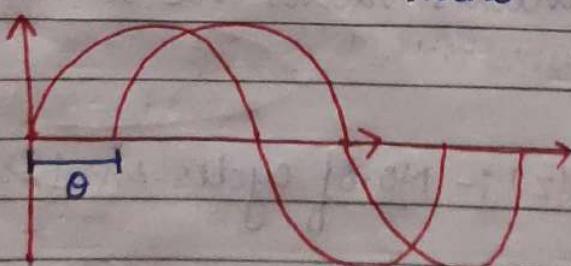


(h) Phase / Phase Angle :-

Fraction of T.P of alternating qty that has elapsed since the current last past through the zero position of reference.

(i) Phase difference :-

Angular dis b/w the points where the 2 curves cross the reference value/in the same dir. line



(j) Avg value :-

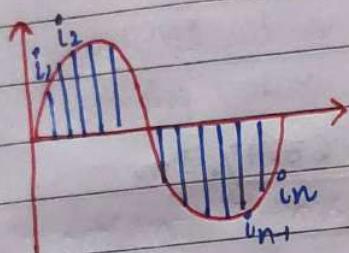
Sum of all instantaneous

Arithmetical avg of all inst. values considered of an alternating qty over one cycle.

$I_{av}, V_{av} \rightarrow \text{Representation}$

(k) Symmetrical Alt. q.ty :-
where +ve half cycle = -ve half cycle.

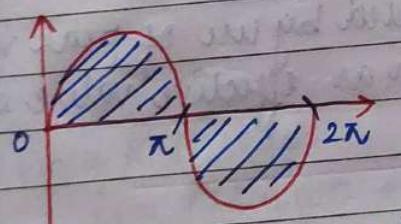
For sym. alt. q.ty, avg value = 0.



$$avg = \frac{i_1 + i_2 + \dots + i_{n-1} - i_n}{n} = 0$$

For unsymmetrical alt. q.ty, avg value $\neq 0$

⇒ Integral Calculus Method for Avg. value.



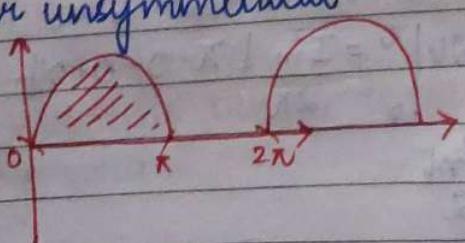
$$I_{av} = \frac{\text{Area of alternation}}{\text{base}}$$

Integration at home

For pure wave form :- we take for half cycle.
base half cycle

$$I_{av} = \frac{\int_0^{\pi} I_m \sin \theta}{\pi} = \frac{2 I_m}{\pi} = 0.637 I_m$$

For unsymmetrical



$$I_{av} = \frac{\int_0^{\pi} I_m (\text{wave eqn})}{2\pi}$$

limit :- Where we see actual waveform
base :- When next cycle start.

Q. Derivation of avg value of current

$$\begin{aligned} I_{av} &= \frac{1}{\pi} \int_0^{\pi} I_0 \sin \theta \, d\theta \\ &= \left[I_0 (-\cos \theta) \right]_0^{\pi} \\ &= \frac{2 I_0}{\pi} = 0.637 I_m = 63.7\% I_m \end{aligned}$$

Date 24 Dec, 2022

(e) Root mean square value :-

(written in capital letters)

$$V = V_m \sin \theta$$

All instruments, Ammeter, Voltmeter measure

RMS value. It is used for calculations.

(1) Protective devices are calculated by use of peak values.

(2) RMS values are also known as effective value & virtual value.

$$I_{rms} = \sqrt{\frac{1}{\pi} \int_0^{\pi} i^2 \, d\theta}$$

$$I_{rms}^2 = \frac{1}{\pi} \int_0^{\pi} I_m^2 \sin^2 \theta \, d\theta = \frac{I_m^2}{\pi} \int_0^{\pi} \sin^2 \theta \, d\theta$$

$$= \frac{I_m^2}{\pi} \int_0^{\pi} \left(\frac{1 - \cos 2\theta}{2} \right) \, d\theta = \frac{I_m^2}{2\pi} \int_0^{\pi} (1 - \cos 2\theta) \, d\theta$$

$$= \frac{I_m^2}{2\pi} \left| \theta - \frac{1}{2} \sin 2\theta \right|_0^{\pi} = \frac{I_m^2}{2\pi} | \pi - 0 - 0 + 0 |$$

$$I_{rms}^2 = \frac{I_m^2}{2}$$

Q1.

Ans

Q2.

(2)

(3)

(4)

$$\therefore I_{\text{rms}} = \frac{I_m}{\sqrt{2}} = 0.707 I_m$$

(m) Form factor :-

It is the ratio of RMS value of AC to Avg value of AC for pure sinusoidal wave.

$$F.F = \frac{\text{RMS value}}{\text{Avg value}} = \frac{0.707 I_m}{0.637 I_m}$$

$$K_f = F.F = 1.1$$

(n) Peak factor / crest factor / Amplitude factor :-

It is the ratio of peak value of AC qty to RMS value of AC qty

$$K_p = \frac{\text{Peak value}}{\text{RMS value}} = \sqrt{2} = 1.414$$

Q1. Find RMS value

$$i_2 = 12 \sin \omega t + 5 (\sin \omega t - 3\pi/2) + 8 + 24 (\sin \omega t - 5\pi)$$

$$\begin{aligned} \text{Ans. } I_{\text{rms}} &= \sqrt{\left(\frac{12}{\sqrt{2}}\right)^2 + \left(\frac{5}{\sqrt{2}}\right)^2 + 8^2 + \left(\frac{24}{\sqrt{2}}\right)^2} \\ &= \sqrt{\frac{973}{2}} = 486.5 \end{aligned}$$

Q2. A sinusoidal varying current AC of 50 Hz max value of 15A. Write eqn for instantaneous value.

(1) Current after 1200 sec.

(2) Find time taken to reach 10A for 1st time.

(3) Avg value.

A2:-

$$\nu = 60 \text{ Hz}$$

$$I_m = 15 \text{ A}$$

$$\omega = 2\pi\nu = 120\pi$$

(ii) $I_{t=0} = I_m \sin \omega t = 15 \sin(120\pi) \left(\frac{1}{200}\right) = 15 \sin\left(\frac{\pi}{5}\right)$
 $= 15 \sin(0.6) = 14.266$

(iii) $I_t = 10 = 15 \sin(120\pi t)$

$$\sin^{-1}\left(\frac{2}{5}\right) = 120\pi t = \frac{\sin^{-1}(2/5)}{120\pi} = t$$

(iv) Avg value = $\frac{2(15)}{\pi} = 9.55 \text{ A}$

i) Instantaneous current = $i = 15 \sin 120\pi t$

Q3. An AC source sinusoidal has current RMS value of 40A at 50Hz frequency. Write the expression of

(i) Instantaneous Current

(ii) Current at 0.02 sec after passing through max +ve value.

A3. $I_{RMS} = 40 \text{ A}$; $\nu = 50 \text{ Hz}$

$$I_m = I_{RMS} \Rightarrow I_m = \sqrt{2} I_{RMS} = \sqrt{2}(40) = 40\sqrt{2} \text{ A}$$

$\sqrt{2}$

$$\omega = 2\pi\nu = 100\pi$$

$$i = I_m \sin \omega t$$

$$= 40\sqrt{2} \sin 100\pi t$$

HW ques Half Wave Rectifier Form factor: 1.57 (Derivation)

Q1. Peak form factor for half wave.

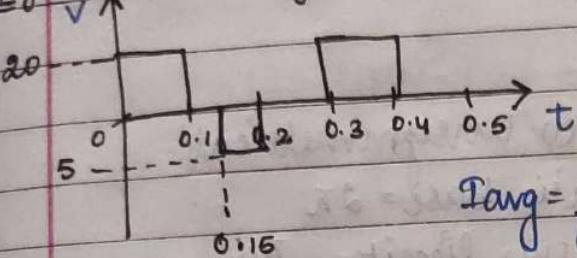
$$40\sqrt{2} = 40\sqrt{2} \sin 100\pi t$$

$$\pi/2 = 100\pi t \quad t = 1/200$$

$$t = 1/200 + 0.02 = 0.07$$

$$40\sqrt{2} \sin 7\pi = I_{req} = 0$$

Q4. Find Average & RMS value



$$I_{avg} = \frac{1}{T} \left[\int_0^{0.1} 20 dt + \int_{0.1}^{0.2} -5 dt \right]$$

$$I_{avg} = \frac{1}{0.5} \left[20t \Big|_0^{0.1} + (-5t) \Big|_{0.1}^{0.2} \right]$$

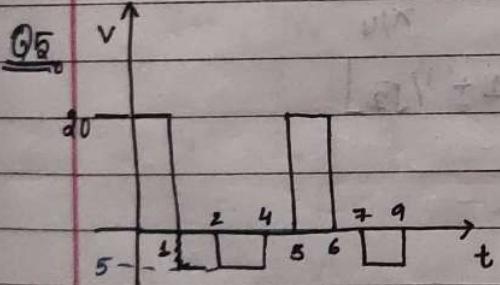
$$= \frac{10}{3} \left[20(0.1) - (5(0.2) - 5(0.15)) \right]$$

$$= \frac{10}{3} [2 - (1 - 0.75)] = \frac{10}{3} \times 1.75 = \frac{17.5}{3} = I_{avg}$$

-: I rms at end :-

Date:- 28 DEC, 2022

Find Avg & RMS value.



$$V_{avg} = \frac{1}{T} \int V(t) dt$$

$$= \frac{1}{6} \left[\int_0^1 (20 \cdot dt) + \int_2^4 (-5 \cdot dt) \right]$$

$$= \frac{1}{6} \left[20t \Big|_0^1 - 5t \Big|_2^4 \right]$$

$$= \frac{1}{6} [20(1) - 20(0) - (5(4) - 5(2))]$$

$$= \frac{1}{6} [20 - 10] = \frac{10}{6}$$

$$RMS = \sqrt{(V_{avg})^2} = \sqrt{\frac{1}{5} \left[\int V(t)^2 dt \right]}$$

$$= \sqrt{\frac{1}{5} \left[\int_0^1 (20^2 dt)^2 + \int_2^4 (5^2 dt)^2 \right]}$$

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xx 0/15 3

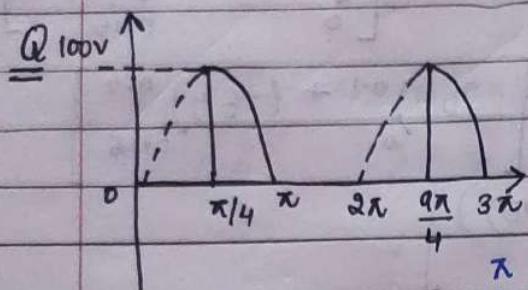
100
26 4

$$\frac{\theta}{t} = \omega$$

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$$\sqrt{\frac{1}{5} \left(\int_0^1 400(t) + 25t \right)_4^2}$$

$$= \sqrt{\frac{1}{5} (400 + 50)} = \sqrt{\frac{450}{5}} = \sqrt{90}$$



- (i) unsymmetrical
- (ii) base = 2π
- (iii) limit = $\pi/4 \rightarrow \pi$

$$V_{avg} = \frac{1}{2\pi} \int_{\pi/4}^{\pi} 100 \sin(\omega t) dt \quad \begin{matrix} \omega t \rightarrow 0 \\ dt \rightarrow d\theta \end{matrix}$$

$$= \frac{1}{2\pi} (100) \left[-\cos \theta \right]_{\pi/4}^{\pi} \\ = \frac{100}{2\pi} \left[-1 + \frac{1}{\sqrt{2}} \right]$$

$$= 27.18$$

$$V_{rms} = \sqrt{\frac{1}{2\pi} \int (100)^2 (\sin \theta)^2 d\theta} \quad 2\sin^2 \theta = 1 - \cos 2\theta$$

$$= \sqrt{\frac{10000}{2\pi} \int_{\pi/4}^{\pi} \sin^2 \theta d\theta}$$

$$= \sqrt{\frac{10000}{4\pi} \int_{\pi/4}^{\pi} (1 - \cos 2\theta) d\theta}$$

$$= \sqrt{\frac{2500}{\pi} \left[\theta - \frac{\sin 2\theta}{2} \right]_{\pi/4}^{\pi}}$$

put $\pi = 3.14$

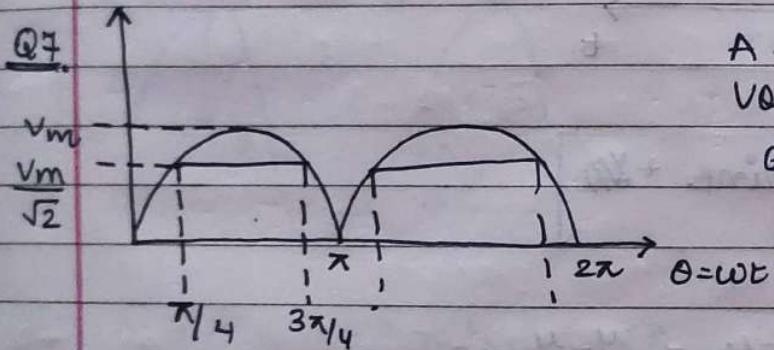
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$$= \sqrt{\frac{2500}{\pi}} \left[\frac{\pi - \sin \frac{\pi}{4}}{2} - \frac{\pi}{4} + \frac{\sin 2(\pi/4)}{2} \right]$$

$$= \sqrt{\frac{2500}{\pi}} \left[\frac{3\pi}{4} + \frac{1}{2} \right]$$

$$= \sqrt{\frac{3(25)(100)^2}{4} + \left(\frac{2500}{\pi} \right) \left(\frac{1}{2} \right)}$$

$$= \sqrt{1875 + 398.08} = \sqrt{2,273.08} = 47.67$$



A full Rectified Sinusoidal Voltage clipped at $1/\sqrt{2}$ of its max value.

$$V_{avg} = \frac{1}{\pi} \left[\int_0^{\pi/4} V_m \sin \theta d\theta + \int_{\pi/4}^{3\pi/4} V_m d\theta + \int_{3\pi/4}^{\pi} V_m \sin \theta d\theta \right]$$

$$= \frac{1}{\pi} \left[V_m \left[-\cos \theta \right]_0^{\pi/4} + V_m \left[\theta \right]_{\pi/4}^{3\pi/4} + V_m \left[-\cos \theta \right]_{3\pi/4}^{\pi} \right]$$

$$= \frac{1}{\pi} \left[-V_m \left[\cos \frac{\pi}{4} - \cos 0 \right] + V_m \left[\frac{3\pi}{4} - \frac{\pi}{4} \right] + V_m \left[\cos \pi - \cos \frac{3\pi}{4} \right] \right]$$

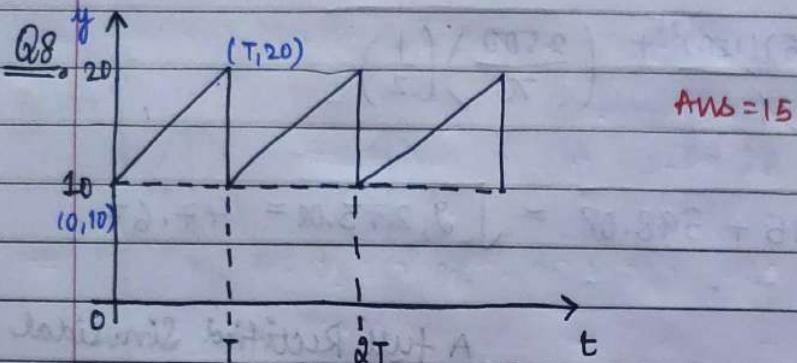
$$= \frac{1}{\pi} \left[-V_m \left[\frac{1 - \frac{\sqrt{2}}{2}}{\sqrt{2}} \right] + V_m \left[\frac{\pi}{2} \right] - V_m \left[-1 - \left(-\frac{1}{\sqrt{2}} \right) \right] \right]$$

$$= \frac{1}{\pi} \left[-V_m \left[\frac{1 - \sqrt{2}}{\sqrt{2}} \right] - V_m \left[\frac{-1 + 1}{\sqrt{2}} \right] + \frac{V_m \pi}{2\sqrt{2}} \right]$$

$$= \frac{1}{\pi} \left[-2V_m \left[\frac{1 - \sqrt{2}}{\sqrt{2}} \right] + \frac{V_m \pi}{2\sqrt{2}} \right] = V_m \left[\frac{-2 \left(1 - \frac{\sqrt{2}}{2} \right) + \frac{\pi}{2}}{2\sqrt{2}} \right]$$

$$V_m \left(\frac{(-0.636)(-0.414)}{1.414} + 0.353 \right)$$

$$V_m (0.186 + 0.353) = V_m (0.54)$$



$$y_{avg} = \frac{1}{T} \int_0^T [y_{line} + y_{sp}]$$

$$\text{eqn of line} \Rightarrow \frac{y_2 - y_1}{x_2 - x_1} = \frac{y - y_1}{x - x_1}$$

$$\frac{20 - 10}{T - 0} = \frac{y - 10}{x - 0}$$

$$\frac{10}{T} = \frac{y - 10}{x}$$

$$10x = yT - 10T$$

$$10(t) = yT - 10T \quad (x=t)$$

$$\frac{10(t) + 10(T)}{T} = y$$

$$y = \frac{10t}{T} + 10$$

$$y_{avg} = \frac{1}{T} \int_0^T \left[\left(\frac{10t}{T} + 10 \right) dt + \int_0^T 10 dt \right]$$

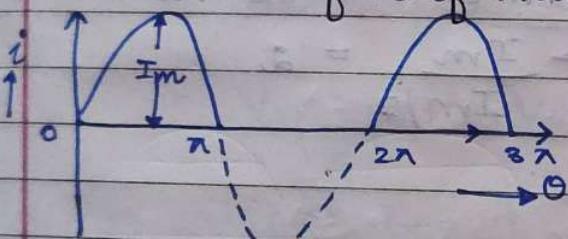
$$\frac{1}{T} \left[\int_0^T \left(\frac{10t}{T} \right)^2 dt + \int_0^T 10 \right]$$

$$\frac{1}{T} \left[\frac{10}{T} \left(\frac{t^2}{2} \right)_0^T + 10T \right]$$

$$\frac{1}{T} \left[\frac{10}{T} \left(\frac{T^2}{2} \right) + 10T \right]$$

$$5 + 10 = 15$$

RMS value of Half Wave Rectifier



$$I_{RMS} = \sqrt{\frac{1}{2\pi} \int_0^\pi I_m^2 \sin^2 \theta d\theta}$$

$$= \sqrt{\frac{I_m^2}{2\pi} \int_0^\pi \left[\frac{1 - \cos 2\theta}{2} \right] d\theta}$$

$$= \sqrt{\frac{I_m^2}{2\pi} \left(\frac{\theta}{2} + \frac{\sin 2\theta}{4} \right)_0^\pi}$$

$$= \frac{I_m}{2} \sqrt{\frac{1}{\pi} \left(\pi - \frac{\sin 2\pi}{2} - 0 - \frac{\sin 0}{2} \right)}$$

$$I_{RMS} = \frac{I_m}{2}$$

AVERAGE VALUE OF HALF WAVE RECTIFIER :-

$$I_{av} = \frac{1}{2\pi} \int_0^\pi I_m \sin \theta d\theta$$

$$= \frac{I_m}{2\pi} \left[-\cos \theta \right]_0^\pi = \frac{I_m}{\pi}$$

FORM FACTOR OF HALF WAVE RECTIFIER :-

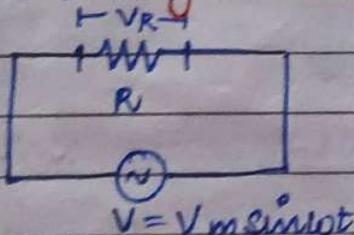
$$F.F = \frac{\text{RMS value}}{\text{Avg value}} = \frac{I_m/2}{I_m/\pi} = \frac{\pi}{2} = 1.57$$

PEAK FORM FACTOR OF HALF WAVE RECTIFIER

$$P.F = \frac{\text{Peak value}}{\text{RMS value}} = \frac{I_m}{I_m/2} = 2$$

Date :- 29 Dec, 2022.

AC through Pure RESISTIVE CIRCUIT



$$\text{Voltage} = V_m \sin \omega t = v - 2$$

$$\text{instantaneous current} = i$$

$$\text{V drop across R is } V_R = iR - 1$$

$$\text{for equilibrium } i = 2$$

$$V_R = iR = V_m \sin \omega t$$

$$i = \frac{V_m}{R} \sin \omega t$$

$$\text{for } \sin \omega t = 1 \quad i = \frac{V_m}{R} = I_m$$

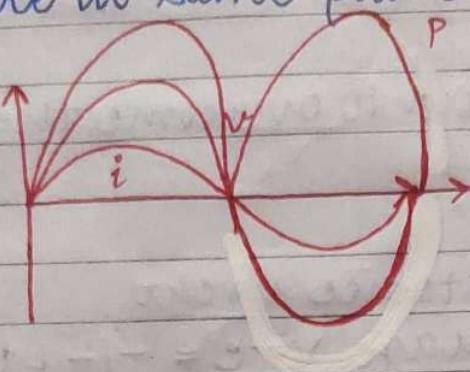
$$i = I_m \sin \omega t - 3$$

Comparing ② & ③

$$\text{for } v = V_m \sin \omega t$$

$$i = I_m \sin \omega t$$

v, i are in same phase. for only R ckt



$$\begin{aligned}
 \text{Instantaneous power} &= v i = P \\
 &= (V_m \sin \omega t)(I_m \sin \omega t) \\
 &= V_m I_m \sin^2 \omega t \\
 &= V_m I_m \left(\frac{1 - \cos 2\omega t}{2} \right) \\
 &= \frac{V_m I_m}{2} - \frac{V_m I_m \cos 2\omega t}{2} \quad \text{variable.} \quad (4)
 \end{aligned}$$

For average power.

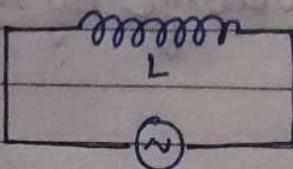
over complete cycle, the variable part in 4 is zero. we are left with only $\frac{V_m I_m}{2}$

$$P = \frac{V_m I_m}{2} = \frac{V_m}{\sqrt{2}} \frac{I_m}{\sqrt{2}} = V_{rms} \cdot I_{rms}$$

$$P_{avg} = V \cdot I$$

- (a) Power is always +ve and the expression of power is $V_{rms} I_{rms}$. Unit = Watts
- (b) NO part of power cycle becomes -ve at any time. and power is never zero in purely resistive ckt.

AC through purely INDUCTIVE CIRCUIT



$V = V \sin \omega t$
when an alternating voltage

all this voltage is used to overcome the self induced emf. $e = -L \frac{di}{dt}$

As there is no resistance in ckt.

$$\text{Hence applied voltage } V = -e = -\left(-L \frac{di}{dt}\right) = L \frac{di}{dt}$$

$$V_m \sin \omega t = L \frac{di}{dt}$$

$$\int di = \frac{V_m}{L} \sin \omega t dt$$

$$I = \frac{V_m}{\omega L} \sin(\omega t - \pi/2)$$

$$I = \frac{V_m}{X_L} \sin(\omega t - \pi/2)$$

$\omega L = X_L$ = Inductive reactance = Ω

Inductive reactance is the resistance offered by inductor to alternating current

for $\sin(\omega t - \pi/2)$

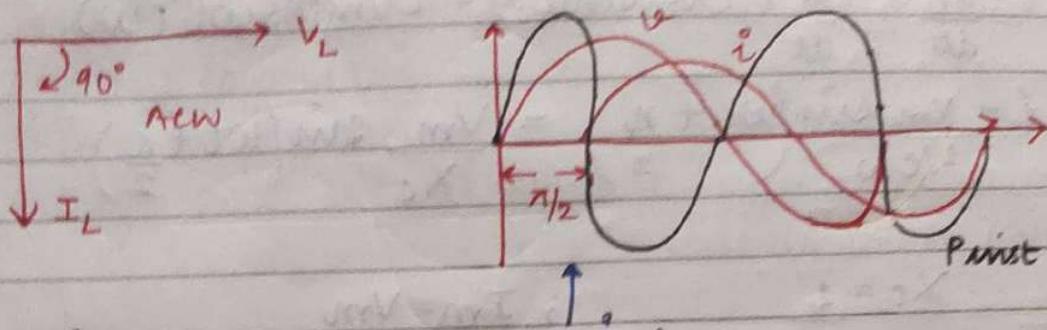
$$i = \frac{V_m}{X_L} = I_m$$

For a L ckt

$$V = V_m \sin \omega t$$

$$i = I_m \sin(\omega t - \pi/2)$$

current lags the applied voltage by $\pi/2$



(Jiska Max phile vo leading)

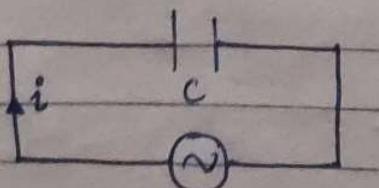
$$\begin{aligned}
 \text{Instantaneous Power} &= V \cdot i \\
 &= (V_m \sin \omega t) (I_m (\sin \omega t - \frac{\pi}{2})) \\
 &= -V_m I_m \sin \omega t \cos \omega t \\
 &= -\frac{V_m I_m}{2} \sin 2\omega t \rightarrow \text{fluctuating (variable)}
 \end{aligned}$$

Avg Power = 0

In a pure Inductive & capacitive ckt, average power across full cycle is zero.
(NO consumption of Power in pure L & C in avg but at instant it consumes power).

Power system

AC through Pure Capacitive Alone



$$V = V_m \sin \omega t$$

$$\text{Let } V = V_m \sin \omega t$$

V = pot. diff across plates

q = charge on plates

$$q = CV$$

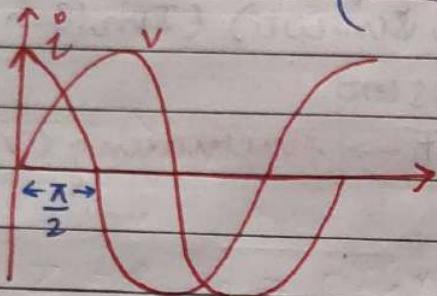
$$= C V_m \sin \omega t$$

$$i = \frac{dq}{dt} = \frac{d}{dt} (C V_m \sin \omega t) = C V_m \cos \omega t (\omega)$$

$$i = \frac{V_m \cdot \sin(\omega t + \frac{\pi}{2})}{X_C} = \frac{V_m}{X_C} \sin(\omega t + \frac{\pi}{2})$$

$$X_C = \frac{1}{\omega C} ; I_m = \frac{V_m}{X_C}$$

$$i = I_m \sin(\omega t + \frac{\pi}{2})$$



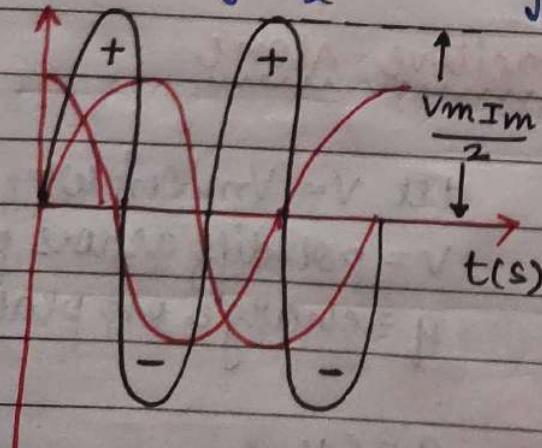
Instantaneous Power

$$P = Vi = (V_m \sin \omega t) (I_m \sin(\omega t + 90^\circ))$$

$$= V_m I_m \sin \omega t \cos \omega t$$

$$= \frac{1}{2} V_m I_m \sin 2\omega t$$

$$\text{Power avg} = \frac{1}{2} V_m I_m \int_0^{2\pi} \sin 2\omega t dt = 0$$



1 Horse power = 786 Watt

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POWER SYSTEM

(i) Apparent Power (S)

It is given by the product of rms values of applied voltage and circuit current.

$$\therefore S = VI = (IZ) \cdot I = I^2 Z = \text{volt amperes (VA)}$$

(ii) Active / Real Power (P)

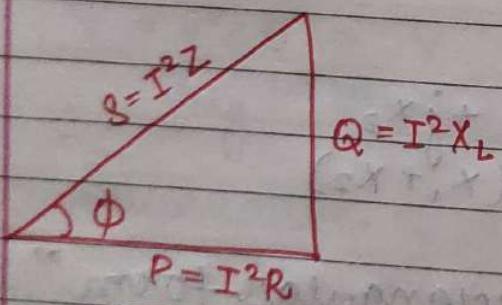
It is the power which is actually dissipated by circuit Resistance.

$$P = I^2 R = VI \cos \phi = \text{Watt}$$

(iii) Reactive Power (Q)

It is the power developed in the inductive reactance of the circuit / capacitance reactance (consume in one half cycle, give back in other half cycle)

$$Q = I^2 X_L = I^2 \cdot Z \sin \phi = I \cdot (IZ) \sin \phi = VI \sin \phi \\ = \text{volt-amperes-reactive.}$$



$$S^2 = P^2 + Q^2$$

$$S = \sqrt{P^2 + Q^2}$$

$$\cos \phi = \frac{P}{S}$$

Q4. continue

$$I_{rms} = \sqrt{\frac{10}{3} \left[\int_0^{0.1} 400 dt + \int_{0.15}^{0.2} 25 dt \right]}$$

$$= \sqrt{\frac{10}{3} \left(400 \times \frac{0.1}{10} + 25 \left(\frac{0.5}{10} - \frac{0.15}{100} \right) \right)} \\ = \sqrt{\frac{10}{3} (40 + 5 - 3.75)} = \sqrt{137.5} \text{ A}$$

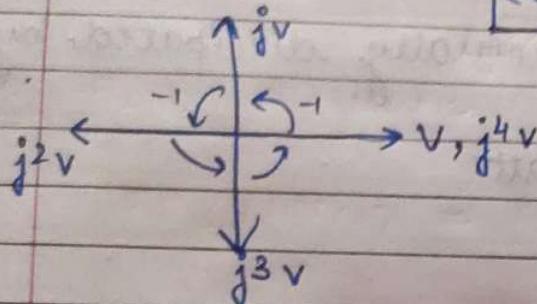
Mathematical Representation of phasors

(A) Rectangular form

$$j^2 = -1$$

$$j = \sqrt{-1}$$

$$Z = R + jX$$



$$Z = a + jb = R + jX$$

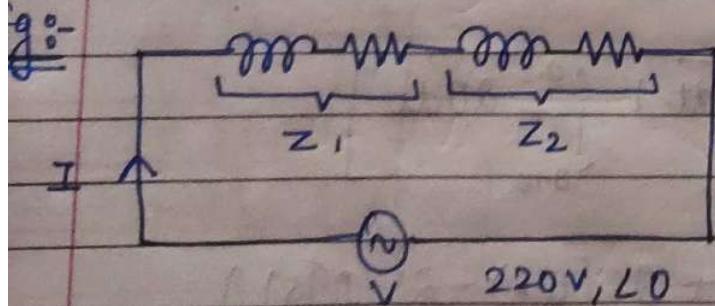
a = Real part

b = Imaginary part

$$Z_1 = R_1 + jX_1 ; Z_2 = R_2 + jX_2$$

$$Z_1 + Z_2 = (R_1 + R_2) + j(X_1 + X_2)$$

"Add/Sub we go it in Rectangular form"



$$\text{net Impedance} = Z_1 + Z_2$$

$$|Z| = \sqrt{R^2 + X^2}$$

$$\tan \phi = \frac{X}{R}$$

(B) TRIGONOMETRICAL FORM

$$\text{Real part } = a = V \cos \phi$$

$$\text{Imag. part } = b = V \sin \phi$$

$$\vec{V} = V \cos \phi + V j \sin \phi$$

$$\vec{V} = V (\cos \phi + j \sin \phi)$$

(C) Exponential form

$$e^{j\phi} = \cos \phi + j \sin \phi$$

$$e^{-j\phi} = \cos \phi - j \sin \phi$$

$$e^{j(\phi+\theta)} = \cos(\theta+\phi) + j \sin(\theta+\phi)$$

(D) Polar form

$$\vec{V} = V \angle \theta = V \angle -\theta$$

↓ mag → Phase ∠.

"Multiplication of phasors" "Divide of phasors".

$$A \angle \theta, B \angle \alpha$$

$$A \cdot B = AB \angle (\theta + \alpha)$$

$$\frac{A}{B} = \frac{A}{B} \angle (\theta - \alpha)$$

Q. $Z = 3 + j5 ; V = 220V, \angle 0 ; I = ?$

Ans. $I = \frac{V}{Z}$

$$|Z| = \sqrt{3^2 + 5^2} = 4Y \quad \theta = \tan^{-1} \left(\frac{5}{3} \right)$$

$$Z = 4Y \angle 0, V = 220 \angle 0$$

$$\text{coil} = R + jX_L$$

Lead & Lag

CLASSTIME Pg. No.
Date / /

$$I = \frac{220}{Y} L(0 - \theta)$$

$A L \theta \rightarrow n^{\text{th}} \text{ power}$

$$A^n L n \theta$$

$$n^{\text{th}} \text{ root } A^{\frac{1}{n}} \angle \frac{\theta}{n}$$

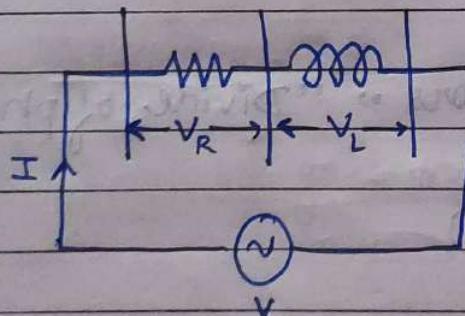
Eg:- $5 L 60^\circ, 4^{\text{th}} \text{ power}$

$$5^4 \angle (4)60^\circ = 625 \angle 240^\circ$$

$$4^{\text{th}} \text{ root} = (5)^{\frac{1}{4}} \angle \frac{60^\circ}{4} = \sqrt[4]{5} \angle 15^\circ$$

R-L Series Circuit :-

R-L series :- coil



$$V = \sqrt{V_R^2 + V_L^2} = \sqrt{(IR)^2 + (IX_L)^2}$$

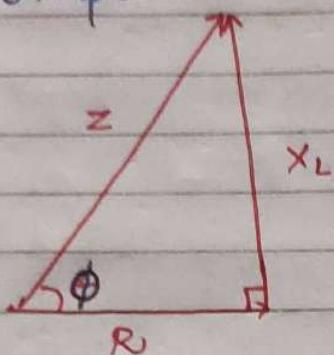
$$V = I \sqrt{R^2 + X_L^2}$$

$$\frac{V}{I} = Z = \sqrt{R^2 + X_L^2}$$

$$\text{Impedance} = \sqrt{R^2 + X_L^2}$$

$$\tan \theta = \frac{X_L}{R} = \frac{\omega L}{R}$$

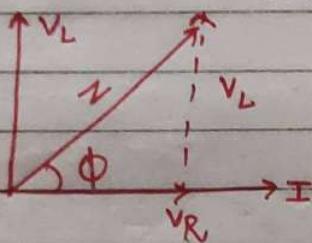
Impedance Δ ,



$$\cos \phi = \frac{R}{Z} = \frac{\text{Resistance}}{\text{Impedance}}$$

$$0 \leq \cos \phi \leq 1$$

bcs base ckt's are pure Resistive ($\cos \phi = 1$) and pure Inductive/Capacitive ($\cos \phi = 0$)



Applied V & I are not in phase
 I is lagging V by ϕ with V .

$$\text{if } V_m \sin \theta = V \\ I = I_m \sin(\theta - \phi)$$

$$P = VI = V_m \sin \theta \times I_m \sin(\theta - \phi) \\ = V_m I_m \sin \theta \sin(\theta - \phi)$$

$$= \frac{V_m}{\sqrt{2}} \frac{I_m}{\sqrt{2}} \cos \phi - \frac{V_m}{\sqrt{2}} \frac{I_m}{\sqrt{2}} \cos(\omega t - \phi)$$

$$P = P_{avg} = \frac{V_m}{\sqrt{2}} \frac{I_m}{\sqrt{2}} \cos \phi = V_{rms} I_{rms} \cos \phi$$

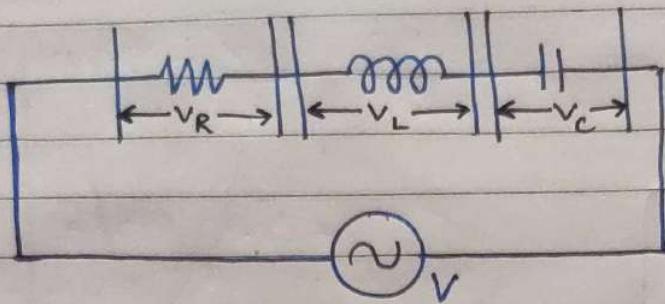
$$P = VI \cos\phi = \frac{VI \cdot R}{Z} = \frac{V \cdot I \cdot R}{Z} = I^2 R \text{ Watt}$$

Power is only consumed by ckt.

R-C series circuit

#

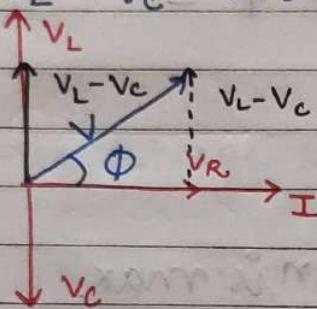
R-L-C Series Circuit



$V_L > V_C \Rightarrow$ Inductive ckt

$V_L < V_C \Rightarrow$ Capacitive ckt

FOR $V_L > V_C$



I lags applied voltage by ϕ angle

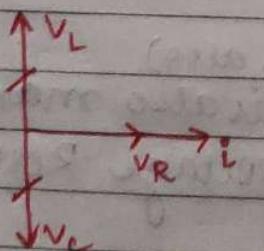
$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

SERIES RESONANCE :-

Condition :- $X_L = X_C$ or $V_L = V_C$

Resonance :- Any ac circuit which behaves like purely resistive circuit i.e. V & I are in same phase, i.e. net reactive component of circuit is zero.

$$V_L - V_C = 0$$



Total voltage is around resistive part of ckt.
V is in phase with I.
 $V_R = V$

At Resonance

$$V_L = V_C$$

$$I X_L = I X_C$$

$$X_L = X_C$$

$$\omega L = \frac{1}{\omega C}$$

$$\omega^2 = \frac{1}{LC}$$

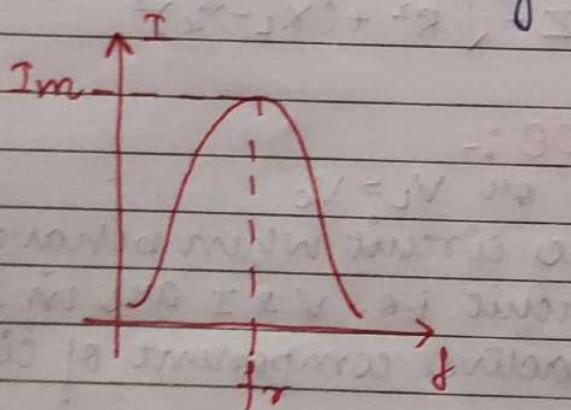
$$f = \frac{1}{2\pi\sqrt{LC}}$$

→ As VR is in phase with $\text{I} \rightarrow \cos \phi = 1$

$$\rightarrow Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$Z = R$$

→ Current at Resonating cond'n is max.



Radio & Communication
ckt Applications.

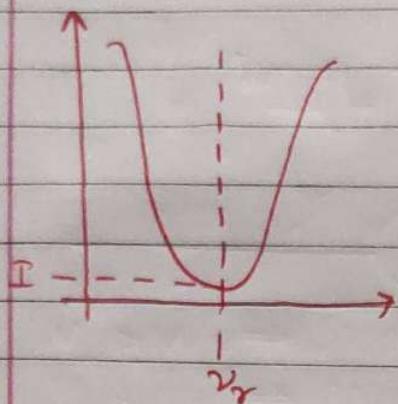
(Voltage Magnification ckt)

Series resonance is also called Voltage Resonance
& acceptor circuit.

Voltage across each component is also maximum
(L, C also)
with current hence called Voltage Resonance

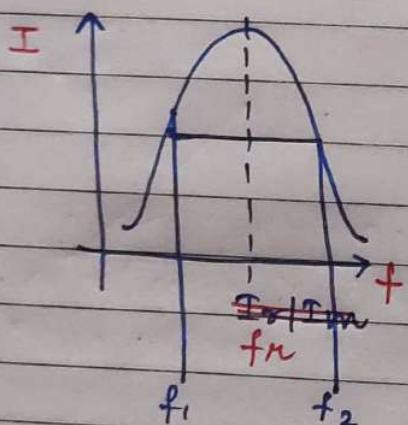
As ckt accepts max current from the ckt
It is acceptor circuit.

Parallel Resonance (current / rejec^ttor resonance)



BANDWIDTH :-

The range of freq where $I = 70.7\% \cdot I_{max}$



$$BW = f_2 - f_1$$

f_1 & f_2 are half power points
Power drawn is half at
these points.

$$f_r = \sqrt{f_1 f_2}$$

Q-factor (Quality factor of coil) :-

Q-factor = $\frac{\text{V developed across } L \text{ or } C}{\text{Applied voltage}} = \frac{I_r X_L}{I_r R} = \frac{1}{R} \sqrt{\frac{L}{C}}$

(Der.)

$\frac{Q_r}{B_r}$, Resonating frequency
Bandwidth

Q factor decides designing of coil
It does not depend upon frequency.