

## CLASS TEST

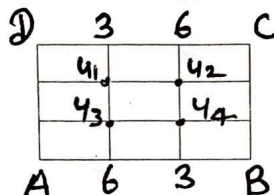
Third Semester, Dec. 2023

Paper Code: ES- 201

Subject: Computational Methods

Time: 1 Hrs.

Max. Marks ; 30

**Note : Attempt Q.No. 1 Which is compulsory and any two more questions from remaining.**Q1. (a) Find  $u_1, u_2, u_3$  and  $u_4$  initially for  $u_{xx} + u_{yy} = 0$  with the help of the figure. (3) CO4

(b) Solve the system of equation by Gauss elimination method

$$2x - y + 3z = 9, x + y + z = 6, x - y + z = 2 \quad (4) \quad \text{CO3}$$

(c) Given  $\frac{dy}{dx} = \frac{y-x}{y+x}$ , with the initial condition  $y=1$  at  $x=0$ . Find  $y$  for  $x=0.1$  and  $x=0.2$  (3) CO4

Using Euler's method.

Q2. Solve the following system of equation by Cholesky's method (10) CO3

$$x + y + 3z = 6, x + 5y + 5z = 20, 3x + 5y + 19z = 106$$

Q3. By using Runge- Kutta fourth order method to find  $y$  for  $x=0.1$  in step of  $h = 0.1$  if  $\frac{dy}{dx} = x + y^2$ , Given that  $y(0) = 1$ . (10) CO4

Q4. Find the value of  $u(x, t)$  satisfying the parabolic equation  $\frac{\partial u}{\partial t} = 4 \frac{\partial^2 u}{\partial x^2}$  and the boundary

conditions  $u(0, t) = 0, u(8, t) = 0$ , and  $u(x, 0) = 4x - \frac{1}{2}x^2$  at the points  $x = i; i = 0, 1, 2, 3, 4 \dots$  and

$t = \frac{1}{8}j : j = 0, 1, 2, 3, 4, 5$ . (10) CO4