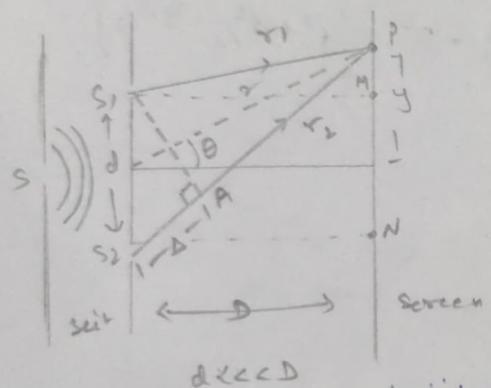
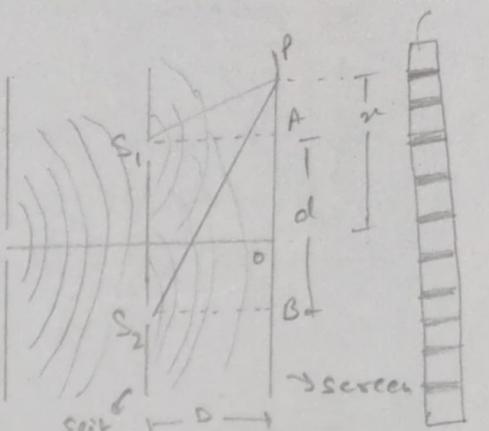


## \* Young's Double Slit exp. :-

- Monochromatic light used with same wavelength for mega.
- Fir yeh light wave 2 slits se jazab hain
- Two waves interfere and equally spaced bright & dark bands are formed on screen.

Note:- centre mein hamseh bright fringe banegi kyunki Slit 1 and Slit 2 jo rays travel kengi unko centre mein Jane ke liye same dist. travel kerna padega iska mtlb path diff. is 0. so centre mein hamseh bright fringe hoti hai.



- let mune 'p' per fringe nikalna hoti ki bright banega ya dark banega to yeh Bright aur dark depend krega path diff. pr.
- Because S<sub>1</sub> se P aur pt. A to P th dono ka dist. same hoti or dusre wale ko 'D' dist. jyada chalna padta.

to itna extra chala wahi uske path diff. hoti.

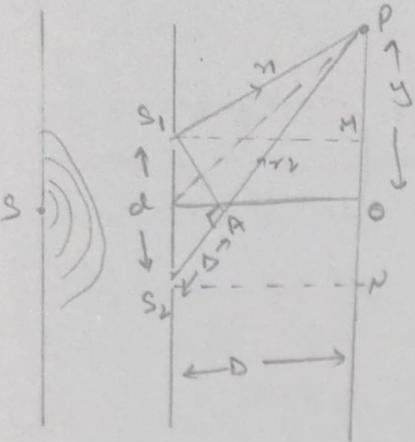
$$\rightarrow (n=0, 1, 2, 3)$$

*remember always* Agar path diff.  $\rightarrow \Delta = n\lambda$  wua to pt. P pe bright banegi.  
aur path diff.  $\rightarrow \Delta = (2n-1)\lambda/2$  wua to pt. P pe dark banegi.

## \* Derivation :-

- Kunko ab path diff. nikalna so, step are :-  
 → (i.e. S<sub>1</sub>MP)      → (i.e. S<sub>2</sub>NP).  
 1. Hum 2 triangles denge one for S<sub>1</sub>P and another for S<sub>2</sub>P  
 2. fir dono triangles mein pythagora theorem lega denge.  
 3. Jo 2 eqns banengi dono ko subtract krenge.  
 4) final step.  $d \ll D$  so, S<sub>1</sub>P  $\approx$  S<sub>2</sub>P  $\approx$  D last mein D likh denge.

*Note* \* Fringe width ( $\beta$ ) - smallest. b/w two consecutive dark or bright fringes.



Here path diff. =  $S_2 P - S_1 P$

$$\text{so, } \Delta = S_2 P - S_1 P \quad \text{--- (1)}$$

In  $\triangle S_1 PM$ : triangle find kya?

$$(S_1 P)^2 = (S_1 M)^2 + (PM)^2 \rightarrow \text{Pythagoras lagaya.}$$

$$(S_1 P)^2 = D^2 + (y - d/2)^2 \quad \text{--- (2)}$$

In  $\triangle S_2 PN$ : triangle find kya?

$$(S_2 P)^2 = (S_2 N)^2 + (PN)^2 \rightarrow \text{Pythagoras lagaya.}$$

$$(S_2 P)^2 = D^2 + (y + d/2)^2 \quad \text{--- (3)}$$

Subtracting eq (3) & eq (2)

$$(S_2 P)^2 - (S_1 P)^2 = D^2 + (y + d/2)^2 - \{D^2 + (y - d/2)^2\}$$

$$(S_2 P - S_1 P)(S_2 P + S_1 P) = D^2 + (y^2 + d^2/4 + 2yd/2) - D^2 - (y^2 + d^2/4 - 2yd/2)$$

*Lekar padhe tha  
yon path difference  
since  $d \ll \lambda$*

$$= 4yd \quad \text{i.e. } S_2 P \approx S_1 P \approx D$$

so,  $\Delta (D + D) = [4yd + 4yd]$

$$\Delta 2D = 2yd$$

$$4 = \frac{\Delta D}{D}$$

*4 ki value aa path diff.  
ke sams mein*

Linear position of Bright fringe

$$\text{toh } \Delta = n\lambda \text{ put karlo}$$

so,  $y_n = \frac{n\lambda D}{2}$  *Bright fringe ki position*

Linear position of Dark fringe

$$\text{toh } \Delta = (n-1)\lambda/2 \text{ put karlo.}$$

$$y_{n-1} = \frac{(n-1)\lambda D}{2d}$$

- Bright fringe width

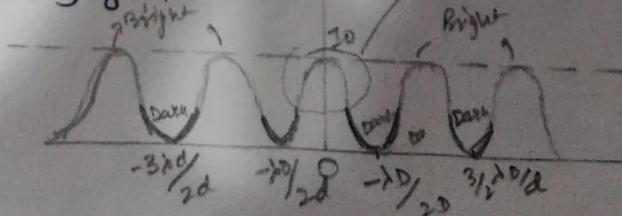
$$B = y_n - y_{n-1}$$

$$B = \frac{n\lambda D}{2} - \frac{(n-1)\lambda D}{2}$$

$$B = \frac{\lambda D}{2}$$

Bright fringe ki fringe width.

\* Intensity graph



$$B = y_n - y_{n-1}$$

$$= (2n-1) \frac{\lambda D}{2d} - [2(n-1)-1] \frac{\lambda D}{2d}$$

$$= \frac{\lambda D}{2d} [(2n-1) - (2n-2-1)]$$

$$= \frac{\lambda D}{2d} [-1+3]$$

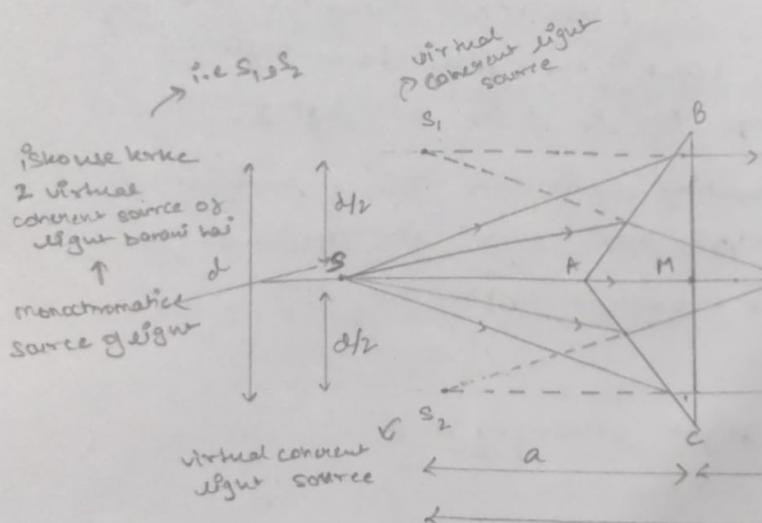
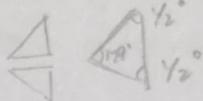
$$B = \lambda D / d$$

*Bright aur dark fringe width same*

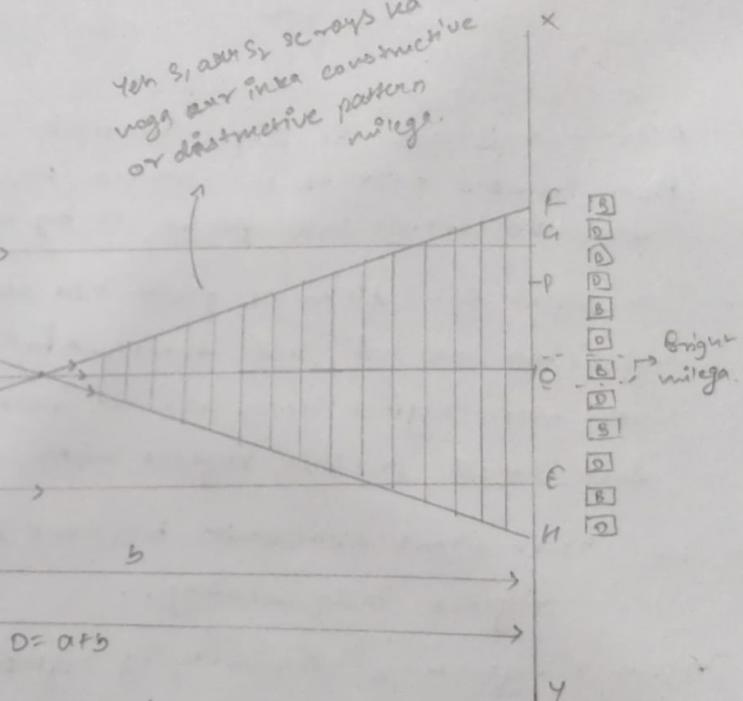
*aa mi haai pha matlo do no  
ke beech ka dist. same hoga*

## \* Fresnel Biprism's

- Agar interference phenomena ke study kerna hai toh uski pehli requirement hui hui 'coherent sources', isko banane ke aleg aleg methods hui un mein se ek 'Fresnel Biprism' hui.
- It is an optical device which is used to produce two coherent sources of light by phenomenon of refraction of light. In this we use division of wavefront method to produce two coherent sources of light.
- Isme 2 prism jode hue note by their base.



Yeh  $S_1$  aur  $S_2$  se rays ka superposition (region) hoga aur itna constructive or destructive pattern milenge.



→ Ab dekhenge ki ek particular pt. 'P' pe humhe intensity max. milgi ya min. milgi.

for Bright fringe

$$\text{path diff.} = S_2 P - S_1 P = n\lambda \quad (r=0, 1, 2, \dots)$$

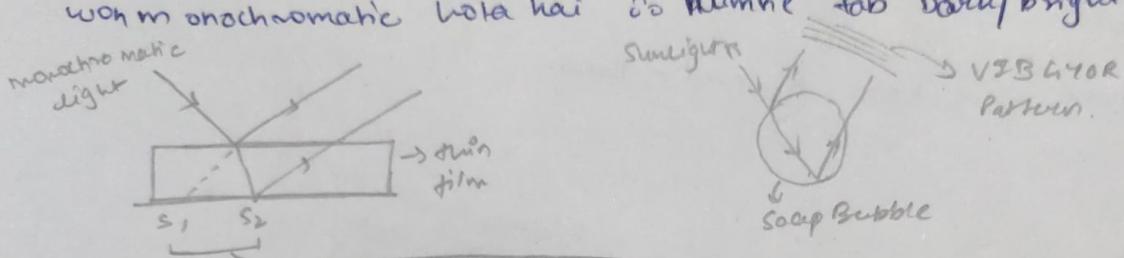
for dark fringe

$$\text{path diff.} = S_2 P - S_1 P = (2n+1)\lambda/2$$

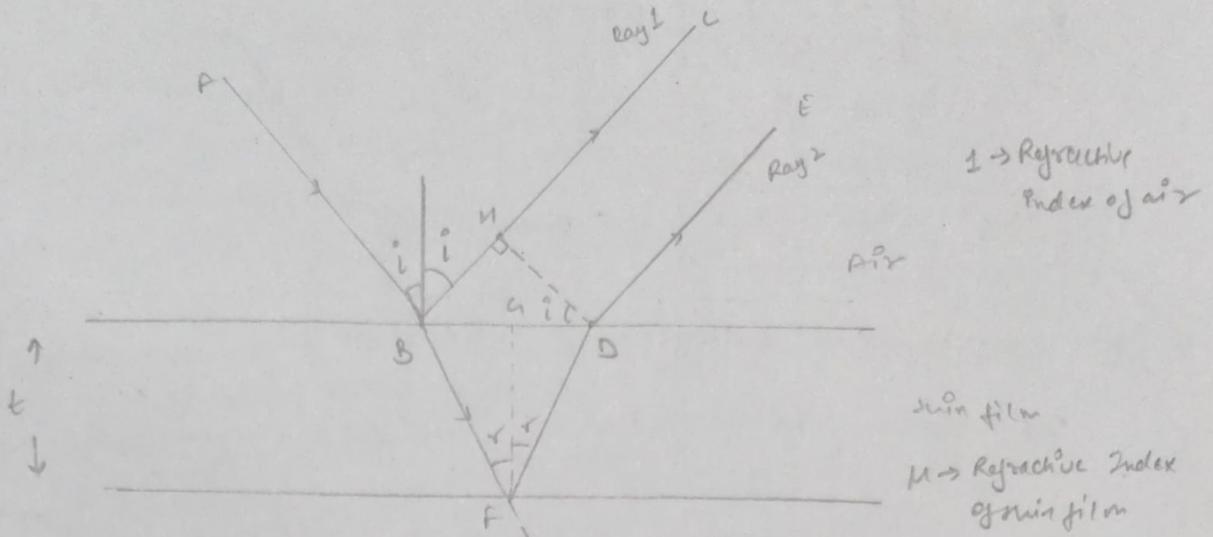
( $n=0, 1, 2, \dots$ )

## \* Interference in thin films :-

- Thin film interference is natural phenomenon in which light waves reflected by upper and lower boundaries of thin film interfere with one another, giving interfringe pattern. (fringes)
- But in soap bubble humhe VIBGYOR pattern milta ~~not~~ dark/Bright fringes because soap bubble bubble jo light part hai woh sunlight noti hai i.e. polychromatic aur hum so labse main use karte hai woh monochromatic nota hai so humhe tab Dark/bright fringes milte hai.



- Also, interference ke liye humko 2 light sources chahiye hote hai But hamare pass ek hi source hai light therefore hum reflected wale ko dotted kerke piche le ayege to S<sub>1</sub> & S<sub>2</sub> mil jayenge.
  - Tab light thin film pe parti hai starting mein toh small portion hi reflected nota hai max. transmit ho jata hai aur fir ander dusri barri mein reflect nota hai to max. transmit ho jata hai aur that small portion reflect nota.  
So, i.e. Thin films transmit incident light strongly and [imp] reflect only weakly.
- After 2 reflections intensity of reflected rays drop to negligible strength,  
so we consider first 2 reflected rays only.
- These 2 rays are derived from same incident ray but appear to come from two source located below the film. i.e. S<sub>1</sub> & S<sub>2</sub>
  - The sources are virtual coherent sources. The reflected waves L & L' travel along parallel paths and interfere.
  - Condition for maxima and minima can be deduced once we have calculated optical path difference b/w 2 rays at point of their meeting.



Path difference :-  
 Ray 2 itna extra chalne hai  
 Ray 1 itna extra chalne hai

$$\Delta = \mu(BF + FD) - t(BH) \quad \text{--- (1)}$$

In  $\triangle BFD$   $\rightarrow BF = FD$   $\rightarrow$  angle equal hai toh sides bhi equal hongi.

$$\cos\gamma = FH/BF \rightarrow BF = FH/\cos\gamma = t/\cos\gamma$$

$$\text{since } BF = FD \text{ toh } FD = t/\cos\gamma$$

$$\text{so, } BF + FD = \frac{2t}{\cos\gamma} \quad \text{--- (2)}$$

$$\text{Now, } BH = HD \rightarrow BD = 2BH$$

$$\tan\gamma = BF/FH \Rightarrow BH = FH \tan\gamma \Rightarrow BH = t \tan\gamma$$

$$BH = 2t \tan\gamma$$

In  $\triangle BHD$

$$\angle BHD = 90^\circ, \angle BHD = 90^\circ, \angle BDH = i^\circ$$

$$\sin i^\circ = BH/BD \rightarrow BH = BD \sin i^\circ$$

$$BH = 2t \tan\gamma \sin i^\circ \quad \text{--- (3)}$$

From Snell's law

$$\sin i^\circ / \sin r^\circ = \mu \rightarrow \sin i^\circ = \mu \sin r^\circ$$

$$BH = 2t \tan\gamma (\mu \sin r^\circ)$$

$$B = \frac{2pt \sin^2 r^\circ}{\cos\gamma} \quad \text{--- (4)}$$

$i \rightarrow$  Refractive Index of air

thin film

$\mu \rightarrow$  Refractive Index of thin film

Pt. H & D se dono rays saath chalne shuru ki hai

④

using eqs ② & ④ in ①

$$\begin{aligned}\Delta_a &= \mu \left[ \frac{2t}{\cos r} \right] - \left[ \frac{2\mu t \sin^2 r}{\cos r} \right] \\ &= \frac{2\mu t}{\cos r} [1 - \sin^2 r] = \frac{2\mu t}{\cos r} [\cos^2 r] \\ \boxed{\Delta_a = 2\mu t \cos r} &\rightarrow \text{path diff.}\end{aligned}$$

so, for constructive Interference (Maxima) Bright fringes  
 $\Rightarrow$  aisa YDSE mein Dark ke liye  
 $2\mu t \cos r = (2m+1) \lambda/2$   $\forall m = 0, 1, 2, 3, \dots$  nota that

for destructive interference (minima) Dark fringes.

$$2\mu t \cos r = m\lambda \quad \forall m = 0, 1, 2, \dots$$

$\hookrightarrow$  aisa YDSE mein nota that

YDSE ka weta ho gya for Bright.

- YDSE ka weta ho gya aise isliye hum kyonki air ka refractive Index '1' nota hai aur thin film ka refractive index ' $\mu$ ' air wale se zyada hai i.e.  $\mu > 1$  isliye jab bhi gyada Refractive Index wale se hamare light reflect hoi hai rohne ke mesh  $\rightarrow$  shift i.e.  $180^\circ$  shift ho jati hai.

\* Working dekhlo ab iski :-

- let us consider a transparent film of uniform thickness 't' bounded by 2 parallel surfaces. Let refractive index of film be ' $\mu$ ' & air be '1'  
let us consider plane waves from a monochromatic source falling on thin film at an angle of incidence ' $i$ '.

Part of ray such 'AB' is reflected along 'BC', and part of it is transmitted into film along 'BF'.

Transmitted ray 'BF' makes an angle 'r' with normal to surface at pt. 'G'.  
Ray 'BF' is in turn partly reflected back in to film along 'FD'

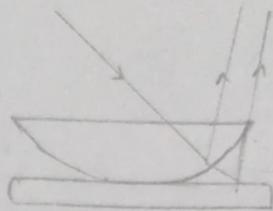
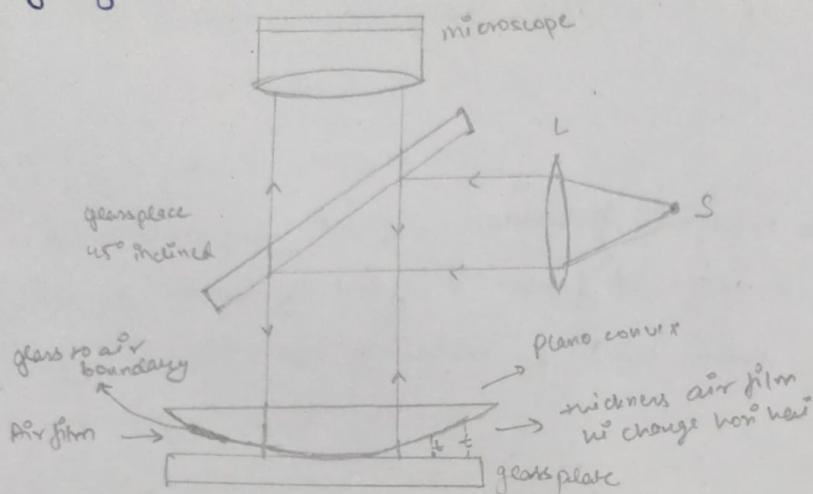
The ray 'FD' is transmitted at upper surface & travels along 'DE'.

Since film boundaries are parallel. the reflected rays 'BC' & 'DE' will be parallel to each other.

now as travelling along paths 'BC' and 'BF DF' are derived from a single incident wave AB.  $\therefore$  they are coherent & can produce interference.

## \* Newton's Ring :-

- Newton's ring is a phenomenon in which interference pattern is created by reflection of light b/w 2 surfaces, typically a spherical surface and an adjacent touching flat surface.
- Isme jinges circular hoti hai.



- Monochromatic light from an extended source S is rendered parallel by a lens 'L'. It is incident on glass plate inclined at  $45^\circ$  to horizontal, and is reflected normally down to plano convex lens placed on flat glass plate.
  - Part of light incident on system is reflected from glass to air boundary. The remaining light is transmitted through air film.
  - Then it again reflects from air to glass boundary.
  - The two rays reflected from top and bottom of air film interfere to produce darkness and brightness.
  - Condition of Brightness or darkness depends on path difference b/w 2 reflected rays, which in turn depends on thickness of film.
- $\Rightarrow$  remember agar centre pr light incident nori hai toh isme hamse dark jinge milega centre mein. leunki centre pr thickness 0 hoti hei.

We know that optical path diff. b/w rays is  
 $\Delta a = 2\mu t \cos r \rightarrow$  reflection angle.  
 refractive index of  
 air film  
 thickness.

for normal incidence of light  
 $\hookrightarrow$  yaha optics mein normal ka mtlb  $0^\circ$  hota hai

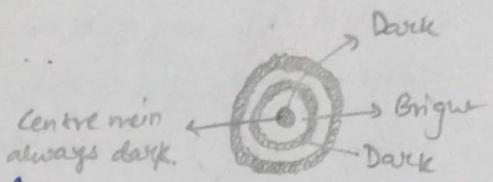
$$\Delta a = 2\mu t \cos 0^\circ$$

$$= 2(1)t (\cos 0^\circ)$$

$$\Delta a = 2t \rightarrow$$
 Yeh hamara 2 rays ke beech  
 ka path diff. hoti

for constructive interference / Maxima / Bright fringes :-

$$2t = (2m+1) \frac{\lambda}{2} \quad m=0, 1, 2, 3, \dots$$



for destructive interference / Minima / Dark fringes :-

$$2t = m\lambda \quad m=0, 1, 2, 3, \dots$$

Yeh YOSE ka neta ho gaya because light waves changes phase by  $180^\circ$  when reflect from surface of medium with higher refractive index than that of medium in which they are travelling.

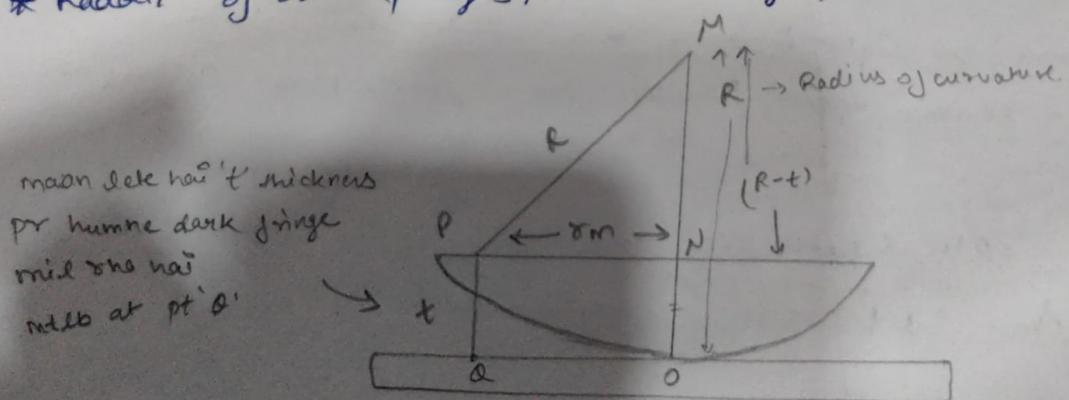
- Why Newton's rings are circular?

Ans. The thickness of air film at point of contact is zero and gradually increases as we move outward.

- The locus of points where air film has same thickness then fall on a circle whose centre is point of contact.

Generally circular isliye hoti hai lekin kamra lens circular hota hai (i.e. plano convex) aur due to varying thickness of air gap b/w surfaces.

\* Radius of Dark fringes / Newton Rings.:-



In  $\triangle PNM$  using pythagoras.

$$PM^2 = PN^2 + MN^2$$

$$R^2 = (r_m)^2 + (R-t)^2$$

$$R^2 = r_m^2 + R^2 + t^2 - 2Rt$$

$$r_m^2 = 2Rt - t^2$$

As  $R \gg t$ ,  $2Rt \gg t^2$

↳ lens ke radius se thickness bhot kam hai  
almost negligible.

$$\text{so, } r_m^2 \approx 2Rt \quad \rightarrow \quad r_m = \sqrt{2Rt}$$

W.K.T condition for darkness at  $\theta$  is

$$2t = m\lambda \quad \rightarrow \quad t = m\lambda/2$$

$$r_m^2 = 2Rm\lambda/2 \quad \rightarrow \quad r_m^2 = m\lambda R$$

$$r_m = \sqrt{m\lambda R} \quad \text{for } m=1,2,3,4, \dots$$

The radii of dark fringes can be found by using

$$\text{for } m=1,2,3, \dots$$

$$r_1 = \sqrt{1\lambda R} \quad r_3 = \sqrt{3\lambda R}$$

$$r_2 = \sqrt{2\lambda R}$$

so, we can see that  $\underbrace{r_m \propto \sqrt{\lambda}}$  → mtlb wavelength badhega toh  
fringes ka radius badhega.

thus radius of  $m^{\text{th}}$  dark ring is proportion to underroot of wavelength.

\* Ring ~~not~~ diameter.

- Yeh radius ka double ho jayega,

$$\text{so, } D_m = 2r_m$$

$$D_m = 2\sqrt{2Rt}$$

$$\text{or } D_m = 2\sqrt{m\lambda R}$$

- Spacing b/w rings :-

$$D_m = 2\sqrt{m\lambda R} \quad m=1,2,3,4, \dots$$

$$D_1 = 2\sqrt{\lambda R}$$

$$D_2 = 2\sqrt{2\lambda R} = 2(1.4)\sqrt{\lambda R} = 2.8 \quad )^{+6}$$

$$D_3 = 2\sqrt{3\lambda R} = 2(1.7)\sqrt{\lambda R} = 3.4 \quad )^{+6}$$

$$D_4 = 2\sqrt{4\lambda R} = 2(2)\sqrt{\lambda R} = 4 \quad )^{+6}$$

→ Abhi yeh gap normal aur equal  
hai but dhore dhore yeh gap  
kam hota jayega. jaise ki  
hum 'm' ki value badi denge.

- Rings get closer and closer, as 'm' increases. this is why  
rings are not evenly spaced.

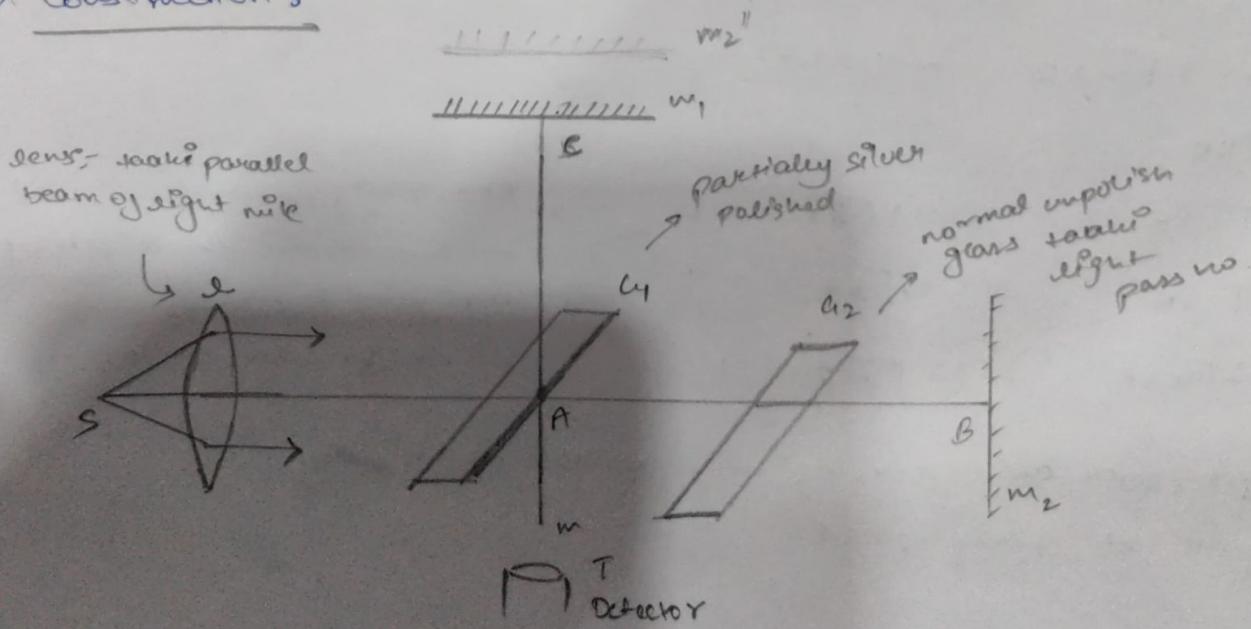
## \* Michelson Interferometer B-

- It is an instrument in which phenomenon of interference is used to make precise measurements of wave lengths, refractive index and distance.
- (10)
- m<sub>1</sub>, m<sub>2</sub> → 2 mirrors perpendicular  
mean length hole hai*
- C<sub>1</sub> → partially silver glass place  
Detector → Jaha fringes mitenge.*
- light source se nikal ke C<sub>1</sub>,  
se reflect hole m<sub>1</sub> jata hai  
air transmit hole m<sub>2</sub> jata  
fir waha se both waves reflect  
hole hai aur dono rays detector  
ke pass jaake interference krti hai.*
- 
- R<sub>1</sub> and R<sub>2</sub>  
Detector pr interference  
longi*
- m<sub>1</sub> m<sub>2</sub>*
- C<sub>1</sub>*
- R<sub>1</sub> R<sub>2</sub> m<sub>1</sub> m<sub>2</sub>*
- Detector*

## \* Principle:-

- In michelson interferometer, a beam of light from an extended source is divided into 2 parts of equal intensities by partial reflection and refraction.
- These beams travel in two mutually perpendicular direction and come together after reflection from plane mirror.
- The beams overlap on each other and produce interference fringes.

## \* Construction:-

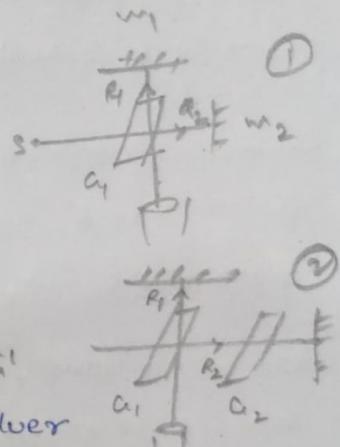


- It consists of beam splitter ' $G_1$ ', a compensating plate ' $G_2$ ', and two plane mirrors  $m_1$  &  $m_2$ . The beam splitter  $G_1$  is partially silvered plane parallel glass plate.
- Ccompensating plate  $G_2$  is simple plane parallel glass plate having same thickness as  $G_1$ .
- 2 plates  $G_1$  &  $G_2$  are held parallel to each other and are inclined at angle  $\theta = 45^\circ$  with respect of mirror  $m_2$ .
- mirror  $m_1$  is mounted on carriage and can be moved with help of micrometer screw.
- plane mirrors  $m_1$  and  $m_2$  can be made perfectly perpendicular with help of fine screws attached to them.
- Interference bands are observed in field of view of detector.

### \* Working :-

# Compensating plate sangha pehle :-

- Compensation basically hamare dono rays ke path difference ko same banata hai.
- Diagram ① mein Ray 1, teen baar silver glass plate se guzarti hai i.e.  $G_1$   
 (i) Source se glass plate mein enter (ii) mirror  $m_1$  se  $G_1$   
 (iii) glass plate se mirror  $m_2$  reflect ho ke silver glass plate tere gya.
- Diagram ② mein Ray 1, teen baar guzari shi nai But ab ray 2 bhi 3 baar guzari shi nai i.e.  
 (i)  $G_1$  se  $G_2$  (ii) mirror  $m_1$  se  $G_2$   
 (iii)  $G_2$  se mirror



~~But~~ But To Ray 2 hai woh bas ek baar guzarti hai  
 i.e. glass plate ~~se~~ <sup>mirror</sup> se glass plate.

Isliye hum compensating plate use karte hai jies.

- Diagram ② mein Ray 1 3 baar guzari shi nai But

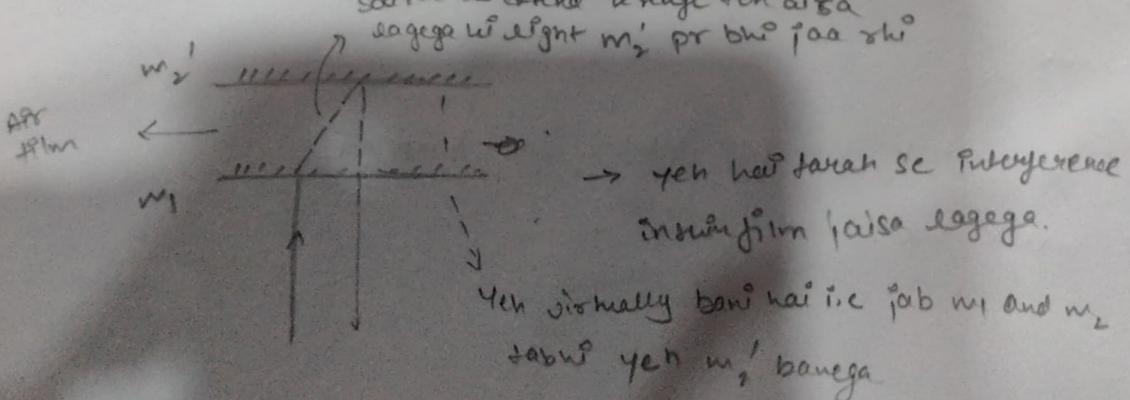
ab ray 2 bhi 3 baar guzari shi nai i.e.

- (i)  $G_1$  se  $G_2$
- (ii) mirror  $m_1$  se  $G_2$
- (iii)  $G_2$  se mirror

ab unke path diff. match ho gya hai. Isse humhe bridges ache nailte hai.

## \* Working :-

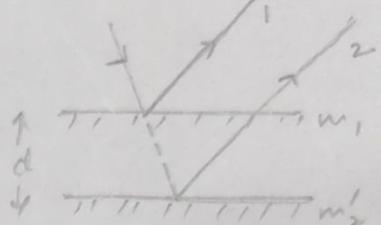
- (12)
- monochromatic light from extended source  $S$  is rendered parallel by means of lens  $L$  and is made incident on beam splitter  $G_1$ . It is partly reflected at back surface of  $G_1$  along  $AC$  and partly transmitted along  $AB$ .
  - Beam  $AC$  travels normally toward plane mirror  $m_1$  and is reflected back along same path and comes out along  $AT$ .
  - Transmitted beam travel toward mirror  $m_2$  and is reflected along same path. It is reflected at back surface of  $G_1$ , and proceeds along  $AT$ .
  - The two beams received along  $AT$  are produced from single source through division of amplitude and are hence coherent.
  - The superposition of these beams leads to interference and produce interference fringes. Interference ke liye coherent source required hona h.
  - From construction, it is clearly seen that light ray starting from source  $S$  and undergoing reflection at mirror  $m_1$  passes through glass plate  $G_1$ , three times.
  - On other hand, in absence of plate  $G_2$ , the ray reflected at  $m_2$  travels through glass plate  $G_1$  only once.
  - For compensating this path difference, a compensating plate  $G_2$  of some thickness is inserted to path  $AB$  and held exactly parallel to  $G_1$ .
  - If we look into instrument from  $T$ , we see mirror  $m_1$  and in addition we see virtual image,  $m'_2$  of mirror  $m_2$ . Depending on position of mirror, image  $m'_2$  may be in front of, or behind, or exactly coincide with mirror  $m_2$ . Iska mtlb dekhlo ab.



## \* Circular fringes :-

- Circular fringes are produced with monochromatic light when mirrors  $m_1$  and  $m_2$  are exactly perpendicular to each other.
- Situation is similar to an air film enclosed b/w mirror  $m_1$  and  $m_2'$ , but diff. is that in case of real film b/w 2 surfaces, multiple reflection take place, whereas in this case only two reflection takes place.

$$m_2'm_1 = d.$$



total path diff. b/w 2 beams given by

$$\Delta a = 2d \cos \theta \rightarrow \theta \text{ is angle of observation i.e. } \text{w.r.t. sc. observe for the fr.}$$

- For constructive interference (maxima)

$$2d \cos \theta = (2m+1)\lambda/2 \quad \& \quad m = 0, 1, 2, 3, \dots$$

- For destructive interference (minima)

$$2d \cos \theta = m\lambda \quad \& \quad m = 0, 1, 2, 3, \dots$$

• again  $m_1$  and  $m_2'$  don't coincide b/w  
toh dark fringe milga bss