UNIT-01

$$A_{i} = \frac{qx}{qn} = t(x^{i}A)$$

$$\beta = \beta_0 + x \gamma_0' + \frac{x_2}{x_2} \gamma_0'' + \frac{x_3 \gamma_0''}{3!} + ---$$

Rolle's Theorum

then 3 attent one point CE (a,b) so

Mean Value theorem

(i) same Rolle's rem

tun 3c E (a,b) so that

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

Bisection Method

let for = one le

Suppose, f(0) = -49

+ (1) = -49 2 700+

+ (2) = +49 3 110 bloo them

1st Approx.

and Approx.

12 = 1.5+2 = 1.75; f(1.75) = +ue

3 od Approx .

so on till required accuracy.

Secant Method

Su ppose, +(0) = - up

+(17=-4 Xo

f(2)=+ue xx,

$$x_{n+1} = x_{n-1} + (x_n) - x_n + (x_{n-1})$$

$$+ (x_n) - + (x_{n-1})$$

1/2 = Ko + (Ki) - X1 + (KO)

+(xi) - +(xo)

Xz = similarly -

Newton Raphson Method

let fox)=0

Suppose, for=-ue + (1) = - ue 2 most livs

let Xo = 1 or 2 or 1+2 = 1.5 abofind f'(x)

$$x^{n-1} - x^{1} = x^{0} - \frac{f(x^{0})}{f(x^{n-1})}$$

$$x^{0} = x^{n-1} - \frac{f(x^{0})}{f(x^{n-1})}$$

$$y = 1 - x^{1} = x^{0} - \frac{\epsilon(x^{0})}{\epsilon(x^{0})}$$

Absolute Essor: If x is true value of x' its Approximate value. Eaz | X - X'|

Relative Error: $E_R = \frac{X - X^2}{X}$

Inherent cooosse Errors which are already present in the statement of a problem before its solution.

Rounding errors: Errors which arise from the process of rounding off the numbers.

Truncation errors: Errors caused by using Approximate results.

! Do it your self : + fibonaces · Golden Search - Newton's Mutual Steepest - Nelder-Mead Afgo.

in that Box $f(x+hu) = f(x) + \frac{u}{1!} \Delta f(x) + \frac{u(u-1)}{2!} \Delta^2 f(x)$ Interval + u(u-1)(u-2) 13f(x) + --> New ton Backward: $f(x+hu) = f(x) + u \nabla f(x) + \underline{u(u+1)} \nabla^2 f(x)$ $u = \frac{x - x_{0}}{x - x_{0}} = \frac{x - x_{0}}$ # Numerical integration : $I = \int_{\alpha}^{b} f(x) dx \quad ; \quad h = \frac{b-a}{h}$ # Lagrange's interpolation for unequal interval 1) Trapezoidal Rule: x 5 6 9 11 y 12 13 14 16 $\int_{0}^{\infty} f(x) dx = \frac{h}{2} \left[(y_{0} + y_{n}) + 2(y_{1} + y_{2} + - y_{n-1}) \right]$ $f(x) = (x-6)(x-9)(x-11) \times 12$ (5-6) (5-9)(5-11) . for any no. of interval. $\frac{(x-5)(x-9)(x-11)}{(6-5)(6-9)(6-11)} \times 13$ 2 Simpson 1 Rule: (Even interval) Ja f(x) dx = 1 [(yo+yn)+4(y1+y3+--)+ (x-5) (x-6) (x-11) x 14 2 (42+ 44+ 46+--) 3 Simpson 3 Rule: (for Multiple of 3) + (x-2)(x-e)(x-d) x 18 (11-5) (11-6) (11-9) $\int_{a}^{b} f(x) dx = \frac{3h}{8} \left[(y_{0} + y_{1}) + 3(y_{1} + y_{2} + y_{4} + -) \right]$ # Newton Divided Difference: +2(43+86+89+--)] x / + (x) | st(x) | s2 + (x) $\frac{12}{6-5} = 1 \sqrt{\frac{\frac{1}{3}-1}{6-5}} = -\frac{1}{6}$ **%** 5 # Gauss quadatur formula x_1 6 x_2 9 x_3 11 x_4 13 x_5 11 x_6 16 x_6 11 x_6 16 x_6 11 x_6 16 x_6 11 x_6 16 x_6 11 x_6 dus - I= 1 + 00 dx step D: change interval [a,b] into [-1,1] using | X = b-at+ b+a Step @ : Seussithet x in f(x) given : x=10 $f(x) = f(x_0) + (x - x_0) \Delta f(x_0) + (x - x_0)(x - x_1) \Delta^2 f(x_0)$ Step 3: Comula integrand. + (x-16) (x-x1) (x-x2) 13+(x0) + --one - point: 1 fandx = 2 f(0) two-point: [+ (x) dx = f(-1)+(1) three-point: (+ (x) dy = = = = = = = = + 8 f(e) + 8 f(e) + 5 (1/35) Made with 💚 by Hemant

UN94-02

Interpolation

> Newton forward:

UN:7-03 # LU Decomposition Methods. # Gauss Elimination Method. Consider the system of eq"1. # Dolittle: a11x+a12y+ 9132 = b1 azı 4 + azzy + azzz = bz 2 A = LU 931 x+932y+9332 = b3 $U = \begin{bmatrix} u_{11} & u_{12} & u_{13} \\ 0 & u_{22} & u_{23} \end{bmatrix}$ Comunt in Matrix form AX=B L= 100 an an ang ang Ty = bi be [l31 l32 \$] 00 433 921 922 923 2 b2 b3 3 LY=B : LUX = B make Augmented matrix, C=[A:B] where, $y = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$ Solve to find an a12 913 : 51 921 922 923: b2 a31 a32 a33 : b3 (4) UX = 4 " use Row trons formations? from this we can find x (x,y,z) reg. Sol. 2 # Crout's: Convert back to system of egs. C11 X+ (128+ (132 = d1 Some Procedure as Dolittle $L = \begin{bmatrix} q & 0 & 0 \\ b & c & 0 \end{bmatrix} \quad U = \begin{bmatrix} q & h \\ 0 & i \end{bmatrix}$ ChdeckC22y + C232 = d2 C332 = d3 Now, solve truse to get us Anney City) with # chalesky's: A -> motox. # Gouss Jordan Conditions ? A is symmetric i e At = A

is positive definite. Similar to Gaus Elimination $\chi = d_1$ $\chi = d_2$ $\chi = d_3$ (a) A = LLT EL A= [900] [abd] # Eigen Value Problem 8 Power method. Ex. [3 -5][] = [-2] Eigen Volue Eigen Vultor | [d e f] [00 f $Ax_{0} = \begin{bmatrix} -2 & 4 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} +8 \\ -6 \end{bmatrix} = \begin{bmatrix} +8 \\ -6 \end{bmatrix} = \begin{bmatrix} -8x_{2} \\ -0.75 \end{bmatrix} = \begin{bmatrix} -8$ ap potes astests (9) LT X = 4 so on till we get some Value of Successive iteration Made with \heartsuit by Hemant

y (n+1) yo+ h [f(xo,yo)+f(x1,y,(n))] (Modified) y = yo + /x + (x,y) dx Put n =0,1,2,3, Is+ Approx. -Step 1st Approx . Ist Approx . I (1) = yo + 1 [f(xo, yo) + f(xo, yo)] $y_1 = y_0 + \int_{x_0}^{x} f(x, y_0) dx$ and Approx. -Similarly. 12 [f(xo, yo) + f(x1, y(1))] 12= 40 + 1x + (x,y,) dx and so on. till required accuracy. Doing this till the desiral degree of accuracy obtained. · if two consecutive values of yiki & yiki are Same then $y_1 = y_1^{(k)}$ Preceding in the # Toylosis Series (f(x,y) = y = dy) Some manner, $y_1 = y_0 + hy_0' + \frac{h^2}{21}y_0'' + \frac{h^3}{3!}y_0''' +$ J2, y3, --- are Col culated. (X= Ko+h) ## Runge - Kutta (Second Order) h=(x-x0) Minday X = Xo-h $\frac{dy}{dx} = f(x,y) \quad , \quad g(x_0) = g_0$ $y_2 = y_1 + hy_1' + \frac{h^2}{2!}y_1'' + \frac{h^3}{3!}y_1''' + \cdots$ To find 8 (Ki) and so on --- $K_1 = h f(x_n, y_n)$ #Eulen's Method $k_2 = hf(x_n + h, y_n + k_1)$ Comider, dy = f(x,y); y(x0) = y0 Jn+1 = Jn+ 1 (K1+K2) To find: Y(xn) = In (Insticus) # Runge - Kutta (4th Order) Acc. to Euler's Muthod, egn. (1) $K' = Pt(x^{u,i}A^{u})$ yn = yn-1 + h. f(Kn-1, yn-1), n=1,2,3k2 = hf (Nn+ 1/2) 4n+ k1) k3 = hf (xn+ 1/2 18n + k2) width of differenting $p = \frac{1}{X^{\nu} - X^{\rho}} = x^{\nu} - x^{\nu-1} = x^{\nu} - x^{\rho}$ ky=hf (xn+h, yn+k3) n + no. of interval. (let any n=5,10,etc) then Computer Put n=1, y= yo+hf (xo, yo) wägsted mean $\rightarrow k = \frac{1}{6} (k_1 + 2k_2 + 2k_3 + k_4)$ of K1, K2, K3 & K4 Put n=2, y2 = 9, +h f(x1, y1) # Adams-Bash Porth Prudictor Connector Method: and so on. Consider, du = f(x,y) with initial y(x0) = yo from Euler's Method, Starting from find y(xi), y(x2), y (x3) using Any methods. To find: y (xn) must be 4 storating Value of y. Then Calculate _ fo = f (xo, yo), f, , f2, f3 Point to = 34 = 33 + 1 (55 f3 - 59 f2 + 37 f1 - 9 fo) d1, y2, y3, --- yn find fy=f(xy)yw) Connector -> 44 = 43 + 1/24 (9 fy + 19f3 - 5f2 + fi) again find fy Lagain Corrector. Made with w by Hemant

Modified Euler's Method. (x = xo+h)

Step O:- (y, (0) = yo + h f (xo, yo) (Euler Method)

40- +PMU

Picard's Method.

Milne Predictor - Corrector Method:

dy = f(x,y) with in that Cond y(x)=you To find y (xp) 14 Find y(x1), y(x2), y(x3) using they Muthod Then Calculate:

fo = f(x0,y0) = f1 = f(x1,y1)

f2 = f(x2,y2) - f3 = f(x3,y3) Milne's Corrector formular. yy = y + h (f + yf + fy) to find better value of yy, we repeat this step ontill by remain unchanged. H Numerical Solution of Partial Diff. 194.
(Parabolic, hypexbolic, elliptical) $a \frac{\partial^2 \phi}{\partial x} + b \frac{\partial^2 \phi}{\partial x^2} + c \frac{\partial^2 \phi}{\partial y^2}$ 1770 Hyperbola , 2 charach both 0=0 Pana bola 0>0 Ellipse. No Soln. Made with by Hemant