How Population Structure Shapes Neighborhood Segregation¹

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This study provides a framework for understanding how population composition conditions the relationship between individuals' choices about group affiliation and aggregate patterns of social separation or integration. The substantive focus is the role of income inequality in racial residential segregation. The author identifies three population parameters—between-group inequality, within-group inequality, and relative group size—that determine how income inequality between race groups affects racial segregation. She uses data from the Panel Study of Income Dynamics to estimate models of individual-level residential mobility and incorporates these estimates into agent-based models. She then simulates segregation dynamics under alternative assumptions about (1) the relative size of minority groups and (2) the degree of correlation between race and income among individuals. The author finds that income inequality can have offsetting effects at the high and low ends of the income distribution. She demonstrates the empirical relevance of the simulation results using fixed-effects, metro-level regressions applied to 1980-2000 U.S. census data.

Sociologists have a long-standing interest in how population composition constrains patterns of inequality and social separation. The idea originated in Simmel's texts on intersecting social affiliations (Simmel 1906, 1950) and was later elaborated in Blau's theory of social structure (Blau 1974,

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1977; Blau and Schwartz 1984). This body of work is motivated by the observation that people occupy multiple social positions simultaneously; for example, each person has an age, sex, income, nationality, occupation, and race. These attributes are often correlated, and the degree of correlation has implications for how individuals' in-group tendencies aggregate into patterns of social separation or integration.

Blau's central theorem is that a weaker correlation in social differences promotes intergroup contact (Blau 1977, p. 586). At one extreme, we can imagine a world in which social characteristics of individuals are orthogonal; for example, there is no correlation between race and income or education and sex. Blau's theory implies that social affinities that lead to segregation along one dimension will tend to reduce social separation along other dimensions because a person's in-group members for one attribute will contain many out-group members on other attributes. At the other extreme, there is complete consolidation in social attributes; for example, the incomes of whites never overlap with those of blacks, and even the highest-educated woman is still less educated than the least educated man. In this case, Blau's theory suggests that social processes that produce separation along one dimension will reinforce separation on other dimensions.

Blau's ideas inform a great deal of contemporary work that investigates how population parameters shape marriage patterns, occupational and residential segregation, and network homophily (e.g., Marsden 1987; Tienda and Lii 1987; Kalmijn 1998; Moody 2001; Wimmer and Lewis 2010). However, while Blau's original framework is compelling, it conflates two dimensions of the correlation between social attributes: within-attribute variation versus between-attribute variation. The extent to which sorting on multiple attributes exacerbates or attenuates social separation depends on the explicit configuration of these two dimensions.

This study extends Blau's work to investigate how choices about social grouping based on one attribute can exacerbate or attenuate segregation on another correlated attribute. The specific application is the role of racial and economic factors in generating patterns of racial residential segregation. Blau's theory suggests that if both racial and economic factors matter in residential mobility and race and income are highly correlated (i.e., minorities are poorer, on average, than whites), racial segregation will be higher than if race and income were uncorrelated. Within the segregation literature, this line of reasoning is referred to as the *spatial assimilation hypothesis*, which argues that racial and ethnic differences in residence reflect status differences among groups (Gordon 1964; Alba and Logan 1993).

ming files. I am grateful to Rick Riolo and Sarah Cherng for computational support. Please direct correspondence to Elizabeth Bruch, Department of Sociology, University of Michigan, 500 South State Street, Ann Arbor, Michigan 48109. E-mail: ebruch@umich.edu

The spatial assimilation hypothesis is typically contrasted with the *place stratification hypothesis*, which emphasizes barriers to mobility such as discrimination and racial steering. The place stratification hypothesis posits that racial and ethnic minorities are excluded from white neighborhoods, and this limits the ability of even the socially mobile members of these groups to reside in the same communities as comparable whites (Alba and Logan 1993, p. 1391).

Studies attempting to assess the degree to which status differences between blacks and whites explain high levels of black-white segregation show that racial segregation varies little by the education or income status of blacks (Massey and Fischer 1999), and high-income blacks typically live in poorer areas than high-income whites (Alba, Logan, and Stults 2000). This is generally taken as evidence in favor of the place stratification hypothesis. My aim is to show that the dynamics of racial residential segregation resulting from sorting across multiple, correlated social attributes are more complicated and nuanced than is captured in either the place stratification or the spatial assimilation hypothesis, as changes in income inequality among race groups can have opposite and offsetting effects at the high and low ends of the income distribution.

The correlation between race and income is composed of two parts: between-race and within-race income inequality. Between-race income inequality reflects average differences in income between race groups, for example, as captured by the ratio of black median income to white median income. Within-race income inequality reflects within-race income heterogeneity. Given some baseline level of racial segregation, any increase in black-white income inequality increases the average income differences between black and white neighborhoods. Under conditions of low within-race income inequality, substantial between-race income inequality reinforces race-based patterns of residential mobility, thus exacerbating segregation. But under moderate to high within-race income inequality, high between-race income inequality has different effects at opposite ends of the income distribution.

Consider the case in which blacks are substantially poorer, on average, than other race groups. Poor blacks experience greater racial isolation. But more affluent blacks must choose between higher-income, nonblack neighborhoods and poorer, black neighborhoods. Some of them remain in black neighborhoods. But a nontrivial proportion, as I show below, end up in nonblack areas. In the event of elimination or substantial attenuation of between-race income inequality, the decrease in racial isolation that poor blacks experience is partially counterbalanced by an increase in neighborhood proportion black experienced by higher-income blacks. These offsetting effects attenuate the total change in racial segregation that occurs as a result of changes in between-race income inequality.

I begin with a review of classic and contemporary approaches to studying residential segregation with a specific focus on studies examining the role of income in racial residential segregation. I then outline a basic analytical model for understanding the macrolevel consequences of microlevel sorting processes involving multiple attributes that considers (1) the level of correlation between the relevant social attributes (i.e., their joint distribution), (2) the relative size of each social group in the population, and (3) the relative importance of different attributes in individuals' decisions about unit.² The model extends Blau's original thesis to provide a more nuanced account of how different dimensions of population distributions condition the degree to which a given regime of in-group preferences results in aggregate patterns of segregation. It also provides several predictions concerning how the joint distribution of the population by race and income influences racial segregation.

The balance of the article tests the empirical validity of these predictions. The analysis consists of three parts: (1) simulation experiments that use artificial populations in a highly stylized city, (2) simulation experiments that use real populations and geography, and (3) a metro area—level statistical analysis of how between- and within-race income inequality and the size of the black population correspond to changes in segregation in major American cities between 1980 and 2000. All simulation experiments assume that agents' mobility behavior follows empirical patterns of residential choice as reflected in the Panel Study of Income Dynamics (PSID).

Overall, the results suggest that income inequality affects racial segregation, but in ways that are masked when one focuses only on average income disparities among race groups or ignores the feedback between racial and economic processes. Under empirically plausible levels of within-race income inequality, higher between-group income inequality increases the salience of economic factors in residential mobility decisions. The end result is that high-income blacks live in whiter neighborhoods than they would otherwise. At the same time, poorer blacks are racially (and economically) isolated. Whether these offsetting processes result in a net increase or decrease in segregation depends on the relative size of the black population, the salience of racial versus economic factors in residential mobility decisions, and the shape of the income distribution.

Although the arguments and analyses presented in this work refer to the case of residential segregation, the results apply more generally to any social context or institution—for example, families, friendship networks—in which individuals make decisions about group affiliation based on multiple social attributes. The article concludes with a discussion of how these

² I use the word "unit" to refer to the social unit that individuals select into or out of (e.g., neighborhoods, schools, marriages, or church groups).

results might be extended to other contexts in which people sort themselves into groups on the basis of multiple group attributes.

THE ROLE OF INCOME IN RACIAL SORTING

Sociology and demography have a long tradition of empirical studies trying to disentangle the causes of racial segregation between whites and blacks. Explanations for existing patterns of segregation typically focus on three potential mechanisms (Quillian 2002; Charles 2003). The first explanation emphasizes the role that preference for living among one's own ethnic group (or avoiding other ethnic groups) plays in the formation and maintenance of racially segregated neighborhoods (Farley et al. 1978; Clark and Ware 1997; Emerson, Yancey, and Chai 2001; Krysan and Farley 2002). The second explanation emphasizes the importance of institutional barriers that limit blacks' access to white neighborhoods (Yinger 1995; Galster and Godfrey 2005). The third line of work focuses on racial differences in economic resources (e.g., Clark 1986, 2007; Clark and Ware 1997). The logic is that—given that whites, on average, have higher incomes than other ethnic groups—white households can live in neighborhoods with higher prices, effectively creating an affordability constraint that limits access to lowerincome minority groups even in the absence of institutional discrimination.

The most common strategies researchers use to investigate the role of economic factors in race/ethnic segregation are standardization methods applied to aggregate census data, or regression-based decomposition applied to individual-level data. Aggregate studies typically compute the amount of race segregation that would be expected if race groups sorted only on the basis of economic factors (i.e., indirect standardization) or compare the racial neighborhood composition of white and nonwhite households in the same income or educational bracket to see if higher-status minorities experience the same sorts of neighborhoods as their white counterparts (e.g., Taueber and Taueber 1969; Farley 1977; Simkus 1978; Massey and Fischer 1999; Iceland, Sharpe, and Steinmetz 2005). The microlevel analyses—often referred to as "locational attainment" models—examine individuals' residential choices conditional on education, income, or wealth (e.g., Alba and Logan 1993; South and Crowder 1997; Alba et al. 2000; Crowder, South, and Chavez 2006). In all cases, the goal is to see whether racial differences in neighborhood composition persist after standardizing/conditioning on economic attributes and segregation by income. This literature demonstrates that socioeconomic status differences explain only a small part of blacks' segregation from whites (although this portion may be increasing, as evidenced by Fischer [2003]).

There are two problems with these approaches. First, these methods ignore the underlying structural constraints imposed by the joint distribution

of attributes within the population. The reality is that there are very few neighborhoods in American cities that are both affluent and predominantly black. Figure 1 shows the joint distribution of neighborhood proportion black and neighborhood median income across all metropolitan statistical areas in 2000. Each data point represents a census block group; the points are scaled relative to the proportion of black households in the neighborhood with an annual income of \$50,000 or more. Thus larger circles denote a greater number of high-income blacks in the neighborhood. Overall, we see that high-income blacks tend to live in either poorer black neighborhoods or predominantly nonblack areas. Only 38 block groups in the United States at that time both had a median income of at least \$75,000 and were at least 30% black. Fourteen of these are in the Washington, D.C.-Baltimore metro area and seven are in Chicago. A census block group generally contains between 600 and 3,000 people with an optimum size of 1,500. Given that 32% of the total black population in the United States in 2000 earned at least \$50,000 and given that black survey respondents consistently express a desire to live in neighborhoods with a significant black presence (cf. Farley et al. 1978; Farley, Fielding, and Krysan 1997; Krysan and Farley 2002), this suggests an unmet demand for middle-class black neighborhoods. Where those neighborhoods are not available, higher-income blacks

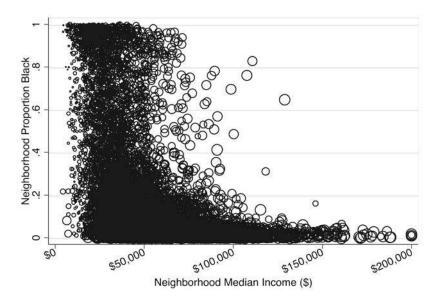


Fig. 1.—Joint distribution of neighborhood median income and neighborhood proportion black, all metro area census block groups in 2000. Points are scaled relative to the proportion of black households in a neighborhood earning \$50,000 or more.

may be forced to choose between neighborhoods where their own racial group is well represented and neighborhoods where their economic or educational group is well represented.

The second problem with approaches using both aggregate and individual-level data is that the statistical methods and logic of argument implicitly assume that economic segregation reflects sorting based purely on economic factors, and thus one can partition out economic factors by standardizing on income or comparing the segregation of people with different races but the same income or wealth. This would be a reasonable assumption if people actually selected neighborhoods only on the basis of economic factors or if income/wealth and race were independently assigned characteristics. In this case, any changes in racial composition would not affect residential mobility based on income/wealth, and vice versa. However, when people select neighborhoods on the basis of both racial and economic factors, then the total amount of income segregation reflects not only inequalities in income but also the correlation between race and income, the relative size of the minority population, and residential mobility by both race and income (see also Sethi and Somanathan 2004). In other words, because both race and income matter in residential mobility decisions and because race and income are correlated attributes of individuals, there is feedback between processes that generate racial segregation and processes that generate economic segregation. Under these circumstances, standard statistical approaches cannot reveal the relative contributions of racial and economic factors to observed neighborhood patterns. An alternative approach is to dynamically simulate neighborhood formation and change under alternative assumptions about residential choice behavior and the joint distribution of race and income within the population.

The most widely cited model of feedback between individuals' decisions and population dynamics is Schelling's (1971, 1978) model of residential tipping. Using rudimentary computational models applied to artificial agents, he showed how the preferences of individuals about where to live give rise to (often unanticipated) aggregate patterns of residential segregation. These patterns, moreover, may be at odds with the majority of individuals' preferences (Pancs and Vriend 2007). The Schelling model assumes a highly styled city populated by two race groups: blacks and whites. Both race groups are assumed to be willing to live in any neighborhood as long as its own race group is the local majority. This model has been extended by a number of scholars over the years to incorporate different assumptions about racial preferences (Bruch and Mare 2006, 2009; Fossett 2006), explicit geography (Benenson, Hatna, and Or 2009), and social class (Benard and Willer 2007). But simulation approaches have not been used to explicitly tease apart how racial composition, income inequality, and residential mobility combine to generate racial segregation patterns. More generally, we

lack an analytic framework for understanding how sorting along multiple attributes such as race, income, or age affects inequality across social units. In the next section, I describe the key parameters of such a framework and provide a preliminary sketch of how they fit together.

A FRAMEWORK FOR UNDERSTANDING SORTING ON MULTIPLE ATTRIBUTES

Blau's Theory of Social Structure

Blau's approach is based on Simmel's (1950) insights about the importance of quantitative dimensions for social life. Blau (1977, p. 278) defines social structure as the joint distribution of social attributes within the population. One key component of social structure is the degree of diversity in the population along a given attribute, for example, ethnic diversity. Another key component is the extent to which various social distinctions are related, for example, the correlation between ethnicity and income (Blau, Blum, and Schwartz 1982, p. 46). Blau's two major theorems relate to these features of social structure. First, Blau postulates that greater diversity on an attribute counteracts in-group tendencies to seek like others on the basis of that attribute. In other words, with preferences held constant, greater diversity is associated with greater social integration. Second, Blau argues that a weaker correlation among socially salient attributes leads to greater social integration. The reason is that in a world in which people hold many weakly correlated, intersecting affiliations, any person who is an in-group member on one dimension is likely to be an out-group member on other dimensions.³

This study extends Blau's framework in three different ways. First, in both his theoretical and empirical work, Blau conflates two aspects of the association between attributes: between- versus within-attribute variation.⁴ Blau's theory holds up only under certain configurations of between- and within-group variance. Second, Blau recognizes that both the size of social

³ Blau's theory was originally formulated to apply to bivariate associations between pairs of attributes but was later revised to specify that an intersection of multiple attributes is necessary to promote intergroup relations (see Blau 1977; Blau and Schwartz 1984, p. 90). I restrict my analysis to only two variables for simplicity and because my methodological approach (simulation) allows me to artificially control for all other sources of variation, but the argument can be extended to multiple attributes.

⁴ Empirically, Blau operationalizes the association between any two attributes as their bivariate correlation. This is Cramer's V for two nominal variables, the correlation ratio (η) for one nominal and one interval variable, and the Pearson's correlation coefficient for two interval variables (see Blau, Beeker, and Fitzpatrick 1984; Blau and Schwartz 1984). All these measures include elements describing the variance between attributes and total variance; this implicitly also represents within-group variance. But the components are not analytically separated.

groups and the correlation between social attributes matter but does not consider how these two features of population composition interact. In the case of residential segregation, I show that the extent to which income inequality between race groups contributes to racial segregation depends on the relative size of racial groups. Finally, Blau's empirical tests focus on marriage, a unit that requires only two people. I articulate how the size of social units (neighborhoods) might condition how the joint distribution of attributes shapes aggregate patterns of social separation or integration and provide an alternative test of Blau's argument based on neighborhoods (a social unit that is substantially larger than marriage).

The Role of Between- and Within-Group Heterogeneity in Segregation Dynamics

Let us consider how different dimensions of the joint distribution of attributes condition the relationship between individuals' preferences for neighbors and aggregate patterns of segregation. Figure 2 shows four black-white income distributions that illustrate variation in within- and between-race income inequality. Panels A and B assume a low level of within-race income inequality whereas panels C and D assume a high level of within-race income inequality, whereas panels B and D show a low level of between-race income inequality. In all cases, blacks and whites have the same within-race income inequality. But in panels A and C, blacks have a median income of \$30,000 while whites have a median income of \$60,000; compare this with a median income of \$60,000 for whites and \$55,000 for blacks as shown in panels B and D.

We know from studies of revealed and stated preferences that people prefer to live where their own group is the local majority (see Charles 2003, pp. 182–85), and it is reasonable to assume that people prefer to live in a neighborhood where their own income is not less than the average income of the neighborhood. For the same preference regime, we would expect racial segregation to be higher under panel A as compared to panel C and under panel B as compared to panel D. The reason is simple: with between-race income inequality held constant, greater within-race income heterogeneity implies an increased level of within-race variation in residential mobility behavior, which would lead to lower levels of racial segregation. But it is less clear what levels of racial segregation we might expect under panel A as compared to panel B or under panel C as compared to panel D. In other

⁵ The Gini index for the income distributions shown in fig. 2, panels A and B, is 0.15, and the Gini index for the income distributions shown in panels C and D is 0.55.

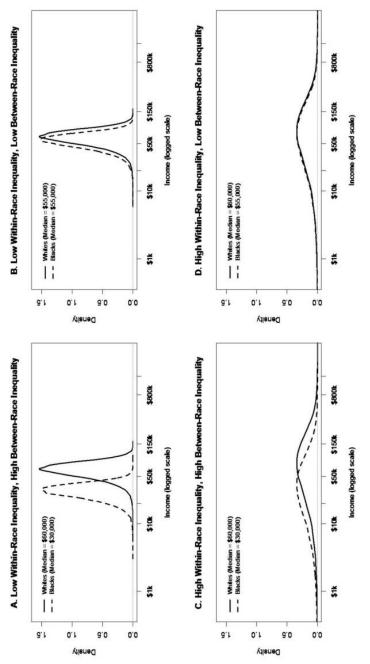


Fig. 2.—Stylized patterns of between- and within-race income inequality

words, with within-race income variation held constant, how might racial segregation change if we increase between-race income inequality?

When we increase average income differences between blacks and whites, we also increase the average income difference between black and white neighborhoods. When within-race income variation is small (as shown in fig. 2, panels A and B), higher-income blacks may not feel a strong pull toward higher-income white areas. However, under higher within-race income heterogeneity (as shown in panels C and D), with preferences held constant, higher-income blacks will experience greater salience of economic factors in residential mobility decisions.⁶ Thus they are less likely to choose poorer black neighborhoods and more likely to move into neighborhoods where their own income group has greater representation. More generally, for a sufficiently high level of within-race income heterogeneity, any increase in between-race income inequality will decrease the attractiveness of black neighborhoods for more affluent blacks and thus increase their willingness to move into white, affluent neighborhoods. This decrease in the average neighborhood percent black experienced by higher-income blacks will be "offset" by the increased racial isolation of lower-income blacks. Of course, at higher levels of black-white income inequality, high-income blacks make up a smaller part of the total black population. Thus the extent to which these opposing processes result in a net increase, decrease, or no change in segregation depends on the shape of the income distribution and the relative salience of racial versus economic factors in residential mobility decisions.

Critical Numbers, Income Inequality, and the Size of the Metro Black Population

If increased income inequality between blacks and whites leads to a decrease in the average neighborhood proportion black experienced by affluent blacks, then a substantial decrease in or elimination of income differences between blacks and whites will result in an increase in the average neighborhood proportion black experienced by affluent blacks. There are two possible reasons why a convergence in income between blacks and

⁶There are two ways of increasing the relative influence of a variable's effect on outcomes: (1) by increasing its coefficient and (2) by increasing its variance.

⁷ Affluence or high income may be defined in relative or absolute terms. One absolute measure of affluence is twice the median metro household income. A relative measure for blacks would be all black households with a household income in the top decile of the black income distribution. In this analysis I use an absolute measure of affluence. However, I explored analyses using both relative and absolute measures of affluence. Both definitions lead to the same substantive conclusions. The key difference is that, for an absolute measure of affluence, higher levels of black-white income inequality imply fewer black neighbors for affluent blacks but also fewer numbers of affluent blacks (and greater numbers of poor blacks).

whites may lead to an increase in the average proportion black experienced by affluent blacks. First, an elimination or substantial attenuation of blackwhite income inequality may result in sufficient numbers of middle-class blacks to generate sustainable middle-class black neighborhoods. Neighborhoods require a critical number of households to be sustainable. For example, 1,000 households might not be able to maintain their own neighborhood (with clearly defined boundaries that protect property values and the quality of public schools) but 10,000 can. The poorer blacks are relative to whites, the less likely it is that there are sufficient numbers of higher-income blacks to support higher-income black neighborhoods. In addition, the smaller the size of the black community, the harder it is to form economically distinct black neighborhoods. It is no accident that the two cities with established black, middle-class communities—Atlanta and Washington, D.C.—are also areas with a sizable black population. Cities with larger minority populations can sustain more economically diverse minority neighborhoods.8

Second, a decrease in black-white income inequality may lead to an increased flow of black households moving into higher-income white areas. Because whites are willing to tolerate only a small minority black neighborhood (Farley et al. 1993, 1994; Charles 2000), this may prompt local white residents to move out, resulting in a net increase in the average proportion black experienced by affluent blacks in these areas. Here, again, the size of the black population matters. For a given level of black-white income inequality, a larger black metro population implies a greater number of nonpoor black households moving into nonpoor white areas. Thus we might expect the threshold level of black-white income inequality that leads to an out-migration of white residents to be lower when the black metro population is larger.

The above argument suggests two testable hypotheses. First, for moderate to high levels of within-race income inequality, I expect a negative relationship between black-white income inequality and the neighborhood proportion black experienced by poor blacks and a positive relationship between black-white income inequality and the neighborhood proportion black experienced by affluent blacks. Second, because the two mechanisms that might explain an increase in the neighborhood proportion black for affluent blacks (outlined in the previous section) are both predicated on having a "critical mass" of higher-income black households, I expect the relationship between between-race income inequality and the average proportion black

⁸ This line of reasoning also suggests that if neighborhoods were smaller, the critical size of the black population would also decrease. More generally, units that require smaller numbers of people—e.g., church groups as compared to school districts—may be able to sustain greater levels of social separation on multiple social attributes. However, an analysis of unit size is outside the scope of this work.

experienced by affluent blacks to be nonlinear and depend on the size of the black population. Because previous studies have not explicitly examined the roles of between- and within-race income inequality in racial segregation, there is no prior research regarding these hypotheses. The balance of the article uses simulation and fixed-effects models to test these predictions.

SIMULATION EXPERIMENTS

I use agent-based models to explore how the joint distribution of income and race shapes patterns of racial residential segregation. The overarching strategy is to explore what segregation dynamics occur under alternative assumptions about the relative size of race/ethnic groups and the degree of within- and between-race income inequality, holding mobility behavior constant. The first set of simulation results are based on a theorized set of agents moving within a highly styled city ("stylized model"). This approach allows me to exercise complete control over the three parameters of interest: betweenrace income inequality, within-race income inequality, and the relative size of the minority population. It provides a highly controlled test of the hypothesis that, when within-group income inequality is high, a convergence in income inequality between blacks and whites results in offsetting effects at the high and low ends of the black income distribution. However, the agentbased model uses a very stylized geography and population. For example, the model assumes a world of only blacks and whites and sets the initial distribution of the agents to a state of complete integration. To more firmly attach these results to real cities and segregation patterns, I also implement a more realistic agent-based model ("empirically grounded model") that simulates segregation dynamics using empirical populations and highly realistic geography for three cities: Atlanta, Chicago, and Los Angeles. Table 1 summarizes the two agent-based models used in the analysis.

Specifying Agent Behavior

Both simulation models assign agents a model of residential choice behavior on the basis of statistical estimates from the PSID. These models describe the probability that a person with a given race and household income will select a new neighborhood (or stay put), given the racial and economic composition of the current neighborhood, as well as all potential destinations.

Data.—The PSID is a nationally representative, longitudinal survey of U.S. residents and their families. The survey began in 1968 with approximately 5,000 families. Panel families were interviewed annually between 1968 and 1997 and every two years thereafter. New families have been added to the panel as children and other members of the original panel families form separate households. I use the PSID's Geocode Match Files

TABLE 1
AGENT-BASED MODELS USED IN ANALYSIS

	Stylized Model	${ m Empirical~Model}^{ m a}$
Population	34,000 households Blacks and whites	Drawn from 2000 STF 3A census data 20% sample of all households
Geography	Metro percent black: 15 or 30 200×200 grid	Blacks, whites, Asians, and Hispanics GIS map of city blocks
Initial distribution	Each cell represents one housing unit Random	Each block can hold multiple households Corresponds to 2000 population at census-tract level
Neighborhoods	5×5 subsections of the grid	Census block groups
Agent behavior	Empirically estimated from PSID	Empirically estimated from PSID
Comparisons	Systematically vary within- and between-race inequality	Empirical population composition Blacks assigned white income distribution

^a Empirical model initialized for three cities: Atlanta, Chicago, and Los Angeles.

to link the addresses of individual respondents at each interview to their corresponding census-tract identifiers. These identifiers make it possible to trace the mobility of PSID respondents across neighborhoods between successive interviews. I merge the geocoded PSID data with decennial census data. To maintain consistency across survey years, I analyze two-year mobility windows. Additional moves within years do not enter into the analysis. Because my analysis focuses on urban segregation dynamics, I restrict my sample to person-years in which the respondent was living in metropolitan areas in adjacent interview years. Periods when respondents were living in rural areas or moved between rural and urban areas are excluded from the analysis. 10 Table 2 summarizes the information available in the PSID sample. Each respondent may contribute up to four residential mobility decisions, one for each two-year time interval. The 12,144 respondents provide information on 28,232 biannual mobility decisions. In most cases, these are decisions to remain in the current unit. However, 10,698 are moves between census tracts within a given metro area. The remaining cells of the table describe neighborhood attributes of the chosen tract in each time interval.¹¹ Thus, for the 1991–93 interval, this refers to the residence in 1993. We see that, on average, PSID respondents tend to live in areas with higher median incomes than their own. We also see a small but steady decrease in the neighborhood proportion black experienced by black respondents. White PSID respondents live in overwhelmingly white neighborhoods. Overall, the neighborhood patterns observed in the data are consistent with the moderate to high levels of racial segregation observed in the United States.

⁹I use linear interpolation to impute values of census variables for years in between censuses. For example, to compute the proportion black in a given tract in 1992, I calculate

$$PctBlack_{_{1992}} = PctBlack_{_{1990}} + \left(\frac{PctBlack_{_{2000}} - PctBlack_{_{1990}}}{10}\right) \times 2.$$

¹⁰One drawback of the PSID is that Hispanics and Asians are underrepresented in the original sample. This is a result of the original sampling being done in 1968, just before the increase in the U.S. Asian and Hispanic populations. This underrepresentation was partially remedied in 1990 by the temporary addition of 2,000 Latino households and by the later addition of 511 families headed by post-1968 immigrants or their adult children. To maximize representation of Hispanics and Asians and maintain a manageable sample size, I restrict my sample years to 1990–2000. Following Crowder and Downey (2010), I limit the sample to respondents who were classified as heads of households either at the beginning or at the end of a mobility window, as the residential choice of the household head usually determines the mobility of the rest of the household. This strategy avoids double counting moves made by multiple members of the household. The end result is an effective sample of 12,684, consisting of 5,892 whites, 3,830 blacks, 2,281 Hispanics, and 141 Asians. Given the small number of Asians, all Asian-specific estimates should be treated with skepticism.

¹¹To ease comparisons, all income values are scaled to 2000 dollars.

	Total	White	Black	Asian	Hispanic
Residential mobility decisions:					
1991–93	8,142	3,465	2,493	29	2,155
1993–95	8,635	3,757	2,642	33	2,203
1995–97	5,566	3,199	1,940	113	314
1997–99	5,889	3,295	2,080	125	389
Moves between tracts:					
1991–93	1,912	763	681	8	460
1993–95	3,691	1,499	1,220	14	958
1995–97	2,587	1,268	939	91	283
1997–99	2,508	1,289	973	66	180
Household median income (\$):					
1991–93	22,802	38,080	14,280	58,191	17,791
1993–95	22,939	36,171	15,312	48,392	17,289
1995–97	28,890	40,660	19,612	38,520	19,284
1997–99	31,930	43,363	23,690	43,631	22,660
Neighborhood proportion black:					
1991–93	.242	.060	.621	.126	.099
1993–95	.236	.061	.606	.101	.092
1995–97	.244	.063	.581	.089	.072
1997–99	.246	.065	.571	.065	.073
Neighborhood proportion Hispanic:					
1991–93	.121	.040	.030	.101	.359
1993–95	.139	.050	.045	.112	.406
1995–97	.092	.063	.071	.179	.486
1997–99	.106	.068	.084	.173	.531
Neighborhood proportion Asian:					
1991–93	.025	.026	.016	.121	.034
1993–95	.026	.027	.017	.090	.035
1995–97	.209	.030	.019	.139	.053
1997–99	.031	.031	.020	.154	.046
Neighborhood median income (\$):					
1991–93	37,661	53,491	34,631	52,437	36,713
1993–95	40,512	54,824	36,213	55,370	38,714
1995–97	48,248	62,409	41,265	61,054	43,547
1997–99	49,645	64,105	42,960	71,201	45,167

Note.—All incomes are scaled to 2000 dollars.

Statistical approach.—My analysis of residential mobility is based on discrete choice (conditional logit) models for residential location (McFadden 1974, 1978; Bruch and Mare 2012). The models incorporate the effects of individuals' personal attributes as well as their opportunities for mobility, that is, characteristics of all neighborhoods to which they might move. To define a meaningful choice set, I limit the analysis to moves that occur within the same metro area. ¹² I assume that the potential destinations con-

¹² This excludes less than 5% of all between-tract moves.

sidered by PSID respondents consist of all census tracts within their metro area. The sample includes both owners and renters.¹³

The discrete choice model focuses on the effects of race/ethnic and economic composition of neighborhoods on residential choice. In each two-year period, individuals face the probability of staying within their neighborhood or moving to another neighborhood within the same metro area. The model assumes that the potential utility that an individual expects from each potential destination (including the decision not to move) is a function of his or her race/ethnicity, household income, the race/ethnic composition of each potential destination, the median income of each potential destination, the 20th percentile housing price of each potential destination, and whether a given destination requires that the individual move or stay in his or her current neighborhood. Housing prices are calculated from the distribution of neighborhood residents' monthly gross rent and monthly mortgage payments. The 20th percentile price represents a lower bound of affordability. For the *i*th individual who is considering the *j*th neighborhood destination in the *t*th period, the utility can be written as

$$U_{ijt} = F(\text{Ethnicity}_i, \text{ Household Income}_i, \text{ Neighborhood Ethnic}$$

$$\text{Composition}_{ji}, \text{ Neighborhood Median Income}_{jt},$$

$$\text{Neighborhood 20th Percentile Price}_{jt},$$

$$\text{Neighborhood Median Income}_{jt}, D_{ijt})',$$

$$(1)$$

where D_{ijt} equals one if the potential destination j is the origin tract for individual i in year t and zero otherwise.

I estimate the effect of these factors using a conditional logit model for discrete choice. In particular, if p denotes the probability of choosing the jth neighborhood in the tth period by the ith individual, the model can be written as

$$p_{ijt}(x_{ijt}) = \frac{\exp(\beta x_{ijt})}{\sum_{k \in C(i)} \exp(\beta x_{ikt})},$$
(2)

where x_{ijt} and x_{ikt} denote vectors of attributes of census tracts j and k (possibly interacted with traits of individuals), β denotes a vector of pa-

¹³ I assume that the same mobility process applies to both owner and renter households. This is a simplifying assumption that is unlikely to be true in practice. At a minimum, owners tend to move less frequently than renters, and owners are also likely to be more sensitive to neighborhood racial and economic composition. I tried to estimate the models allowing for separate coefficients for owners and renters, but the PSID does not have enough nonwhite owners in the sample to generate stable estimates. The current estimates should therefore be viewed as a weighted combination of owner and renter mobility behavior.

rameters to be estimated, and C(i) denotes the set of potential destinations available to individual i. In the present application, this is defined as all census tracts within the metro area that the person is residing in at the beginning of the mobility interval. Thus the choice set will vary across PSID respondents, depending on their geographic location.¹⁴ I specify Huber-White robust standard errors to account for the clustering of mobility decisions within individuals across years.¹⁵

The models allow for the following types of effects. First, all else equal, people are more likely to choose to remain in their current place of residence rather than move. As shown in (1), this is represented as a dummy variable that equals one if the tract in question is the current tract of residence and zero for all other potential destinations. I also allow for the possibility that people evaluate the racial and economic composition of their own neighborhood differently from all other potential destinations. For example, people may be less sensitive to changes in neighborhood prices in their current neighborhood due to tenure discounts.

Second, I include information on the race/ethnic composition of each tract, which may affect its attractiveness to potential movers. The model allows for the possibility that this effect is nonlinear. For example, some groups may have a taste for diversity. To incorporate these effects, I include linear and quadratic terms for the proportions in each of the four race/ethnic groups (non-Hispanic whites, Hispanics, non-Hispanic blacks, non-Hispanic Asians) as separate variables in the discrete choice model. Third, I allow members of race/ethnic groups to have different responses to neighborhood racial composition. Individuals are likely to prefer areas where their own group is well represented and may display group-specific

¹⁴ An issue with this type of model is the heavy burden associated with computing choice probabilities for each possible destination neighborhood for each individual in the sample. It is possible to obtain consistent estimates of the discrete choice model by drawing a choice-based sample from the set of possible destinations (McFadden 1978; Ben-Akiva and Lerman 1985; Mare and Bruch 2012). I subsample the alternatives to obtain a modified version of the discrete choice model, which is

$$p_{ijt}(x_{ijt}) = \frac{\exp(\beta x_{ijt} - \ln q_{ijt})}{\sum_{k \in C(i)} \exp(\beta x_{ikt} - \ln q_{ikt})},$$

where q_{ijt} denotes the (known) probability of sampling the jth census tract for the ith individual in the tth year. I draw a stratified sample within the 28,232 person-years in my sample such that each person-year is represented at least once in the sample. I design the stratification according to the following rules: (1) If the potential destination tract is either the origin or the chosen tract, $q_{ijt} = 1.0$. (2) If the tract is neither the origin nor the chosen tract, select at random with $q_{ijt} \ll 1.0$, where the value of q_{ijt} varies proportionally to the total number of tracts in the PSID respondent's metro area. I estimate the discrete choice model using software for a standard conditional logit model in which the coefficient of $\ln q_{ij}$ is constrained to be equal to 1.0. See Ben-Akiva and Lerman (1985) for a more detailed discussion of (and justification for) this procedure.

¹⁵ These models are estimated in Stata using the clogit command with the cluster option.

tendencies to be drawn to or avoid areas populated predominantly by other groups. In addition, I allow the effects of housing costs to vary by household income by including a variable that is the ratio of housing costs to household income. I also allow for the possibility that people evaluate neighborhood income relative to their own income. I explore a variety of specifications of the discrete choice model that include alternative combinations of these effects. ¹⁶

Results.—The parameter estimates (reported in table A1 in app. A) indicate that, over the course of a two-year window, individuals are more likely to remain in their own neighborhoods than to move. Beyond that, it is difficult to interpret the model from parameters alone especially given the three-way interactions. Further insights can be obtained from the predicted probabilities of neighborhood choice as a function of neighborhood racial and economic composition. Figure 3 shows the probability of choosing a neighborhood on the basis of housing costs. Separate profiles are shown for movers (people who changed census tracts in the two-year interval) and stayers (people who remained in the same census tract over the two-year interval). Looking at panel A, we see the expected patterns: poorer households are highly constrained with regard to what neighborhoods are available to them. As household income increases, individuals are more likely to move into areas with higher prices. Panel B, which shows the probabilities for stayers, indicates that overall there is a gradually declining probability associated with choosing to remain in the current neighborhood as a function of neighborhood prices. The exception is the poorest households, which (if they are lucky enough to find themselves already living in a very expensive neighborhood) have a high probability of remaining there.

Figure 4 shows the probability of choosing a neighborhood on the basis of neighborhood median income. We see that, conditional on prices and other factors, people tend to choose areas where the median income is similar to their own. The same pattern is observed among stayers although curves are significantly more graduated, consistent with the results observed for neighborhood prices. In practice, neighborhood prices and neighborhood median

¹⁶ Low-income households often have highly fluctuating incomes (Duncan et al. 1984). In a number of cases, PSID households are observed moving into units where the yearly cost of that unit exceeds their reported yearly household income. To avoid these issues, I limit the analysis to households earning at least \$10,000 a year and spending less than 75% of their income on housing. Note that the models do not include interactions between the race of the household head and the economic composition of the neighborhood or interactions between individuals' household income and the racial composition of the neighborhood. I tried to estimate these parameters but ran into colinearity issues. Past work suggests that higher-income blacks may be less able than whites to transform their economic capital into quality housing (e.g., Crowder et al. 2006). If this is the case, my simulation results may overstate the extent to which economic sorting matters relative to racial sorting.

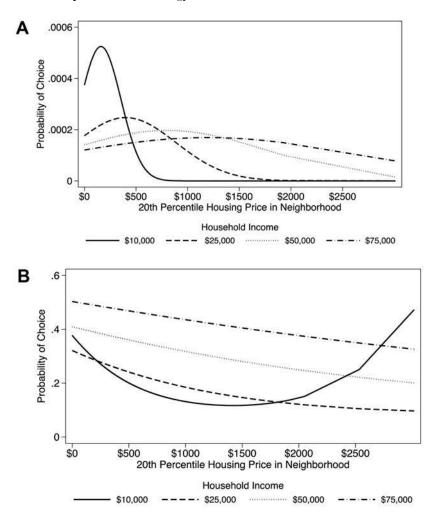
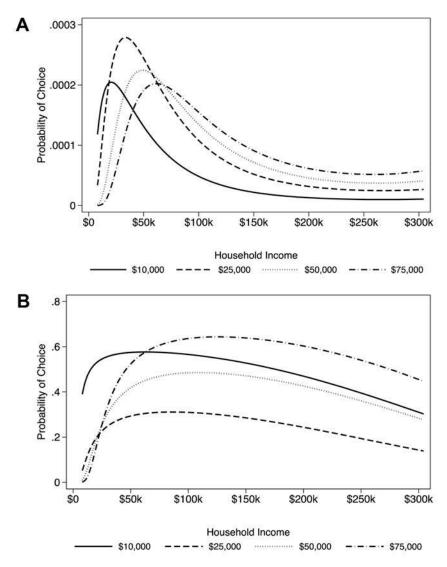


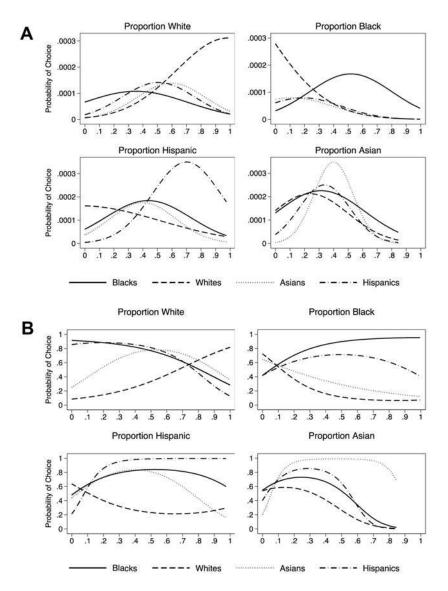
Fig. 3.—Probability of choosing a housing unit by monthly housing costs: A, movers; B, stayers.

income are highly correlated, so it is difficult to separate out their effects on mobility. Figure 5 shows the probability of choosing a new neighborhood or remaining in one's current neighborhood on the basis of neighborhood racial composition. Although the model produces estimates of residential preferences for all four race/ethnic groups, estimates for Asians are not reliable because they are based on a very small number of moves (table 2). Thus I confine my discussion to the other three race/ethnic groups. Among movers, we see that whites have a strong tendency to move into predominantly



 $F_{\rm IG.}$ 4.—Probability of choosing a housing unit by neighborhood median income: A, movers; B, stayers.

white neighborhoods and avoid black neighborhoods. Blacks tend to choose integrated areas where they are neither the overwhelming majority nor the minority. Hispanics tend to select majority Hispanic areas. Among stayers, we see that whites' probability of remaining in the current neighborhood sharply decreases with neighborhood proportion black. In contrast, both



 $F_{\rm IG}$. 5.—Probability of choosing a housing unit by neighborhood racial composition: A, movers; B, stayers.

blacks and Hispanics are willing to remain in their current area with increasing proportions of whites, up until a white majority. Hispanics and blacks are more or less equally willing to remain in their current neighborhood regardless of neighborhood proportion own-group, as long as they have some baseline representation. Note that these are all "net" effects after controlling for economic factors. Overall, we see that all race/ethnic groups display a tendency to live among their own group, although they distinguish among potential out-group neighbors. There is also variation in the extent to which different race groups are willing to tolerate out-group neighbors. The parameters from the discrete choice models are assigned to agents in two different simulation models, described in the next sections.

Agent-Based Models

Stylized model.—The stylized agent-based model consists of a 200×200 grid with 40,000 cells. ¹⁷ Each cell corresponds to a housing unit. This lattice is populated with approximately 34,000 agents, each representing one household. To allow agents to move relatively freely on the lattice, 15% of the cells on the lattice are vacant. Agents respond only to the ethnic and economic composition in their immediate neighborhood or other potential neighborhood destinations; they have no information about the overall level of segregation in the city. Agents' neighborhoods are defined as 5×5 cell subregions of the city. These neighborhoods are designed to approximate census tracts or another objectively defined boundary. Housing units are identical, and rents are uniform within each neighborhood.

Agents in this model differ along two dimensions: race and income. For ease in interpreting the results, I assume a world consisting only of two race groups: whites and blacks. I simulate segregation dynamics assuming that the city percentage black is either 15% or 30%. I assign the agents incomes that follow an empirically plausible parametric distribution, Singh-Maddala, which allows me to systematically manipulate the degree of income inequality between and within ethnic groups. This function has the advantage that I can specify both the median income and the overall level of inequality by changing the values of the distribution parameters. The distribution has the density

¹⁷The model was programmed and executed in Netlogo (http://ccl.northwestern.edu/netlogo/). The source code is available from the author by request.

¹⁸ The Singh-Maddala distribution function fits empirical income distributions extremely well, far better than other functions typically used to model income including the gamma, Pareto, and the lognormal (Singh and Maddala 1976; McDonald and Ransom 1979; McDonald 1984).

$$f(x) = \alpha q \frac{x^{\alpha - 1}}{\beta^{\alpha} (1 + [x/\beta]^{\alpha})^{1+q}}, \tag{3}$$

where $\alpha>0,\ \beta>0,\ q>0$, and $x\geq0$. By modifying β (scale parameter), I can manipulate the median income. By modifying α and q (shape parameters), I can manipulate the shape of the distribution and thus the overall level of income inequality. Appendix B provides more details about the specific parameters used to generate each income distribution.

I hold whites' median incomes constant at approximately \$60,000 but specify the black income distribution to have a median income of approximately \$25,000, \$40,000, or \$60,000.\text{\text{19}} These regimes are referred to as high inequality, moderate inequality, and income equality. I also examine segregation dynamics under different levels of within-race income heterogeneity. For any given simulation, I assume that both race groups have the same level of within-group income variation. Within-race income heterogeneity is summarized by the Gini coefficient.\text{\text{20}} I specify that levels of within-race income inequality range from a Gini index of 0.15 to a Gini index of 0.75.\text{\text{\text{21}}}

At the start of the simulation, the agents are randomly distributed across the city. Then, one agent is randomly sampled and given an opportunity to move. The agent evaluates his current unit and 100 randomly sampled destination units according to the race-appropriate statistical choice function estimated from the PSID data. The agent then decides to move or stay put with probabilities proportional to relative differences in neighborhood desirability. Given the costs of moving, agents often choose to remain in their current place of residence. Each time an agent moves, he changes the composition of the neighborhood he left behind and the neighborhood he moves into. Over time, the choices available to present agents are a result of previous mobility decisions.

I run the agent-based models to a dynamic equilibrium, where the agents may still be moving but aggregate segregation levels are no longer changing. In practice, this occurs after approximately 3 million time steps. Racial segregation is measured by the index of dissimilarity, which captures the

¹⁹Because the residential choice and hedonic pricing models are scaled to the incomes of renter households and prices of rental units, I keep the distributions within that approximate range.

²⁰ The Gini coefficient is an overall summary measure of income inequality and varies between zero (complete equality) and one (complete inequality, where one person or household has all the income and the others have none).

²¹ To put this in context, the Gini index computed for the U.S. income distribution in 2009 was approximately 0.47, up from 0.40 in 1980 (DeNavas-Walt, Proctor, and Smith 2010).

evenness of the distribution of people by race across neighborhood units within a city. This classic measure of racial segregation is not without its limitations—most notably, it is insensitive to the macrolevel spatial configuration of neighborhoods—but it is widely used in the literature and has a straightforward, intuitive meaning. I supplement this summary statistic with local neighborhood compositional measures, for example, the average neighborhood proportion black experienced by blacks in different income strata.²²

As neighborhood composition changes, neighborhood attractiveness (and therefore housing prices) will also change. I update housing prices at regular intervals to reflect changes in neighborhood desirability using hedonic pricing equations that predict logged house prices on the basis of neighborhood ethnic and income composition (see Sheppard [1999] for an overview of the specification and estimation of hedonic pricing models for housing markets). These pricing equations are estimated from 2000 census block group data for Atlanta.²³ I regress logged median monthly housing costs on block group racial and income composition to determine the relationship between neighborhood characteristics and expected housing costs. The coefficients and associated standard errors from these models are reported in the first panel of table B1 in appendix B. The prices estimated by the model are plausible and are well within the range of rents observed for households. Neighborhoods with higher median incomes or more white residents tend to have higher rents. Neighborhoods with a substantial number of black residents have lower rents.

Empirically grounded model.—While the stylized model allows for highly structured experiments that generate easily interpretable results, this approach assumes a world that consists of only two groups—whites and blacks—and starts from a state of complete integration. It is difficult to extrapolate from these results to real-world segregation patterns. Thus, I also explore segregation dynamics using an empirically grounded agent-based model of segregation dynamics that recreates the geographic and population

 $^{^{22}}$ Owing to both small fluctuations in the initial distribution of agents across the stylized city and also the probabilistic nature of the residential choice process, there are very small fluctuations in the final reported segregation statistics over multiple runs of the same model. For example, calculated indices of dissimilarity may vary across runs by $\pm /-0.003$ of a point. These fluctuations do not affect any of the subsequent conclusions reported in this article.

²³ Atlanta has a primarily black-white population and a wide range of neighborhood types (high-income black neighborhoods, low-income black neighborhoods, high-income white neighborhoods, low-income white neighborhoods, and mixed neighborhoods). The agent-based model produces the same substantive conclusions when a sample of all metro neighborhoods in the United States is used to estimate the hedonic pricing equations.

distribution of three U.S. cities: Los Angeles, Atlanta, and Chicago.²⁴ In each case, the model uses geographic information systems (GIS) data at the block, block group, and tract levels to create a realistic space in which the agents move about. Agents live in housing units nested within census blocks, and their neighborhoods are defined relative to real-world geographic barriers such as freeways, rivers, and major roads. The population of agents and their initial spatial distribution match those of Atlanta, Chicago, or Los Angeles in 2000.²⁵ I simulate segregation dynamics assuming that agents' mobility behavior corresponds to the residential choice models estimated from the PSID and compare segregation outcomes under empirical income distributions to outcomes assuming income equality between blacks and whites. All moves occur within city boundaries.

Table 3 shows the population density, size, and racial and economic composition of Los Angeles, Atlanta, and Chicago in 2000.26 Column 1 shows the race/ethnic composition of each city. Atlanta is almost two-thirds black, with Asians and Hispanics making up only 3% of the total population. Los Angeles is multiethnic: Hispanics represent almost half (47%) of the total population, while blacks are a little over one-tenth of the total population. Chicago has roughly equal numbers of blacks and whites and has a substantial Hispanic population (26%). Columns 2 and 3 show the median income and the within-race income inequality (as captured by the Gini index) for each race group.²⁷ In both Los Angeles and Chicago, the black median income is roughly one-half that of whites. Atlanta has the highest blackwhite income inequality of the three cities, with the black median income a little more than one-third that of whites. Los Angeles has higher within-race income inequality, as compared to Atlanta and Chicago. In all three cities, within-race income inequality is higher among blacks than among whites. Columns 4 and 5 report total population size and land area for each city. Atlanta is much smaller than Los Angeles and Chicago, with a population of less than half a million people compared with well over 2 million for the

²⁴The model is written in Java and uses the REPAST and Java Unified Mapping Platform (JUMP) libraries. Technical details about the model implementation may be found in app. D.

²⁵ These three cities were chosen because of their variation in demographic makeup. Los Angeles is a multiethnic city with a small (less than 10%) black population and a sizable Hispanic population. Atlanta has a large black population and a very small Hispanic and Asian population. Chicago has a more balanced multiethnic composition with substantial numbers of whites, blacks, and Hispanics.

²⁶ The cities are defined using census place boundaries. See chap. 9 of the Census Bureau's Geographic Areas Reference Manual (http://www.census.gov/geo/www/garm.html) for more information.

²⁷ The Gini index is computed from census data using the procedure described in detail in Nielsen and Alderson (1997). I use the executable program (prln04.exe) downloadable from Nielsen's web site: http://www.unc.edu/~nielsen/data/data.hlm.

TABLE 3
EMPIRICAL POPULATIONS

Race/Ethnic Group	% of Population (1)	Median Income (\$) (2)	Income Inequality (3)	Population (4)	Total Area (Square Miles) (5)
Los Angeles:					
White	33	44,841	.45	3,964,820	469
Black	11	27,310	.46		
Asian	10	37,186	.42		
Hispanic	47	28,759	.43		
Atlanta:					
White	33	60,936	.38	416,474	132
Black	61	23,128	.41		
Asian	2	37,759	.40		
Hispanic	5	36,545	.42		
Chicago:					
White	34	46,680	.38	2,896,016	234
Black	36	29,086	.45		
Asian	4	40,519	.39		
Hispanic	26	36,543	.39		

NOTE.—Within-race income inequality is measured by the Gini index. U.S. census data for places were downloaded from the National Historic Geographic Information System website.

other two cities. It also covers a smaller area, 132 square miles, compared with 234 for Chicago and 469 for Los Angeles.

I initialize the agent-based model using tables from the 2000 Census Summary Files 3A data that describe the joint distribution of race/ethnicity and income for all households in a given census tract. Each agent is a household, and the population represents a 20% sample of all households living in each census tract.²⁸ Agents are assigned to one of four exclusive race/ethnic groups: blacks, whites, Hispanics, and Asians. Income is categorical and is defined as the midpoint of the 16 2000 census income categories: \$0-\$9,999, \$10,000-\$14,999, \$15,000-\$19,999, \$20,000-\$24,999, \$25,000-\$29,999, \$30,000-\$34,999, \$35,000-\$39,999, \$40,000-\$44,999, \$45,000-\$49,999, \$50,000-\$59,999, \$60,000-\$74,999, \$75,000-\$99,999, \$100,000-\$124,999, \$125,000-\$149,999, \$150,000-\$199,999, and \$200,000 or more.²⁹ For the open-ended, highest income interval, I assign agents an

²⁸Owing to computational constraints, I could not simulate segregation dynamics using the entire population of each city. The 20% sample generates a sparser population distribution than actual 2000 Atlanta and Los Angeles. I experimented with household samples ranging from 5% to 30%. Once the sample reaches around 15%, changing the sample size did not seem to qualitatively change the results.

²⁹I decided to make income categorical largely for efficiency reasons. When agents' incomes are categorical, the program can store utilities associated with all possible agent types. Four race groups and 16 income categories result in 64 different agent types. This

income of \$250,000.³⁰ Within each neighborhood, I specify that an additional 15% of all housing units are vacant.³¹ Neighborhoods are defined as all housing units situated within the same census block group.³² Agents are initially distributed in space such that at the census-tract level the distribution of households in the model corresponds to the distribution of households in 2000 Chicago, Los Angeles, or Atlanta.³³

In each time step, a 0.01% sample of households is given an opportunity to choose a new neighborhood. Each agent evaluates the neighborhood it is currently living in and a 10% sample of all vacant housing units in the metro area.³⁴ The agent then moves to a new destination or stays put with probabilities proportional to the weights calculated in the utility function. Over time, the neighborhood options confronted by agents change as a function of previous mobility decisions. As neighborhoods change, housing prices change as well. I update housing prices using city-specific hedonic re-

dramatically speeds up the model, as each agent can look up its utility associated with a given neighborhood rather than calculating this value for each potential destination.

³⁰I experimented with other values for the open-ended interval, ranging from \$220,000 to \$400,000. Changing this value did not change the results.

³¹ Unfortunately, it is very difficult to calculate true neighborhood vacancy rates from the decennial census. The census lists metro area vacancy rates at around 5%. However, most units that are available for rent or purchase remain occupied until the new household moves in. Units listed as vacant in the census tend to be vacation homes or units that are not habitable (e.g., boarded up, burned out, etc.). I experimented with alternative metro vacancy rates (e.g., a metro vacancy rate of 10%). Changing the overall vacancy rate did not seem to change the qualitative results from the model, but it did change the speed of convergence. I did not experiment with varying the vacancy rate across neighborhoods within the metro area.

³² As Grannis (1998) has shown, block group boundaries are defined using geographic barriers (such as busy streets, parks, and highways), which correspond well to the layout of pedestrian-friendly streets. In addition, neighborhood social networks are bounded within what Grannis calls "tertiary" communities, areas within which houses can be connected without crossing a major or nonresidential street. Block groups are similar to or nest within tertiary communities.

³³ The tables needed to initialize the model are not available below the census-tract level, but the agent-based model geography is specified at the census block level. To initialize the model, I read in census tract data but distribute agents randomly to all blocks within the census tract. This has the effect of blurring segregation patterns at small levels of geography. However, since most researchers define census tracts as neighborhood boundaries, this strategy essentially preserves between-neighborhood segregation.

³⁴I limit the agents' consideration sets to a subsample of all vacant housing units for two reasons. From a computational standpoint, it is more efficient to manipulate lists containing a subset of all vacant units in the metro area. But there is also a substantive justification for this modeling decision. Given the time and effort involved in learning about available options, we would expect that people restrict their housing search to only a subset of vacant units. Indeed, marketing researchers and decision theorists have shown that, when making a decision, individuals typically restrict their options to a subset of all possibilities and then assess this reduced "consideration set" (Shocker et al. 1991; Payne, Bettman, and Johnson 1993).

gression models estimated from 2000 data. As discussed in the previous section, the models predict how median housing prices change as a function of changes in neighborhood median income and racial composition. The coefficients from these hedonic regression models are reported in table C1 in appendix C. Note that the simple pricing models omit many factors relevant to housing valuation (e.g., number of rooms; presence of fireplaces, garages, or swimming pools; structure type; age of unit; distance to central businesses). However, the predictive validity of these pricing equations is surprisingly robust to a number of omitted variables and specification errors, although the coefficients lose their structural interpretation (Butler 1982). Plots of fitted versus observed prices (available from the author) show that the predicted prices correspond closely to actual values.

I compare results under two scenarios: (1) a world in which agents have their empirical income distributions and (2) a world in which blacks' incomes follow the same distribution as those of whites.³⁵ The second scenario preserves initial empirical levels of racial segregation. I run the agent-based models until the spatial distribution of agents reaches a dynamic equilibrium in which agents may still be moving but the composition of neighborhoods is no longer changing. In practice, this occurs after approximately 50,000 time steps. I then calculate overall measures of segregation as well as the average neighborhood experienced by low-, middle-, and high-income blacks.³⁶

Results

Stylized model.—The simulations using artificial populations and geography produce three key findings. First, the extent to which between-race income inequality affects racial segregation depends on the level of within-race income inequality. When within-group income inequality is low, income differences between blacks and whites significantly increase levels of racial segregation. Table 4 shows the black-white index of dissimilarity across various scenarios. We see that when within-group income inequality is low (i.e., Gini = 0.15), an increase from medium to high black-white income inequality increases racial segregation by roughly 0.09 when the city

³⁵To assign blacks the white income distribution, I first calculate the proportion of whites in each of the 16 census income categories. I then assign each black household a new income according to its position in the income distribution. For example, the household at the 10th percentile of the black income distribution receives the income of the white household at the 10th percentile of the white income distribution.

³⁶ High-income blacks include black agents with a household income of at least \$75,000, middle-income blacks are those with a household income greater than \$20,000 and less than \$75,000, and low-income blacks are defined as those with a household income of less than \$20,000.

TABLE 4
SEGREGATION OUTCOMES UNDER DIFFERENT ASSUMPTIONS
ABOUT WITHIN- AND BETWEEN-RACE INEQUALITY

	RACIAL COMPOSITION			
INEQUALITY REGIME	15% Black	30% Black		
Gini = .15:				
High	.88	.93		
Medium	.79	.86		
None	.74	.82		
Gini = .35:				
High	.80	.85		
Medium	.73	.82		
None	.71	.79		
Gini = .55:				
High	.65	.73		
Medium	.64	.72		
None	.59	.68		
Gini = .75:				
High	.47	.55		
Medium	.45	.51		
None	.44	.50		

NOTE.—"High" refers to a regime in which blacks' median income is \$25,000. "Medium" refers to a regime in which blacks' median income is \$40,000. "None" refers to a regime in which there is no black-white income inequality and blacks' median income is \$60,000. In all cases, whites' median income is \$60,000.

proportion black is 0.15 and roughly 0.07 when the city proportion black is 0.3. In contrast, when within-race income inequality is high, for example, with a Gini index of 0.75, an increase in black-white income inequality has a much smaller effect on racial segregation. In between these two extremes, we see that the increase in racial segregation associated with increasing between-race income inequality attenuates at higher levels of within-race inequality.

Second, this process results from offsetting effects at the high and low ends of the income distribution. Figure 6 shows the average proportion black experienced under different inequality regimes by blacks at different income strata. The figure reports results under scenarios assuming a within-race Gini index of 0.35 and 0.55. In both cases, decreasing black-white income inequality results in a steady decline in the average proportion black experienced by poorer blacks. But the opposite relationship holds among the higher-income blacks. Here, a convergence in incomes between blacks and whites results in an increase in exposure to black neighborhoods. This offsetting is more pronounced when the black population is 15% of the total population than when it is 30% of the total population and also when within-race income inequality is 0.35 compared to 0.55. This is consistent with the argument that the extent to which offsetting occurs

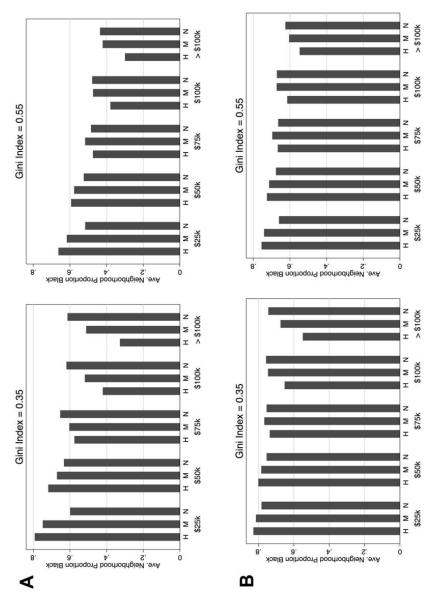


Fig. 6.—Average neighborhood proportion black experienced by blacks of different income strata under alternative between- and within-race inequality regimes: A, city 15% black; B, city 30% black. H = high between-race inequality, M = moderate between-race inequality. and N = no between-race inequality.

depends on the relative size of the black population and the degree of withinrace heterogeneity.

Third, when blacks are poorer, on average, than whites, high-income blacks will live in poorer neighborhoods, on average, than their white counterparts. Note that this pattern is also found in U.S. census data (cf. Logan 2011). Since the model by design excludes the possibility of institutional racism, this effect may be due to the forced choice these blacks must make between their racial and economic affiliations. Figure 7 shows the average neighborhood income experienced by blacks in different income strata. Here we see blacks at all points in the income distribution experience an increase in neighborhood median income as black incomes reach parity with those of whites. The figure also shows that the increase in neighborhood median income experienced by blacks across different levels of blackwhite income inequality is more pronounced when the city is 30% black than when the city is 15% black. One might be tempted to attribute this to the fact that a city in which blacks' incomes are less than whites' will be poorer overall when the population proportion black is larger. But there is no change in the average median income experienced by whites across different regimes of between-race income inequality.³⁷

Overall, I find that at moderate to high levels of within-race income inequality, the decrease in racial segregation that results from an attenuation or elimination of black-white inequality is a result of offsetting processes at the high and low ends of the income distribution. The effect is magnified when the black population is smaller relative to that of whites. These results are useful insofar as many factors are implicitly "held constant" in the simulation. But it is difficult to know whether the same patterns occur under more realistic circumstances. In the next section, I replicate a subset of these experiments using a more realistic agent-based model.

Empirically grounded model.—For the most part, the results from the realistic simulation models confirm the findings discussed in the previous section. Figure 8 shows the average neighborhood proportion black experienced by black agents in models that approximate the geography and racial makeup of Chicago, Los Angeles, and Atlanta under two scenarios: empirical income inequality and black-white income equality. Panel A

³⁷The figures for whites are not shown because of space constraints but are available from the author by request.

³⁸Note, however, that the PSID discrete choice models assume no unobserved heterogeneity in residential mobility behavior. This preference heterogeneity could potentially be important because of the asymmetry in the effects of income and race on choice. A preference for racial diversity can induce a higher-income black household to move into a neighborhood that is less expensive than what it can afford, but a preference for economic diversity may not be able to induce a low-income black household to move into a neighborhood that it cannot afford.

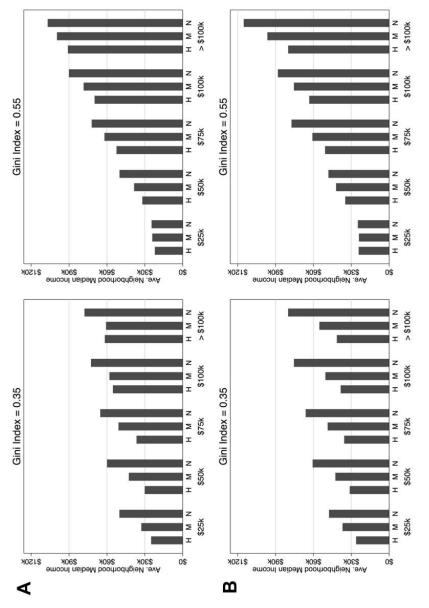
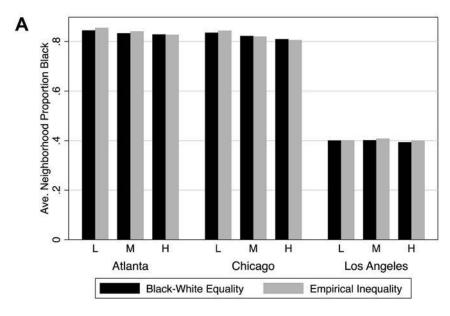


FIG. 7.—Average neighborhood median income experienced by blacks under alternative between-race inequality regimes: A, city 15% black; B, city 30% black. H = high between-race inequality, M = moderate between-race inequality, and N = no between-race inequality.



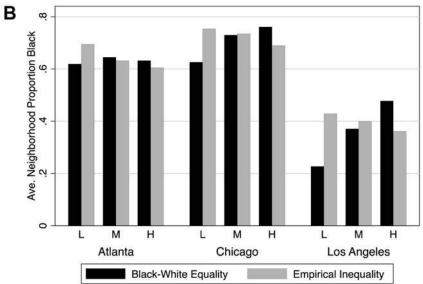


Fig. 8.—Neighborhood outcomes for low-, middle-, and high-income blacks: A, results at initialization; B, results at equilibrium.

reports the average neighborhood proportion black experienced at model initialization. We see that the neighborhood composition experienced by blacks in each of the three income categories is fairly constant across the two scenarios, and the average proportion black experienced by Los Angeles blacks is far lower than that experienced by blacks in Atlanta and Chicago. There is also a slight variation in the average proportion black experienced by blacks across income categories within cities. For example, in Atlanta the average proportion black experienced by high- and low-income blacks, respectively, is 0.827 and 0.845. Panel B of the figure shows the average neighborhood proportion black experienced at model equilibrium. Overall, these results support the offsetting argument and findings laid out in the previous section. A convergence in income between blacks and whites results in opposite effects for high- and low-income blacks. Moreover, this effect is more pronounced in Los Angeles, where the black population is smaller in relative size than in Atlanta and Chicago.

However, across all cases, the model equilibrium suggests a greater level of within-race variation in neighborhood racial experiences than is present at model initialization. In addition, while the simulation results under empirical levels of income inequality preserve key features of black-white segregation under income inequality (e.g., affluent blacks live in areas that have fewer black neighbors than poor blacks), the agent-based model does not preserve initial levels of segregation observed in 2000. Rather, for both the "empirical inequality" and "black-white income equality" cases, the model suggests that over time, all black households will experience a substantial decline in exposure to black neighbors.

One possible reason for this is that the model is projecting mobility over a very long time frame, in the absence of any outside systemic shocks. But other factors may also contribute to this predicted decline in segregation. First, the model assigns the same preference parameters to agents in all three cities, but there may be heterogeneity in preferences across areas. Second, the model does not distinguish between owners and renters. Since owned and rented housing are segregated in space and there are racial disparities in homeownership, this omits a potentially important feature of segregation processes. Third, the model assumes that agents have full information about a sample of available housing units from all over the county. In practice, we expect households to hear about only a small subset of available units or to look for units in only a handful of neighborhoods. Finally, the agent-based model assumes no discrimination on the part of real estate agents, landlords, and lenders. Any of these factors can result in the agent-based model predicting a decline in racial segregation.

On the one hand, there is no reason to expect that an agent-based model—even one that perfectly captures segregation dynamics in a given city—will reproduce or maintain exact patterns of segregation in a specific geographic

area because it is unlikely that existing neighborhoods are in equilibrium. So projecting mobility forward in time would be expected to change neighborhood conditions, even in a model that perfectly captures segregation dynamics. On the other hand, I want to ensure that the model is providing inferences that accurately capture mechanisms at work in real cities. Thus, as a final test of the framework, I examine 1980–2000 neighborhood change data from the 100 largest U.S. metro areas to see if, controlling for the relative size of the black population and within-race income inequality, a change in between-race inequality results in the predicted offsetting effects for high-and low-income blacks.

THE RELATIONSHIP BETWEEN INCOME INEQUALITY AND RACIAL SEGREGATION IN U.S. METRO AREAS, 1980–2000

The goal of this analysis is to determine the degree to which offsetting occurs in real cities. I estimate the effect of between- and within-race income inequality on the average neighborhood experiences of low- and high-income blacks using a set of fixed-effects models that control for time-varying and time-invariant metro attributes as well as changes over time common across all metro areas.³⁹

Data and Methods

I use U.S. Census Bureau data from the 1980 Summary File 3A, the 1990 Summary File 4A, and the 2000 Summary File 3A (GeoLytics 2004). I impose consistent metropolitan area definitions across census years to ensure the comparability of the results over time. I restrict my sample to the 100 metro areas with the largest populations in 2000; these areas account for 62% of the total U.S. population. Following past work looking at neighborhood change over time (Jargowsky 1996; Reardon and Bischoff 2011), I further constrain my sample to include only metro areas in which there were at least 10,000 black families in 1980, 1990, and 2000. This results in a final estimation sample of 93 metro areas.

There are two outcome variables: the average neighborhood proportion black experienced by affluent black families and the average neighborhood proportion black experienced by poor black families. Affluence is measured relative to the income distribution of each metro area and is defined as twice the metro median family income. Neighborhoods are defined as census tracts.

³⁹ This analysis is inspired by the strategy used by Reardon and Bischoff (2011) to assess the role of income inequality in explaining levels of income segregation. The untransformed independent variables used in the analysis are constructed identically to those in their original study. Their app. B contains a detailed description of these covariates.

The three predictors of interest are metro between-race income inequality (BRI), which is measured as a ratio of black median family income to white median family income; metro within-race income inequality (WRI), which is captured by the black Gini index; and the relative size of the black population (BP). If offsetting occurs in real neighborhoods, we would expect that (1) under sufficiently high WRI, an increase in BRI results in a decrease in the neighborhood proportion black experienced among affluent blacks and an increase in the neighborhood proportion black experienced by poor blacks; and (2) the effect of BRI is nonlinear and depends on the relative size of the black population. Taken together, these imply an interaction effect between WRI and BRI, an interaction effect between BRI and BP, and potentially higher-order effects of BRI, WRI, and BP.

More formally, I estimate the effect of changes in within- and betweenrace inequality on changes in the average neighborhood proportion black (NPB) experienced by affluent or poor blacks as

$$\begin{aligned} \text{NPB}_{my}^{\text{AFFLUENT/POOR}} &= \sum_{i=1,2j=1,2} \sum_{j=1,2} \zeta_{ij} \text{WRI}_{my}^{j} \text{BRI}_{my}^{i} \\ &+ \sum_{i=1,2} \sum_{j=1,2} \gamma_{ij} \text{BRI}_{my}^{j} \text{BP}_{my}^{i} \\ &+ \sum_{i=1,2} \varphi_{i} \text{WRI}_{my}^{i} + \sum_{i=1,2} \delta_{i} \text{BP}_{my}^{i} + \sum_{i=1,2} \beta_{i} \text{BRI}_{my}^{i} \\ &+ \theta_{m} + \Delta_{v} + \vartheta X_{mv} + \varepsilon_{mv}, \end{aligned}$$

$$(4)$$

where m indexes metropolitan areas, y indexes census years, BP and BRI are as defined above, and the superscripts i and j denote linear and squared terms. The first line of equation (4) captures the hypothesis that, at sufficiently high levels of WRI, the average proportion black experienced by affluent (poor) blacks will be lower (higher) at higher levels of BRI. The second line captures the hypothesis that the effect of BRI varies nonlinearly with the relative size of the black population. The third line of equation (4) includes all lower-order terms, and the fourth line of the model includes metropolitan area (θ_m) and decade (Δ_y) fixed effects.

The metro fixed effects control for all features of metro areas that are constant over decades; the year fixed effects capture all metro-invariant factors that change over time that might be associated with the neighborhood experiences of whites and blacks. To ensure that my results are not confounded by attributes of metro areas that change over time, the model also includes a set of time-varying covariates (X_{my}) . These include logged population size, unemployment rate, the proportion of the population under 18 years of age, the proportion of the population over 65, the proportion of the population 25 years old or older with less than a high school education, the proportion foreign born, and per capita income. Because each metro

area contributes three data points, I compute bootstrapped standard errors to take into account the clustered nature of the observations.

Table 5 presents summary statistics for both the outcome measures and the focal covariates. We see that, on average, affluent blacks live in areas with lower concentrations of blacks than poor blacks do. However, blacks at all points in the income spectrum live disproportionately with other blacks, given metro population composition. Over time, the average proportion black experienced by both affluent and poor blacks has decreased. The black Gini index has been increasing over time, and the income gap between blacks and whites has increased slightly since 1980. These findings are consistent with other research documenting trends in racial segregation and income inequality (e.g., Reardon and Bischoff 2011; DeNavas-Walt, Proctor, and Smith 2012).

Figure 9 plots the relationship between black-white income inequality, the black Gini index, and the size of the black population for all metro areas across all years. Different markers denote different years, and the size of the marker is proportional to the total number of blacks in the metro area. We see that there is a substantial correlation between black-white income inequality and the black Gini index; areas with high black-white income inequality also have substantial income inequality within the black population. We also see that areas with larger black populations (in absolute value) tend to have greater black-white income inequality. There is only one metro-decade observation in which the ratio of black median income to

TABLE 5 Average Neighborhood Proportion Black (NPB) and Between- and Within-Race Income Inequality Trends, 1980-2000

	1980	1990	2000	Change
Average NPB for affluent blacks	.455	.376	.360	10
	(.200)	(.188)	(.198)	
Average NPB for poor blacks	.554	.498	.466	09
	(.208)	(.211)	(.215)	
Metro proportion black (BP)	.121	.126	.139	.02
	(.086)	(.087)	(.092)	
Between-race income inequality (BRI)	.625	.595	.605	02
	(.071)	(.091)	(.103)	
Within-race income inequality (WRI)	.405	.425	.432	.03
	(.021)	(.034)	(.029)	
Total metro areas	93	93	93	

Note.—Between-race income inequality is captured by the ratio of black median income to white median income; within-race income inequality is captured by the black Gini index. Sample includes observations from the 100 largest metro areas in 2000, excluding observations from the seven metro areas that had fewer than 10,000 black families in all three decades.

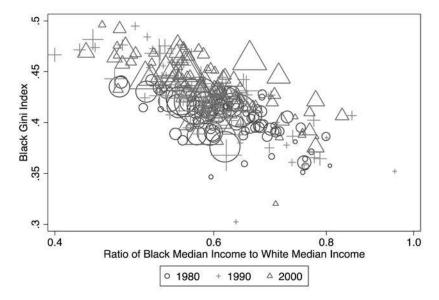


Fig. 9.—Relationship between Gini index (WRI) and ratio of black median income to white median income (BRI). The size of a marker is proportional to the total number of black households in a metro area.

white median income is close to 1.0, El Paso, Texas, in 1990, which has a very small black population.

Results

I estimate regression models using mean-deviated transformations of the covariates. Inspection of the data revealed no evidence of higher-order effects of within-race income inequality (the black Gini coefficient), so these parameters are omitted from the analysis. Table 6 reports the final model. Columns 1 and 2 of the table present results in which the outcome variable is the average neighborhood proportion black experienced by affluent blacks, while columns 3 and 4 present results in which the outcome variable is the average neighborhood proportion black experienced by poor blacks. Model 1 reports results using only metro and year fixed effects, while model 2 reports results using both the metro and year fixed effects and also the time-varying metro variables. Because of the fixed effects, the coefficients capture the average within-metro association over time between the focal attributes and the average neighborhood proportion black experienced by affluent or poor blacks.

TABLE 6
ESTIMATED EFFECT OF BETWEEN- AND WITHIN-RACE INCOME INEQUALITY
ON AVERAGE NEIGHBORHOOD PROPORTION BLACK

	Оитсом	E VARIABLE: AV		ORHOOD
	Experience Bla	by Affluent cks	Experienc Bla	e by Poor cks
	Model 1 (1)	Model 2 (2)	Model 1 (3)	Model 2 (4)
BRI	.236	.435*	334**	099
	(.198)	(.245)	(.153)	(.158)
BRI^2	5.205***	4.458**	.561	.586
	(1.255)	(1.526)	(.823)	(.840)
BP	1.201	1.482*	1.317**	1.236**
_	(1.058)	(.889)	(.572)	(.445)
BP^2	-3.415*	-1.197	.858	.359
	(1.973)	(2.123)	(1.321)	(1.898)
$BRI \times BP \dots$	394	233	973	.839
	(1.935)	(1.766)	(2.297)	(1.634)
$BRI \times BP^2 \dots \dots$	-67.591**	-44.231*	-11.468	-13.465
	(21.567)	(19.393)	(18.462)	(18.813)
$BRI^2 \times BP \dots$	10.227	12.189	-6.535	-3.812
2 2	(11.876)	(13.953)	(12.302)	(11.538)
$BRI^2 \times BP^2 \dots \dots$	-387.490***	-311.780***	-46.249	-32.040
	(105.547)	(93.497)	(69.733)	(85.336)
WRI	470	.235	-1.037**	863***
	(.522)	(.518)	(.401)	(.253)
$Year = 1990 \dots$	097***	103*	053***	085**
	(.013)	(.043)	(.006)	(.026)
$Year = 2000 \dots \dots$	115**	099	095***	138**
	(.020)	(.064)	(.012)	(.041)
Intercept	.431***	3.171**	.535***	2.095**
	(.021)	(1.059)	(.020)	(.779)
Model specification:	**	**		**
Metro and year fixed effects	Yes	Yes	Yes	Yes
Metro-year covariates		Yes		Yes
Adjusted R^2	.942	.964	.968	.976

Note.—N=279. Variables are specified as deviations from mean values. Bootstrapped SEs are in parentheses. Sample includes observations from the 100 largest metro areas in 2000, excluding observations from the seven metro areas that had fewer than 10,000 black families in all three decades. Coefficients on time-varying metro covariates and fixed effects are not shown. Metro-year covariates include city proportion black, racial diversity, metro population size, unemployment rate, proportion under age 18, proportion over age 65, proportion with a high school diploma, proportion foreign born, and per capita income.

^{*} P < .05.

^{**} P < .01.

^{***} P < .001.

Looking at the first panel of results, we see that there is strong evidence of a nonlinear, positive association between black-white income inequality and the average proportion black experienced by affluent blacks. The statistically significant coefficients for interactions between black-white income inequality and metro proportion black also support the second hypothesis: that the relationship between black-white income inequality and the average neighborhood proportion black experienced by affluent blacks depends on the relative size of the black population. The quadratic effect of metro proportion black is also statistically significant, implying that, all else equal, a larger black metro population is associated with a greater average proportion black experienced by affluent blacks. Note that none of the variables associated with within-race income inequality are statistically significant.

The second panel reports results in which the average neighborhood proportion black experienced by poor blacks is the outcome variable. Here we see a weak negative relationship between black-white income inequality and the average neighborhood proportion black experienced by poor blacks; this effect becomes statistically insignificant once I control for the time-varying metro covariates. There is no strong evidence that the effect of income inequality on the average proportion black experienced by poor blacks depends on the relative size of the black population. However, the main effect of metro proportion black is positive and statistically significant; poor blacks experience a higher number of black neighbors in areas with larger black populations. In contrast to the case for affluent blacks, the coefficient on within-race income inequality is statistically significant. Higher levels of black income inequality are associated with a lower average neighborhood proportion black for poor blacks.

Because of the transformations, interactions, and higher-order effects, it is difficult to grasp the substantive implications of the numbers reported in table 6. Figure 10 graphically illustrates the relationship between blackwhite income inequality and the neighborhood experiences of poor and affluent blacks, assuming that the metro percentage black is 1\%, 5\%, 10\%, or 20%. The lines are drawn using coefficients from model 2 (which controls for time-varying metro characteristics); all other variables are held constant at their mean values. In panel A, we see clearly the nonlinear and interactive relationship between black-white income inequality, black population size, and the average neighborhood proportion black experienced by affluent blacks. At very high levels of black-white income inequality, a decrease in black-white income inequality results in a decrease in the average proportion black experienced by affluent blacks. However, at lower levels of black-white income inequality, a decline in black-white income inequality results in an increase in the average proportion black experienced by affluent blacks, except in the case in which the black population is very

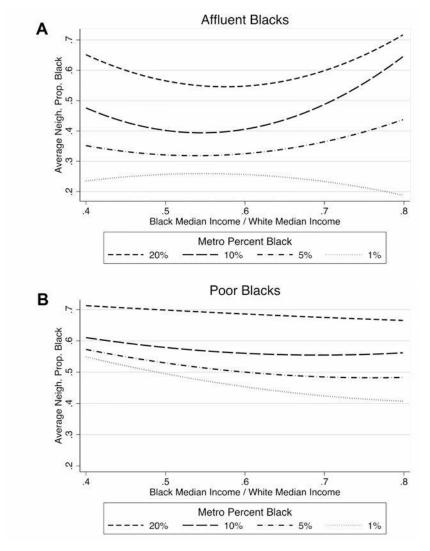


Fig. 10.—Predicted relationship between between-race income inequality and neighborhood composition by metro percent black, U.S. census data, 1980–2000.

small (1% of the total population). This increase is more pronounced when blacks are greater than 10% of the metro population. In contrast, in panel B, we see that a decrease in the level of black-white income inequality results in a corresponding decrease in the average proportion black experienced by poor blacks.

Overall, the results suggest that offsetting occurs in real populations when the black population is sufficiently large relative to the rest of the metro population and when black-white income inequality is not too extreme. Recall that the average metro percentage black in the top 100 metro areas is around 12%, sufficiently large to generate the offsetting effect.

CONCLUSION

People are separated in many contexts and, within each context, along multiple social attributes. Friendship networks are typically composed of people who share the same aspirations, family backgrounds, race, and education (Fischer 1982; Marsden 1987; Moody 2001). Within neighborhoods, we observe clustering by age, income, race, ethnicity, political affiliation, and sexual orientation (Massey and Denton 1988; Bishop 2008). Marriages and families bring together individuals with similar religion, education, age, and social class background (Kalmijn 1998; Schwartz and Mare 2005). Sociologists have a long-standing interest in the degree to which status attributes are correlated within individuals and across social contexts. To the extent that the same social dimensions characterize separation across multiple contexts and to the extent that key social attributes tend to be highly correlated among individuals, their effects will reinforce one another and consolidate group differences (Simmel 1908; Lenski 1954; Blau 1977; Blau and Schwartz 1984).

There are three potential pathways through which social differentiation along multiple attributes can occur. First, people may evaluate others on the basis of only one attribute, but that attribute is correlated with other characteristics that affect group composition. For example, the 1990s ban on affirmative action in college admissions in Texas and California state schools meant an elimination of race-based consideration. But since race and Scholastic Aptitude Test scores are highly correlated, the end result was a significant drop in admission rates for blacks and Hispanics. Second, people may care about multiple, uncorrelated group characteristics. For example, children tend to choose friends who resemble them in race/ethnicity and sex. The result is that friendship networks are segregated by both race and gender, but these reflect separate sorting processes. Third, people may care about multiple, correlated group characteristics. For example, individuals care about both the racial and economic composition of their neighborhoods and race and income are correlated attributes of individuals. Whites and Asians are, on average, wealthier than blacks and Hispanics. In this case, there is residential segregation by both race and income, and the processes that govern segregation by race and segregation by income are interrelated. The extent to which sorting along one dimension magnifies or

attenuates inequalities along other dimensions depends on the joint distribution of relevant traits within a population.

This study focuses on the segregation patterns that result from people sorting on multiple, correlated attributes. I propose an analytical framework that explicates the role of between- and within-race income inequality on racial segregation dynamics. The focal mechanism is offsetting: under sufficiently high levels of within-race income heterogeneity, increasing between-race income inequality can have opposite effects at the high and low ends of the income distribution. The effect is nonlinear and depends on the relative size of the black population, suggesting a kind of critical mass. I evaluate the empirical evidence supporting offsetting using empirically grounded agent-based models (where agents' behavior is specified on the basis of statistical estimates of residential mobility from the PSID) and also fixed-effects models of the relationships among between-race income inequality, within-race income inequality, and relative group size.

I first use a highly stylized agent-based model consisting of only two race/ethnic groups (blacks and whites) to explore how racial and economic sorting jointly produce segregation outcomes under different assumptions about the relative size of the minority population and the level of income inequality between and within race groups. The goal is to develop intuition for why, when, and how between- and within-group income inequality affect racial segregation. I find that when there is sufficient within-race income inequality, an increase in between-race income inequality increases lower-income blacks' exposure to black neighbors but decreases higher-income blacks' exposure to black neighbors. Depending on the size of the minority group and the degree of between- and within-race income inequality, the end result may be a substantial decrease in racial segregation or virtually no decrease in racial segregation.

Next, I explore segregation dynamics in an empirically grounded agent-based model that specifies the demographic composition, geography, and the initial population distribution approximate Chicago, Los Angeles, or Atlanta in 2000. While this model offers less analytical tractability than the highly stylized model discussed above, it offers more empirical plausibility (e.g., a realistic starting level of segregation and a multiethnic racial context). I compare segregation dynamics under empirical income distributions with segregation outcomes assuming income parity between blacks and whites. The results provide support for the offsetting mechanism; the elimination of black-white income inequality increases higherincome blacks' exposure to black neighbors and decreases poorer blacks' exposure to black neighbors. In all three cases, the convergence in income results in a small net decrease in segregation.

Finally, I use 1980–2000 U.S. census data to test whether the offsetting mechanism can help explain segregation dynamics in the 100 largest Ameri-

can cities. I estimate metropolitan-area-level statistical models of how the average proportion black experienced by high- and low-income blacks changes as a function of between-race income inequality, within-race income inequality, and the relative size of the black population. The models include fixed effects for metro areas and decade and also control for time-varying features of metro areas. The statistical analysis supports the offsetting mechanism but suggests that it comes into play only at moderate or low levels of black-white income inequality and when the black population is relatively at least 5% of the total population.

Taken together, the simulation and empirical analyses support the argument that offsetting is a potentially important and unrecognized mechanism that can attenuate the total change in racial segregation occurring with a convergence in income between blacks and whites. Theoretically, the results provide an analytical account of how the correlation among attributes and relative population size interact with in-group preferences to give rise to aggregate patterns of social separation and integration. I also suggest several key parameters—the size of race/ethnic groups and the degree of between- and within-race income variation—that determine how income inequality shapes overall levels of racial segregation. Methodologically, the analysis lays out an alternative to the conventional strategy for assessing the role of differences in income on racial segregation, one that allows income and racial sorting to be dynamically interdependent.

The Role of Offsetting in Segregation Dynamics

A natural question to ask is, How much should we revise our understanding of the role of economic factors in racial segregation processes in light of this study? The dominant finding in the empirical literature is that economic parity between blacks and whites does not result in a substantial net decrease in segregation, which is often taken as evidence that income inequities among racial groups do not play a critical role in driving patterns of racial segregation. This study suggests that the small effect of income is due to opposing processes that occur at the high and low ends of the income distribution. At moderate to high levels of segregation, higher-income blacks often must choose between living among economically similar households and living among racially similar households. As the incomes of blacks reach parity with those of whites, the decrease in racial isolation experienced by poor blacks is offset by the increase in racial isolation experienced by higher-income blacks.⁴⁰ Depending on the level of between- and within-

⁴⁰There is ample evidence to suggest that whites are not willing to tolerate more than a token number of black neighbors (Farley et al. 1993, 1997; Bobo and Zubrinsky 1996; Charles 2001). Thus, whites' behavior no doubt plays a key role in this process.

race income inequality and the relative size of the black population, the end result may be a net decrease in racial segregation, a net increase in racial segregation, or no change in racial segregation. The findings from this study suggest that we move beyond the distinctions emphasized by "spatial assimilation" and "place stratification"—which focus our attention primarily on between-group differences—and rather consider how both between- and within-race inequality shape neighborhood formation and change.

The extent to which income inequality affects racial segregation depends on the level of income inequality in the population. A key contribution of this work is to draw attention to the distinct roles of between- and withinrace heterogeneity in residential mobility decisions. While there is a large body of work exploring the role of between-race inequality in segregation dynamics, within-race heterogeneity has received far less attention. However, it is well established that the last 40 years have been characterized by growing income inequality, and inequality among blacks is growing faster than income inequality among whites (Piketty and Saez 2003; Autor, Katz, and Kearney 2006, 2008). This increase has been reflected in residential patterns; income segregation is on the rise overall, and since 1980 income segregation has been greater among blacks than among whites (Reardon and Bischoff 2011). At the same time, the black-white gap in median income has stagnated; it is 3 percentage points smaller today than it was in 1979 (DeNavas-Walt, Cleveland, and Webster 2003). I have shown that, with between-race income inequality held constant, an increase in within-race income inequality will lead to greater divergence in the residential mobility behavior of high- and low-income blacks. This suggests that the offsetting mechanism may play a greater role today than in the past.⁴¹

One important consideration, however, is the self-limiting aspect of the offsetting mechanism. When between-race income inequality is high, the average proportion black experienced by higher-income blacks may be lower, but there are fewer of these households to offset the higher average proportion black experienced by higher-income blacks. Thus, offsetting has

⁴¹Note that the simulation models assume that residential mobility behavior remains constant even as the joint distribution of population attributes changes. In reality, we might expect the relative importance of racial and economic factors in residential mobility decisions to shift with a change in between- or within-race income inequality. For example, an elimination of black-white income inequality might result in a decrease in the relative importance of racial factors in residential mobility decisions as households no longer associate the in-migration of blacks with a drop in housing values. In this case, a reduction or elimination of income inequality between race groups might not lead to the offsetting changes in neighborhood racial composition experienced by high- and low-income blacks as predicted by the model. Conversely, an increase in overall levels of income inequality may heighten individuals' awareness of economic factors in residential mobility decisions. In this case, offsetting will be more pronounced as higher-income blacks are more willing to trade off on racial factors to live among their economic peers.

its greatest net impact on overall levels of segregation at moderate to low levels of between-race inequality. Also, in the case of very high between-race inequality, a decrease in between-race inequality will likely produce a reduced racial isolation for both high- and low-income blacks. This point was illustrated in figure 10, which showed that in U.S. metro areas, an increase in income parity between blacks and whites results in greater racial isolation for affluent blacks only when the ratio of black median income to white median income is 0.6 or more.⁴² Thus, offsetting occurs only in situations in which there is sufficient overlap in the incomes of whites and blacks.

The Role of Offsetting in Other Contexts

The framework developed for this study can be applied to other cases in which individuals sort themselves into units on the basis of multiple correlated attributes. For example, high school students select friends who resemble them in race, gender, grade in school, and family background. In a school where minority groups are poorer than whites, a black or Hispanic student coming from a more affluent household must choose between peers who resemble her in family income and peers who resemble her in race. Were income disparities between whites and minority groups to be eliminated, this choice would not be necessary. Along these lines, Moody (2001) documents a nonlinear relationship between racial heterogeneity within schools and the odds of having a same-race friend. He attributes this to a change in preferences, arguing that as racial heterogeneity in schools increases, the preference for a same-race friend also increases. He notes that the nonlinearity suggests a "critical mass" type relationship in which preferences change only once racial diversity in the school crosses a given threshold. An alternative explanation is that preferences remain constant, but the increase in racial heterogeneity leads to a critical number of minority group members who meet friendship criteria along multiple dimensions. The larger the size of the minority group, the lower the level of racial heterogeneity necessary to generate this critical number. 43

Sociology has a long tradition of formal analysis investigating how structural factors such as the size and composition of populations constrain what social groupings are possible (e.g., Simmel 1908; Blau 1977; Rytina and Morgan 1982; McPherson 1983; Blau and Schwartz 1984; Wimmer and Lewis 2010). However, there is little knowledge of how this process

⁴² In 2000, approximately half of the top 100 largest U.S. cities had levels of black-white income inequality such that the ratio of black median income to white median income was at least 0.6.

 $^{^{43}}$ Note that Moody (2001) controls for school size but does not interact this parameter with the racial heterogeneity measure.

unfolds dynamically or how the joint distribution of traits in the population interacts with individuals' multidimensional preferences to generate macrolevel patterns of inequality. Blending agent-based models with empirical analyses provides one potentially fruitful strategy for assessing how population composition interacts with individual behavior to generate population patterns of social separation or integration.

APPENDIX A Parameter Estimates from Discrete Choice Models, PSID

TABLE A1
COEFFICIENTS FROM DISCRETE CHOICE MODELS, PSID

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		Сон	EFFICIENT ESTIMA	TES
Racial factors: %black 421 .641 .512 %black² -3.083 .652 .000 black × %black 5.146 .725 .000 black × %black² 583 .721 .419 Hispanic × %black² .359 .891 .687 Hispanic × %black² .223 1.157 .847 %Hispanic ° -3.64 1.145 .750 Hispanic × %Hispanic ° -3.64 1.145 .750 Hispanic × %Hispanic ° -3.704 1.299 .004 Hispanic × %Hispanic ° -3.704 1.299 .004 Black × %Hispanic ° -7.65 1.484 .606 %Asian ° -7.65 1.484 .606 %Asian ° -1.611 .667 .016 %Asian ° -1.049 1.548 .498 Asian × %Asian ° -17.687 4.865 .000 %white² -2.242 .258 .000 %white × %white² 2.010 .313 .000 Dij × %black ° -3.002 1.226 .014 <t< th=""><th>Variable</th><th>β</th><th>SE</th><th>P-value</th></t<>	Variable	β	SE	P-value
%black 421 .641 .512 %black -3.083 .652 .000 black × %black 5.146 .725 .000 black × %black² 583 .721 .419 Hispanic × %black .359 .891 .687 Hispanic × %black² .223 1.157 .847 %Hispanic² -2.144 .906 .018 %Hispanic × %Hispanic 8.121 1.078 .000 Hispanic × %Hispanic² -3.704 1.299 .004 Hlack × %Hispanic² -3.704 1.299 .004 Black × %Hispanic² -7.65 1.484 .606 %Asian -1.611 .667 .016 %Asian² -1.049 1.548 .498 Asian × %Asian 14.985 2.602 .000 Asian × %Asian² 14.985 2.602 .000 %white × %white² 2.010 .313 .000 \$0\$*** -2.242 .258 .000 \$0*** -9.302 1.226 .014 \$0**** -1.935	$\overline{D_{ij}}$	5.983	.519	.000
%black × %black 5.146 .725 .000 black × %black 5.146 .725 .000 black × %black -583 .721 .419 Hispanic × %black .359 .891 .687 Hispanic × %black² .223 1.157 .847 %Hispanic · %Hispanic -2.144 .906 .018 %Hispanic × %Hispanic 8.121 1.078 .000 Hispanic × %Hispanic² -3.704 1.299 .004 Black × %Hispanic² -3.704 1.299 .004 Black × %Hispanic² -7.765 1.484 .606 %Asian -1.611 .667 .016 %Asian² -1.611 .667 .016 %Asian × %Asian 14.985 2.602 .000 Asian × %Asian² -17.687 4.865 .000 white × %white² -2.242 .258 .000 white × %white² 2.010 .313 .000 D _{ij} × %black -3.002 1.226 .014 D _{ij} × %black × %black -1.935 1.055 .067	Racial factors:			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		421	.641	.512
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	%black ²	-3.083	.652	.000
Hispanic × %black .359 .891 .687 Hispanic × %black² .223 1.157 .847 %Hispanic -2.144 .906 .018 %Hispanic × %Hispanic 8.121 1.078 .000 Hispanic × %Hispanic² -3.704 1.299 .004 Hispanic × %Hispanic² -3.704 1.299 .004 Black × %Hispanic² -3.705 1.484 .606 %Asian -1.611 .667 .016 %Asian² -1.049 1.548 .498 Asian × %Asian 14.985 2.602 .000 Asian × %Asian² -17.687 4.865 .000 %white² -2.242 .258 .000 white × %white² 2.010 .313 .000 D_{ij} × %black² -3.002 1.226 .014 D_{ij} × %black² -1.935 1.055 .067 D_{ij} × black × %black -1.935 1.055 .067 D_{ij} × Hispanic × %black -1.940 1.603 .226 D_{ij} × Hispanic × %black 4.367 2.219	black × %black	5.146	.725	.000
Hispanic \times %black² .223 1.157 .847 %Hispanic -2.144 .906 .018 %Hispanic \times %Hispanic 8.121 1.078 .000 Hispanic \times %Hispanic² -3.704 1.299 .004 Black \times %Hispanic² -3.704 1.299 .004 Black \times %Hispanic² -3.704 1.299 .004 %Asian \times %Hispanic² -7.65 1.484 .606 %Asian -1.611 .667 .016 %Asian² -1.049 1.548 .498 Asian \times %Asian² 14.985 2.602 .000 Asian \times %Asian² -17.687 4.865 .000 white² -2.242 .258 .000 white \times %white² 2.010 .313 .000 D_{ij} \times %black -3.002 1.226 .014 D_{ij} \times %black -1.935 1.055 .067 D_{ij} \times black \times %black -1.935 1.055 .067 D_{ij} \times Hispanic \times %black -1.488 1.572 .344 D_{ij} \times Hispanic \times %Hispanic	$black \times \%black^2 \dots \dots$	583	.721	.419
%Hispanic -2.144 .906 .018 %Hispanic² 364 1.145 .750 Hispanic × %Hispanic 8.121 1.078 .000 Hispanic × %Hispanic² -3.704 1.299 .004 Black × %Hispanic 1.386 1.107 .211 Black × %Hispanic² -7.65 1.484 .606 %Asian -1.611 .667 .016 %Asian² -1.049 1.548 .498 Asian × %Asian 14.985 2.602 .000 Asian × %Asian² -17.687 4.865 .000 white² -2.242 .258 .000 white × %white² 2.010 .313 .000 D_{ij} × %black -3.002 1.226 .014 D_{ij} × %black² 6.126 1.529 .000 D_{ij} × black × %black -1.935 1.055 .067 D_{ij} × black × %black² -1.940 1.603 .226 D_{ij} × Hispanic × %black² -2.746 4.274 .521 D_{ij} × %Hispanic × %black² -2.746	Hispanic × %black	.359	.891	.687
%Hispanic 2 364 1.145 .750 Hispanic \times %Hispanic 8.121 1.078 .000 Hispanic \times %Hispanic 2 -3.704 1.299 .004 Black \times %Hispanic 2 1.386 1.107 .211 Black \times %Hispanic 2 -7.65 1.484 .606 %Asian 2 -1.611 .667 .016 %Asian 2 -1.049 1.548 .498 Asian \times %Asian 2 -1.049 1.548 .498 Asian \times %Asian 2 -17.687 4.865 .000 %white 2 -2.242 .258 .000 white \times %white 2 2.010 .313 .000 D_{ij} \times %black 2 -3.002 1.226 .014 D_{ij} \times %black 2 6.126 1.529 .000 D_{ij} \times black \times %black 2 -1.940 1.603 .226 D_{ij} \times Hispanic \times %black 2 -1.940 1.603 .226 D_{ij} \times Hispanic \times %black 2 -2.746 4.274 .521 D_{ij} \times %Hispanic 2 2.698 2.460 2.73 </td <td>$Hispanic \times \%black^2 \dots$</td> <td>.223</td> <td>1.157</td> <td>.847</td>	$Hispanic \times \%black^2 \dots$.223	1.157	.847
%Hispanic 2 364 1.145 .750 Hispanic \times %Hispanic 8.121 1.078 .000 Hispanic \times %Hispanic 2 -3.704 1.299 .004 Black \times %Hispanic 2 1.386 1.107 .211 Black \times %Hispanic 2 -7.65 1.484 .606 %Asian 2 -1.611 .667 .016 %Asian 2 -1.049 1.548 .498 Asian \times %Asian 2 -1.049 1.548 .498 Asian \times %Asian 2 -17.687 4.865 .000 %white 2 -2.242 .258 .000 white \times %white 2 2.010 .313 .000 D_{ij} \times %black 2 -3.002 1.226 .014 D_{ij} \times %black 2 6.126 1.529 .000 D_{ij} \times black \times %black 2 -1.940 1.603 .226 D_{ij} \times Hispanic \times %black 2 -1.940 1.603 .226 D_{ij} \times Hispanic \times %black 2 -2.746 4.274 .521 D_{ij} \times %Hispanic 2 2.698 2.460 2.73 </td <td>%Hispanic</td> <td>-2.144</td> <td>.906</td> <td>.018</td>	%Hispanic	-2.144	.906	.018
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	%Hispanic ²	364	1.145	.750
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$Hispanic \times \% Hispanic \dots$	8.121	1.078	.000
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$Hispanic \times \% Hispanic^2 \dots$	-3.704	1.299	.004
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Black × %Hispanic	1.386	1.107	.211
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$Black \times \%Hispanic^2 \dots$	765	1.484	.606
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	%Asian	-1.611	.667	.016
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	%Asian ²	-1.049	1.548	.498
$\begin{array}{llllllllllllllllllllllllllllllllllll$		14.985	2.602	.000
$\begin{array}{llllllllllllllllllllllllllllllllllll$	$Asian \times \%Asian^2 \dots$	-17.687	4.865	.000
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	%white ²	-2.242	.258	.000
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	white \times % white ²	2.010	.313	.000
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$D_{ii} \times \%$ black	-3.002	1.226	.014
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$D_{ii} \times \% \mathrm{black}^2 \ldots \ldots$	6.126	1.529	.000
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		-1.935	1.055	.067
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		-1.940	1.603	.226
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		4.367	2.219	.049
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		-2.746	4.274	.521
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		-1.488	1.572	.344
$D_{ij} \times$ Hispanic × % Hispanic² -1.666 2.488 .503 $D_{ij} \times$ black × % Hispanic 3.036 1.712 .076 $D_{ij} \times$ black × % Hispanic² -3.160 3.369 .348 $D_{ij} \times$ % Asian 5.805 1.587 .000 $D_{ij} \times$ % Asian² -10.838 3.816 .005 $D_{ij} \times$ Asian × % Asian -12.251 5.176 .018		2.698	2.460	.273
$D_{ij} \times$ Hispanic × % Hispanic² -1.666 2.488 .503 $D_{ij} \times$ black × % Hispanic 3.036 1.712 .076 $D_{ij} \times$ black × % Hispanic² -3.160 3.369 .348 $D_{ij} \times$ % Asian 5.805 1.587 .000 $D_{ij} \times$ % Asian² -10.838 3.816 .005 $D_{ij} \times$ Asian × % Asian -12.251 5.176 .018	$D_{ii} \times \text{Hispanic} \times \% \text{Hispanic} \dots$.102	1.357	.940
$D_{ij} \times$ black \times %Hispanic ² -3.160 3.369 .348 $D_{ij} \times$ %Asian 5.805 1.587 .000 $D_{ij} \times$ %Asian ² -10.838 3.816 .005 $D_{ij} \times$ Asian \times %Asian -12.251 5.176 .018		-1.666	2.488	.503
$D_{ij} \times$ black \times %Hispanic ² -3.160 3.369 .348 $D_{ij} \times$ %Asian 5.805 1.587 .000 $D_{ij} \times$ %Asian ² -10.838 3.816 .005 $D_{ij} \times$ Asian \times %Asian -12.251 5.176 .018		3.036	1.712	.076
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		-3.160	3.369	.348
$D_{ij}^{i} \times \% A \sin^{2} \dots -10.838$ 3.816 .005 $D_{ij} \times A \sin \times \% A \sin \dots -12.251$ 5.176 .018		5.805	1.587	.000
$D_{ij} \times Asian \times \% Asian \dots -12.251$ 5.176 .018	$D_{ii} \times \% A sian^2 \dots$		3.816	
		22.061	12.896	.087

TABLE A1 (Continued)

	Сов	FFICIENT ESTIMA	TES
Variable	β	SE	P-value
$D_{ij} \times \%$ white ²	.350	.534	.512
$D_{ij} \times \text{white} \times \% \text{white}^2 \dots \dots$	989	.208	.000
Economic factors:			
Income ratio	-1.215	.121	.000
Income ratio ²	.002	.000	.000
$D_{ij} \times \text{income ratio} \dots \dots$.479	.124	.000
$D_{ij}^{\circ} \times \text{income ratio}^2 \dots \dots$	016	.010	.123
Price ratio	2.075	.693	.003
Price ratio ²	-4.654	1.092	.000
$D_{ij} \times \text{price ratio} \dots \dots$	-3.858	1.370	.005
$D_{ij}^{\circ} \times \text{price ratio}^2 \dots \dots$	5.176	2.021	.010
Median income	031	.003	.000
Median income ²	.000	.000	.000
$D_{ij} \times \text{median income}_{2} \dots \dots$.031	.005	.000
$D_{ij}^{\circ} \times \text{median income}^2 \dots$.000	.000	.055

Note.—N = 951,719; log likelihood = -39,308. Observation unit is person-years. Income ratio is the ratio of household income to neighborhood median income; price ratio is the ratio of the 20th percentile monthly rent in the neighborhood to monthly household income (one-twelfth of annual income). Median income is in \$1,000s.

APPENDIX B

Parameters Used for Singh-Maddala Distributions

The theoretical income distributions used in the stylized agent-based model are generated from the Singh-Maddala statistical distribution. The three-parameter Singh-Maddala distribution is the four-parameter generalized beta II distribution with shape parameter p=1. It is also known as the Burr distribution, Pareto IV, beta-P, and generalized log-logistic distribution. See Kleiber and Kotz (2003) for more information. Table B1 shows the parameters used to generate each distribution. I use the rsinmad function in the "sinmad" R statistical package to generate random deviates. Files containing simulated income distributions are available from the author by request.

TABLE B1
PARAMETERS USED TO GENERATE INCOME DISTRIBUTIONS FOR
HYPOTHETICAL POPULATIONS

		PARAMETER	
Median Income (\$)	a	q	Scale
Gini index .15:			
63,331	1.05	3.51	270,000
40,855	1.05	3.51	175,000
26,960	1.05	3.51	117,000

Table B1 (Continued)

		PARAMETER	
Median Income (\$)	a	q	Scale
Gini index .35:			
64,500	1.80	3.51	150,000
40,854	1.80	3.51	95,000
27,411	1.80	3.51	64,000
Gini index .55:			
63,256	4.80	3.51	87,000
41,321	4.80	3.51	56,000
27,643	4.80	3.51	37,000
Gini index .75:			
63,256	4.80	3.51	87,000
41,321	4.80	3.51	56,000
27,643	4.80	3.51	37,000

Note.—These income distributions were generated using the R package VGAM, which contains the function "rsinmad." The function simulates random deviates from a Singh-Maddala distribution with specified parameters.

APPENDIX C

Hedonic Pricing Models

Housing prices in the agent-based model are updated using estimates from a hedonic pricing model. This model was estimated from Census 2000 Summary Tape File 3A for Los Angeles and Atlanta. The coefficients are shown in table C1.

TABLE C1 Hedonic Pricing Equations

	ouleWalue						
.336	•	β	SE	P-Value	β	SE	P-Value
005	5 .000	533	.002	000.	437	.005	000.
	1 .876	554	.003	000.	628	.007	000.
		037	.003	000.	223	900.	000.
	•	.426	.002	000.	.156	.003	000.
%white ² –.246 .009	000.	456	.002	000.	127	.004	000.
		238	.002	000.	144	.004	000.
-1.887	2 .000	.504	.003	000.	.387	.010	000.
Median income (in \$1,000s)		.027	.021	000.	.020	000.	000.
	000.	000.	000.	000.	000.	000.	000.
Constant		6.128	.001	000.	6.028	.003	000.
N	145		2,445,250			1,319,150	
	4		.882			.772	

NOTE.—Estimated from 2000 Census STF3A data. Outcome is logged median neighborhood monthly housing costs. Units are neighborhoods (census tracts), weighted by the total number of households living in the area.

APPENDIX D

Technical Details for Geographically and Demographically Grounded Agent-Based Models of Segregation Dynamics

This appendix describes some of the technical details of the model implementation for the empirically grounded agent-based model discussed in the section on simulation experiments. The model is written in Java and uses the REPAST (http://repast.sourceforge.net/) and JUMP (http://www.vivid solutions.com/jump/) libraries. I use unified modeling language (UML) diagrams to graphically represent the object-oriented programing code. UML lays out a set of well-defined and standardized schematics-independent of any specific programming language—for representing the underlying logic of a model. This technique has become the gold standard for describing objectoriented programming code (Fowler 2003), and there has recently been a call for agent-based modelers to incorporate these diagrams into documentation and publications (Bersini 2012). The two UML diagrams I make use of below are class diagrams (which describe the variables and methods contained within a given module of the program) and sequence diagrams (which describe how different aspects of the model interact). More detailed discussion of the basic architecture of agent-based models can be found in Macal and North (2005).

The model consists of 12 main classes. Figure D1 shows the overall class structure of the model. Note that each class denotes a particular type of agent, each with its own attributes (variables) and things that it does (methods). The main class, *Mirar* (model of income, race, and residence), controls the overall sequence of actions executed by the model. It contains the functions that both set up the initial physical environment and populate it with agents. This class also executes a series of commands to sample and move agents in each time step. The MirarUtils class contains all the small helper functions used within the model. For example, all the random distributions (multinomial, binomial) used within various parts of the model are managed within this class. The Block, BlockGroup, and CensusTract classes generate the different levels of geography. Blocks are nested within block groups, which are nested within tracts. Several classes exist solely to manage different components of the model. For example, the AgentHandler class contains commands that gather, sort, and sample from the population of agents while the Census Unit Handler class manages interactions among the census tracts, block groups, and blocks. This class also computes all segregation measures used in the model. The JumpHandler class contains commands to manage the spatial information (GIS) used in the model and to generate a display of the agents distributed across the urban landscape. The Mediator class manages interactions between census units, geographic relationship among census units, and agents. Thus, for example, when agents want to get information about the neighborhood associated with their cur-

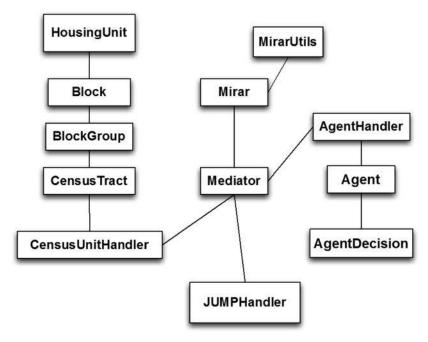


Fig. D1.—Overall class structure

rent housing unit or other potential destinations, these requests are handled through the Mediator. Finally, the *AgentDecision* class holds the PSID coefficients used to calculate utility. This class also contains all the functions used to compute various dimensions of neighborhood composition (e.g., neighborhood proportions black, white, Asian, and Hispanic).

Figure D2 shows selected variables and methods for the *Agent* and *AgentDecision* classes. Each agent has a unique race, income, and place of residence (HousingUnit). Agents are also assigned a memory, which records all housing units that agent has lived in over the course of the simulation. To calculate the desirability of their current unit and all potential destination units, agents are assigned an AgentDecision. The program was designed such that, in theory, each agent could have a unique decision rule. The variables held by the AgentDecision include the agent to which it is associated as well as a matrix of coefficients used in the calculation of utility. For the results reported in this study, these coefficients come from the PSID. The AgentDecision class uses attributes of its associated agent to plug in the appropriate race and income attributes for calculating utility values.

Figure D3 shows how various pieces of the agent-based model interact for a given mobility decision. The Mediator class samples a subset of agents

Agent race income memory housingUnit agentDecision move(ArrayList vacantHousingUnitList) moveIn(HousingUnit) SetMemory(ArrayList locationList) AgentDecision agent **PSIDcoefficients** getPctBlackInNeighborhood() getPctWhiteInNeighborhood() getPctHispanicInNeighborhood() getPctAsianInNeighborhood() getMedianIncomeInNeighborhood() getPriceOfUnit() computeUtilityForOwnUnit() computeUtilityForVacantUnits() selectUnit() getBlock()

Fig. D2.—Agent and agent decision class

and gives each one an opportunity to move. Each agent makes a call to its associated AgentDecision, which in turn asks the HousingUnit and Blocks associated with each potential destination to provide information about their neighborhood racial and economic composition. This information is used to calculate utilities associated with the current housing unit and all potential destinations. The AgentDecision class then passes those utilities to the MirarUtils class, which turns them into probabilities (by dividing by the sum of the utilities) and samples one unit using those probabilities. The MirarUtils class returns the chosen unit to the AgentDecision class, which in turn passes it back to the Agent.

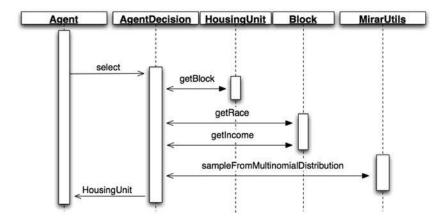


Fig. D3.—Sequence diagram for mobility decision process

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