

STRENGTH OF MATERIALS - GATE

Kulasekaran

February 8, 2023

Contents

1	Composition, Resolution and Equilibrium of Forces	2
1.1	Force	2
1.2	Force systems	2
1.2.1	Collinear	2
1.2.2	Concurrent	2
1.2.3	Coplanar	2
1.2.4	Coplanar Concurrent	3
1.2.5	Non-Coplanar Concurrent	3
1.2.6	Coplanar Non-Concurrent	3
1.2.7	Non-Coplanar Non-Concurrent	3
1.3	Triangular Law of forces	3
1.4	Parallelogram Law of forces	3
1.5	Polygon Law of forces	4
1.6	Resolution of Forces	4
1.7	Equilibrium state	4
1.8	Lami's Theorem	4
2	Analysis of Simple trusses	6
3	Friction	7
4	Work and Energy	8
5	Virtual work	9
6	Center of Gravity and Moment of Inertia	10
7	Impulse and Momentum	11
8	Lagrangian Equation	12

Chapter 1

Composition, Resolution and Equilibrium of Forces

1.1 Force

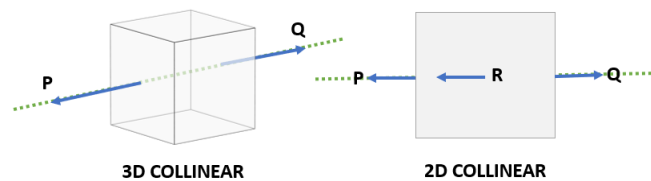
- It is the action of one body on another that changes the state of being (rest/uniform motion) of the object on which it is being applied
 - 3 things are needed to define a force: Magnitude, direction, Point of application
 - According to Newton's first law: $Force = Mass * Acceleration$
-

1.2 Force systems

- **Coplanar** - 2D system
- **Non-Coplanar** - 3D system

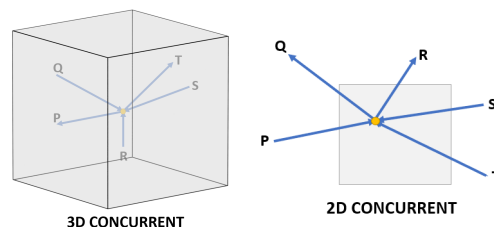
1.2.1 Collinear

- Two or more forces whose line of action is same



1.2.2 Concurrent

- Two or more forces which meet at a common point



1.2.3 Coplanar

- Forces that are on the same plane

1.2.4 Coplanar Concurrent

- Forces that are on the same plane and meet at a common point as well

1.2.5 Non-Coplanar Concurrent

- Forces are not on the same plane but meet at a common point

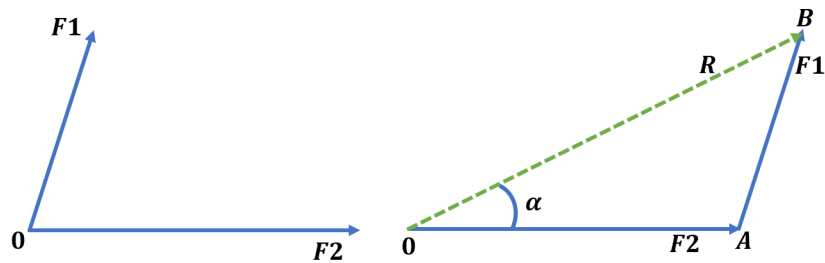
1.2.6 Coplanar Non-Concurrent

- Forces are on the same plane but don't meet at a common point

1.2.7 Non-Coplanar Non-Concurrent

- Forces are neither on the same plane nor meet at a common point

1.3 Triangular Law of forces

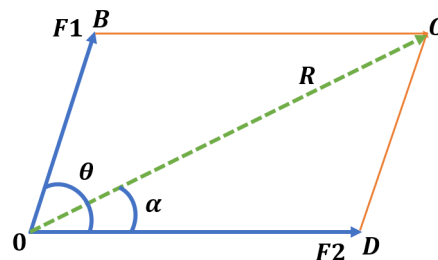


- Two concurrent forces acting on a body is represented in magnitude and direction by two sides of a triangle taken in order, then their third side will represent the resultant of two forces in the direction and magnitude taken in opposite order

$$R = \sqrt{F_1^2 + F_2^2} \quad \alpha = \cos^{-1} \left(\frac{F_1}{R} \right) = \sin^{-1} \left(\frac{F_2}{R} \right)$$

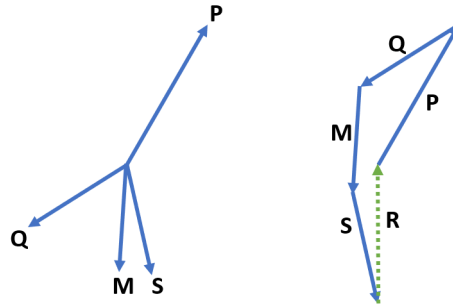
1.4 Parallelogram Law of forces

- If two concurrent forces are represented in magnitude as the two sides of a parallelogram, then the resultant of these two forces is the diagonal of the parallelogram



$$R = \sqrt{F_1^2 + 2F_1F_2 \cos \theta + F_2^2}$$

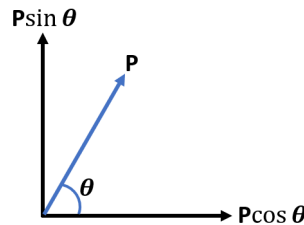
1.5 Polygon Law of forces



- The triangular law can be extended to the polygon law. *If a number of coplanar concurrent forces are represented in magnitude and direction by the sides of a polygon, taken in order, then their resultant can be represented by the closing side of the polygon*

1.6 Resolution of Forces

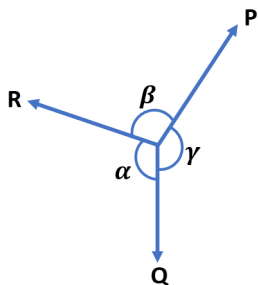
- The concept of replacing a single force at some angle with two of its component in the vertical and horizontal direction is called Resolution of forces.



1.7 Equilibrium state

- A body is said to be in equilibrium if it is at rest or moving with uniform velocity. **Under equilibrium state, the resultant of the force system will be zero.**

1.8 Lami's Theorem



If 3 coplanar concurrent forces are in equilibrium, then each force is proportional to the sine of the angle between the other two sides

$$\frac{P}{\sin \alpha} = \frac{Q}{\sin \beta} = \frac{R}{\sin \gamma}$$

Chapter 2

Analysis of Simple trusses

.

Chapter 3

Friction

•

Chapter 4

Work and Energy

•

Chapter 5

Virtual work

.

Chapter 6

Center of Gravity and Moment of Inertia

.

Chapter 7

Impulse and Momentum

•

Chapter 8

Lagrangian Equation

•