$\begin{array}{c} {\rm UMC~202} \\ {\rm PROBLEM~SET~2} \end{array}$

- (1) Use Newton's method to find solutions accurate to within 10^{-5} to the following problems
 - (a) $x^3 2x^2 5 = 0$ on the interval [1, 4].
 - (b) $x^2 2xe^{-x} + e^{-2x} = 0$ on the interval [0, 1].
 - (c) $x^3 3x^2(2^{-x}) + 3x(4^{-x}) 8^{-x} = 0$ on the interval [0, 1].
- (2) Use Newton's method, secant method and method of False position for finding the approximations of the two zeros, one in [-1,0] and other in [0,1] to within 10^{-6} accuracy of $f(x) = 230x^4 + 18x^3 + 9x^2 221x 9$. Use the end points of the interval as initial guesses for the secant method, method of False position and the midpoint for Newton's method.
- (3) Let $f(x) = e^x x 1$.
 - (a) Show that f has a zero of multiplicity 2 at x = 0.
 - (b) Find the rate of convergence for the Newton's method.
 - (c) Is any modification in the Newton's method improves the rate of convergence.