

Binary and Ternary Search

3 4 7 9

3 7 14 23

Q. Given an array of n positive integers. Your task is to divide it into k contiguous non-empty segments so that the maximum sum on the segment is the minimum possible.

Link:

<https://codeforces.com/edu/course/2/lesson/6/3/practice/contest/285083/problem/B>

$k \leq n$

2 3 4 6

Ans ≥ 6 ans Ans ≤ 15

Left = 6 and right = 15

Between = $6 + 15/2 = 10$

If we can divide our segments such that the maximum sum of our segments is ≤ 10 .

2 3 4 // 9

6 // 6

Left = 6 and Right 10

Between = $(6+10)/2 = 8$

2 3 // 5

4 // 4

6 // 6

Not Possible

Left = 9 Right = 10

Middle = $19/2 = 9$

2 3 4 // 9

6 // 6

Left = 9 right = 9

Break ans = 9

Counter case: 1 1 1 1 1 1 1 1 1 1 10

```
int count(vector<int> &v, int lim)
{
    int c = 1, cursum = 0;
    for (auto num : v)
    {
        if (cursum + num > lim)
        {
            c++;
            cursum = num;
        }
        else
            cursum += num;
    }
    return c;
}

int maxsum(vector<int> &v, int k)
{
    int n = v.size();
    int sum = 0, mx = 0;
    for (auto num : v)
    {
        mx = max(mx, num);
        sum += num;
    }
    int lb = mx, ub = sum, ans = sum;
    while (lb <= ub)
```

```

    {
        int md = lb + (ub - lb) / 2;
        if (count(v, md) <= k)
        {
            ans = md;
            ub = md - 1;
        }
        else
        {
            lb = md + 1;
        }
    }
    return ans;
}

```

Aggressive Cows -

<https://www.spoj.com/problems/AGGRCOW/>

```

double eps = 1e-9;
while (ub - lb > eps)
{
    double md = lb + (ub - lb) / 2;
    if (count(v, md) <= k)
    {
        ans = md;
        ub = md;
    }
    else
    {
        lb = md;
    }
}

double eps = 1e-9;
double lb = 0, ub = 1e9;
while (abs(ub - lb) > eps)
{
    double md = lb + (ub - lb) / 2;
    if (md * md <= n)
    {

```

```

        ans = md;
        lb = md;
    }
    else
    {
        ub = md;
    }
}

```

$O(\log((ub-lb)/eps))$

Q. There are n people on a straight line. They need to gather at one point. The i -th person's current position is $x[i]$ and his maximum speed $v[i]$. Find out the minimum time they require to gather at the same point.

Link:

<https://codeforces.com/edu/course/2/lesson/6/3/practice/contest/285083/problem/A>

```

1 2 3 4
2 1 6 3
x = 2
0.5 0 0.16 0.67

```

$[x[i]-md*v[i], x[i]+md*v[i]]$

```

bool check(double t)
{
    double l[n], r[n];
    for (int i = 0; i < n; i++)
    {
        l[i] = x[i] - t * v[i];
        r[i] = x[i] + t * v[i];
    }
    double li = l[0], ri = r[0];
    for (int i = 0; i < n; i++)
    {
        li = max(li, l[i]);
    }
}

```

```

        ri = min(ri, r[i]);
    }
    if (ri - li > eps || abs(ri - li) <= eps)
        return true;
    else
        return false;
}

double eps = 1e-9;
double lb = 0, ub = 2e9;
while (abs(ub - lb) > eps)
{
    double md = lb + (ub - lb) / 2;
    if (check(md))
    {
        ans = md;
        ub = md;
    }
    else
    {
        lb = md;
    }
}

```

if(ri>li)

if(ri+eps>li)

for(int i=0;i<;i++)

{

}

if(r>l-eps)

1 4

3 7 3 4

5 10 5 4

https://atcoder.jp/contests/zone2021/tasks/zone2021_c

```
if(ri-li>-eps)
```

```
ri>=li
```

```
1e-6
```

```
1e-9
```

```
2 - 1e-20
```

```
2 + 1e-20
```

```
10 0 0 0 0
```

```
0 10 0 0 0
```

```
0 0 10 0 0
```

```
0 0 0 10 0
```

```
0 0 0 0 10
```