

# CSE340 SPRING 2020

## Homework 5

### DUE Monday 13 April 2020

**PLEASE READ THE FOLLOWING CAREFULLY**

- **Your Answers for ALL problems must be types**
- **On Gradescope, you should submit the Answers to separate problems separately.**

Assume stack memory allocation for nested scopes is used (which means that memory for variables in a scope is allocated on the stack and that it is deallocated when the scope is exited). Consider the following code below and the box-circle diagram to the right which illustrates the situation at point 1.

```

struct T {
    int *a;
    struct T* next;
};

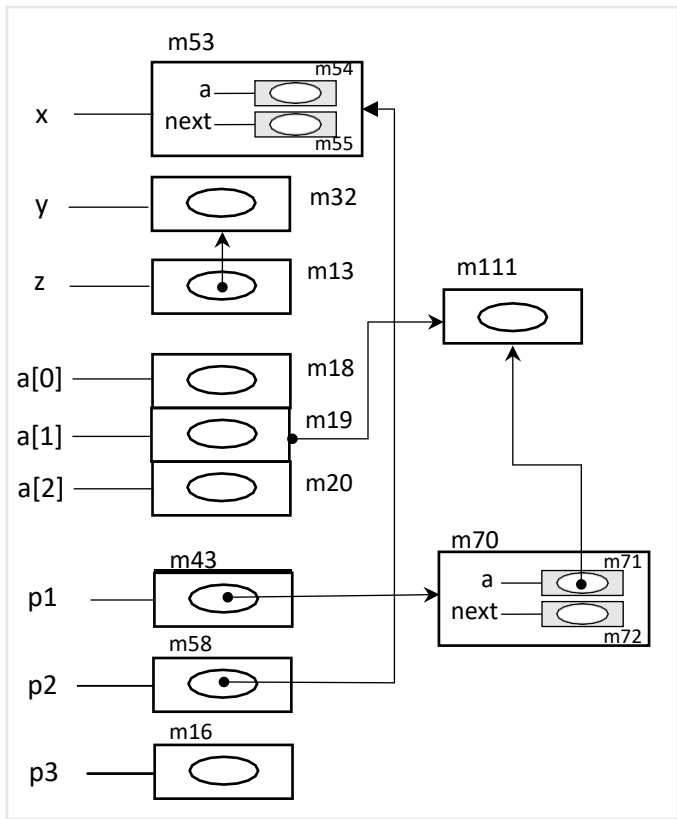
int *y;
int **z;
int **w;
struct T x;
struct T* p1;
struct T* p2;
struct T** p3;

void f()
{ // the following malloc() call allocates m102
  // (which is not shown in the diagram because
  // f() is called after point 1)
  y = (int *) malloc(sizeof(int));
  x.a = y;
}

main()
{ p1 = (struct T*) malloc(sizeof(struct T));
  p2 = &x ;
  { int* a[3];
    a[1] = (int *) malloc(sizeof(int));
    (*p1).a = a[1];
    z = &y ;
    w = &a[1];                // point 1
  }
  f();                        // point 2
  free(y);
  (*p1).next = &x;           // point 3
  // point 4
}

```

# PROBLEM 1



**Question 1.** What is the location associated with \*p1 at point 1?

m70

**Question 2.** What is the location associated with \*z at point 2?

m32

**Question 3.** What is the location associated with \*(x.a) at point 2?

m102

**Question 4.** What is the location associated with \*((\*p1).next) at point 2?

m72

**Question 5.** What are the dangling references, if any, at point 2?

None

**Question 6.** What are the locations that are garbage, if any, at point 3?

p1, a[1]

**Question 7.** What are the dangling references, if any, at point 3?

y, x.a

**Question 8.** Assume that the following is executed at point 3 (this applies only to this question):

```
p3 = &p1;
*p3 = &((*p1).next);
```

This will results in news arrows, if any, from where to where?

p3 gets a value from p1 location and \*p3 gets a value from \*p1.next location

**Question 9.** Assume the following is executed at point 4:

```
p2 = (struct T*) malloc(sizeof(struct T));
(*p1).next = p2;
p1 = p2;
```

what location become garbage due to the execution of the code?

m70

**Question 10.** If we execute free(p2) after the code above, what are the new dangling references, if any, that result from that?

p1,p2

**Question 11.** What is an alias of x at point 1 (the alias should have a variable other than x. Something like \*&x does not count)

p2

**Question 12.** What is an alias of a[0] at point 1. The alias should have a variable other than a.

None

## PROBLEM 2: Lambda Calculus

**Question 1.** Write a non-recursive lambda expression to compute the  $n$ 'th Fibonacci number. The Fibonacci numbers are defined as follows

$$\begin{aligned} F_1 &= 1 \\ F_2 &= 1 \\ F_n &= F_{n-1} + F_{n-2} \text{ if } n > 1 \end{aligned}$$
  
$$\begin{aligned} \text{First} &= \lambda T. T \text{ tru} \\ \text{Second} &= \lambda T. (T \text{ fls}(T \text{ tru})) \\ \text{Third} &= \lambda T. (T \text{ fls}(T \text{ fls})) \\ \text{Tuple} &= \lambda c. \lambda a. \lambda b. \text{pair}(c \text{ pair}(a \ b)) \\ \text{Init} &= \text{Tuple } 0 \ 0 \ 1 \\ \text{Body} &= \lambda T. \text{Tuple}(\text{plus}(\text{Second } T)(\text{Third } T))(\text{Third } T)(\text{First } T) \\ \text{Fib} &= \lambda n. (\text{iszero } n) \\ &\quad 0 \\ &\quad (\text{gteq } n \ 1) \\ &\quad \quad (\text{equal } n \ 1) \\ &\quad \quad \quad 1 \\ &\quad \quad \quad (\text{Third}(\text{prd } n) \ (\text{Body}) \ (\text{Init})) \end{aligned}$$

**Question 2.** Write a recursive lambda expression to compute the  $n$ 'th Fibonacci number.

$$\begin{aligned} g &= \lambda \text{Fib}. \lambda n. (\text{gteq } n \ 2) \\ &\quad (\text{plus}(\text{Fib}(\text{prd } n)) \ (\text{Fib}(\text{prd}(\text{prd } n)))) \\ &\quad n \\ \text{FibRec} &= \text{fix } g \end{aligned}$$

**Question 3.** Write a non-recursive lambda expression to calculate the sum of the first  $n$  squares:

$$1^2 + 2^2 + 3^2 + 4^2 + \dots + n^2$$
  
$$\begin{aligned} \text{Init} &= \text{pair } 0 \ 1 \\ \text{Body} &= \lambda p. \text{pair}(\text{plus}(\text{fst } p)(\text{times}(\text{snd } p)(\text{snd } p)))(\text{succ}(\text{snd } p)) \\ \text{Sum} &= \lambda n. (\text{iszero } n) \\ &\quad 0 \\ &\quad (\text{fst}(n \ \text{Body} \ \text{Init})) \end{aligned}$$

You should not use a closed-form formula for the sum

**Question 4.** Write a recursive lambda expression to calculate the sum of the first  $n$  squares:

$$1^2 + 2^2 + 3^2 + 4^2 + \dots + n^2$$

You should not use a closed-form formula for the sum

$$\begin{aligned} g &= \lambda \text{Sum}. \lambda n. (\text{gteq } n \ 2) \\ &\quad (\text{plus}(n \ \text{prd}(\text{Sum } n)) \\ &\quad \quad n) \\ \text{SumRec} &= \text{fix } g \end{aligned}$$

## PROBLEM 3: Type Systems

This problem refers to the type system of the Go Programming Language. You can find the specification at <https://golang.org/ref/spec>. In particular you should consult the section on types: [https://golang.org/ref/spec#Properties\\_of\\_types\\_and\\_values](https://golang.org/ref/spec#Properties_of_types_and_values).

I expect you to consult the specification to answer the questions below.

**Question 1.** What is the term used in the Go language to refer to type compatibility?

Assignability

**Question 2.** What term is used in the Go language to refer to type equivalence?

Identity

**Question 3.** Can a function type with a variable number of parameter be identical to a function type with a fixed number of parameters?

No, there identity types are not the same.

**Question 4.** If two types are structurally equivalent according to the definition we covered in class, would the two types be identical according to the Go language? Explain or give a counterexample.

Yes, because golang uses underlying type to determine if types are equivalent.

**Question 5.** If two types are identical according to the Go language, are the two types structurally equivalent according to the definition we covered in class? Explain or give a counterexample.

Yes, in order to be identical you have to have structural equivalence.

The following are examples given in the Go language spec

```
type (
    A0 = []string
    A1 = A0
    A2 = struct{ a, b int }
    A3 = int
    A4 = func(A3, float64) *A0
    A5 = func(x int, _ float64) *[]string
)

type (
    B0 A0
    B1 []string
    B2 struct{ a, b int }
    B3 struct{ a, c int }
    B4 func(int, float64) *B0
    B5 func(x int, y float64) *A1
)

type    C0 = B0
```

For the following questions, you should give explanations that are more specific than what is given in the specification document.

**Question 6.** Are A2 and B2 in the example above identical? Why?

Yes, because the field names and types are identical so the struct types are equivalent.

**Question 7.** Are struct {a, b int} and struct {a, c int} identical? Why?

No, because b and c don't have the same field names so the struct types are not equivalent.

**Question 8.** Are struct {a, b int} and B2 in the example above identical? Why?

Yes, because the field names and types are identical so the struct types are equivalent.

**Question 9.** What is the return type of the function type A5 in the example above?

The return type is a pointer to string array

**Question 10.** Explain why A4 and A5 are identical.

A4 and A5 are identical because the arguments and return type are of the same type.