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Probability Assignment 2

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Question: The number lock of a suitcase has 4 wheels, each labelled with ten digits i.e., from 0 to 9. The lock opens with a sequence of four digits with no repeats. What is the probability of a person getting the right sequence to open the suitcase? **Solution:** Define random variable X_i such that

$$X_i = \begin{cases} 1, & \text{correct number choosen in } i^{th} \text{ wheel} \\ 0, & \text{otherwise} \end{cases}$$
 (1)

and

$$P_{X_i}(1) = \frac{1}{10 - i} \tag{2}$$

$$P_{X_i}(0) = 1 - \frac{1}{10 - i} \tag{3}$$

$$=\frac{9-i}{10-i}\tag{4}$$

Let E be event of getting the right sequence. Since X_i are independent of each other, hence

$$Pr(E) = \prod_{i=0}^{3} P_{X_i}(1)$$

$$= P_{X_0}(1) \times P_{X_1}(1) \times P_{X_2}(1) \times P_{X_3}(1)$$

$$= \frac{1}{10} \times \frac{1}{9} \times \frac{1}{8} \times \frac{1}{7}$$

$$= \frac{1}{5040}$$
(5)