

back substitution

$$\begin{bmatrix} 2 & 3 & -4 \\ 0 & 7/2 & 1 \\ 0 & 0 & 16/7 \end{bmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 12 \\ 6 \\ -16/7 \end{pmatrix}$$

$$z = b_3 / a_{33}$$

to get x & y
 $12 - 2a_{13}z - 3a_{12}z$

$$a_{22}y + a_{23}z = b_2$$

substitute z ; subtract $a_{23}z$
 from b_2 , $(b_2 - a_{23}z)$

$$\begin{matrix} a_{11} & a_{12} & a_{13} \\ 0 & a_{21} & a_{23} \\ 0 & 0 & a_{33} \end{matrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$$

$i = n-1$
 $i = 2$ for $i = n, 1$

$j = 3$ for $j > i$

$$b_i' = b_i - a_{ij} b_j$$

$b_2' = b_2 - a_{23} b_3$ end

$z = 7$

$$b_i' \rightarrow \frac{b_i}{a_{ii}}$$

only for $i = 3$

1 for $i = n, 2$ $i \geq 1$
 2 for $j > i$ $j = 2, j \geq 3$
 3 $b_i' = b_i - a_{ij} b_j$
 4 end
 5 $b_i' \rightarrow \frac{b_i}{a_{ii}}$ only for $i = 3$

First $i = n = 3$ I go directly to (5)

$$b_3' \rightarrow \frac{b_3}{a_{33}} (= 7)$$

2nd $i = n - 1 = 2$, I go to line (2)
 $j = 3$, $b_2' = b_2 - a_{23} b_3$
 but b_3 is already $b_3' = 7$