Consider the function  $f(x) = \frac{x^3}{e^x - 1}$ 

- 1. Evaluate  $\int_0^\infty f(x)dx$  using Monte Carlo method. Since the integral extends to infinity which can not be simulated, try different maximum values  $(x_{max})$  to examine which one is sufficient.
- (i) Generate  $10^4$  uniform random numbers between 0 and  $x_{max}$  and evaluate the integration over a sample size of 100, 500 and  $10^4$ . (note: use a 19-20 digit integer number as SEED)
- (ii) Make histograms (do not use python inbuilt list) of the integration values for sample size N= 100, 500 and check the  $1/\sqrt{N}$  law for Monte Carlo integration.
- (iii) What is the optimum value of  $x_{max}$ ? Plot the histogram of x for the optimum  $x_{max}$ .