Chapter 14 Algebraic equations 1

14.1 Solving by inspection

number puzzles

Solve these number puzzles.

- 1. I am thinking of a certain number. If I add 3 to that number, the answer is 13. What is the number?
- 2. I am thinking of a certain number. If I multiply that number by 5, the answer is 30. What is the number?
- 3. I am thinking of a certain number. If I multiply that number by 3 and then add 4 to the result, the answer is 19.
 - (a) Is the number 3? Give a reason for your answer.
 - (b) Is the number 4? Give a reason for your answer.
 - (c) Is the number 5? Give a reason for your answer.
 - (d) Is the number 6? Give a reason for your answer.

Number puzzles like those above can be shortened by using letter symbols as placeholders for unknown numbers. In the case of question 1 we can write the following number sentence: x + 3 = 13.

In the case of a number sentence such as x + 3 = 13 we cannot say whether it is true or false until we have determined the value of the unknown. The value of the unknown that makes the number sentence (an **equation**) true is called the **solution** of the number sentence.

For the number sentence x + 3 = 13, the solution is x = 10 because it makes the number sentence true.

A mathematical statement such as x + 3 = 13 that could be true or false depending on the value of x, is called an **open number sentence** or an **equation**.

To make a number sentence **true** means to find its **solution**.

the solution is there to see

The solution to the number sentence x + 4 = 20 can be seen at once. The value of x is 16 simply because 16 + 4 = 20. In this case, we say we solve the number sentence by **inspection**.

Solve these number sentences (equations) by inspection.

1. (a)
$$x - 8 = 8$$

(c)
$$\frac{16}{x} = 8$$

(e)
$$5 \times x = 40$$

2. (a)
$$84 \div x = 7$$

(c)
$$x + 56 = 100$$

(b)
$$x + 7 = 20$$

(d)
$$\frac{x}{16} = 2$$

(f)
$$8 \times x = 40$$

(b)
$$36 \div x = 4$$

(d)
$$100 - x = 56$$

14.2 Solving by the trial and improvement method

Sometimes you cannot see the solution of a number sentence (an equation) at once. Look at the following number puzzle or equation, for example:

I am thinking of a number. $6 \times the \ number - 11 = 43$. What is the number? In this case, you will have to try many different possible solutions until you identify the correct one. Here we can use a method known as **trial and improvement** to determine the solution. It is shown in the table below.

Possible solution	Test	Conclusion
Try 5	6 × 5 - 11 = 30 - 11 = 19	5 is too small
Try 10	6 × 10 - 11 = 60 - 11 = 49	10 is too big
Try 8	6 × 8 - 11 = 48 - 11 = 37	8 is too small
Try 9	6 × 9 - 11 = 54 - 11 = 43	9 is the solution

Copy the tables below. Solve the following equations by means of the trial and improvement method. In each case, the solution is a number between 1 and 20.

 $1.2 \times x + 13 = 37$

Possible solution	Test	Conclusion

 $2.14 \times x - 21 = 77$

Possible solution	Test	Conclusion

 $3.7 \times x + 8 = 71$

Possible solution	Test	Conclusion

 $4.4 \times x + 7 = 31$

Possible solution	Test	Conclusion

 $5.10 \times x + 11 = 141$

Possible solution	Test	Conclusion

solving by inspection or trial and improvement

Solve the following equations by inspection or by the trial and improvement method:

1. (a)
$$x + 5 = 2 \times x$$

(c)
$$2 \times q = 18 - q$$

2. (a)
$$y + 6 = 4 \times y$$

(c)
$$4 \times z = 18 + z$$

(e)
$$42 \div m = 35 - 29$$

(b)
$$k \times 5 = 20 + k$$

(d)
$$3 \times t = t + 22$$

(b)
$$5 \times p = 18 + 2 \times p$$

(d)
$$x \times 5 = 20$$

(f)
$$3 \times x - 2 = x + 6$$

14.3 Describing problem situations with equations

from words to equations

Write an equation using a letter symbol as a placeholder for the unknown number to describe the problem in each of the situations below.

- 1. There are 30 learners in a class. *x* learners are absent and 19 are present.
- 2. There are 70 passengers on a bus. At a bus stop m passengers get off. There are now 23 passengers on the bus.
- 3. A boy buys a bicycle for R1 260 on lay-by. How many payments of R90 each must he make to pay for the bicycle? Let x be the number of payments to be made.
- 4. Five people share a total cost of R240 equally amongst themselves. Let *c* be the cost per person.
- 5. As chool charges R100 a day for the use of its training facilities for athletes plus R30 per athlete per day for food and use of equipment. A team of athletes paid R400 for a day's practice. Let *x* be the number of athletes attending the training.
- 6. Bennie has R54 with which to buy chocolates for his friends. Each chocolate costs R6. How many chocolates can he buy for that amount? Let *x* be the number of chocolates that Bennie can buy.

- 7. Write an equation to calculate the area of a rectangle with length 2,5 cm and breadth 2 cm. Let *A* represent the area of the rectangle.
- 8. There are 38 girls in Grade 7. This is 6 more than double the number of boys.
- 9. Janine is 12 years old. Her father's age is 7 years plus three times Janine's age.

making sense of equations

- 1. Rajbansi Taxi Service charges R10 per kilometre travelled and a standard charge of R30 per trip. Consider the equation below about a taxi trip:
 - $10 \times t + 30 = 80$
 - (a) Explain what each number and letter symbol stands for in the equation.
 - (b) Why is *t* multiplied by 10 in the equation?
- 2. The cost of an adult's ticket for a music concert is four times the cost of a child's ticket. An adult's ticket costs R240. The equation below represents this problem: $4 \times x = 240$
 - (a) What does x represent?
 - (b) Why is *x* multiplied by 4?
 - (c) Solve the equation by inspection.
 - (d) How much does a child's ticket cost?
- 3. There are 12 eggs in a carton. Consider the equation below:

$$12 \times c = 72$$

- (a) What does the letter symbol *c* represent in the equation?
- (b) What value of *c*makes the equation true?
- (c) What does the number 72 represent?