

Lab Exercise - 11

Q1.

a) $5 + 2j$

⇒ So the real part is 5 (a)
imaginary part is 2. (b)

also,

complex number (z) = $a + bj$
ie.

$$z = r(\cos \theta + j \sin \theta)$$

to find r:

$$r = |z| = \sqrt{a^2 + b^2}$$

$$= \sqrt{(5)^2 + (2)^2}$$

$$= \sqrt{25 + 4} \Rightarrow \sqrt{29}$$

$$\approx 5.385$$

$$\approx 5.39$$

to find θ ;

since $a > 0$ so,

$$\theta = \tan^{-1} \left(\frac{b}{a} \right)$$

$$\theta = \tan^{-1} \left(\frac{2}{5} \right)$$

$$\theta = \tan^{-1} (0.4)$$

$$\theta = 0.3805 \Rightarrow 0.38$$

now,

polar value (z) = $r(\cos \theta + j \sin \theta)$
 $= 5.39(\cos 0.38 + j \sin 0.38)$

$$z = 5.39 (\cos 0.38 + j \sin 0.38)$$

and exponential form \Rightarrow

$$5.39 e^{j(0.38 \times j)}$$

b) $5 - 2j$

\Rightarrow so the real part is $\Rightarrow a = 5$
 imaginary part is $\Rightarrow b = -2$

also,

complex number $(z) = a + bj$
 ie.

$$z = r(\cos \theta + j \sin \theta)$$

to find r :

$$r = |z| = \sqrt{a^2 + b^2}$$

$$= \sqrt{(5)^2 + (-2)^2}$$

$$= \sqrt{25 + 4} \Rightarrow \sqrt{29}$$

to find θ ;

$$\theta = \tan^{-1}(b/a)$$

$$= \tan^{-1}(-2/5)$$

$$\theta \Rightarrow \tan^{-1}(-0.4)$$

$$\theta \Rightarrow -0.38$$

now,

polar value $(z) = r(\cos \theta + j \sin \theta)$
 ie.

~~$$z = \sqrt{29} (\cos 0.38 + j \sin 0.38)$$~~

$$z = \sqrt{29} (\cos (-0.38) + j \sin (-0.38))$$

& exponential form is $\sqrt{29} e^{j \times (-0.38)}$

c) $6 + 4j$

$$\Rightarrow \text{real part (a)} = 6$$

$$\text{imaginary part (b)} = 4$$

also, complex number $(z) = a + bj$
ie.

$$z = r (\cos \theta + j \sin \theta)$$

find r :

$$r = |z| = \sqrt{a^2 + b^2}$$

$$= \sqrt{(6)^2 + (4)^2}$$

$$= \sqrt{36 + 16} = \sqrt{52}$$

find θ :

$$\theta = \tan^{-1} (b/a)$$

$$= \tan^{-1} (4/6) \Rightarrow 0.583$$

now,

polar value $(z) = \sqrt{52} (\cos (0.583) + j \sin (0.583))$

exponential form = $\sqrt{52} e^{j * (0.583)}$

$$d) 5-5j$$

$$\Rightarrow \text{real part} \Rightarrow a = 5$$

$$\text{imaginary part} \Rightarrow b = -5$$

also, complex number $(z) = a + bj$
ie.

$$z = r (\cos \theta + j \sin \theta)$$

also θ :

$$\theta = \tan^{-1}(-5/5)$$

$$\theta = -\pi/4 = \tan^{-1}(-1) \Rightarrow -\pi/4$$

also r :

$$r = |z| = \sqrt{a^2 + b^2} \Rightarrow \sqrt{5^2 + (-5)^2}$$

$$= \sqrt{25 + 25} = \sqrt{50}$$

now,

$$\text{polar value } (z) = \sqrt{50} (\cos(-\pi/4) + j \sin(-\pi/4))$$

$$\text{exponential form} = \sqrt{50} e^{j * (-\pi/4)}$$

$$c) 2 + 3j$$

real part $\Rightarrow a = 2$

imaginary part $\Rightarrow b = 3$

also, complex number $= (z) = a + bj$
ie.

$$z = r (\cos \theta + j \sin \theta)$$

for r :

$$r = |z| = \sqrt{a^2 + b^2}$$

$$r = \sqrt{13}$$

for θ :

$$\theta = \tan^{-1} (3/2)$$

$$= \tan^{-1} (1.5) \Rightarrow 0.98$$

now,

$$\text{polar value } (z) = \sqrt{13} (\cos 0.98 + j \sin 0.98)$$

also,

$$\text{exponential form} = \sqrt{13} e^{j * 0.98}$$

Ex. 2

① $2e^{j\frac{\pi}{3}}$

Euler's formula: $e^{ix} = \cos(x) + j\sin(x)$

$$x = \frac{\pi}{3}$$

$$Z = 2 \cdot \left(\cos \frac{\pi}{3} + j \cdot \sin \frac{\pi}{3} \right)$$

$$Z = 2 \cdot \cos \frac{\pi}{3} + 2 \sin \frac{\pi}{3} j$$

$$Z = \frac{2 \cdot 1}{2} + \frac{2 \cdot \sqrt{3}}{2} j$$

$$\boxed{Z = 1 + \sqrt{3}j}$$

② $-4e^{j\frac{\pi}{6}}$

Using Euler's formula, we have:

$$x = \frac{\pi}{6}$$

$$Z = -4 \cdot \left(\cos \frac{\pi}{6} + j \cdot \sin \frac{\pi}{6} \right)$$

$$Z = -4 \cos \frac{\pi}{6} - 4 \sin \frac{\pi}{6} j$$

$$Z = -4 \cdot \frac{\sqrt{3}}{2} - 4 \cdot \frac{1}{2} j$$

$$\boxed{Z = -2\sqrt{3} - 2j}$$

$$(3) \quad 5 \cdot \left(\cos \frac{\pi}{3} + j \cdot \sin \frac{\pi}{3} \right)$$

Using Euler's formula, we have:

$$5 \cos \frac{\pi}{3} + 5 \sin \frac{\pi}{3} j = 5 \cdot \frac{1}{2} + 5 \frac{\sqrt{3}}{2} j$$

$$= \boxed{\frac{5}{2} + \frac{5\sqrt{3}}{2} j}$$

$$(4) \quad 2 \cdot \left(\cos \frac{\pi}{4} + j \cdot \sin \frac{\pi}{4} \right)$$

Using Euler's formula, we have:

$$2 \cos \frac{\pi}{4} + 2 \sin \frac{\pi}{4} j = 2 \cdot \frac{\sqrt{2}}{2} + 2 \cdot \frac{\sqrt{2}}{2} j$$

$$= \boxed{\sqrt{2} + \sqrt{2} j}$$

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$$z_1 = 2 + 3j ; z_2 = -1 + 4j$$

for $z_1 \Rightarrow$ real part $\Rightarrow a = 2$
imaginary part $\Rightarrow b = 3$

also, complex number $= (z) = a + bj$
ie.

$$z = r (\cos \theta + j \sin \theta)$$

$$\theta = \tan^{-1} (b/a)$$

$$\theta = \tan^{-1} (3/2)$$

$$\theta = \tan^{-1} (1.5) = 0.98$$

also $r :$

$$r = |z| = \sqrt{a^2 + b^2}$$
$$= \sqrt{4 + 9}$$
$$= \sqrt{13}$$

now,

polar value $(z) = \sqrt{13} (\cos(0.98) + j \sin(0.98))$

also,

exponential form $= \sqrt{13} e^{j(0.98)}$

for $z_2 \Rightarrow$ real part $\Rightarrow -1$
imaginary part $\Rightarrow 4$

also,

complex number $\Rightarrow (z) = a + bj$
ie.

$$z = r (\cos \theta + j \sin \theta)$$

$$r = |z| = \sqrt{a^2 + b^2} = \sqrt{1 + 16} \\ = \sqrt{17}$$

also,

$$\theta = \tan^{-1}(b/a)$$

$$= \tan^{-1}(4/-1)$$

$$\theta = \tan^{-1}(-4)$$

$$\theta = -1.32$$

now,

$$z = \sqrt{17} \left(\cos(-1.32) + j \sin(-1.32) \right)$$

also,

$$\text{exponential form} = \sqrt{17} e^{j(-1.32)}$$

Sh Rectangular form:

$$(z_1)^2 = (2+3j)(-1+4j) = -5+12j$$

$$= 4+9j^2+12j$$

$$z_1/z_2 = \frac{(2+3j)}{(-1+4j)}$$

$$= \frac{(2+3j)(-1+4j)}{(-1+4j)(-1-4j)}$$

$$= \frac{(-2-11j)}{17}$$

Sh Polar form:

$$\text{for } (z_1)^2: (-5+12j)^2$$

$$\sqrt{(25+144)} e^{j \tan^{-1}(12/-5)}$$

$$= 13 e^{j \tan^{-1}(-67.38^\circ)}$$

$$= 13 e^{j \tan^{-1}(-67.38^\circ)}$$

In exponential form is

for: $(z_1)(z_2) = 13 e^{(j - 67.38)^\circ}$

for: $z_1/z_2 = \frac{\sqrt{17}}{17} e^{(-j(75.96)^\circ)}$

$$= \frac{\sqrt{17}}{17} e^{(-j(75.96)^\circ)}$$

Now, while comparing, we find that is

$z_1 \times z_2$ in polar form is $13 e^{(j * (-67.38)^\circ)}$

$z_1 \times z_2$ exponential form is $13 e^{(j * (-67.38)^\circ)}$

And

z_1/z_2 polar form: $\frac{\sqrt{(4+121)}}{17} e^{(j * (-80.537)^\circ)}$

z_1/z_2 in exponential is $\frac{\sqrt{17}}{17} e^{(j * (-75.96)^\circ)}$