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## Kelvin Programming Competition Coding Problem Handout

Track II: The VIP Track  
December 7th, 2025

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# Background

In this competition, we will focus on one engineering challenge related to *health & well-being*. Specifically, it is about *sleep* - one of the most significant aspects of our physical health.

## HypnosTech - The Sleep Architect

*“Sleep is the golden chain that ties health and our bodies together.”*  
— Thomas Dekker

In today's fast-paced life, sleep disorders have become a major problem affecting the physical and mental health of billions of people worldwide. Chronic lack of deep sleep can lead to weakened immunity, anxiety, and even cognitive impairment.

To address this crisis, *HypnosTech*, a health technology company founded by Glasgow College alumni, has developed a revolutionary smart sleep aid pillow. This device goes beyond passively monitoring sleep; it actively induces the brain to enter specific sleep stages by playing specific soundscapes—such as white noise, rain sounds, and forest wind sounds—through bone conduction technology.

However, the human brain's sleep state is a highly complex and random process. Incorrect audio guidance may wake the user, producing the opposite effect. Furthermore, neuroscientific research indicates that the brain requires a 'synchronization period' to adapt to a new soundscape. Frequent switching breaks this synchronization, creating a '**Cognitive Switching Penalty**'. Instead of inducing sleep, rapid changes force the brain into an alert state, allowing it to process new stimuli and effectively reducing the sleep quality score. Therefore, the algorithm must balance the immediate benefit of a better sound against the cost of disrupting the current state.

As the lead backend algorithm engineer at HypnosTech, your task is to design the core scheduling algorithm. You need to generate **an optimal "sleep aid score"** based on each user's **brainwave characteristics (state transition probabilities)** to maximize the user's **sleep recovery quality** within a limited time.

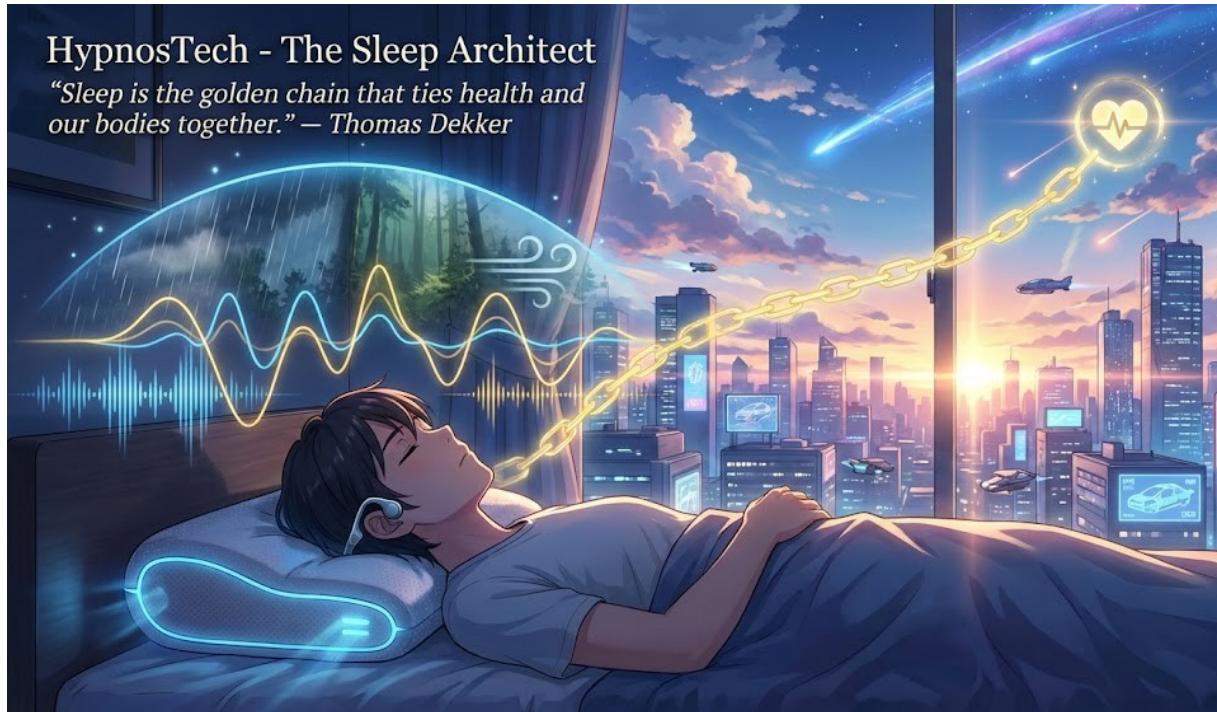
# Objective

Your objective is to write a program that generates an **audio playback sequence** with a duration of **T minutes**, maximizing the total sleep integral produced by this sequence in terms of **mathematical expectation**. The program needs to automatically calculate the optimal action path based on the **input state transition matrix** and **reward function**. You may choose to use **C**, **C++** or **Python** to complete the challenge.

As the emphasis of this challenge is coding, we have provided all the mathematical knowledge you need to engineer the solution in *Mathematical Model*. The guidelines for the program input and output formats are given in *Input & Output*. Meanwhile, to help you understand how your solution will be evaluated, we also attach the detailed rubrics we use to grade your programs in *Rubrics*. In the *Appendix*, we include some example input & output and codes to help you write code more effectively.

---

***Happy & Healthy Coding, Master Programmers!***



# Mathematical Model

## 3.1 Table of Notations

The following symbols are used throughout the model definition:

Symbol	Definition
$T$	Total duration of the sleep session (minutes)
$N$	Number of discrete sleep states (e.g., Awake, Deep Sleep)
$M$	Number of available soundscapes (actions)
$S_t$	The state of the brain at minute $t$ ( $S_t \in [S_0, \dots, S_{N-1}]$ )
$a_t$	The action selected at minute $t$ ( $a_t \in [a_0, \dots, a_{M-1}]$ )
$L$	The wandering cycle period for the time-variant reward system
$\mu$	The system's average reward centroid
$R_{initial}(s)$	The initial base reward input for state $s$
$R(s, t)$	The calculated reward obtained for being in state $s$ at time $t$
$P_{i,j}^{(a)}$	Probability of moving from state $i$ to $j$ under action $a$
$C_{i,j}$	Cost penalty when switching actions while moving from state $i$ to $j$
$I(\cdot)$	The indicator function, which equals 1 if the condition is true, and 0 otherwise

## 3.2 States

The brain has  $N$  discrete states. Example with  $N = 5$ :

- $S_0$ : Awake
- $S_1$ : Light Sleep
- $S_2$ : Deep Sleep
- $S_3$ : REM
- $S_4$ : Waked Up

### 3.3 Actions

The system supports  $M$  types of soundscapes (sound effects), e.g.,  $A_0$  (silence),  $A_1$  (white noise),  $A_2$  (thunderstorm sound).

### 3.4 Dynamics

#### 3.4.1 Transition Matrix

For each action  $a \in [a_0, \dots, a_{M-1}]$ , there is an  $N \times N$  matrix  $P^{(a)}$ .  $P_{i,j}^{(a)}$  represents the probability of transitioning to state  $j$  in the next minute when the current state is  $i$  and sound effect  $a$  is playing.

#### 3.4.2 Generalized Cognitive Switching Penalty

To model the biological cost of changing neural states, the switching penalty is defined by a Cost Matrix  $C_{N \times N}$ . Let  $C_{i,j}$  be the cost of switching soundscapes ( $a_t \neq a_{t-1}$ ) when the brain transitions from State  $i$  to State  $j$ .

The penalty at time  $t$  is calculated as:

$$\text{Penalty}_t = I(a_t \neq a_{t-1}) \cdot C_{S_{t-1}, S_t} \quad (3.1)$$

For  $t = 1$ , assume  $a_{t-1} = a_0 = 0$ . Noted that in basic cases, this matrix simplifies to a uniform structure where all off-diagonal costs equal a constant 0. For example,  $C_{i,j} = 0$  for all  $i \neq j$ .

#### 3.4.3 Time-Variant Reward System (Value Wandering)

Rewards follow a **Mean-Reverting Process**. They follow a Mean-Reverting Process with an invariant centroid, preventing the brain from "locking" into a single state. As time progresses, high-value states naturally drift towards the system average, while low-value states recover, periodically inverting their relative advantages. The reward for state  $s$  at time  $t$  is calculated as:

$$R(s, t) = \mu + (R_{initial}(s) - \mu) \cdot \cos\left(\frac{2\pi t}{L}\right) \quad (3.2)$$

Where:

- $\mu$ : The system's average reward centroid ( $\mu = \frac{1}{N} \sum_{i=0}^{N-1} R_{initial}(s_i)$ ).
- $L$ : The wandering cycle period. If  $L = 0$ , rewards remain static:  $R(s, t) = R_{initial}(s)$ .
- $R_{initial}(s)$ : The base reward input for state  $s$ .

Noted that if  $L = 0$  in the input, the rewards remain static ( $R(s, t) = R_{initial}(s)$ ).

#### 3.4.4 Initial Condition

The system is in State 0 ( $S_0$ ) at time  $t = 0$  with a probability of 1.0.

- $P(S_0 = 0) = 1.0$
- $P(S_0 = k) = 0$  for all  $k \neq 0$

---

### 3.4.5 Calculation Implications

- **First Transition:** The probability distribution of the state at  $t = 1$  ( $S_1$ ) depends entirely on the transition row for State 0 in the matrix of the chosen action  $a_1$ :

$$P(S_1 = j) = P_{0,j}^{(a_1)} \quad (3.3)$$

- **First Penalty:** For  $t = 1$ , the penalty calculation uses  $S_0 = 0$ .

$$\text{Penalty}_1 = I(a_1 \neq 0) \cdot C_{0,S_1} \quad (3.4)$$

## 3.5 Optimization Objective

### Objective Function:

Let  $A = [a_1, a_2, \dots, a_T]$  be the sequence of actions chosen for each minute  $t$ .

The total expected score  $J(A)$  is defined as:

$$J(A) = E \left[ \sum_{t=1}^T (R(S_t, t) - \text{Penalty}_t) \right] \quad (3.5)$$

Where :

- $S_t$  is the random variable representing the sleep state at time  $t$ .
- $I(\cdot)$  is the indicator function (1 if switching occurs, 0 otherwise).
- $E[\cdot]$  is the expectation taken over the stochastic transitions defined by matrices  $P(a_t)$ .

### Optimization Problem:

Find the optimal sequence  $A^*$  such that:

$$A^* = \underset{a_1, \dots, a_T}{\operatorname{argmax}} J(A) \quad (3.6)$$

# Input & Output

All data is read through standard input (stdin).

## 4.1 Input Format

The input consists of the following structure:

```
T N M L Type
R0 R1 ... RN-1
[Switching Penalty Matrix]
[Matrix block Action 0]
[Matrix block Action 1]
...
[Matrix block Action M-1]
```

### Line 1: Four integers

- $T$ : Total duration (minutes).
- $N$ : Number of states.
- $M$ : Number of sound effects.
- $L$ : Cycle period for reward wandering. If  $L = 0$ ,  $R(s, t) = R_{initial}(s)$ .
- $Type$ : Constraint mode identifier.

### Line 2: Base Rewards

- $N$  integers representing the initial base rewards  $R_{initial}(s)$ .

### Switching Penalty Matrix

An  $N \times N$  integer matrix block always follows, regardless of the  $Type$  value.

- If  $Type = 1$  (Generalized Matrix Penalty Mode): The value at row  $i$ , column  $j$  represents the specific switching penalty  $C_{i,j}$ .
- If  $Type = 0$  (Uniform Penalty Mode): The matrix block is still provided to maintain input format consistency, but all values in this matrix will be 0. Your program should ignore the values in this matrix and assume the penalty is 0 (Static  $K = 0$ ).

## Matrix Blocks

The following  $M$  blocks each represent a transition matrix for a sound effect. Each block contains  $N$  rows, with  $N$  floating-point numbers (0.0 to 1.0) per row. The number in the  $i$ -th row and  $j$ -th column represents  $P(State_i \rightarrow State_j)$ . The sum of each row is guaranteed to be 1.0.

## 4.2 Output Format

Output a single line containing the sequence of sound effect IDs formatted as a JSON-style list:

$$[a_1, a_2, \dots, a_T]$$

Each integer represents the sound effect ID selected for this minute (from 0 to  $M-1$ ). Separators must strictly be a comma followed by a space.

### Example Input:

For input examples, please refer to the Appendix *Raw Input.txt*.

### Example Output:

```
[1, 1, 1, 1, 0, 0, 0, 0, 0, 2, 2, 2, 2, 2, 1, 1, 1, 0, 0]
```

# Rubrics

## 5.1 Scoring Mechanism: God's-eye View and Time Penalty

The competition consists of 10 test cases. The total score is calculated using the following formulas:

$$Score_{base}^i = \min(Score_{raw}^i, Score_{standard}^i) \quad (5.1)$$

$$Score_{bonus}^i = \max(0, Score_{raw}^i - Score_{standard}^i) \times \frac{1}{1 + \log(1 + T_{use_i})} \quad (5.2)$$

$$Score_{final} = \sum_{i=1}^{10} (Score_{base}^i + Score_{bonus}^i) \quad (5.3)$$

Where:

- $Score_{raw}^i$ : The expected value calculated by the evaluation system using precise matrix multiplication based on your output sequence.
- $Score_{standard}^i$ : The qualification target score officially set by the Competition Committee.
- $Score_{base}^i$ : Capped at the standard score.
- $Score_{bonus}^i$ : Awarded only if the raw score exceeds the standard, scaled by computational efficiency.
- $T_{use}^i$ : The algorithm's running time on the  $i$ -th test case.

Note: Illegal output results in a score of 0.

## 5.2 Test Cases

### Basic cases (30%):

- Constraints: No penalty ( $Type = 0$ )
- States Reward: Constants ( $L = 0$ )
- Size:  $T \leq 50, M = 10, N = 5$

**Performance test cases (40%):**

- Constraints: Switching Penalty Matrix ( $Type = 1$ )
- States Reward: Constants ( $L = 0$ )
- Size:  $1000 \leq T \leq 3000, M = 80, N = 40$

**Ultimate test cases (30%):**

- Constraints: Switching Penalty Matrix ( $Type = 1$ )
- States Reward: Time-Variant Reward System ( $L = T$ )
- Size:  $1000 \leq T \leq 3000, M = 80, N = 40$

### 5.3 Submission and Grading Policy

- **Single File Submission:** Upload exactly **one program file** (recommended name “**main**”).
- **Error Penalty:** Runtime errors, crashes, or formatting non-compliance result in a score of 0 for that test case.
- **Environment:** Python 3.12, Clang 12, GCC 10.
- **Notes:** We have provided sample code frameworks in C, C++, and Python for your reference, which also facilitates scoring and testing. You can view them in the Appendix.

# Appendix

## 6.1 Example I/O

### 6.1.1 Example Input & Example Solution Code

Code 6.1: How an input file generated (C)

```

1 #include <vector>
2 #include <iostream>
3
4 using namespace std;
5
6 // Part 1: Data Structure Definition (Schema)
7 struct InputData {
8     // --- Header (Line 1) ---
9     int T;           // Total Duration (e.g., 20 mins)
10    int N;          // Number of States (e.g., 5 states)
11    int M;          // Number of Actions (e.g., 3 sound effects)
12    int L;          // Wandering Cycle (e.g., 20 mins, 0 = static)
13    int Type;       // Mode: 0 = Static Penalty, 1 = Matrix Penalty
14
15    // --- Base Rewards (Line 2) ---
16    vector<int> BaseRewards; // Size: [N]
17
18    // --- Penalty Configuration (Line 3) ---
19    // If Type == 0: Only use StaticK
20    // If Type == 1: Use PenaltyMatrix
21    int StaticK;
22    vector<vector<int>> PenaltyMatrix; // Size: [N] [N]
23
24    // --- Transition Probabilities (Block 4...) ---
25    // Structure: [ActionID] [FromState] [ToState]
26    // Size: [M] [N] [N]
27    vector<vector<vector<double>>> Probabilities;
28 };
29

```

```

30 // Part 2: Example Data Instance (N=5, M=3)
31 // This corresponds to the input: "20 5 3 20 1 ..."
32 InputData ExampleCase = {
33     // 1. Header: T=20, N=5, M=3, L=20, Type=1 (Matrix Mode)
34     .T = 20,
35     .N = 5,
36     .M = 3,
37     .L = 20,
38     .Type = 1,
39
40     // 2. Base Rewards (for States 0, 1, 2, 3, 4)
41     .BaseRewards = { 0, 20, 50, 100, 0 },
42
43     // 3. Penalty Matrix (Type=1 active)
44     // Cost to switch FROM row_i TO col_j
45     .PenaltyMatrix = {
46         { 0, 10, 20, 50, 100 }, // From State 0
47         { 10, 0, 10, 20, 100 }, // From State 1
48         { 20, 10, 0, 10, 100 }, // From State 2
49         { 50, 20, 10, 0, 100 }, // From State 3
50         { 0, 0, 0, 0, 0 } // From State 4 Waked Up - No
cost to switch
51     },
52
53     // 4. Transition Matrices (3 Actions x 5x5 Matrix)
54     .Probabilities = {
55         // --- Action 0 (Silence / Initial) ---
56         {
57             {0.9, 0.1, 0.0, 0.0, 0.0}, // From S0: Mostly stays
awake
58             {0.5, 0.5, 0.0, 0.0, 0.0}, // From S1: Unstable
59             {0.1, 0.1, 0.8, 0.0, 0.0}, // From S2: Returns to Deep
Sleep
60             {0.0, 0.0, 0.1, 0.9, 0.0}, // From S3: Good REM
retention
61             {1.0, 0.0, 0.0, 0.0, 0.0} // From S4: Waked up stays
awake
62         },
63
64         // --- Action 1 (White Noise) ---
65         {
66             {0.5, 0.5, 0.0, 0.0, 0.0}, // From S0: Helps fall
asleep
67             {0.1, 0.8, 0.1, 0.0, 0.0}, // From S1: Stabilizes
Light Sleep
68             {0.0, 0.2, 0.7, 0.1, 0.0}, // From S2: Deep sleep

```

```

    slightly disturbed
69        {0.0, 0.0, 0.2, 0.8, 0.0}, // From S3: REM OK
70        {1.0, 0.0, 0.0, 0.0, 0.0} // From S4
71    },
72
73    // --- Action 2 (Thunderstorm) ---
74    {
75        {0.2, 0.2, 0.2, 0.2, 0.2}, // From S0: Chaos (High
variance)
76        {0.2, 0.2, 0.2, 0.2, 0.2}, // From S1
77        {0.2, 0.2, 0.2, 0.2, 0.2}, // From S2
78        {0.2, 0.2, 0.2, 0.2, 0.2}, // From S3
79        {1.0, 0.0, 0.0, 0.0, 0.0} // From S4
80    }
81 }
82 };

```

### 6.1.2 Example input file format

**Note:** Input will be in the form of a txt file. Here are the data inside *Raw Input.txt*

```

1 20 5 3 20 1
2 0 20 50 100 0
3 0 10 20 50 0
4 10 0 10 20 0
5 20 10 0 10 0
6 50 20 10 0 0
7 0 0 0 0 0
8 1.0 0.0 0.0 0.0 0.0
9 0.9 0.1 0.0 0.0 0.0
10 0.5 0.5 0.0 0.0 0.0
11 0.1 0.1 0.8 0.0 0.0
12 0.0 0.0 0.1 0.9 0.0
13 0.5 0.5 0.0 0.0 0.0
14 0.1 0.8 0.1 0.0 0.0
15 0.0 0.2 0.7 0.1 0.0
16 0.0 0.0 0.2 0.8 0.0
17 1.0 0.0 0.0 0.0 0.0
18 0.2 0.2 0.2 0.2 0.2
19 0.2 0.2 0.2 0.2 0.2
20 0.2 0.2 0.2 0.2 0.2
21 0.2 0.2 0.2 0.2 0.2
22 1.0 0.0 0.0 0.0 0.0

```

### 6.1.3 Example output format

**Format Specification:**  $[a_1, a_2, \dots, a_T]$

- The output must start with [ and end with ].
- $a_t$ : An integer representing the Sound Effect ID selected for the  $t^{\text{th}}$  minute ( $0 \leq a_t < M$ ).
- **Separator:** Between any two integers, strictly use a comma followed by a space (, ).

Example Output: [1, 1, 1, 1, 0, 0, 0, 0, 0, 2, 2, 2, 2, 2, 1, 1, 1, 0, 0]

### 6.1.4 Solution templates in C, C++, and Python

**Code 6.2:** Solution template (C) *main.c*

```

1 /**
2 * 2025 Lord Kelvin Programming Competition - Solution Template
3 * Language: C (C11 Standard Recommended)
4 * * Usage:
5 * - Compile: gcc -O3 solution.c -o solution -lm
6 * - Local Test: ./solution < input.txt
7 * - CodeGrade: Automatically feeds data via stdin
8 */
9
10 #include <stdio.h>
11 #include <stdlib.h>
12 #include <math.h>
13 #include <string.h>
14
15 // =====
16 // 1. Constants & Data Structures
17 // =====
18
19 // Maximum constraints defined based on "Ultimate test cases"
20 // Ref: Section 5.2 Test cases [cite: 145, 149]
21 #define MAX_T 3005
22 #define MAX_N 45
23 #define MAX_M 85
24
25 #ifndef M_PI
26 #define M_PI 3.14159265358979323846
27 #endif
28
29 typedef struct {
30     int T; // Total duration
31     int N; // Number of states
32     int M; // Number of sound effects
33     int L; // Wandering cycle period

```

```

34     int Type; // 0 = No Penalty, 1 = Matrix Penalty
35 } Config;
36
37 typedef struct {
38     Config cfg;
39
40     // Initial base rewards R_initial(s)
41     int initial_rewards[MAX_N];
42
43     // System average reward centroid (mu)
44     double mu;
45
46     // Switching Penalty Matrix C_{i,j}
47     // Access: penalty_matrix[from_state][to_state]
48     int penalty_matrix[MAX_N][MAX_N];
49
50     // Transition Matrices P^(a)
51     // Access: transition_matrices[action_id][from_state][to_state]
52     double transition_matrices[MAX_M][MAX_N][MAX_N];
53
54 } ProblemData;
55
56 // =====
57 // 2. Logic Helpers (Math Model)
58 // =====
59
60 /**
61 * Calculate Reward R(s,t)
62 * Implements the Time-Variant Reward System.
63 * Ref: Section 3.4 [cite: 60, 61]
64 */
65 double get_reward(const ProblemData* data, int state, int t) {
66     // Case 1: Constant Rewards (L=0) [cite: 64]
67     if (data->cfg.L == 0) {
68         return (double)data->initial_rewards[state];
69     }
70
71     // Case 2: Wandering Rewards (L > 0) [cite: 60]
72     double r_init = (double)data->initial_rewards[state];
73     double cosine_term = cos((2.0 * M_PI * t) / (double)data->cfg.
74         L);
75     return data->mu + (r_init - data->mu) * cosine_term;
76 }
77

```

```

78 /**
79 * Calculate Switching Penalty
80 * Ref: Section 3.4 [cite: 52, 109, 110]
81 */
82 int get_penalty(const ProblemData* data, int prev_state, int
83 curr_state, int prev_action, int curr_action) {
84 // If actions are the same, cost is 0 [cite: 52]
85 if (prev_action == curr_action) return 0;
86
87 // If Type is 0 (Uniform/Static Mode), logic forces 0 penalty
88 // [cite: 110]
89 if (data->cfg.Type == 0) return 0;
90
91 // =====
92 // 3. Input Parsing (TODO)
93 // =====
94
95 void read_input(ProblemData* data) {
96 // Initialize standard streams for speed if possible (less
97 // critical in C than C++)
98
99 // -----
100 // TODO: Implement Data Reading Logic Here
101 // -----
102
103 // Ref: Section 4.1 Input Format [cite: 93-112]
104 // 1. Read Header: T, N, M, L, Type
105 // 2. Read Initial Rewards (N integers)
106 // 3. Read Penalty Matrix (N x N integers)
107 // 4. Read Transition Matrices (M blocks of N x N doubles)
108 // ... Write your scanf code here ...
109 }
110
111 // -----
112 // 4. Core Algorithm (Solver)
113 // -----
114
115 /**
116 * Fill the result array with the sequence of actions.
117 * Size of result array is data->cfg.T.
118 */
119 void solve(const ProblemData* data, int* result_actions) {
120 // -----

```

```

121 // TODO: Implement your Optimization Algorithm Here
122 // -----
123 // Objective: Maximize expected score J(A) [cite: 79]
124 // Starting state S_0 is always 0. [cite: 67]
125
126 // Example Placeholder: Fill with 0s
127 for (int t = 0; t < data->cfg.T; ++t) {
128     result_actions[t] = 0;
129 }
130 }
131
132 // =====
133 // 5. Output Formatting
134 // =====
135
136 void print_output(const int* actions, int T) {
137     // Format specification: [a1, a2, ..., aT] [cite: 254]
138     // Separator: Comma followed by a space [cite: 257]
139
140     printf("[");
141     for (int i = 0; i < T; ++i) {
142         printf("%d", actions[i]);
143         if (i < T - 1) {
144             printf(", ");
145         }
146     }
147     printf("]\n");
148 }
149
150 // =====
151 // Main Entry Point
152 // =====
153
154 int main() {
155     // Allocate data on stack (static size allows this)
156     // If stack size is an issue on some systems, make this static
157     // or global.
158     static ProblemData data;
159
160     // 1. Read Input
161     read_input(&data);
162
163     // 2. Solve
164     if (data.cfg.T > 0 && data.cfg.T <= MAX_T) {
165         // Allocate result array
166         int result_actions[MAX_T];

```

```

166     solve(&data, result_actions);
167
168     // 3. Output
169     print_output(result_actions, data.cfg.T);
170 }
171
172 return 0;
173 }
174 }
```

**Code 6.3:** Solution template (C++) *main.cpp*

```

1 /**
2 * 2025 Lord Kelvin Programming Competition - Solution Template
3 * Language: C++20
4 * * Usage:
5 * - Compile: g++ -O3 main.cpp -o solution
6 * - Local Test: ./solution < input.txt
7 * - CodeGrade: Automatically feeds data via stdin
8 */
9
10 #include <iostream>
11 #include <vector>
12 #include <cmath>
13 #include <iomanip>
14 #include <numeric>
15
16 using namespace std;
17
18 // =====
19 // 1. Data Structure Definitions
20 // =====
21
22 struct Config {
23     int T; // Total duration [cite: 101]
24     int N; // Number of states [cite: 102]
25     int M; // Number of sound effects [cite: 103]
26     int L; // Wandering cycle period [cite: 104]
27     int Type; // 0 = Uniform Penalty, 1 = Generalized Matrix
                // Penalty [cite: 106]
28 };
29
30 struct ProblemData {
31     Config cfg;
```

```

32
33     // Initial base rewards R_initial(s)
34     // Size: N
35     vector<int> initial_rewards;
36
37     // Switching Penalty Matrix C_{i,j}
38     // Size: N x N
39     // Note: Always read this matrix regardless of Type [cite:
40         108]
41     vector<vector<int>> penalty_matrix;
42
43     // Transition Matrices P^(a)
44     // Structure: [Action_ID] [From_State] [To_State]
45     // Size: M x N x N
46     vector<vector<vector<double>>> transition_matrices;
47
48     // System average reward centroid (mu), calculated
49     // automatically
50     double mu;
51 }
52 // =====
53 // 2. Helper Functions (Math Model)
54 // =====
55 /**
56 * Calculate Reward R(s,t)
57 * Formula: R(s,t) = mu + (R_initial(s) - mu) * cos(2*pi*t / L) [cite: 60]
58 */
59 double get_reward(const ProblemData& data, int state, int t) {
60     if (data.cfg.L == 0) {
61         return (double) data.initial_rewards[state];
62     }
63
64     double r_init = data.initial_rewards[state];
65     // cos takes radians
66     double cosine_term = cos((2.0 * M_PI * t) / (double) data.cfg.L
67                             );
68     return data.mu + (r_init - data.mu) * cosine_term;
69 }
70 /**
71 * Calculate Switching Penalty
72 * Penalty = I(a_t != a_{t-1}) * C_{s_{t-1}, s_t} [cite: 52]
73 */

```

```

74 int get_penalty(const ProblemData& data, int prev_state, int
75     curr_state, int prev_action, int curr_action) {
76     // If Type is 0, penalty is 0 (Uniform mode) [cite: 110]
77     if (data.cfg.Type == 0) return 0;
78
79     // No penalty if action doesn't change
80     if (prev_action == curr_action) return 0;
81
82     return data.penalty_matrix[prev_state][curr_state];
83 }
84 // =====
85 // 3. Input Parsing (TODO)
86 // =====
87
88 ProblemData read_input() {
89     ProblemData data;
90
91     // -----
92     // TODO: Implement Data Reading Logic Here
93     // -----
94     // Refer to Section 4.1 Input Format in the Problem Statement.
95     //
96     // Step 1: Read Header (T, N, M, L, Type) [cite: 100]
97     // Step 2: Read N integers for initial_rewards [cite: 107]
98     // *Tip: Calculate 'mu' (average of rewards) here.
99     // Step 3: Read Switching Penalty Matrix (N x N) [cite: 108]
100    // Step 4: Read Transition Matrices (M blocks, each N x N) [
101        cite: 111]
102
103    // ... Write your cin code here ...
104
105 }
106
107 // -----
108 // 4. Core Algorithm (Solver)
109 // =====
110
111 vector<int> solve(const ProblemData& data) {
112     // Result vector to store action for each minute t=1 to T
113     vector<int> actions(data.cfg.T);
114
115     // -----
116     // TODO: Implement your Optimization Algorithm Here
117     // -----

```

```

118 // Objective: Maximize J(A) [cite: 80]
119 // You can use Dynamic Programming (DP), Greedy, or MCTS.
120
121 // Placeholder: This fills the array with 0s. Replace this
122 // logic.
123 for (int t = 0; t < data.cfg.T; ++t) {
124     actions[t] = 0;
125 }
126
127 }
128
129 // =====
130 // 5. Output Formatting
131 // =====
132
133 void print_output(const vector<int>& actions) {
134     // Format must be strictly: [a1, a2, ..., aT] [cite: 117]
135     cout << "[";
136     for (size_t i = 0; i < actions.size(); ++i) {
137         cout << actions[i];
138         if (i < actions.size() - 1) {
139             cout << ", ";
140         }
141     }
142     cout << "]" << endl;
143 }
144
145 // =====
146 // Main Entry Point
147 // =====
148
149 int main() {
150     // Optimize Standard I/O Speed
151     ios_base::sync_with_stdio(false);
152     cin.tie(NULL);
153
154     // Read Data
155     ProblemData data = read_input();
156
157     // Solve
158     if (data.cfg.T > 0) {
159         vector<int> result = solve(data);
160         print_output(result);
161     }
162 }
```

```
163 return 0;
164 }
```

**Code 6.4:** Solution template (Python) *main.py*

```
1 #!/usr/bin/env python3
2 import sys
3 import math
4 from typing import List, Optional
5
6 # =====
7 # 1. Data Structure Definitions
8 # =====
9
10 class Config:
11     def __init__(self):
12         self.T: int = 0 # Total duration (minutes)
13         self.N: int = 0 # Number of states
14         self.M: int = 0 # Number of sound effects (actions)
15         self.L: int = 0 # Wandering cycle period (0 = Static)
16         self.Type: int = 0 # 0 = No Penalty, 1 = Matrix Penalty
17
18 class ProblemData:
19     def __init__(self):
20         self.cfg = Config()
21
22         # Initial base rewards R_initial(s)
23         self.initial_rewards: List[int] = []
24
25         # System average reward centroid (mu), calculated during
26         # input
27         self.mu: float = 0.0
28
29         # Switching Penalty Matrix C_{i,j}
30         # Dimensions: [N] [N] - Cost of switching from state i to j
31         self.penalty_matrix: List[List[int]] = []
32
33         # Transition Matrices P^(a)
34         # Dimensions: [M] [N] [N] - P(from_state -> to_state) given
35         # Action
36         self.transition_matrices: List[List[List[float]]] = []
37 # =====
38 # 2. Logic Helpers (Handles Basic/Ult. Cases)
```

```

38 # =====
39
40 def get_reward(data: ProblemData, state: int, t: int) -> float:
41     """
42     Calculates R(s,t).
43     Handles both 'Basic/Performance' (L=0) and 'Ultimate' (L>0)
44     cases.
45     Ref: Section 3.4 - Time-Variant Reward System
46     """
47     # Case 1: Static Rewards (L=0)
48     if data.cfg.L == 0:
49         return float(data.initial_rewards[state])
50
51     # Case 2: Time-Variant Rewards (L > 0)
52     # Formula: R(s,t) = mu + (R_initial(s) - mu) * cos(2*pi*t / L)
53     r_init = data.initial_rewards[state]
54     cosine_term = math.cos((2 * math.pi * t) / data.cfg.L)
55
56     return data.mu + (r_init - data.mu) * cosine_term
57
58 def get_penalty(data: ProblemData, prev_state: int, curr_state: int,
59                 prev_action: int, curr_action: int) -> int:
60     """
61     Calculates Switching Penalty.
62     Handles 'Basic' (Type=0) and 'Performance/Ultimate' (Type=1)
63     cases.
64     Ref: Section 3.4 - Dynamics
65     """
66
67     # No penalty if the action does not change
68     if prev_action == curr_action:
69         return 0
70
71     # Case 1: Uniform/No Penalty Mode (Type=0)
72     if data.cfg.Type == 0:
73         return 0
74
75     # Case 2: Generalized Matrix Penalty Mode (Type=1)
76     # Penalty = C_{prev_state, curr_state}
77     return data.penalty_matrix[prev_state][curr_state]
78
79 # =====
80 # 3. Input Parsing (TODO)
81 # =====
82
83 def read_input() -> Optional[ProblemData]:
84     """

```

```

81     Reads all data from stdin adhering to the competition Input
82         Format.
83     """
84     try:
85         # Read all tokens at once for performance (crucial for T
86         # =3000)
87         input_data = sys.stdin.read().split()
88         if not input_data:
89             return None
90
91         iterator = iter(input_data)
92         data = ProblemData()
93
94         # -----
95         # TODO: Implement Data Reading Logic Here
96         #
97         # 1. Header: T, N, M, L, Type
98         # 2. Base Rewards: N integers (Calculate data.mu here)
99         # 3. Penalty Matrix: N*N integers (Always read it, even if
100            Type=0)
101        # 4. Transition Matrices: M blocks of N*N floats
102        #
103        # Use `val = next(iterator)` to fetch the next token.
104
105        pass # Remove this pass when implementing
106
107        return data
108
109    # =====
110    # 4. Core Algorithm (Solver)
111    # =====
112
113    def solve(data: ProblemData) -> List[int]:
114        """
115            Generates the optimal action sequence [a_1, ..., a_T].
116        """
117        actions = [0] * data.cfg.T
118
119        # -----
120        # TODO: Implement your Optimization Algorithm Here
121        #
122        # NOTE:
123        # - For Basic Cases (Small T, N, M)

```

```
124     # - For Performance/Ultimate (Large T)
125     return actions
126
127 # =====
128 # 5. Output Formatting
129 # =====
130
131 def print_output(actions: List[int]):
132     """
133     Formats the output strictly as [a1, a2, ..., aT].
134     """
135     # Using specific formatting to ensure ", " separator
136     formatted_str = "[" + ", ".join(map(str, actions)) + "]"
137     print(formatted_str)
138
139 # =====
140 # Main Entry Point
141 # =====
142
143 if __name__ == "__main__":
144     # Increase recursion depth just in case (optional)
145     sys.setrecursionlimit(5000)
146
147     data = read_input()
148
149     if data and data.cfg.T > 0:
150         result = solve(data)
151         print_output(result)
```