

Teleportation

```
!pip install qiskit
!pip install qiskit_aer
from qiskit import QuantumCircuit
from qiskit.quantum_info import
Statevector,partial_trace
from qiskit_aer import Aer
from math import sqrt
from qiskit.visualization import plot_histogram
qc = QuantumCircuit(3,2)
# state that want to teleport
state = [1/sqrt(2),1/sqrt(2)]
qc.initialize(state,0)
qc.h(1)
qc.cx(1,2)
qc.draw()
state = Statevector(qc)
state.draw('latex') # MSB is ist
qc.cx(0,1)
qc.h(0)
```

```
qc.measure(0,0)
qc.measure(1,1)
backend = Aer.get_backend('aer_simulator')
result = backend.run(qc,shots=1).result()
measurment_result =
list(result.get_counts().keys())[0][::-1] # reversing for
readability
measurment_result
if measurment_result == '11':
    qc.x(2)
    qc.z(2)
elif measurment_result == '10':
    qc.z(2)
elif measurment_result == '01':
    qc.x(2)
backend = Aer.get_backend('statevector_simulator')
result = backend.run(qc).result()
state = result.get_statevector()
state.draw('latex') # msb ist , so teleported qubit ist.
```

Superdense Coding

```
from qiskit import QuantumCircuit
from qiskit.visualization import *
from qiskit_aer import Aer
qc = QuantumCircuit(2,2)
qc.h(0)
qc.cx(0, 1)
qc.draw()
bit = '01'
if bit=='00':
    pass
elif bit=='01':
    qc.x(0)
elif bit=='10':
    qc.z(0)
elif bit=='11':
    qc.x(0)
    qc.z(0)
# Bob decodes
qc.cx(0,1)
qc.h(0)
```

```
qc.measure(0,0)
qc.measure(1,1)
sim = Aer.get_backend('aer_simulator')
result = sim.run(qc,shots=1).result()
counts = result.get_counts()
print(counts)
```

Deutsch-Jozsa Algorithm

```
! pip install qiskit_aer
```

```
def constant_oracle(n):
```

```
    """
```

```
    when  $f(x) = 0$  or  $1$  (constant) , then for input  $xy$  ,  
    output will be  $xy$  (same)
```

```
    """
```

```
    oracle = QuantumCircuit(n + 1)
```

```
    # oracle.x(n) # for  $f(x)=1$ 
```

```
    return oracle
```

```
def balanced_oracle(n):
```

```
    """
```

```
    when  $f(x)$  is balanced , then outputs will half  
    opposite,
```

```
    so just applying operations  $y \oplus f(x)$  , for all  $x$ 
```

```
    """
```

```
    oracle = QuantumCircuit(n + 1)
```

```
    for i in range(n):
```

```
        oracle.cx(i, n)
```

```
    return oracle
```

```
from qiskit import QuantumCircuit
from qiskit_aer import Aer
from qiskit.visualization import plot_histogram
import matplotlib.pyplot as plt

def deutsch_jozsa(f_oracle, n):
    # n+1 bits(input) and n for classical bit(output)
    qc = QuantumCircuit(n + 1, n)

    # Step 1: Setting up y
    qc.x(n)
    qc.h(n)

    # Step 2: Hadamard transform to input x
    for i in range(n):
        qc.h(i)
    qc.barrier()

    # Step 3: Append the oracle f(x)
    qc = qc.compose(f_oracle, qubits=range(n + 1))
    qc.barrier()
```

```
# Step 4: Apply Hadamard again to input qubits
for i in range(n):
    qc.h(i)
# Step 5: Measure input qubits
for i in range(n):
    qc.measure(i, i)
return qc

# Choose number of input bits
n = 3

# Preparing Uf
oracle = constant_oracle(n)
dj_circuit = deutsch_jozsa(oracle, n)
dj_circuit.draw()
sim = Aer.get_backend('aer_simulator')
result = sim.run(dj_circuit).result()
f = result.get_counts()
f
```

Shor's Algo

Shor's Algorithm

```
import numpy as np
from qiskit import QuantumCircuit, transpile
from qiskit_aer import Aer
import math

def qft_dagger(n):
    circuit = QuantumCircuit(n)
    for j in range(n // 2):
        circuit.swap(j, n - j - 1)
    for j in range(n):
        for k in range(j):
            circuit.cp(-np.pi / float(2 ** (j - k)), k, j)
        circuit.h(j)
    return circuit

def modular_exponentiation(n_count, a, N):
    circuit = QuantumCircuit(n_count + 4, n_count)
    for x in range(n_count):
        for q in range(4):
```



```

power = (2 ** x) % N
if (a ** power % N) & (1 << q):
    circuit.cx(x, n_count + q)
return circuit

def run_shor(N=15, a=7):
    print(f"\n Shor's Algorithm: Factoring N={N} with
a={a}\n")
    if N % 2 == 0:
        print("N is even, factor: 2")
        return
    if int(N ** (1 / float(2))) ** 2 == N:
        print(f"N is a square, factor: {int(N ** (1 / float(2)))}")
    n_count = 4
    circuit = QuantumCircuit(n_count + 4, n_count)
    circuit.h(range(n_count))
    oracle = modular_exponentiation(n_count, a, N)
    circuit.append(oracle, range(n_count + 4))
    qft = qft_dagger(n_count)
    circuit.append(qft, range(n_count))
    circuit.measure(range(n_count), range(n_count))

```

```

simulator = Aer.get_backend('qasm_simulator')
result = simulator.run(transpile(circuit, simulator),
shots=1000).result()

counts = result.get_counts()
print("Measurement Results:", counts)

factors = set()

for measured in counts:
    measured_int = int(measured, 2)
    if measured_int == 0:
        continue
    fraction = measured_int / (2 ** n_count)
    denominators = []
    x = fraction
    for _ in range(10):
        a = int(1 / x) if x != 0 else 0
        denominators.append(a)
        x = 1 / x - a if x != 0 else 0
    if x < 1e-6:
        break
    r = 1

```

```

for d in denominators:
    r = 1 / (d + 1 / r) if r != 0 else d
    r = int(round(1 / r))
    if r % 2 == 0 and r > 0:
        factor1 = math.gcd(a ** (r // 2) - 1, N)
        factor2 = math.gcd(a ** (r // 2) + 1, N)
        if 1 < factor1 < N:
            factors.add(factor1)
        if 1 < factor2 < N:
            factors.add(factor2)
    if factors:
        print(f"Factors of {N}: {sorted(list(factors))}")
    else:
        print("No non-trivial factors found. Try a different a.")
if __name__ == "__main__":
    run_shor()

```

Grover's Algo

```
! pip install qiskit_aer
from qiskit import QuantumCircuit
from qiskit_aer import Aer
from qiskit.circuit.library import MCXGate
from qiskit.visualization import plot_histogram ,
plot_bloch_multivector
import numpy as np
def oracle(n,x):
    qc = QuantumCircuit(n)
    s = []
    for ind , i in enumerate(x): # x is from least to
mostsignificant
        if i == '0':
            s.append(ind)
            qc.x(ind)
    # multicontrolled controlled z
    qc.h(n-1)
    qc.mcx(list(range(n-1)),n-1)
    qc.h(n-1)
```

```
if s:
    for i in s:
        qc.x(i)
    return qc
```

```
def diffusion(n):
    qc = QuantumCircuit(n,n)
    qc.h(range(n))
    qc.x(range(n))
    # multicontrolled z gate
    qc.h(n-1)
    qc.mcx(list(range(n-1)),n-1)
    qc.h(n-1)
    qc.x(range(n))
    qc.h(range(n))
    return qc
```

```
def grovers_algo(n,x,iterations=1,m=1):
    if iterations == 'auto':
        iterations = int(np.floor((np.pi/4) * np.sqrt(2**n/m)
        ))
```

```
    qc = QuantumCircuit(n,n)
```

```

qc.h(range(n))
# two operations of Grover's operation
for _ in range(iterations):
    print("iteration")
    qc.barrier(label='iter start')
    # ist Uf (sign flip) assuming 2 bit input and x' = 11
    qc = qc.compose(oracle(n,x))
    qc.barrier()

    # 2nd W (Diffusion Operation)
    qc = qc.compose(diffusion(n))
    qc.barrier(label='iter end')
    qc.measure(range(n),range(n))
    return qc

qc = grovers_algo(5,x='10111',iterations='auto')
qc.draw()

sim = Aer.get_backend('aer_simulator')
result = sim.run(qc).result()

plot_histogram(result.get_counts()) # x is most
significant to least significant

```

BB84

```
from qiskit import QuantumCircuit
from qiskit_aer import Aer
from qiskit.visualization import plot_histogram
from copy import deepcopy
from numpy import random
import numpy as np

def basis(index):
    basis=[]
    for i in index:
        if i == 0:
            basis.append('Z')
        else:
            basis.append('X')
    return basis

def prep_qubit(bits,basises,n):
    qc = QuantumCircuit(n,n)
    for ind , (bit , basis) in enumerate(zip(bits,basises)):
        if basis == 'Z':
            if bit == 1:
                qc.x(ind)
```

```

    elif basis == 'X':
        if bit == 0:
            qc.h(ind)
        elif bit == 1:
            qc.h(ind)
            qc.z(ind)
    return qc

def measure_qubit(o_basis , qc , eve=False):
    for ind , basis in enumerate(o_basis):
        if basis == 'Z':
            qc.measure(ind,ind)
        elif basis == 'X':
            qc.h(ind)
            qc.measure(ind,ind)
    sim = Aer.get_backend('aer_simulator')
    result = sim.run(qc,shots=1).result()
    results = result.get_counts().keys()
    return list(results)[0][::-1] # because qiskit writes msb
first

def bb84_sender(n):
    alice_bits = random.randint(2,size=n)

```



```

alice_basis_ind = random.randint(2,size=n)
alice_basis = basis(alice_basis_ind)
ciper_qubits = prep_qubit(alice_bits,alice_basis,n)
return ciper_qubits , alice_basis , alice_bits
ciper_qubits ,alice_basis , alice_bits= bb84_sender(12)
def bb84_eve(n):
    eve_basis_ind = random.randint(2,size=n)
    eve_basis = basis(eve_basis_ind)
    data =
measure_qubit(eve_basis,ciper_qubits.copy(),eve=True
)
    return data , eve_basis
eve_bits , eve_basis = bb84_eve(12)
# making eve_bits string to array of int
eve_recieved_bits = []
for d in data:
    eve_recieved_bits.append(int(d))
eve_recieved_bits = np.array(eve_recieved_bits)
# ciper_qubits =
prep_qubit(eve_recieved_bits,eve_basis,12) #uncomm
ent to include eve intercept
def bb84_reciever(n):

```

```

    bob_basis_ind = random.randint(2,size=n)
    bob_basis = basis(bob_basis_ind)
    data = measure_qubit(bob_basis,ciper_qubits)
    return data , bob_basis
data , bob_basis = bb84_reciever(12)
# making data string to array of int
bob_recieved_bits = []
for d in data:
    bob_recieved_bits.append(int(d))
bob_recieved_bits = np.array(bob_recieved_bits)
alice_bits
bob_recieved_bits
alice_basis = np.array(alice_basis)
bob_basis = np.array(bob_basis)
no = []
for ind ,(al,bo) in
enumerate(zip(alice_basis,bob_basis)):
    if al == bo:
        no.append(ind)
for i in no:
    print(alice_bits[i] , bob_recieved_bits[i])

```