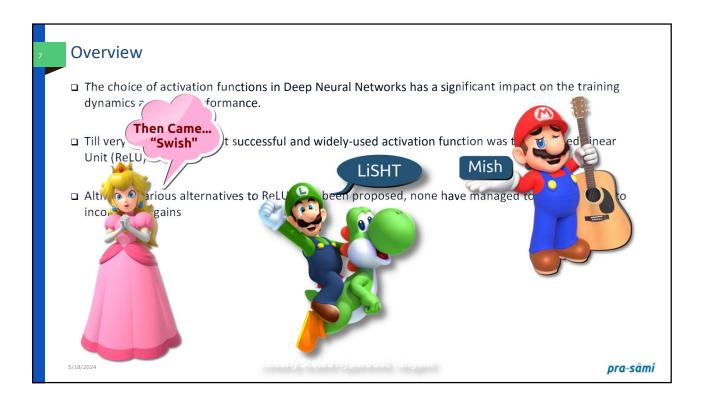


Activation Function

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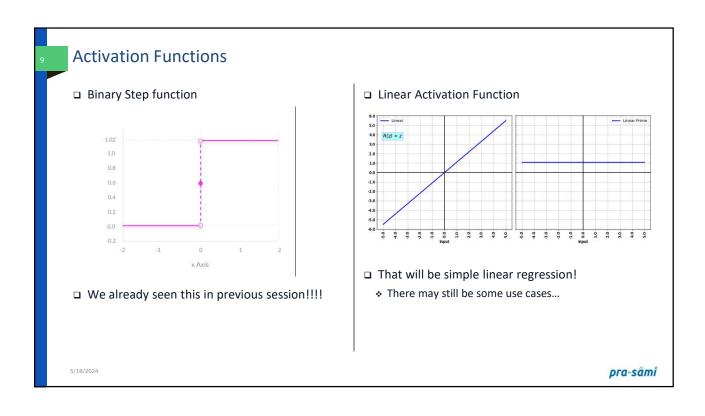
Overview

- □ The choice of activation functions in Deep Neural Networks has a significant impact on the training dynamics and task performance.
- □ Till very recently, the most successful and widely-used activation function was the Rectified Linear Unit (ReLU)
- □ Although various alternatives to ReLU have been proposed, none have managed to replace it due to inconsistent gains



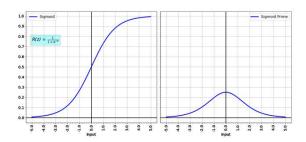
Activation Functions

- ☐ Activation functions is a function attached to each neuron in the network
 - It determines whether it should be activated ("fired") or not, based on whether each neuron's input is relevant for the model's prediction
- □ Activation functions also help normalize the output of each neuron to a range:
 - ❖ Between 1 and 0 or
 - Between -1 and 1
 - Or other desired ranges
- □ Need to be computationally lightweight
 - It is calculated for each neuron for every data instance (row)
- □ It's a mathematical gate that turns a neuron on or off



Non-Linear Activation Functions There are many popular activation functions Sigmoid / Logistic Softmax Tanh (Hyperbolic Tangent) ReLU (Rectified Linear Unit) Leaky ReLU Parametric ReLU Swish Lisht Mish Stay tuned... it's an active research area...

Sigmoid



- □ Takes a real value as input and outputs another value between 0 and 1 i.e. [0,1]
- □ It's easy to work with; Most suitable as activation functions
- ☐ Non-linear, continuously differentiable, monotonic, and has a fixed output range
- ☐ Good for binary classification tasks

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Sigmoid – drawbacks

- □ Towards either end, becomes sluggish
 - Problem of "vanishing gradients"
 - * The network refuses to learn further or is drastically slow
 - Another reason why we need to scale values
- □ Its output isn't zero centered. It makes the gradient updates go too far in different directions.
 - 0 < output < 1, and it makes optimization harder
- □ Sigmoid saturates and kills gradients

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Softmax Function

- □ In physics and statistical mechanics, it is known as the **Boltzmann** distribution or the **Gibbs** distribution.
- □ Formulated by the Austrian physicist and philosopher **Ludwig Boltzmann** in **1868**.
- □ In 1959, **Robert Duncan Luce** proposed the use of the Softmax function for reinforcement learning in his book "Individual Choice Behavior: A Theoretical Analysis".
- ☐ Take vector of N values and convert into vector of N values with sum = 1
- □ Input values are natural numbers (Positive, Negative).
- \Box Output is always numbers between 0 and 1 i.e. $A = \{a \mid real(a) \land 0 \le a \le 1\}$

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Softmax Function

- □ Softmax is multi-class logistic regression,
 - ❖ Takes vector of N values and converts into vector of N values with sum = 1
 - Input values are natural numbers (Positive, Negative).
 - * Output is always numbers between 0 and 1 i.e. $A = \{ a \mid real(a) \land 0 \le a \le 1 \}$
 - * It is differentiable everywhere.
- □ Its helps in representing values as probabilities
 - Smaller the value, smaller the probability and vice versa

Like Sigmoid Activation function, Vanishing Gradient is still a problem!

 $S(\vec{Z}) = \frac{e^{z_i}}{\sum_{i=1}^K e^{z_i}}$

- ☐ Its formula is very similar to Sigmoid function,
 - Sigmoid function is one special case of Softmax
- Softmax is very useful because it converts the scores to a normalized probability distribution
 - * Invariably, multi-layer neural networks end in a penultimate layer which outputs real-valued scores,
 - * It is non-linear in nature. So, it introduces non-linearity in the network enabling it to learn better.

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Softmax vs. Sigmoid

□ Softmax

$$\sigma(z) = \frac{1}{1 + e^{-z}}$$

□ Sigmoid

$$S(\vec{Z}) = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_i}}$$

□ For single class value will be [0, x], Softmax

$$S(\vec{Z}) = \frac{e^{z_i}}{\sum_{j=1}^{K} e^{z_i}}$$

$$S(\vec{Z}) = \frac{e^{z_1}}{e^{z_1} + e^{z_2}}$$

$$S(X) = \frac{e^x}{e^0 + e^x}$$

$$S(X) = \frac{e^x}{1 + e^x}$$

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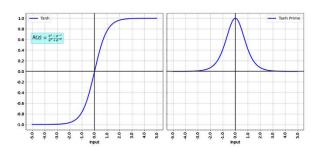
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Softmax vs. Argmax

- □ Both work the same way, Softmax is expected to be a differentiable alternative to argmax
- □ Argmax returns index of highest value and no idea about other values.
- ☐ It is common to train using the Softmax

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Tanh



- ☐ Mathematically shifted version of the sigmoid function with
- Non-linear, but zero-centered
 - Very useful in hidden layers
 - * Helps in centering the data around zero (bring mean closer to zero). Learning next layer becomes easier.
- ☐ The gradient is stronger than sigmoid
 - Derivatives are steeper
- □ Other problems are similar to sigmoid

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Tanh

■ Advantage:

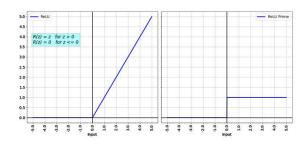
- * The negative inputs will be mapped negative and the zero inputs will be mapped near zero
- * The function is differentiable.
- * The function is monotonic while its derivative is not monotonic.
- Faster convergence for two reason:
 - > Steeper than Sigmoid function
 - > Zero centric output

□ Disadvantage:

- Vanishing gradient have not gone away yet!
- □ Different research papers different views as to why it is better or even it is not always better!
- ☐ And the debate will continue...
- □ Early stages of design, Tanh in intermediate layer is a good starting point

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Rectified Linear Units (ReLU)



- Non-linear function (almost)
- Better performance than Sigmoid or Tan in almost all models
- $\hfill \square$ It avoids and rectifies vanishing gradient problem.
- Q ReLU is less computationally expensive than tanh and sigmoid because it involves simpler mathematical operations.
- □ Suitable for Hidden layers only.

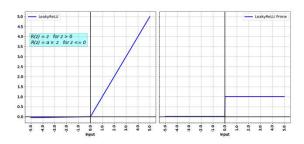
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Rectified Linear Units (ReLU)

- □ Some gradients can be fragile during training and can die.
- □ Could result in Dead Neurons.
- \Box For activations in the region (x<0) of ReLu , gradient will be zero
 - Weights will not get adjusted during descent
 - Neurons which go into that state will stop responding to variations in error/input
 - Dying ReLu problem
- □ The range of ReLu is $[0, \infty]$
 - Can blow up the activation

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Leaky ReLU

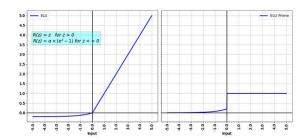


- □ Attempt to fix the "dying ReLU" problem by having a small negative slope (of 0.01, or so).
- □ LeakyRelu is a variant of ReLU; allows a small, non-zero negative values
 - $\Rightarrow R(z_i) = \begin{vmatrix} z_i & if z_i \ge 0 \\ a_i \cdot z_i & if z_i < 0 \end{vmatrix}$
 - * Work–under–progress: benefits across different architectures and domains still being investigated
- ☐ As it possess linearity, it can't be used for the complex Classification.
- □ Lags behind the Sigmoid and Tanh for some of the use cases.

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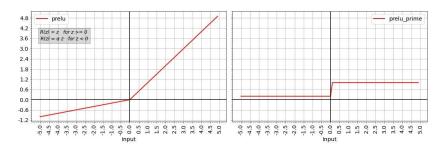
Exponential Linear Unit (ELU)



- ☐ Converges faster; Has alpha constant which should be positive number
- □ ELU is a strong alternative to ReLU.
- □ Unlike to ReLU, ELU can produce negative outputs.
- \Box For x > 0, it can blow up the activation with the output range of [0, ∞].

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Parameterized ReLU



- □ A Parametric Rectified Linear Unit, or PReLU, is an activation function that generalizes the traditional rectified unit with a slope for negative values.
- ☐ The intuition is that different layers may require different types of nonlinearity.

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Parameterized ReLU

$$F(z_i) = \begin{vmatrix} z_i & if z_i \ge 0 \\ a_i \cdot z_i & if z_i < 0 \end{vmatrix}$$

- □ Pick your own parameter
- □ In experiments with convolutional neural networks, PReLus for the initial layer have more positive slopes, i.e. closer to linear.
 - Since the filters of the upper layers are edge or texture detectors,
 - This shows a circumstance where positive and negative responses of filters are respected.
- ☐ In contrast, deeper layers have smaller coefficients
 - Model becomes more discriminative at later layers
 - $\ensuremath{ \bullet}$ While it wants to retain more information at earlier layers.

Challenges with ReLU

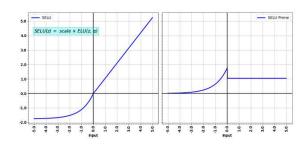
- □ The consistent problem is that its derivative is 0 for half of the values of the input x in the Function, i.e. f(x)=max(0,x)
- ☐ As parameter update algorithm, could used Stochastic Gradient Descent and other optimizers
 - If the parameter itself is 0, then that parameter will never be updated as it just assigns the parameter back to itself
 - ❖ Leading close to 40% Dead Neurons in the Neural network environment where z is negative
 - Various substitutes like Leaky ReLU Prameterized ReLU have unsuccessfully tried to devoid it of this issue.

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Scaled ELU (SELU)

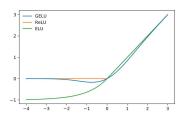


- ☐ Activation was introduced in a 2017 paper by Klambauer et al
- □ Properly initialization, the networks will self-normalize
 - * Each layer's output will roughly be zero-centered with standard deviation equal to one
- ☐ Helps prevent the vanishing or exploding gradients problems

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Gau

Gaussian Error Linear Unit (GELU)



The GELU ($\mu\,=\,0,\sigma\,=\,1$), ReLU, and ELU($\alpha=1$)

□ Contrary to the ReLU, GELU weights its inputs by their value instead of thresholding them by their sign

 $\hfill \Box$ Defines as The GELU activation function is x* $\Phi(x)$,

 $\ \ \, \hbox{ where } \Phi(\textbf{x}): \text{the standard Gaussian cumulative distribution function refer scipy's norm.cdf(\textbf{x})} \\$

$$\mathrm{GELU}(x) = xP(X \le x) = x\Phi(x)$$

$$\star \approx 0.5x(1 + \tanh[\sqrt{2/\pi(x + 0.044715x^3)}])$$

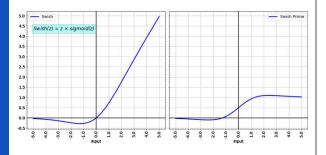
 \star or $x\sigma(1.702x)$,

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Swish



- Google Brain Team proposed a new activation function:
 - \star f(x) = x · sigmoid(x)
- Experiments show that Swish tends to work better than ReLU on deeper models across a number of challenging data sets
 - Simply replacing ReLUs with Swish units improves top-1 classification accuracy on ImageNet by 0.9% for Mobile NASNetA and 0.6% for Inception-ResNet-v2
- The simplicity of Swish and its similarity to ReLU make it easy for practitioners to replace ReLUs with Swish units in any neural network.
- Swish is a smooth, non-monotonic function that consistently matches or outperforms ReLU on deep networks

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Swish

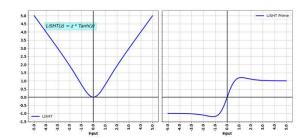
- Unbounded above and bounded below
 - * Non-monotonic attribute that actually creates the difference
- We can train deeper Swish networks than ReLU networks when using BatchNorm (loffe & Szegedy, 2015) despite having gradient squishing property
- With MNIST data set, when Swish and ReLU are compared, both activation functions achieve similar performances up to 40 layers.
- □ Swish outperforms ReLU by a large margin in the range between 40 and 50 layers
 - For less than 40 layers, performance is comparable
- ☐ In very deep networks, Swish achieves higher test accuracy than ReLU.
- □ Swish outperforms ReLU on every batch size, suggesting that the performance difference between the two activation functions remains even when varying the batch size.
- ☐ Gradient descent problem was still there may be to a lesser degree!

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LiSHT Activation Function

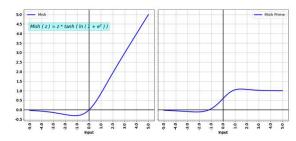


- ☐ The function scale the non-linear Hyperbolic Tangent (Tanh) function by a linear function
 - Help tackle the dying gradient problem
- ☐ According to paper it has outperformed Swish on a number of problems

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Mish



f(z) = z * tanh (softplus (z))= z * tanh (ln (1 + e^z))

- □ Inspired by Swish and has been shown to outperform it in a variety of computer vision tasks
- Mish was "found by systematic analysis and experimentation over the characteristics that made Swish so effective".
- ☐ Mish seems to be the best activation in stock,
 - . But jury is still out

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Reflect...

- □ Which of the following is a common activation function used in last layer of deep neural networks?
 - ❖ A) Linear activation
 - * B) Step function
 - * C) Sigmoid function
 - * D) Exponential function
- □ Answer: C
- What is the vanishing gradient problem in deep neural networks?
 - $\boldsymbol{\div}$ A) The problem of too many layers in the network
 - * B) The problem of exploding gradients during training
 - * C) The problem of slow convergence during training
 - $\ensuremath{\raisebox{.4ex}{\scriptstyle\bullet$}}$ D) The problem of very negligible gradients in early layers
- □ Answer: D

- What is the purpose of the softmax activation function in the output layer of a classification neural network?
 - · A) To introduce non-linearity
 - ❖ B) To convert logits into probabilities
 - ❖ C) To prevent overfitting
 - ❖ D) To reduce the dimensionality of the output
- □ Answer: B
- In deep learning, what does the term "epoch" refer to during training?
 - A) A complete pass through the training dataset
 - ❖ B) The number of layers in the neural network
 - * C) The learning rate of the optimizer
 - * D) The size of the mini-batch used for training
- □ Answer: A

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Reflect...

- What is the role of activation functions in deep neural networks?
 - A) To normalize the input data
- * B) To compute the loss function
- * C) To introduce non-linearity into the network
- * D) To reduce overfitting
- ☐ Answer: C) To introduce non-linearity into the network
- What does the term "backpropagation" refer to in the context of neural networks?
 - * A) The process of adjusting the weights of the network based on the prediction error
 - * B) The process of training the network using labeled data
 - C) The process of selecting the optimal hyperparameters for the network
 - * D) The process of initializing the weights of the network
- Answer: A) The process of adjusting the weights of the network based on the prediction error

- Which of the following is NOT a commonly used activation function in deep neural networks?
 - ❖ A) Sigmoid
 - ❖ B) ReLU (Rectified Linear Unit)
 - ❖ C) Tanh (Hyperbolic Tangent)
 - ❖ D) Linear
- □ Answer: D) Linear

