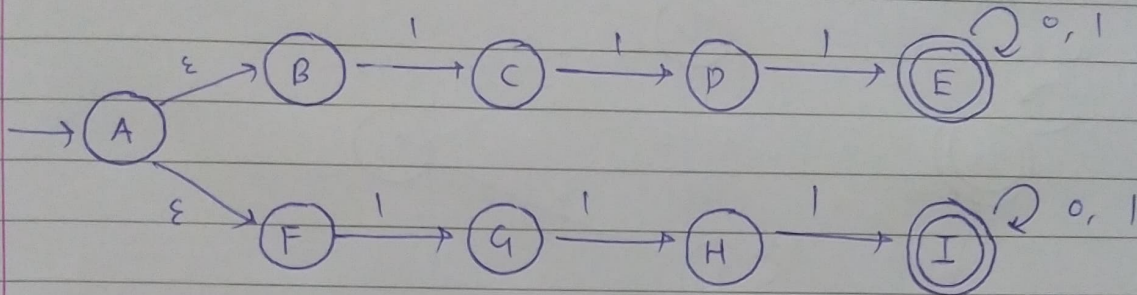


- 1) Create DFA for strings starting or ending with 111.
NFA with ϵ -moves to be converted to DFA.

→ The required NFA would be



Transition table for NFA:

δ	0	1	ϵ
A	ϕ	ϕ	B, F
B	ϕ	C	
C	ϕ	D	
D	ϕ	E	
E	E	E	
F	F	G, F	
G	ϕ	H	
H	ϕ	I	
I	I	I	

Now, find ϵ closure of each state.

$$\{A\} = \{A, B, F\}$$

$$\{B\} = \{B\}$$

$$\{C\} = \{C\}$$

$$\{D\} = \{D\}$$

$$\{E\} = \{E\}$$

$$\{F\} = \{F\}$$

$$\{G\} = \{G\}$$

$$\{H\} = \{H\}$$

$$\{I\} = \{I\}$$

ϵ closure $\{A\} = \{A, B, F\} \rightarrow$ state q_0

$$\delta'(q_0, 0) = \{F\} \rightarrow q_1$$

$$\delta'(q_0, 1) = \{C, F, G\} \rightarrow q_2$$

$$\delta'(q_1, 0) = \{F\} = q_1$$

$$\delta'(q_1, 1) = \{F, G\} \rightarrow q_3$$

$$\delta'(q_2, 0) = \{F\} \rightarrow q_1$$

$$\delta'(q_2, 1) = \{D, F, G, H\} \rightarrow q_4$$

$$\delta'(q_3, 0) = \{F\} \rightarrow q_1$$

$$\delta'(q_3, 1) = \{F, G, H\} \rightarrow q_5$$

$$\delta'(q_4, 0) = \{F\} \rightarrow q_1$$

$$\delta'(q_4, 1) = \{E, F, G, H, I\} \rightarrow q_6^*$$

$$\delta'(q_5, 0) = \{F\} \rightarrow q_1$$

$$\delta'(q_5, 1) = \{F, G, H, I\} \rightarrow q_7^*$$

$$\delta'(q_6, 0) = \{E, F\} \rightarrow q_8^*$$

$$\delta'(q_6, 1) = \{E, F, G, H, I\} \rightarrow q_6^*$$

$$\delta'(q_7, 0) = \{F\} \rightarrow q_1$$

$$\delta'(q_7, 1) = \{F, G, H, I\} \rightarrow q_7^*$$

$$\delta'(q_8, 0) = \{E, F\} \rightarrow q_8^*$$

$$\delta'(q_8, 1) = \{E, F, G\} \rightarrow q_9^*$$

$$\delta'(q_9, 0) = \{E, F\} \rightarrow q_8^*$$

$$\delta'(q_9, 1) = \{E, F, G, H\} \rightarrow q_{10}^*$$

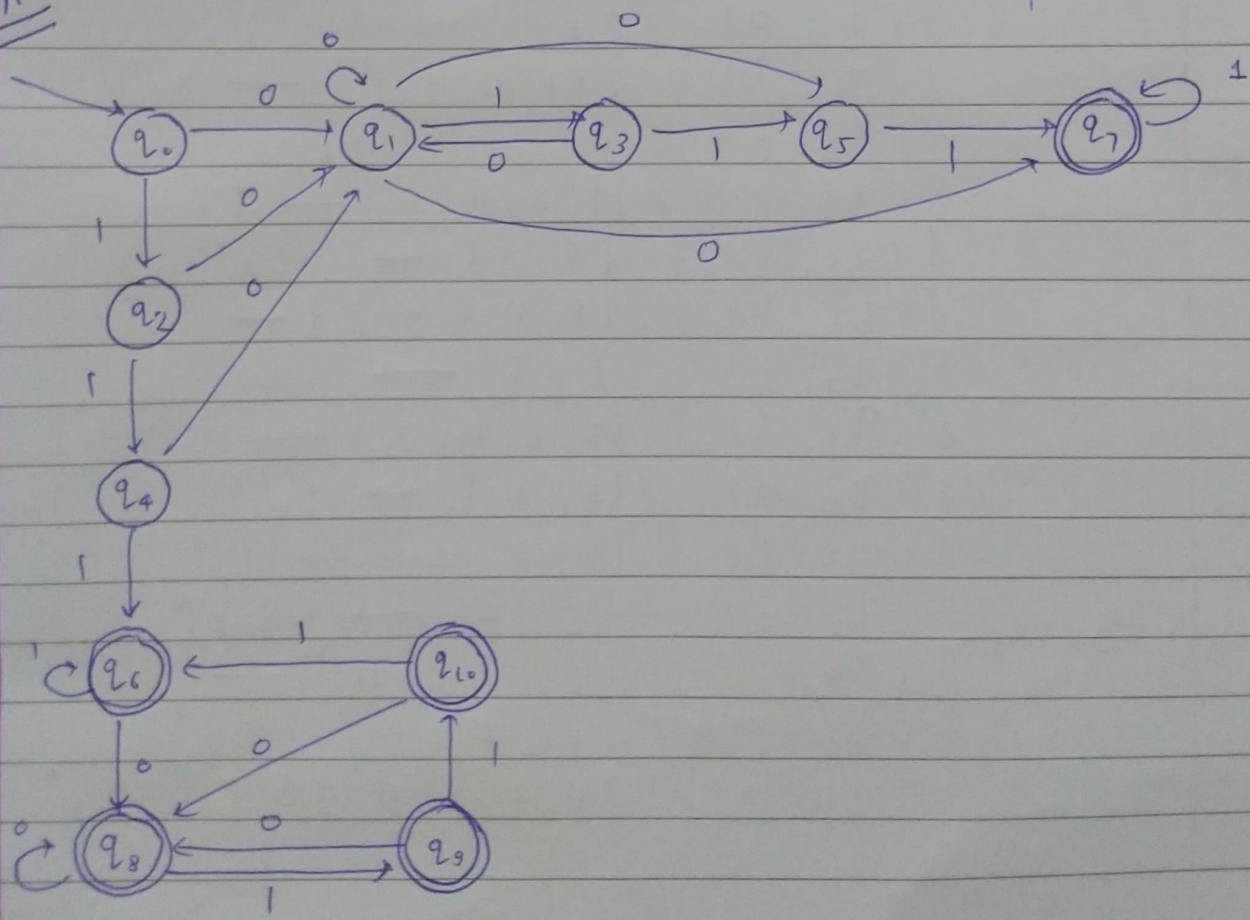
$$\delta'(q_{10}, 0) = \{E, F\} \rightarrow q_8^*$$

$$\delta'(q_{10}, 1) = \{E, F, G, H, I\} \rightarrow q_6^*$$

Transition table:

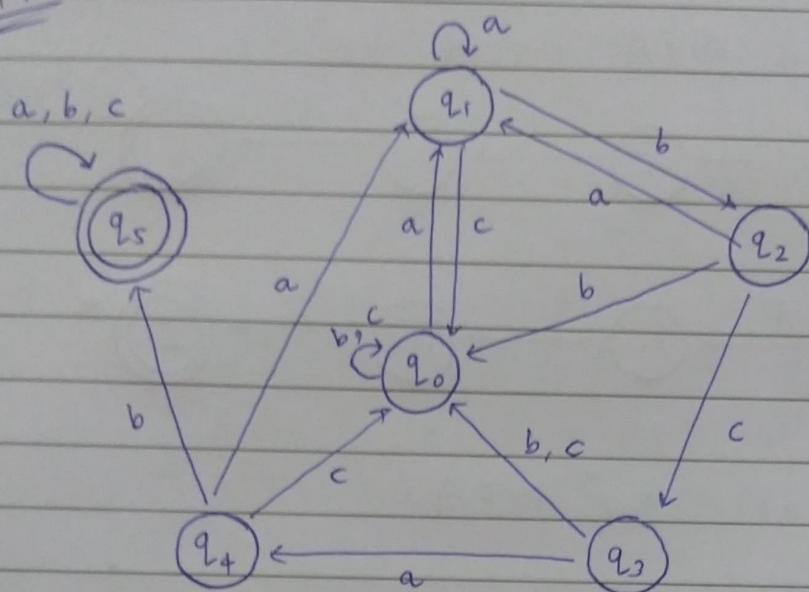
δ'	0	1
q_0	q_1	q_2
q_1	q_1	q_3
q_2	q_1	q_4
q_3	q_1	q_5
q_4	q_1	q_6^*
q_5	q_1	q_7^*
q_6^*	q_8^*	q_6^*
q_7^*	q_1	q_7^*
q_8^*	q_8^*	q_9^*
q_9	q_8^*	q_{10}^*
q_{10}^*	q_8^*	q_6^*

DFA



- 2) Create a DFA that accepts all strings having substring "abcaab".

DFA



$$Q = \{q_0, q_1, q_2, q_3, q_4, q_5\}$$

$$q_0 = \{q_0\} \quad F = \{q_5\}$$

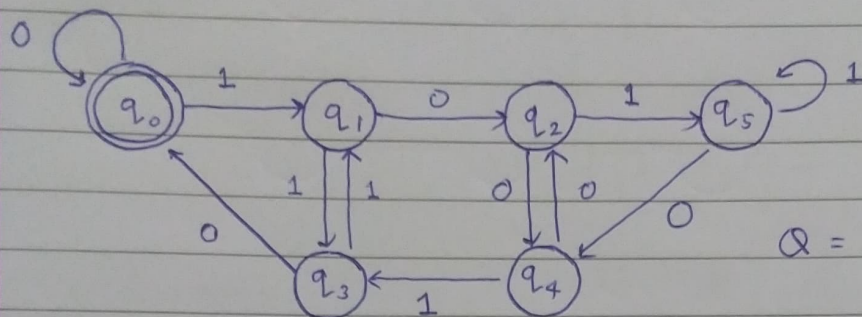
$$\Sigma = \{a, b, c\}$$

Transition table :-

States	a	b	c
q_0	q_1	q_0	q_0
q_1	q_1	q_2	q_0
q_2	q_1	q_0	q_3
q_3	q_4	q_0	q_0
q_4	q_1	q_5	q_0
q_5	q_5	q_5	q_5

3) Create a DFA that accepts all binary strings whose value divide by 5.

→ Consider states $q_0, q_1, q_2, q_3, q_4, q_5$ each representing a remainder after division by 5 respectively.



$$Q = \{q_0, q_1, q_2, q_3, q_4, q_5\}$$

$$\Sigma = \{0, 1\}$$

$$q_0 = \{q_0\}, F = \{q_0\}$$

Transition table:

States	0	1
q_0	q_0	q_1
q_1	q_2	q_3
q_2	q_3	q_4
q_3	q_0	q_1
q_4	q_2	q_3
q_5	q_0	q_5