

# Gate Assignment

EE:1205 Signals and Systems  
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**Question:** A Spectrometer is used to detect plasma oscillations in a sample. The spectrometer can work in the range of  $3 \times 10^{12} \text{ rad s}^{-1}$  to  $30 \times 10^{12} \text{ rad s}^{-1}$ . The minimum carrier concentration that can be detected by using this spectrometer is  $n \times 10^{21} \text{ m}^{-3}$ . The value of  $n$  is \_\_\_\_\_. (Round off to two places)

(Charge on electron =  $-1.6 \times 10^{-19} \text{ C}^{-1}$ , mass of electron =  $9.1 \times 10^{-31} \text{ kg}$  and  $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^{-2}$ ) (GATE PH 35 2022)

**Solution:**

Parameter	Value	Description
$\omega_{p1}$	$3 \times 10^{12} \text{ rad s}^{-1}$	Lower bound of plasma frequency
$\omega_{p2}$	$30 \times 10^{12} \text{ rad s}^{-1}$	Upper bound of plasma frequency
$\Delta\omega_p = \omega_{p2} - \omega_{p1}$	$27 \times 10^{12} \text{ rad s}^{-1}$	Plasma Frequency
$n_0$	$n \times 10^{21}$	Minimum carrier concentration
$e$	$-1.6 \times 10^{-19}$	Charge on electron
$m$	$9.1 \times 10^{-31}$	Mass of electron

TABLE 1  
PARAMETER TABLE

$$\Delta\omega_p = \sqrt{\frac{n_0 e^2}{m \epsilon_0}} \quad (1)$$

$$\Rightarrow n_0 = \frac{(\Delta\omega_p)^2 m \epsilon_0}{e^2} \quad (2)$$

$$n_0 = \frac{(27 \times 10^{12})^2 \times (9.1 \times 10^{-31}) \times (8.85 \times 10^{-12})}{(-1.6 \times 10^{-19})^2} \quad (3)$$

$$\therefore n_0 = 2.83 \times 10^{21} \text{ m}^{-3} \quad (4)$$

$$n = n_0 \times 10^{-21} \quad (5)$$

$$\therefore n = 2.83 \quad (6)$$

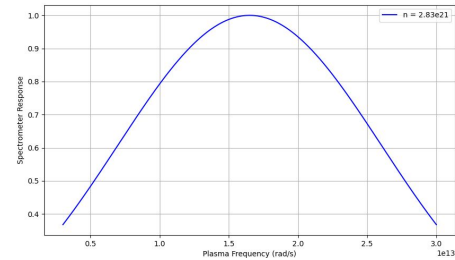


Fig. 1. Plot of Spectrometer response vs Plasma frequency