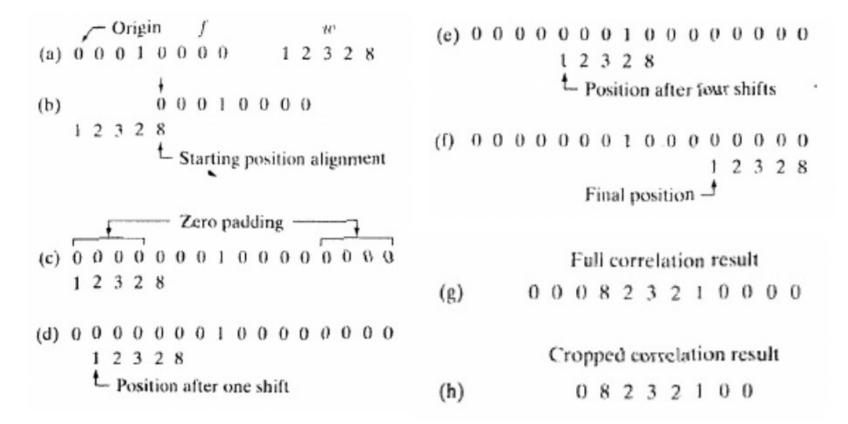
Digital Signal Analysis and Applications Lecture5: Convolution + Correlation + Stats

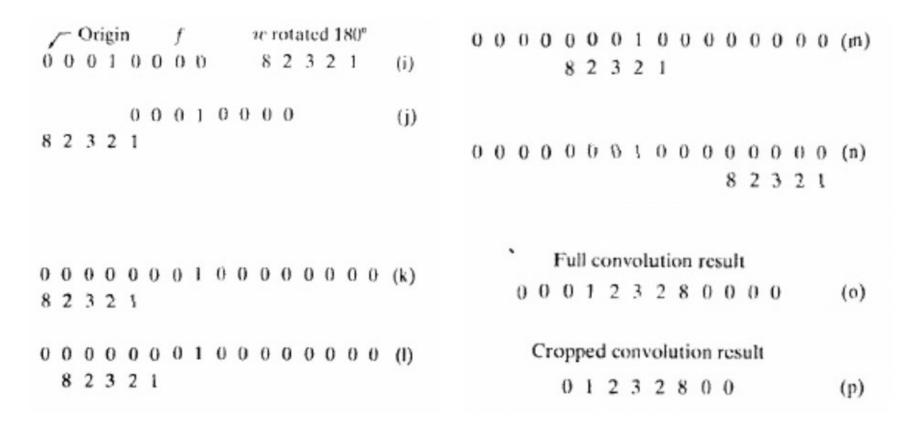
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Correlation



Convolution



Convolution vs Correlation (2D)

| | | | | | | | | | | P () | | 0 | () | | 0 | 0 | 0 | 0 | | | | | | | FIGURE 3.30 Correlation (middle row) and |
|-----------|----|----|------|-----|------------|-----|---------------------------|----|------|---------|------|------|------|-----|----|----------------------------|----|----|----|-----|-----|------|------|----------------|--|
| | | | | | | | | | | () | 0 | 0 | 0 | () | () | () | () | 0 | | | | | | | convolution (last |
| e e | , | _ | Ori | gin | f | (x, | y) | | | U | 0 | 0 | () | 0 | 0 | () | 0 | 0 | | | | | | | row) of a 2-D |
| | () | () | 0 | () | () | | | | | () | 0 | 0 | () | 1 | 0 | () | 0 | 0 | | | | | | | filter with a 2-D |
| | 0 | 0 | | 0 | 0 | | | | y) | 0 | - 7 | 0 | 0 | 0 | 0 | () | 0 | 0 | | | | | | | discrete, unit |
| | 0 | 0 | - 5 | 0 | | | 1 | - | 7.0 | 0 | - 80 | 0 | 0 | 0 | 0 | () | 0 | 0 | | | | | | | impulse. The 0s |
| | 0 | 0 | 0 | 0 | | | 4 | | | .0 | | 0 | 0 | 0 | 0 | () | 0 | 0 | | | | | | | are shown in gray |
| | () | 0 | 0 | 0 | | | 7 | 8 | 9 | 0 | () | 0 | 0 | (b) | | 0 | 0 | 0 | | | | | | | to simplify visual analysis. |
| | _ | _ | Init | iei | (a) pos | | n f | or | ert. | E | ull | corr | rela | | | enl | | | C | ror | mer | d co |) PT | elation result | analysis. |
| | 11 | | -31 | | • | | | | 0 | 0 | | 0 | () | () | | 0 | | 0 | 0 | 200 | - | | | | |
| | 4 | 5 | - 31 | 0 | | 0 | | | 0 | 0 | | 0 | 0 | 0 | | 0 | | 0 | Ü | 9 | | | 0 | | |
| | 17 | 8 | 9 | | 0 | 0 | 0 | 0 | 0 | 0 | | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 6 | 5 | 4 | 0 | | |
| | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | 0 | 9 | 8 | 7 | 0 | 0 | 0 | 0 | 3 | 2 | 1 | 0 | | |
| | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 6 | 5 | 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | |
| | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 8 | 3 | 2 | 1 | 0 | 0 | () | | | | | | | |
| | 0 | () | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | () | 0 | 0 | 0 | () | () | 0 | | | | | | | |
| | 0 | () | 0 | 0 | () | 0 | 0 | () | () | 0 | | 0 | 0 | () | () | 0 | 0 | 0 | | | | | | | |
| | 0 | 0 | 0 | 0 | 0 | () | () | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | 0 | 0 | 0 | | | | | | | |
| | | | | | (c) | | | | | | | | | (d) | | | | | | | (e) | | | | |
| Rotated w | | | | | | F | Full convolution result · | | | | | | | | C | Cropped convolution result | | | | | | | | | |
| | 19 | 8 | 7! | 0 | 0 | () | 0 | () | 0 | () | 0 | 0 | 0 | 0 | 0 | 0 | 0 | () | () | 0 | 0 | 0 | U | | |
| | 16 | 5 | 4 | () | 0 | 0 | () | () | 0 | () | 0 | 0 | 0 | 0 | 0 | 0 | () | 0 | 0 | 1 | 2 | 3 | () | | |
| | 3_ | 2. | 1 | () | 0 | 0 | () | () | 0 | 0 | | () | 0 | 0 | | 0 | () | () | () | 4 | 5 | 6 | | | |
| | | 0 | | () | () | 0 | 0 | 0 | 0 | 0 | | () | 1 | 2 | - | 1) | () | () | 0 | 7 | 8 | - | () | | |
| | 0 | 0 | 0 | 0 | 1 | 0 | () | 0 | 0 | () | 10.0 | () | 4 | 5 | _ | - | () | 0 | () | 0 | 0 | 0 | 0 | | |
| | 0 | 0 | 0 | 0 | 0 | () | | | 0 | 0 | | 0 | 7 | 8 | 9 | (1 | () | 0 | | | | | | | |
| | | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 5.5 | () | 0 | 0 | | 33 | 0 | () | | | | | | | |
| | 0 | 0 | 0 | 0 | 0 | 47 | 0 | 0 | 0 | 0 | () | () | () | 0 | - | | | 0 | | | | | | | |
| | 0 | 0 | 0 | 0 | | () | () | () | U | 0 | 0 | U | | | () | 0 | 1) | 0 | | | (h) | | | | |
| | | | | | (f) | | | | | | | | | (g) | | | | | | | (h) | | | | |

Convolution (2D)

$$w(x,y) \bigstar f(x,y) = \sum_{s=-a}^{a} \sum_{t=-b}^{b} w(s,t) f(x-s,y-t)$$

- Evaluated for all values of displacement variables x and y
- Filter size m × n (notational convenience → m, n are assumed odd)
- a = (m-1)/2 and b = (n-1)/2

Averaging

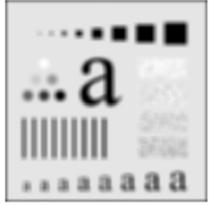






| 4 | 1 | 1 | 1 |
|---------------|---|---|---|
| $\frac{1}{0}$ | 1 | 1 | 1 |
| Э | 1 | 1 | 1 |

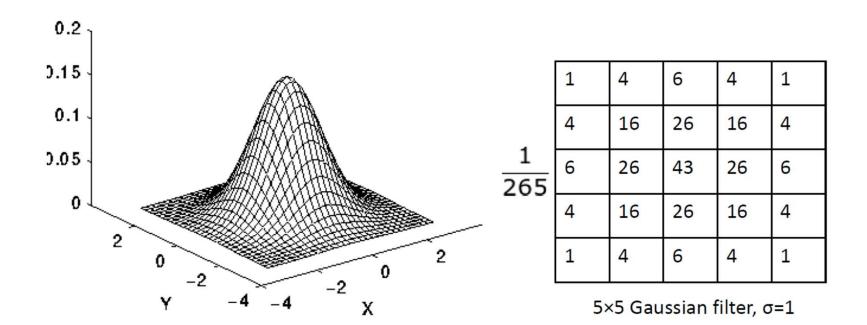






Square averaging filter mask size: 3,5,9,15,35

Averaging



Averaging

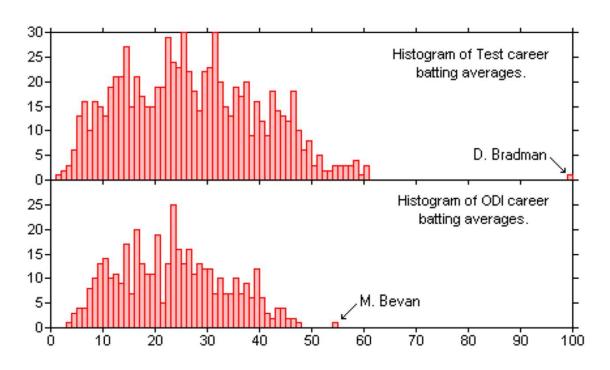








 5×5 Gaussian filter, σ =3



Courtesy: wikipedia

