

Product_Sales_Forecasting

December 23, 2025

1 Product Sales Forecasting

Project Objective

Need and Use of Product Sales Forecasting Effective sales forecasting is fundamental for multiple aspects of retail management and operation, including:

1. **Inventory Management:** Accurate sales forecasts help ensure that stores maintain optimal inventory levels—enough to meet customer demand without overstocking, which can lead to increased costs or waste, especially in the case of perishable goods.
2. **Financial Planning:** Forecasting sales allows businesses to estimate future revenue and manage budgets more effectively. This is crucial for allocating resources to areas such as marketing, staffing, and capital investments.
3. **Marketing and Promotions:** Understanding when sales peaks and troughs are likely to occur enables retailers to plan effective marketing campaigns and promotional offers to boost revenue or manage customer flow.
4. **Supply Chain Optimization:** Sales forecasts inform production schedules, logistics, and distribution plans, ensuring that products are available where and when they are needed, thereby reducing transportation and storage costs.
5. **Strategic Decision Making:** Long-term sales forecasting supports broader business strategies, including store expansions, market entry, and other capital expenditures.

1.1 1. Dataset Loading

```
[3]: # Import Basic libraries
import pandas as pd
import numpy as np

# Import Visualization libraries
import plotly.graph_objs as go
import plotly.express as px
import plotly.io as pio
from plotly.subplots import make_subplots
import matplotlib.pyplot as plt
import seaborn as sns
import warnings
warnings.filterwarnings('ignore')
```

```

# Install MLflow
!pip install mlflow

# Import MLFlow libraries
import mlflow

# Suppress the specific ConvergenceWarning
from statsmodels.tools.sm_exceptions import ConvergenceWarning
warnings.simplefilter("ignore", ConvergenceWarning)

```

```

Collecting mlflow
  Downloading mlflow-3.8.0-py3-none-any.whl.metadata (31 kB)
Collecting mlflow-skinny==3.8.0 (from mlflow)
  Downloading mlflow_skinny-3.8.0-py3-none-any.whl.metadata (31 kB)
Collecting mlflow-tracing==3.8.0 (from mlflow)
  Downloading mlflow_tracing-3.8.0-py3-none-any.whl.metadata (19 kB)
Collecting Flask-CORS<7 (from mlflow)
  Downloading flask_cors-6.0.2-py3-none-any.whl.metadata (5.3 kB)
Requirement already satisfied: Flask<4 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (3.1.2)
Requirement already satisfied: alembic!=1.10.0,<2 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (1.17.2)
Requirement already satisfied: cryptography<47,>=43.0.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (43.0.3)
Collecting docker<8,>=4.0.0 (from mlflow)
  Downloading docker-7.1.0-py3-none-any.whl.metadata (3.8 kB)
Collecting graphene<4 (from mlflow)
  Downloading graphene-3.4.3-py2.py3-none-any.whl.metadata (6.9 kB)
Collecting gunicorn<24 (from mlflow)
  Downloading gunicorn-23.0.0-py3-none-any.whl.metadata (4.4 kB)
Collecting huey<3,>=2.5.0 (from mlflow)
  Downloading huey-2.5.5-py3-none-any.whl.metadata (4.8 kB)
Requirement already satisfied: matplotlib<4 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (3.10.0)
Requirement already satisfied: numpy<3 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (2.0.2)
Requirement already satisfied: pandas<3 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (2.2.2)
Requirement already satisfied: pyarrow<23,>=4.0.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (18.1.0)
Requirement already satisfied: scikit-learn<2 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (1.6.1)
Requirement already satisfied: scipy<2 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (1.16.3)
Requirement already satisfied: sqlalchemy<3,>=1.4.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (2.0.45)

```

Requirement already satisfied: cachetools<7,>=5.0.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (6.2.4)

Requirement already satisfied: click<9,>=7.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (8.3.1)

Requirement already satisfied: cloudpickle<4 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (3.1.2)

Collecting databricks-sdk<1,>=0.20.0 (from mlflow-skinny==3.8.0->mlflow)
 Downloading databricks_sdk-0.76.0-py3-none-any.whl.metadata (40 kB)
 40.1/40.1 kB

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Requirement already satisfied: fastapi<1 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (0.123.10)

Requirement already satisfied: gitpython<4,>=3.1.9 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (3.1.45)

Requirement already satisfied: importlib_metadata!=4.7.0,<9,>=3.7.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (8.7.0)

Requirement already satisfied: opentelemetry-api<3,>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.37.0)

Requirement already satisfied: opentelemetry-proto<3,>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.37.0)

Requirement already satisfied: opentelemetry-sdk<3,>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.37.0)

Requirement already satisfied: packaging<26 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (25.0)

Requirement already satisfied: protobuf<7,>=3.12.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (5.29.5)

Requirement already satisfied: pydantic<3,>=2.0.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (2.12.3)

Requirement already satisfied: python-dotenv<2,>=0.19.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.2.1)

Requirement already satisfied: pyyaml<7,>=5.1 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (6.0.3)

Requirement already satisfied: requests<3,>=2.17.3 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (2.32.4)

Requirement already satisfied: sqlparse<1,>=0.4.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (0.5.4)

Requirement already satisfied: typing-extensions<5,>=4.0.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (4.15.0)

Requirement already satisfied: uvicorn<1 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (0.38.0)

Requirement already satisfied: Mako in /usr/local/lib/python3.12/dist-packages (from alembic!=1.10.0,<2->mlflow) (1.3.10)

Requirement already satisfied: cffi>=1.12 in /usr/local/lib/python3.12/dist-packages (from cryptography<47,>=43.0.0->mlflow) (2.0.0)

Requirement already satisfied: urllib3>=1.26.0 in /usr/local/lib/python3.12/dist-packages (from docker<8,>=4.0.0->mlflow) (2.5.0)

Requirement already satisfied: blinker>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (1.9.0)

Requirement already satisfied: itsdangerous>=2.2.0 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (2.2.0)

Requirement already satisfied: jinja2>=3.1.2 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (3.1.6)

Requirement already satisfied: markupsafe>=2.1.1 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (3.0.3)

Requirement already satisfied: werkzeug>=3.1.0 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (3.1.4)

Collecting graphql-core<3.3,>=3.1 (from graphene<4->mlflow)

 Downloading graphql_core-3.2.7-py3-none-any.whl.metadata (11 kB)

Collecting graphql-relay<3.3,>=3.1 (from graphene<4->mlflow)

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Requirement already satisfied: python-dateutil<3,>=2.7.0 in /usr/local/lib/python3.12/dist-packages (from graphene<4->mlflow) (2.9.0.post0)

Requirement already satisfied: contourpy>=1.0.1 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (1.3.3)

Requirement already satisfied: cycler>=0.10 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (0.12.1)

Requirement already satisfied: fonttools>=4.22.0 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (4.61.1)

Requirement already satisfied: kiwisolver>=1.3.1 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (1.4.9)

Requirement already satisfied: pillow>=8 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (11.3.0)

Requirement already satisfied: pyparsing>=2.3.1 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (3.2.5)

Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.12/dist-packages (from pandas<3->mlflow) (2025.2)

Requirement already satisfied: tzdata>=2022.7 in /usr/local/lib/python3.12/dist-packages (from pandas<3->mlflow) (2025.3)

Requirement already satisfied: joblib>=1.2.0 in /usr/local/lib/python3.12/dist-packages (from scikit-learn<2->mlflow) (1.5.3)

Requirement already satisfied: threadpoolctl>=3.1.0 in /usr/local/lib/python3.12/dist-packages (from scikit-learn<2->mlflow) (3.6.0)

Requirement already satisfied: greenlet>=1 in /usr/local/lib/python3.12/dist-

packages (from sqlalchemy<3,>=1.4.0->mlflow) (3.3.0)
 Requirement already satisfied: pycparser in /usr/local/lib/python3.12/dist-packages (from cffi>=1.12->cryptography<47,>=43.0.0->mlflow) (2.23)
 Requirement already satisfied: google-auth~=2.0 in /usr/local/lib/python3.12/dist-packages (from databricks-sdk<1,>=0.20.0->mlflow-skinny==3.8.0->mlflow) (2.43.0)
 Requirement already satisfied: starlette<0.51.0,>=0.40.0 in /usr/local/lib/python3.12/dist-packages (from fastapi<1->mlflow-skinny==3.8.0->mlflow) (0.50.0)
 Requirement already satisfied: annotated-doc>=0.0.2 in /usr/local/lib/python3.12/dist-packages (from fastapi<1->mlflow-skinny==3.8.0->mlflow) (0.0.4)
 Requirement already satisfied: gitdb<5,>=4.0.1 in /usr/local/lib/python3.12/dist-packages (from gitpython<4,>=3.1.9->mlflow-skinny==3.8.0->mlflow) (4.0.12)
 Requirement already satisfied: zipp>=3.20 in /usr/local/lib/python3.12/dist-packages (from importlib_metadata!=4.7.0,<9,>=3.7.0->mlflow-skinny==3.8.0->mlflow) (3.23.0)
 Requirement already satisfied: opentelemetry-semantic-conventions==0.58b0 in /usr/local/lib/python3.12/dist-packages (from opentelemetry-sdk<3,>=1.9.0->mlflow-skinny==3.8.0->mlflow) (0.58b0)
 Requirement already satisfied: annotated-types>=0.6.0 in /usr/local/lib/python3.12/dist-packages (from pydantic<3,>=2.0.0->mlflow-skinny==3.8.0->mlflow) (0.7.0)
 Requirement already satisfied: pydantic-core==2.41.4 in /usr/local/lib/python3.12/dist-packages (from pydantic<3,>=2.0.0->mlflow-skinny==3.8.0->mlflow) (2.41.4)
 Requirement already satisfied: typing-inspection>=0.4.2 in /usr/local/lib/python3.12/dist-packages (from pydantic<3,>=2.0.0->mlflow-skinny==3.8.0->mlflow) (0.4.2)
 Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.12/dist-packages (from python-dateutil<3,>=2.7.0->graphene<4->mlflow) (1.17.0)
 Requirement already satisfied: charset_normalizer<4,>=2 in /usr/local/lib/python3.12/dist-packages (from requests<3,>=2.17.3->mlflow-skinny==3.8.0->mlflow) (3.4.4)
 Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.12/dist-packages (from requests<3,>=2.17.3->mlflow-skinny==3.8.0->mlflow) (3.11)
 Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/python3.12/dist-packages (from requests<3,>=2.17.3->mlflow-skinny==3.8.0->mlflow) (2025.11.12)
 Requirement already satisfied: h11>=0.8 in /usr/local/lib/python3.12/dist-packages (from uvicorn<1->mlflow-skinny==3.8.0->mlflow) (0.16.0)
 Requirement already satisfied: smmap<6,>=3.0.1 in /usr/local/lib/python3.12/dist-packages (from gitdb<5,>=4.0.1->gitpython<4,>=3.1.9->mlflow-skinny==3.8.0->mlflow) (5.0.2)
 Requirement already satisfied: pyasn1-modules>=0.2.1 in /usr/local/lib/python3.12/dist-packages (from google-auth~=2.0->databricks-sdk<1,>=0.20.0->mlflow-skinny==3.8.0->mlflow) (0.4.2)

Requirement already satisfied: rsa<5,>=3.1.4 in /usr/local/lib/python3.12/dist-packages (from google-auth~=2.0->databricks-sdk<1,>=0.20.0->mlflow-skinny==3.8.0->mlflow) (4.9.1)

Requirement already satisfied: anyio<5,>=3.6.2 in /usr/local/lib/python3.12/dist-packages (from starlette<0.51.0,>=0.40.0->fastapi<1->mlflow-skinny==3.8.0->mlflow) (4.12.0)

Requirement already satisfied: pyasn1<0.7.0,>=0.6.1 in /usr/local/lib/python3.12/dist-packages (from pyasn1-modules>=0.2.1->google-auth~=2.0->databricks-sdk<1,>=0.20.0->mlflow-skinny==3.8.0->mlflow) (0.6.1)

Downloading mlflow-3.8.0-py3-none-any.whl (9.1 MB)

9.1/9.1 MB

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Downloading mlflow_skinny-3.8.0-py3-none-any.whl (2.5 MB)

2.5/2.5 MB

122.3 MB/s eta 0:00:00

Downloading mlflow_tracing-3.8.0-py3-none-any.whl (1.4 MB)

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Downloading docker-7.1.0-py3-none-any.whl (147 kB)

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14.9 MB/s eta 0:00:00

Downloading flask_cors-6.0.2-py3-none-any.whl (13 kB)

Downloading graphene-3.4.3-py2.py3-none-any.whl (114 kB)

114.9/114.9 kB

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Downloading gunicorn-23.0.0-py3-none-any.whl (85 kB)

85.0/85.0 kB

8.4 MB/s eta 0:00:00

Downloading huey-2.5.5-py3-none-any.whl (76 kB)

76.9/76.9 kB

7.3 MB/s eta 0:00:00

Downloading databricks_sdk-0.76.0-py3-none-any.whl (774 kB)

774.7/774.7 kB

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Downloading graphql_core-3.2.7-py3-none-any.whl (207 kB)

207.3/207.3 kB

19.3 MB/s eta 0:00:00

Downloading graphql_relay-3.2.0-py3-none-any.whl (16 kB)

Installing collected packages: huey, gunicorn, graphql-core, graphql-relay, docker, graphene, Flask-CORS, databricks-sdk, mlflow-tracing, mlflow-skinny, mlflow

Successfully installed Flask-CORS-6.0.2 databricks-sdk-0.76.0 docker-7.1.0 graphene-3.4.3 graphql-core-3.2.7 graphql-relay-3.2.0 gunicorn-23.0.0 huey-2.5.5 mlflow-3.8.0 mlflow-skinny-3.8.0 mlflow-tracing-3.8.0

```
[4]: # Read
train = pd.read_csv('/content/TRAIN.csv')
```

```
test = pd.read_csv('/content/TEST.csv')
```

```
[5]: train.sample(5)
```

```
[5]:
```

	ID	Store_id	Store_Type	Location_Type	Region_Code	Date	\
46883	T1046884	71	S2	L5	R1	2018-05-09	
62624	T1062625	134	S1	L4	R1	2018-06-21	
139396	T1139397	192	S1	L1	R3	2019-01-17	
88778	T1088779	31	S1	L5	R2	2018-09-01	
158244	T1158245	275	S4	L1	R1	2019-03-10	

	Holiday	Discount	#Order	Sales
46883	1	No	26	16903.08
62624	0	Yes	59	41364.00
139396	0	Yes	65	45756.00
88778	0	Yes	63	33240.00
158244	0	Yes	103	60051.00

```
[6]: test.sample(5)
```

```
[6]:
```

	ID	Store_id	Store_Type	Location_Type	Region_Code	Date	\
12131	T1200472	238	S1	L1	R2	2019-07-04	
14568	T1202909	159	S2	L1	R3	2019-07-10	
5793	T1194134	337	S4	L2	R1	2019-06-16	
16307	T1204648	159	S2	L1	R3	2019-07-15	
20526	T1208867	72	S1	L2	R3	2019-07-27	

	Holiday	Discount
12131	1	Yes
14568	0	Yes
5793	0	No
16307	0	No
20526	0	No

1.2 2. Observations on Data

```
[7]: train.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 188340 entries, 0 to 188339
Data columns (total 10 columns):
#   Column          Non-Null Count  Dtype
---  -
0   ID              188340 non-null object
1   Store_id        188340 non-null int64
2   Store_Type      188340 non-null object
3   Location_Type   188340 non-null object
```

```

4   Region_Code    188340 non-null  object
5   Date           188340 non-null  object
6   Holiday        188340 non-null  int64
7   Discount       188340 non-null  object
8   #Order         188340 non-null  int64
9   Sales          188340 non-null  float64
dtypes: float64(1), int64(3), object(6)
memory usage: 14.4+ MB

```

```
[8]: test.info()
```

```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 22265 entries, 0 to 22264
Data columns (total 8 columns):
#   Column          Non-Null Count  Dtype
---  ---
0   ID              22265 non-null  object
1   Store_id        22265 non-null  int64
2   Store_Type      22265 non-null  object
3   Location_Type   22265 non-null  object
4   Region_Code     22265 non-null  object
5   Date            22265 non-null  object
6   Holiday         22265 non-null  int64
7   Discount        22265 non-null  object
dtypes: int64(2), object(6)
memory usage: 1.4+ MB

```

```
[9]: train.Date = pd.to_datetime(train.Date)
test.Date = pd.to_datetime(test.Date)
```

```
[10]: train.describe().T
```

```
[10]:
```

	count		mean		min \
Store_id	188340.0		183.0		1.0
Date	188340	2018-09-15 12:00:00	0.000000256	2018-01-01 00:00:00	
Holiday	188340.0		0.131783		0.0
#Order	188340.0		68.205692		0.0
Sales	188340.0		42784.327982		0.0

	25%		50%		75% \
Store_id	92.0		183.0		274.0
Date	2018-05-09 18:00:00	2018-09-15 12:00:00		2019-01-22 06:00:00	
Holiday	0.0		0.0		0.0
#Order	48.0		63.0		82.0
Sales	30426.0		39678.0		51909.0

	max		std
--	-----	--	-----

Store_id	365.0	105.366308
Date	2019-05-31 00:00:00	NaN
Holiday	1.0	0.338256
#Order	371.0	30.467415
Sales	247215.0	18456.708302

```
[11]: test.describe().T
```

```
[11]:
```

	count		mean		min \
Store_id	22265.0		183.0		1.0
Date	22265	2019-06-30 23:59:59.999999744		2019-06-01 00:00:00	
Holiday	22265.0		0.032787		0.0

	25%		50%		75% \
Store_id	92.0		183.0		274.0
Date	2019-06-16 00:00:00		2019-07-01 00:00:00		2019-07-16 00:00:00
Holiday	0.0		0.0		0.0

	max		std
Store_id	365.0		105.368395
Date	2019-07-31 00:00:00		NaN
Holiday	1.0		0.178082

1.3 3. Handling missing values and Preprocessing

```
[12]: train_null = train.isna().sum().sum()
test_null = test.isna().sum().sum()
print(f'There are {train_null} nulls in train dataset and {test_null} nulls in_
↳test dataset.')
```

There are 0 nulls in train dataset and 0 nulls in test dataset.

```
[13]: # Define dataset type in separate column for train and test
train['Train'] = True
test['Train'] = False
```

```
[14]: def decorator(func):
    def wrapper(*args, **kwargs):
        print('='*50)
        result = func(*args, **kwargs)
        print('='*50)
        return result
    return wrapper

@decorator
def df_size(df, typ):
    size = df.memory_usage().sum()/(1024**2)
```

```
print(f'Size of {typ} data is: {size:.2f} MB')
return size
```

```
[15]: # Combine both the dataset into single dataframe
data = pd.concat([train, test])
raw_size = df_size(data, 'Non-Converted')
data.reset_index(drop=True, inplace=True)
# Change Datatypes to optimize sizes
# Store_id as unsigned integer 16 (Range is 1 to 371)
data.Store_id = data.Store_id.astype('uint16')
# Store_Type, Location_Type, Region_Code as categorical
data.Store_Type = data.Store_Type.astype('category')
data.Location_Type = data.Location_Type.astype('category')
data.Region_Code = data.Region_Code.astype('category')
# Holiday and Discount as Boolean
data.Holiday = data.Holiday.astype('bool')
data.replace({'Discount':{'Yes':True, 'No':False}}, inplace=True)
# Drop unnecessary column Transaction ID
data.pop('ID')
data.set_index('Date', inplace=True)
processed_size = df_size(data, 'Converted')
reduction = 100*(raw_size - processed_size)/raw_size
print(f''Reduction in size after processing is: {reduction:.2f}%''')
print('='*50)
```

```
=====
Size of Non-Converted data is: 17.88 MB
=====
Size of Converted data is: 6.43 MB
=====
Reduction in size after processing is: 64.04%
=====
```

```
[16]: data.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 210605 entries, 2018-01-01 to 2019-07-31
Data columns (total 9 columns):
#   Column          Non-Null Count  Dtype
---  -
0   Store_id         210605 non-null  uint16
1   Store_Type       210605 non-null  category
2   Location_Type    210605 non-null  category
3   Region_Code      210605 non-null  category
4   Holiday          210605 non-null  bool
5   Discount         210605 non-null  bool
```

```

6   #Order          188340 non-null   float64
7   Sales           188340 non-null   float64
8   Train           210605 non-null    bool
dtypes: bool(3), category(3), float64(2), uint16(1)
memory usage: 6.4 MB

```

```
[17]: data.describe()
```

```

[17]:
count      Store_id      #Order      Sales
count  210605.000000  188340.000000  188340.000000
mean      183.000000    68.205692   42784.327982
std       105.366279    30.467415  18456.708302
min         1.000000     0.000000     0.000000
25%        92.000000    48.000000   30426.000000
50%       183.000000    63.000000   39678.000000
75%       274.000000    82.000000   51909.000000
max       365.000000   371.000000  247215.000000

```

```

[18]: # Rename #Order column name for ease of use
data.rename(columns={'#Order': 'Order'}, inplace=True)

```

```

[19]: # Assign index to Exogenous variable dataframe
exog_holiday = data.Holiday
exog_discount = data.Discount
exog = pd.concat([exog_holiday, exog_discount, data.Train], axis=1)
exog_train = exog[exog.Train == True][['Holiday', 'Discount']]
exog_test = exog[exog.Train == False][['Holiday', 'Discount']]

```

1.4 4. Feature Engineering

```

[20]: # Developing Features from date
data['Year'] = data.index.year
data['Quarter'] = data.index.quarter
data['Month'] = data.index.month
data['MonthName'] = data.index.month_name()
data['Day'] = data.index.day
data['Week'] = data.index.isocalendar().week
data['Weekday'] = data.index.weekday
data['DayName'] = data.index.day_name()
data['Weekend'] = data.Weekday.apply(lambda x: 'Weekend' if x in [
    5, 6] else 'Weekday')

```

```

[21]: # Additional features
data['S/O'] = round(data.Sales/data.Order, 2)

```

```
[22]: data.sample(5)
```

```
[22]:
```

	Store_id	Store_Type	Location_Type	Region_Code	Holiday	Discount	\
Date							
2019-06-23	332	S2	L5	R1	False	False	
2019-03-31	195	S4	L1	R1	False	False	
2018-12-20	56	S2	L5	R3	False	True	
2019-05-19	290	S1	L1	R3	False	False	
2019-06-19	238	S1	L1	R2	False	False	

	Order	Sales	Train	Year	Quarter	Month	MonthName	Day	Week	\
Date										
2019-06-23	NaN	NaN	False	2019	2	6	June	23	25	
2019-03-31	89.0	44193.0	True	2019	1	3	March	31	13	
2018-12-20	46.0	34593.0	True	2018	4	12	December	20	51	
2019-05-19	45.0	31848.0	True	2019	2	5	May	19	20	
2019-06-19	NaN	NaN	False	2019	2	6	June	19	25	

	Weekday	DayName	Weekend	S/O
Date				
2019-06-23	6	Sunday	Weekday	NaN
2019-03-31	6	Sunday	Weekday	496.55
2018-12-20	3	Thursday	Weekday	752.02
2019-05-19	6	Sunday	Weekday	707.73
2019-06-19	2	Wednesday	Weekday	NaN

```
[23]: # Split the data into train and test before proceeding further
train = data[data.Train == True]
test = data[data.Train == False]
```

1.5 5. EDA

```
[24]: # **Univariate Analysis: Distribution of numerical data**
fig = make_subplots(rows=1, cols=3, subplot_titles=('Order', 'Sales', 'Sales per_
↳Order'))
fig.add_trace(go.Histogram(x=train.Order, marker_color='teal'), row=1, col=1)
fig.add_trace(go.Histogram(x=train.Sales, marker_color='orange'), row=1, col=2)
fig.add_trace(go.Histogram(x=train['S/O'], marker_color='purple'), row=1, col=3)
fig.update_layout(title='Distribution of target parameters', showlegend=False,
↳title_x=0.5, title_y=0.1)
fig.show()
```

```
[25]: # **Bivariate Analysis: Bar Charts**
order_color = 'darkgreen'
sales_color = 'teal'
fig = make_subplots(rows=2, cols=4)
grouped = train.groupby('Store_Type').agg({'Order': 'sum', 'Sales': 'sum'})
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Order,
↳marker=dict(color=order_color)), row=1, col=1)
```

```

fig.add_trace(go.Bar(x=grouped.index, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=1)
grouped = train.groupby('Location_Type').agg({'Order': 'sum', 'Sales': 'sum'})
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Order,
    ↪marker=dict(color=order_color)), row=1, col=2)
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=2)
grouped = train.groupby('Region_Code').agg({'Order': 'sum', 'Sales': 'sum'})
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Order,
    ↪marker=dict(color=order_color)), row=1, col=3)
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=3)
grouped = train.groupby(['Weekday', 'DayName']).agg({'Order': 'sum', 'Sales':
    ↪'sum'}).reset_index()
fig.add_trace(go.Bar(x=grouped.DayName, y=grouped.Order,
    ↪marker=dict(color=order_color)), row=1, col=4)
fig.add_trace(go.Bar(x=grouped.DayName, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=4)
fig.update_layout(title='Order, Sales and Sales/Order distribution',
    ↪showlegend=False, title_x=0.5, title_y=0.85)

fig.update_yaxes(title='Order Volume', row=1, col=1)
fig.update_yaxes(title='Sales Amount', row=2, col=1)

fig.update_xaxes(title='Store Type', row=2, col=1)
fig.update_xaxes(title='Location Type', row=2, col=2)
fig.update_xaxes(title='Region Code', row=2, col=3)

fig.show()

```

```

[26]: # **Top/Bottom 10s**
fig = make_subplots(rows=2, cols=1, subplot_titles=('Top/Bottom 10 Store IDs',
    ↪'))
top_order = train.groupby('Store_id').agg({'Order': 'sum'}).sort_values('Order',
    ↪ascending=False).head(10)
top_sales = train.groupby('Store_id').agg({'Sales': 'sum'}).sort_values('Sales',
    ↪ascending=False).head(10)
bottom_order = train.groupby('Store_id').agg({'Order': 'sum'}).
    ↪sort_values('Order', ascending=False).tail(10)
bottom_sales = train.groupby('Store_id').agg({'Sales': 'sum'}).
    ↪sort_values('Sales', ascending=False).tail(10)
tb_order = pd.concat([top_order, bottom_order])
tb_sales = pd.concat([top_sales, bottom_sales])
fig.add_trace(go.Bar(x=tb_order.index, y=tb_order.Order, name='Order',
    ↪marker=dict(color=order_color)), row=1, col=1)

```

```
fig.add_trace(go.Bar(x=tb_sales.index, y=tb_sales.Sales, name='Sales',
    ↪marker=dict(color=sales_color)), row=2, col=1)
fig.update_layout(xaxis=dict(type='category'),
    xaxis2=dict(type='category'),
    yaxis=dict(title='Order Volume'),
    yaxis2=dict(title='Sales Amount'),
    showlegend=False, width=500)
fig.show()
```

```
[27]: def scatter_plots(df, column):
    categories = df[column].astype('category').unique().sort_values()
    fig = make_subplots(rows=1, cols=len(categories),
        subplot_titles=[str(c) for c in categories])
    for i, category in enumerate(categories):
        fig.add_trace(go.Scatter(x=df[df[column] == category]['Order'],
            y=df[df[column] == category]['Sales'],
            mode='markers', marker=dict(size=2),
            ↪name=category, row=1, col=i+1)
        fig.update_xaxes(range = [0,300], row=1, col=i+1)
        fig.update_yaxes(range = [0,250000], row=1, col=i+1)
    fig.update_layout(title=f'{column} wise Order v/s Sales Scatter Plot', height=
    ↪400, showlegend=False, title_x=0.5)
    fig.show()
```

```
[28]: ignore = False
if not ignore:
    scatter_plots(train, 'Store_Type')
    scatter_plots(train, 'Region_Code')
    scatter_plots(train, 'Location_Type')
    scatter_plots(train, 'Holiday')
    scatter_plots(train, 'Discount')
```

1.5.1 Hypothesis Testing

```
[29]: # **Chi-Square test for dependency**
from scipy.stats import chi2_contingency

@decorator
def chi2test(data, category1, category2, alpha=0.05):
    data = data.groupby(by=[category1, category2]).agg({'Order':'sum', 'Sales':
    ↪'sum'}).reset_index()
    test = chi2_contingency(data.
    ↪pivot(index=category1, columns=category2, values='Order').fillna(0))
    order_dependency = test.pvalue < alpha
    if order_dependency:
```

```

    print(f'Reject the Null Hypothesis. For Order volume, {category1} and
    ↳{category2} are dependent', end=" | ")
    else:
        print(f'Fail to reject the Null Hypothesis. For Order volume, {category1}
    ↳and {category2} are independent', end=" | ")
    print(f'Test statistics:{test.statistic},\tp-value:{test.pvalue}')

    test = chi2_contingency(data.
    ↳pivot(index=category1,columns=category2,values='Sales').fillna(0))
    sales_dependency = test.pvalue < alpha
    if sales_dependency:
        print(f'Reject the Null Hypothesis. For Sales amount, {category1} and
    ↳{category2} are dependent', end=" | ")
    else:
        print(f'Fail to reject the Null Hypothesis. For Sales amount, {category1}
    ↳and {category2} are independent', end=" | ")
    print(f'Test statistics:{test.statistic},\tp-value:{test.pvalue}')

    return {'C1':category1, 'C2':category2,'Order': order_dependency, 'Sales':
    ↳sales_dependency}

```

```

[30]: from itertools import permutations
columns = ['Store_Type', 'Location_Type', 'Region_Code', 'Holiday', 'Discount',
    ↳'MonthName', 'DayName']
dependency_summary = pd.DataFrame([chi2test(train,c1,c2) for c1,c2 in
    ↳list(permutations(columns,2))])

```

```

=====
Reject the Null Hypothesis. For Order volume, Store_Type and Location_Type are
dependent | Test statistics:8560447.197307907,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, Store_Type and Location_Type are
dependent | Test statistics:5347008627.585614,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and Region_Code are
dependent | Test statistics:2063286.1134297573,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, Store_Type and Region_Code are
dependent | Test statistics:1263592484.9694943,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and Holiday are
dependent | Test statistics:27.94049935419796, p-value:3.7379941858049926e-06
Reject the Null Hypothesis. For Sales amount, Store_Type and Holiday are
dependent | Test statistics:21093.7298558246,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and Discount are

```

```

dependent | Test statistics:321.25338064274575,
p-value:2.497032993795113e-69
Reject the Null Hypothesis. For Sales amount, Store_Type and Discount are
dependent | Test statistics:329382.9310341213,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and MonthName are
dependent | Test statistics:767.6808790550784,
p-value:4.541885984630596e-140
Reject the Null Hypothesis. For Sales amount, Store_Type and MonthName are
dependent | Test statistics:554539.2424337461,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and DayName are
dependent | Test statistics:75.9649544550106,  p-value:4.312391037787697e-09
Reject the Null Hypothesis. For Sales amount, Store_Type and DayName are
dependent | Test statistics:52319.79147868339, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Store_Type are
dependent | Test statistics:8560447.197307909,  p-value:0.0
Reject the Null Hypothesis. For Sales amount, Location_Type and Store_Type are
dependent | Test statistics:5347008627.585613,  p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Region_Code are
dependent | Test statistics:373016.05851354415, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Location_Type and Region_Code are
dependent | Test statistics:228540888.13728154, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Holiday are
dependent | Test statistics:21.222613057623803,
p-value:0.00028605478639954726
Reject the Null Hypothesis. For Sales amount, Location_Type and Holiday are
dependent | Test statistics:21296.647804881504,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Discount are
dependent | Test statistics:1260.3760430857506,
p-value:1.2971148482759126e-271
Reject the Null Hypothesis. For Sales amount, Location_Type and Discount are
dependent | Test statistics:724101.2360874555,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and MonthName are
dependent | Test statistics:439.16646867455864,  p-value:1.3959817749676116e-66
Reject the Null Hypothesis. For Sales amount, Location_Type and MonthName are

```



```

dependent | Test statistics:307715.5842903906,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and DayName are
dependent | Test statistics:50.63707711934928,
p-value:0.0011740360390016633
Reject the Null Hypothesis. For Sales amount, Location_Type and DayName are
dependent | Test statistics:38344.05165385948,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and Store_Type are
dependent | Test statistics:2063286.1134297573,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, Region_Code and Store_Type are
dependent | Test statistics:1263592484.9694943,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and Location_Type are
dependent | Test statistics:373016.05851354403, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Region_Code and Location_Type are
dependent | Test statistics:228540888.13728154, p-value:0.0
=====
=====
Fail to reject the Null Hypothesis. For Order volume, Region_Code and Holiday
are independent | Test statistics:5.22312907474964,
p-value:0.15616892563963025
Reject the Null Hypothesis. For Sales amount, Region_Code and Holiday are
dependent | Test statistics:4415.458954381414,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and Discount are
dependent | Test statistics:726.5818658215513,
p-value:3.6135273295344166e-157
Reject the Null Hypothesis. For Sales amount, Region_Code and Discount are
dependent | Test statistics:567114.1191712606,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and MonthName are
dependent | Test statistics:852.9791229987399,
p-value:6.956453417684306e-158
Reject the Null Hypothesis. For Sales amount, Region_Code and MonthName are
dependent | Test statistics:669584.5488212734,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and DayName are
dependent | Test statistics:30.149954668791192,
p-value:0.03601386919680342
Reject the Null Hypothesis. For Sales amount, Region_Code and DayName are
dependent | Test statistics:29839.71437344468,    p-value:0.0

```

```

=====
=====
Reject the Null Hypothesis. For Order volume, Holiday and Store_Type are
dependent | Test statistics:27.94049935419796, p-value:3.7379941858049926e-06
Reject the Null Hypothesis. For Sales amount, Holiday and Store_Type are
dependent | Test statistics:21093.729855824597, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Holiday and Location_Type are
dependent | Test statistics:21.2226130576238,
p-value:0.0002860547863995476
Reject the Null Hypothesis. For Sales amount, Holiday and Location_Type are
dependent | Test statistics:21296.647804881504, p-value:0.0
=====
=====
Fail to reject the Null Hypothesis. For Order volume, Holiday and Region_Code
are independent | Test statistics:5.2231290747496395,
p-value:0.15616892563963033
Reject the Null Hypothesis. For Sales amount, Holiday and Region_Code are
dependent | Test statistics:4415.458954381414, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Holiday and Discount are dependent
| Test statistics:1531.4534101037711, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Holiday and Discount are dependent
| Test statistics:569983.2461383714, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Holiday and MonthName are
dependent | Test statistics:329278.4500446775, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Holiday and MonthName are
dependent | Test statistics:206015674.04294717, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Holiday and DayName are dependent
| Test statistics:70922.4490624049, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Holiday and DayName are dependent
| Test statistics:40319768.89511568, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and Store_Type are
dependent | Test statistics:321.2533806427457,
p-value:2.4970329937951835e-69
Reject the Null Hypothesis. For Sales amount, Discount and Store_Type are
dependent | Test statistics:329382.9310341213, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and Location_Type are

```

```

dependent | Test statistics:1260.3760430857506,
p-value:1.2971148482759126e-271
Reject the Null Hypothesis. For Sales amount, Discount and Location_Type are
dependent | Test statistics:724101.2360874556,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and Region_Code are
dependent | Test statistics:726.5818658215514,
p-value:3.61352732953421e-157
Reject the Null Hypothesis. For Sales amount, Discount and Region_Code are
dependent | Test statistics:567114.1191712606,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and Holiday are dependent
| Test statistics:1531.4534101037711,  p-value:0.0
Reject the Null Hypothesis. For Sales amount, Discount and Holiday are dependent
| Test statistics:569983.2461383714,  p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and MonthName are
dependent | Test statistics:97104.88049468104, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Discount and MonthName are
dependent | Test statistics:59894831.49811946, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and DayName are dependent
| Test statistics:14454.702562989041,  p-value:0.0
Reject the Null Hypothesis. For Sales amount, Discount and DayName are dependent
| Test statistics:9301326.292060012,  p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Store_Type are
dependent | Test statistics:767.6808790550785,
p-value:4.541885984630337e-140
Reject the Null Hypothesis. For Sales amount, MonthName and Store_Type are
dependent | Test statistics:554539.2424337475,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Location_Type are
dependent | Test statistics:439.1664686745586,  p-value:1.3959817749676514e-66
Reject the Null Hypothesis. For Sales amount, MonthName and Location_Type are
dependent | Test statistics:307715.5842903907,  p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Region_Code are
dependent | Test statistics:852.97912299874,
p-value:6.956453417683911e-158
Reject the Null Hypothesis. For Sales amount, MonthName and Region_Code are

```

```

dependent | Test statistics:669584.5488212737,      p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Holiday are
dependent | Test statistics:329278.4500446775,  p-value:0.0
Reject the Null Hypothesis. For Sales amount, MonthName and Holiday are
dependent | Test statistics:206015674.04294714, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Discount are
dependent | Test statistics:97104.88049468104, p-value:0.0
Reject the Null Hypothesis. For Sales amount, MonthName and Discount are
dependent | Test statistics:59894831.4981195,  p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and DayName are
dependent | Test statistics:115360.52602159233, p-value:0.0
Reject the Null Hypothesis. For Sales amount, MonthName and DayName are
dependent | Test statistics:77573972.75065999,  p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Store_Type are
dependent | Test statistics:75.96495445501058, p-value:4.312391037787728e-09
Reject the Null Hypothesis. For Sales amount, DayName and Store_Type are
dependent | Test statistics:52319.79147868339, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Location_Type are
dependent | Test statistics:50.637077119349286,
p-value:0.0011740360390016587
Reject the Null Hypothesis. For Sales amount, DayName and Location_Type are
dependent | Test statistics:38344.05165385942,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Region_Code are
dependent | Test statistics:30.149954668791196,
p-value:0.036013869196803355
Reject the Null Hypothesis. For Sales amount, DayName and Region_Code are
dependent | Test statistics:29839.71437344464,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Holiday are dependent
| Test statistics:70922.4490624049,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, DayName and Holiday are dependent
| Test statistics:40319768.89511567,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Discount are dependent

```

```
| Test statistics:14454.70256298904,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, DayName and Discount are dependent
| Test statistics:9301326.292059988,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and MonthName are
dependent | Test statistics:115360.52602159233, p-value:0.0
Reject the Null Hypothesis. For Sales amount, DayName and MonthName are
dependent | Test statistics:77573972.75065999,  p-value:0.0
=====
```

```
[31]: pd.crosstab(dependancy_summary.C1, dependancy_summary.C2, dependancy_summary.
      ↪Order, aggfunc='max')
```

```
[31]: C2          DayName Discount Holiday Location_Type MonthName Region_Code \
C1
DayName          NaN      True      True          True          True          True
Discount          True      NaN      True          True          True          True
Holiday           True      True      NaN          True          True          False
Location_Type     True      True      True          NaN          True          True
MonthName          True      True      True          True          NaN          True
Region_Code        True      True      False         True          True          NaN
Store_Type         True      True      True          True          True          True

C2          Store_Type
C1
DayName          True
Discount          True
Holiday           True
Location_Type     True
MonthName          True
Region_Code        True
Store_Type         NaN
```

```
[32]: pd.crosstab(dependancy_summary.C1, dependancy_summary.C2, dependancy_summary.
      ↪Sales, aggfunc='max').fillna(0)
```

```
[32]: C2          DayName Discount Holiday Location_Type MonthName Region_Code \
C1
DayName          0      True      True          True          True          True
Discount          True      0      True          True          True          True
Holiday           True      True      0          True          True          True
Location_Type     True      True      True          0          True          True
MonthName          True      True      True          True          0          True
Region_Code        True      True      True          True          True          0
Store_Type         True      True      True          True          True          True
```

C2	Store_Type
C1	
DayName	True
Discount	True
Holiday	True
Location_Type	True
MonthName	True
Region_Code	True
Store_Type	0

```
[33]: # **Mean similarity test**
from scipy.stats import f_oneway, kruskal, anderson, levene
from statsmodels.stats.multicomp import pairwise_tukeyhsd
from itertools import combinations

def decorator(func):
    def wrapper(*args, **kwargs):
        print('~'*100)
        print('~'*100)
        result = func(*args, **kwargs)
        print('~'*100)
        print('~'*100)
        return result
    return wrapper

@decorator
def variance_test(data, category, target, alpha=0.05):
    d = data.groupby(by=category).agg(Mean=(target, 'mean'), Count=(target, 'size')).reset_index()
    print(f'Hypothesis test whether Mean {target} is same for all {category} or not.\n')
    print(d)
    print('='*53)
    cats = sorted(data[category].unique())
    groups = {}
    for cat in cats:
        groups[cat]=data[data[category] == cat][target]

    # Check for Normality test of all categories
    normality_test = True
    print('Criteria check for ANOVA')
    for cat,group in groups.items():
        if not anderson(group).fit_result.success:
            normality_test = False
            print(f'\u033[31m \u274C Group {cat} is not normally distributed.\u033[0m')
            break
    if normality_test:
```

```

    print('\033[32m \u2705 All groups are normally distributed.\033[0m')
# Check for levene test
levene_test = True
_, p_levene = levene(*groups.values())
if p_levene < alpha:
    levene_test = False
    print(f'\033[31m \u274C Variance of all groups are not same.\033[0m')
else:
    print(f'\033[32m \u2705 Variance of all groups are same.\033[0m')

# Perform One-way ANOVA if criteria meets otheriwse perform Kruskal
if normality_test and levene_test:
    print('One-Way ANOVA will be performed.')
    _, p_value = f_oneway(*groups.values())
else:
    print('All criterias not met for ANOVA. Kruskal test will be performed.')
    _, p_value = kruskal(*groups.values())

# Proceed for ttest_ind if one group has different mean
if p_value > alpha:
    print(f'p-Value is {p_value} > {alpha} Significance level.\nWe dont have_
    ↪ enough evidence to reject the Null Hypothesis. All means are same.')
    print('='*53)
    return None
else:
    print(f'p-Value is {p_value} < {alpha} Significance level.\nWe have enough_
    ↪ evidence to reject the Null Hypothesis and at least one mean is different.')
    print('='*53)

tukey = pairwise_tukeyhsd(endog=data[target], groups=data[category], alpha=0.
    ↪ 05)
print(tukey)
# Extract group1 and group2 using the Tukey object attributes
group1 = tukey.groupsunique[tukey._multicomp.pairindices[0]]
group2 = tukey.groupsunique[tukey._multicomp.pairindices[1]]
pair = [f'{a}-{b}' for a,b in list(zip(group1, group2))]
reject = tukey.reject

# Combine group1 and group2 into a DataFrame
group_pairs = pd.DataFrame({'pair': pair, 'reject': reject})
same_mean_pairs = group_pairs[group_pairs['reject'] == False]['pair']
different_mean_pairs = group_pairs[group_pairs['reject'] == True]['pair']
print(f'\033[34m Pairs having different {target} mean are: {"",".
    ↪ join(different_mean_pairs.values)}')
print(f'\033[35m Pairs having same {target} mean are: {"",".
    ↪ join(same_mean_pairs.values)}\033[0m')

```

```
return None
```

```
[34]: from itertools import product
      for category, target in product(columns, ['Order', 'Sales']):
          variance_test(train, category, target)
```

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```

Hypothesis test whether Mean Order is same for all Store_Type or not.

	Store_Type	Mean	Count
0	S1	58.022095	88752
1	S2	40.472799	28896
2	S3	73.663396	24768
3	S4	102.392779	45924

```
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```

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

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Multiple Comparison of Means - Tukey HSD, FWER=0.05

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group1	group2	meandiff	p-adj	lower	upper	reject
S1	S2	-17.5493	0.0	-17.9275	-17.1711	True
S1	S3	15.6413	0.0	15.24	16.0426	True
S1	S4	44.3707	0.0	44.0497	44.6917	True
S2	S3	33.1906	0.0	32.707	33.6742	True
S2	S4	61.92	0.0	61.5007	62.3393	True
S3	S4	28.7294	0.0	28.2891	29.1696	True

```
-----
```

Pairs having different Order mean are: S1-S2,S1-S3,S1-S4,S2-S3,S2-S4,S3-S4

Pairs having same Order mean are:

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```


Hypothesis test whether Mean Sales is same for all Store_Type or not.

	Store_Type	Mean	Count
0	S1	37676.511694	88752
1	S2	27530.828222	28896
2	S3	47063.068209	24768
3	S4	59945.685926	45924

=====

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is $0.0 < 0.05$ Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

=====

Multiple Comparison of Means - Tukey HSD, FWER=0.05

=====

group1	group2	meandiff	p-adj	lower	upper	reject
S1	S2	-10145.6835	0.0	-10402.8539	-9888.513	True
S1	S3	9386.5565	0.0	9113.6974	9659.4156	True
S1	S4	22269.1742	0.0	22050.9148	22487.4336	True
S2	S3	19532.24	0.0	19203.4535	19861.0265	True
S2	S4	32414.8577	0.0	32129.7514	32699.9641	True
S3	S4	12882.6177	0.0	12583.2834	13181.9521	True

Pairs having different Sales mean are: S1-S2,S1-S3,S1-S4,S2-S3,S2-S4,S3-S4

Pairs having same Sales mean are:

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Hypothesis test whether Mean Order is same for all Location_Type or not.

	Location_Type	Mean	Count
0	L1	65.265938	85140
1	L2	94.851456	48504
2	L3	53.156943	29928
3	L4	47.386028	10836
4	L5	41.924131	13932

=====

Criteria check for ANOVA

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is $0.0 < 0.05$ Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

=====

Multiple Comparison of Means - Tukey HSD, FWER=0.05

=====

group1	group2	meandiff	p-adj	lower	upper	reject
--------	--------	----------	-------	-------	-------	--------

L1	L2	29.5855	0.0	29.1962	29.9749	True
----	----	---------	-----	---------	---------	------

```
L1      L3  -12.109    0.0 -12.5689 -11.6491    True
```

L1	L4	-17.8799	0.0	-18.578	-17.1819	True
----	----	----------	-----	---------	----------	------

L1	L5	-23.3418	0.0	-23.9673	-22.7163	True
----	----	----------	-----	----------	----------	------

L2	L3	-41.6945	0.0	-42.1976	-41.1914	True
----	----	----------	-----	----------	----------	------

L2	L4	-47.4654	0.0	-48.1926	-46.7382	True
----	----	----------	-----	----------	----------	------

```
L2      L5 -52.9273    0.0 -53.5852 -52.2695    True
```

```
L3      L4  -5.7709    0.0  -6.5382  -5.0036    True
```

```
L3      L5 -11.2328    0.0 -11.9347 -10.5309    True
```

```
L4      L5  -5.4619    0.0  -6.3385  -4.5853    True
```

Pairs having different Order mean are:

L1-L2,L1-L3,L1-L4,L1-L5,L2-L3,L2-L4,L2-L5,L3-L4,L3-L5,L4-L5

Pairs having same Order mean are:

[illegible]

Hypothesis test whether Mean Sales is same for all Location_Type or not.

	Location_Type	Mean	Count
0	L1	41453.597889	85140
1	L2	59231.480373	48504
2	L3	33072.257756	29928
3	L4	29067.414313	10836
4	L5	25187.787261	13932

=====

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.
 We have enough evidence to reject the Null Hypothesis and at least one mean is different.

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Multiple Comparison of Means - Tukey HSD, FWER=0.05						
group1	group2	meandiff	p-adj	lower	upper	reject

L1	L2	17777.8825	0.0	17546.9501	18008.8149	True
L1	L3	-8381.3401	0.0	-8654.1357	-8108.5446	True
L1	L4	-12386.1836	0.0	-12800.2268	-11972.1403	True
L1	L5	-16265.8106	0.0	-16636.8052	-15894.816	True
L2	L3	-26159.2226	0.0	-26457.6129	-25860.8323	True
L2	L4	-30164.0661	0.0	-30595.4025	-29732.7296	True
L2	L5	-34043.6931	0.0	-34433.8935	-33653.4927	True
L3	L4	-4004.8434	0.0	-4459.9685	-3549.7184	True
L3	L5	-7884.4705	0.0	-8300.8165	-7468.1245	True
L4	L5	-3879.6271	0.0	-4399.5871	-3359.667	True

Pairs having different Sales mean are:

L1-L2,L1-L3,L1-L4,L1-L5,L2-L3,L2-L4,L2-L5,L3-L4,L3-L5,L4-L5

Pairs having same Sales mean are:

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```

Hypothesis test whether Mean Order is same for all Region_Code or not.

	Region_Code	Mean	Count
0	R1	79.626063	63984
1	R2	62.798616	54180
2	R3	63.882436	44376
3	R4	58.674031	25800

```
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```

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

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group1	group2	meandiff	p-adj	lower	upper	reject
R1	R2	-16.8274	0.0	-17.267	-16.3879	True
R1	R3	-15.7436	0.0	-16.2087	-15.2786	True
R1	R4	-20.952	0.0	-21.5072	-20.3968	True
R2	R3	1.0838	0.0	0.6018	1.5658	True
R2	R4	-4.1246	0.0	-4.694	-3.5551	True
R3	R4	-5.2084	0.0	-5.7978	-4.619	True

Pairs having same Order mean are:

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	Region_Code	Mean	Count
0	R1	46765.488405	63984
1	R2	40054.847344	54180
2	R3	42144.517063	44376
3	R4	39743.434249	25800

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

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Criteria check for ANOVA
  All groups are normally distributed.
  Variance of all groups are not same.
All criterias not met for ANOVA. Kruskal test will be performed.
p-Value is 0.0 < 0.05 Significance level.
We have enough evidence to reject the Null Hypothesis and at least one mean is
different.
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Multiple Comparison of Means - Tukey HSD, FWER=0.05
=====
group1 group2 meandiff p-adj lower upper reject
-----
False True -8445.4101 0.0 -8688.8675 -8201.9526 True
-----

```

Pairs having different Sales mean are: False-True

Pairs having same Sales mean are:

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Hypothesis test whether Mean Order is same for all Discount or not.

	Discount	Mean	Count
0	False	61.806153	104051
1	True	76.105637	84289

```

=====
Criteria check for ANOVA
  All groups are normally distributed.
  Variance of all groups are not same.
All criterias not met for ANOVA. Kruskal test will be performed.
p-Value is 0.0 < 0.05 Significance level.
We have enough evidence to reject the Null Hypothesis and at least one mean is
different.
=====

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Multiple Comparison of Means - Tukey HSD, FWER=0.05
=====
group1 group2 meandiff p-adj lower upper reject
-----
False True 14.2995 0.0 14.0304 14.5686 True
-----

```

Pairs having different Order mean are: False-True

Pairs having same Order mean are:

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```

Hypothesis test whether Mean Sales is same for all Discount or not.

	Discount	Mean	Count
0	False	37403.679678	104051
1	True	49426.497620	84289

=====

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is $0.0 < 0.05$ Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

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Multiple Comparison of Means - Tukey HSD, FWER=0.05

group1	group2	meandiff	p-adj	lower	upper	reject
False	True	12022.8179	0.0	11864.2197	12181.4162	True

Pairs having different Sales mean are: False-True

Pairs having same Sales mean are:

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```

Hypothesis test whether Mean Order is same for all MonthName or not.

	MonthName	Mean	Count
0	April	68.212968	21900
1	August	67.128502	11315
2	December	69.479806	11315
3	February	67.453474	20440
4	January	66.933672	22630
5	July	76.048873	11315

6	June	66.174155	10950
7	March	67.761688	22630
8	May	71.100044	22630
9	November	63.416438	10950
10	October	65.460009	11315
11	September	68.509954	10950

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 1.7657332953564353e-282 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

Multiple Comparison of Means - Tukey HSD, FWER=0.05

group1	group2	meandiff	p-adj	lower	upper	reject
April	August	-1.0845	0.0855	-2.2328	0.0639	False
April	December	1.2668	0.0163	0.1185	2.4152	True
April	February	-0.7595	0.295	-1.7241	0.2051	False
April	January	-1.2793	0.0005	-2.2195	-0.3391	True
April	July	7.8359	0.0	6.6876	8.9842	True
April	June	-2.0388	0.0	-3.1997	-0.8779	True
April	March	-0.4513	0.9204	-1.3915	0.4889	False
April	May	2.8871	0.0	1.9469	3.8272	True
April	November	-4.7965	0.0	-5.9574	-3.6357	True
April	October	-2.753	0.0	-3.9013	-1.6046	True
April	September	0.297	0.9996	-0.8639	1.4579	False
August	December	2.3513	0.0	1.0326	3.67	True
August	February	0.325	0.999	-0.8372	1.4872	False
August	January	-0.1948	1.0	-1.3368	0.9472	False
August	July	8.9204	0.0	7.6017	10.239	True
August	June	-0.9543	0.4438	-2.2839	0.3753	False
August	March	0.6332	0.8118	-0.5088	1.7752	False
August	May	3.9715	0.0	2.8296	5.1135	True
August	November	-3.7121	0.0	-5.0417	-2.3825	True
August	October	-1.6685	0.0021	-2.9872	-0.3498	True
August	September	1.3815	0.0334	0.0519	2.7111	True
December	February	-2.0263	0.0	-3.1885	-0.8641	True
December	January	-2.5461	0.0	-3.6881	-1.4041	True
December	July	6.5691	0.0	5.2504	7.8877	True
December	June	-3.3057	0.0	-4.6353	-1.976	True
December	March	-1.7181	0.0001	-2.8601	-0.5761	True
December	May	1.6202	0.0002	0.4782	2.7622	True
December	November	-6.0634	0.0	-7.393	-4.7338	True
December	October	-4.0198	0.0	-5.3385	-2.7011	True

December	September	-0.9699	0.417	-2.2995	0.3598	False
February	January	-0.5198	0.8319	-1.4769	0.4373	False
February	July	8.5954	0.0	7.4332	9.7576	True
February	June	-1.2793	0.0192	-2.4539	-0.1047	True
February	March	0.3082	0.9964	-0.6489	1.2653	False
February	May	3.6466	0.0	2.6895	4.6037	True
February	November	-4.037	0.0	-5.2116	-2.8624	True
February	October	-1.9935	0.0	-3.1557	-0.8313	True
February	September	1.0565	0.1272	-0.1181	2.2311	False
January	July	9.1152	0.0	7.9732	10.2572	True
January	June	-0.7595	0.5865	-1.9141	0.3951	False
January	March	0.828	0.14	-0.1044	1.7604	False
January	May	4.1664	0.0	3.2339	5.0988	True
January	November	-3.5172	0.0	-4.6718	-2.3626	True
January	October	-1.4737	0.0015	-2.6157	-0.3317	True
January	September	1.5763	0.0005	0.4217	2.7309	True
July	June	-9.8747	0.0	-11.2043	-8.5451	True
July	March	-8.2872	0.0	-9.4292	-7.1452	True
July	May	-4.9488	0.0	-6.0908	-3.8068	True
July	November	-12.6324	0.0	-13.962	-11.3028	True
July	October	-10.5889	0.0	-11.9075	-9.2702	True
July	September	-7.5389	0.0	-8.8685	-6.2093	True
June	March	1.5875	0.0004	0.4329	2.7421	True
June	May	4.9259	0.0	3.7713	6.0805	True
June	November	-2.7577	0.0	-4.0982	-1.4173	True
June	October	-0.7141	0.8421	-2.0437	0.6155	False
June	September	2.3358	0.0	0.9953	3.6763	True
March	May	3.3384	0.0	2.4059	4.2708	True
March	November	-4.3452	0.0	-5.4999	-3.1906	True
March	October	-2.3017	0.0	-3.4437	-1.1597	True
March	September	0.7483	0.6098	-0.4063	1.9029	False
May	November	-7.6836	0.0	-8.8382	-6.529	True
May	October	-5.64	0.0	-6.782	-4.498	True
May	September	-2.5901	0.0	-3.7447	-1.4355	True
November	October	2.0436	0.0	0.714	3.3732	True
November	September	5.0935	0.0	3.7531	6.434	True
October	September	3.0499	0.0	1.7203	4.3795	True

Pairs having different Order mean are: April-December, April-January, April-July, April-June, April-May, April-November, April-October, August-December, August-July, August-May, August-November, August-October, August-September, December-February, December-January, December-July, December-June, December-March, December-May, December-November, December-October, February-July, February-June, February-May, February-November, February-October, January-July, January-May, January-November, January-October, January-September, July-June, July-March, July-May, July-November, July-October, July-September, June-March, June-May, June-November, June-September, March-May, March-November, March-October, May-November, May-October, May-September, November-October, November-September, October-September

Pairs having same Order mean are: April-August, April-February, April-March, April-September, August-February, August-January, August-June, August-March, December-September, February-January, February-March, February-September, January-June, January-March, June-October, March-September

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Hypothesis test whether Mean Sales is same for all MonthName or not.

|    | MonthName | Mean         | Count |
|----|-----------|--------------|-------|
| 0  | April     | 40773.681352 | 21900 |
| 1  | August    | 40020.368869 | 11315 |
| 2  | December  | 46477.110199 | 11315 |
| 3  | February  | 40424.350645 | 20440 |
| 4  | January   | 44979.147732 | 22630 |
| 5  | July      | 46585.406232 | 11315 |
| 6  | June      | 44705.726389 | 10950 |
| 7  | March     | 40979.577286 | 22630 |
| 8  | May       | 48115.830407 | 22630 |
| 9  | November  | 38160.962496 | 10950 |
| 10 | October   | 38988.407398 | 11315 |
| 11 | September | 41123.184822 | 10950 |

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Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is  $0.0 < 0.05$  Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

| Multiple Comparison of Means - Tukey HSD, FWER=0.05 |           |            |        |            |            |        |
|-----------------------------------------------------|-----------|------------|--------|------------|------------|--------|
| group1                                              | group2    | meandiff   | p-adj  | lower      | upper      | reject |
| April                                               | August    | -753.3125  | 0.018  | -1441.2331 | -65.3918   | True   |
| April                                               | December  | 5703.4288  | 0.0    | 5015.5082  | 6391.3495  | True   |
| April                                               | February  | -349.3307  | 0.7103 | -927.2051  | 228.5437   | False  |
| April                                               | January   | 4205.4664  | 0.0    | 3642.2406  | 4768.6922  | True   |
| April                                               | July      | 5811.7249  | 0.0    | 5123.8042  | 6499.6455  | True   |
| April                                               | June      | 3932.045   | 0.0    | 3236.6059  | 4627.4842  | True   |
| April                                               | March     | 205.8959   | 0.9895 | -357.3299  | 769.1218   | False  |
| April                                               | May       | 7342.1491  | 0.0    | 6778.9232  | 7905.3749  | True   |
| April                                               | November  | -2612.7189 | 0.0    | -3308.158  | -1917.2797 | True   |
| April                                               | October   | -1785.274  | 0.0    | -2473.1946 | -1097.3533 | True   |
| April                                               | September | 349.5035   | 0.8934 | -345.9356  | 1044.9426  | False  |
| August                                              | December  | 6456.7413  | 0.0    | 5666.7756  | 7246.7071  | True   |
| August                                              | February  | 403.9818   | 0.762  | -292.2581  | 1100.2216  | False  |
| August                                              | January   | 4958.7789  | 0.0    | 4274.6485  | 5642.9093  | True   |
| August                                              | July      | 6565.0374  | 0.0    | 5775.0716  | 7355.0031  | True   |
| August                                              | June      | 4685.3575  | 0.0    | 3888.8359  | 5481.8791  | True   |
| August                                              | March     | 959.2084   | 0.0003 | 275.078    | 1643.3388  | True   |
| August                                              | May       | 8095.4615  | 0.0    | 7411.3311  | 8779.5919  | True   |
| August                                              | November  | -1859.4064 | 0.0    | -2655.928  | -1062.8848 | True   |
| August                                              | October   | -1031.9615 | 0.0012 | -1821.9272 | -241.9957  | True   |
| August                                              | September | 1102.816   | 0.0004 | 306.2944   | 1899.3376  | True   |
| December                                            | February  | -6052.7596 | 0.0    | -6748.9994 | -5356.5197 | True   |
| December                                            | January   | -1497.9625 | 0.0    | -2182.0929 | -813.8321  | True   |
| December                                            | July      | 108.296    | 1.0    | -681.6697  | 898.2618   | False  |
| December                                            | June      | -1771.3838 | 0.0    | -2567.9054 | -974.8622  | True   |
| December                                            | March     | -5497.5329 | 0.0    | -6181.6633 | -4813.4025 | True   |
| December                                            | May       | 1638.7202  | 0.0    | 954.5898   | 2322.8506  | True   |
| December                                            | November  | -8316.1477 | 0.0    | -9112.6693 | -7519.6261 | True   |
| December                                            | October   | -7488.7028 | 0.0    | -8278.6686 | -6698.737  | True   |
| December                                            | September | -5353.9254 | 0.0    | -6150.447  | -4557.4038 | True   |
| February                                            | January   | 4554.7971  | 0.0    | 3981.4399  | 5128.1543  | True   |
| February                                            | July      | 6161.0556  | 0.0    | 5464.8157  | 6857.2954  | True   |
| February                                            | June      | 4281.3757  | 0.0    | 3577.7063  | 4985.0452  | True   |
| February                                            | March     | 555.2266   | 0.0682 | -18.1305   | 1128.5838  | False  |
| February                                            | May       | 7691.4798  | 0.0    | 7118.1226  | 8264.8369  | True   |
| February                                            | November  | -2263.3881 | 0.0    | -2967.0576 | -1559.7187 | True   |
| February                                            | October   | -1435.9432 | 0.0    | -2132.1831 | -739.7034  | True   |
| February                                            | September | 698.8342   | 0.0536 | -4.8353    | 1402.5036  | False  |
| January                                             | July      | 1606.2585  | 0.0    | 922.1281   | 2290.3889  | True   |

|          |           |            |        |            |            |       |
|----------|-----------|------------|--------|------------|------------|-------|
| January  | June      | -273.4213  | 0.9803 | -965.1114  | 418.2687   | False |
| January  | March     | -3999.5704 | 0.0    | -4558.1606 | -3440.9803 | True  |
| January  | May       | 3136.6827  | 0.0    | 2578.0925  | 3695.2728  | True  |
| January  | November  | -6818.1852 | 0.0    | -7509.8753 | -6126.4951 | True  |
| January  | October   | -5990.7403 | 0.0    | -6674.8707 | -5306.6099 | True  |
| January  | September | -3855.9629 | 0.0    | -4547.653  | -3164.2728 | True  |
| July     | June      | -1879.6798 | 0.0    | -2676.2014 | -1083.1582 | True  |
| July     | March     | -5605.8289 | 0.0    | -6289.9594 | -4921.6985 | True  |
| July     | May       | 1530.4242  | 0.0    | 846.2938   | 2214.5546  | True  |
| July     | November  | -8424.4437 | 0.0    | -9220.9653 | -7627.9221 | True  |
| July     | October   | -7596.9988 | 0.0    | -8386.9646 | -6807.0331 | True  |
| July     | September | -5462.2214 | 0.0    | -6258.743  | -4665.6998 | True  |
| June     | March     | -3726.1491 | 0.0    | -4417.8392 | -3034.459  | True  |
| June     | May       | 3410.104   | 0.0    | 2718.4139  | 4101.7941  | True  |
| June     | November  | -6544.7639 | 0.0    | -7347.7878 | -5741.74   | True  |
| June     | October   | -5717.319  | 0.0    | -6513.8406 | -4920.7974 | True  |
| June     | September | -3582.5416 | 0.0    | -4385.5655 | -2779.5176 | True  |
| March    | May       | 7136.2531  | 0.0    | 6577.663   | 7694.8433  | True  |
| March    | November  | -2818.6148 | 0.0    | -3510.3049 | -2126.9247 | True  |
| March    | October   | -1991.1699 | 0.0    | -2675.3003 | -1307.0395 | True  |
| March    | September | 143.6075   | 0.9999 | -548.0826  | 835.2976   | False |
| May      | November  | -9954.8679 | 0.0    | -10646.558 | -9263.1778 | True  |
| May      | October   | -9127.423  | 0.0    | -9811.5534 | -8443.2926 | True  |
| May      | September | -6992.6456 | 0.0    | -7684.3357 | -6300.9555 | True  |
| November | October   | 827.4449   | 0.0334 | 30.9233    | 1623.9665  | True  |
| November | September | 2962.2223  | 0.0    | 2159.1984  | 3765.2462  | True  |
| October  | September | 2134.7774  | 0.0    | 1338.2558  | 2931.299   | True  |

---

Pairs having different Sales mean are: April-August, April-December, April-January, April-July, April-June, April-May, April-November, April-October, August-December, August-January, August-July, August-June, August-March, August-May, August-November, August-October, August-September, December-February, December-January, December-June, December-March, December-May, December-November, December-October, December-September, February-January, February-July, February-June, February-May, February-November, February-October, January-July, January-March, January-May, January-November, January-October, January-September, July-June, July-March, July-May, July-November, July-October, July-September, June-March, June-May, June-November, June-October, June-September, March-May, March-November, March-October, May-November, May-October, May-September, November-October, November-September, October-September

Pairs having same Sales mean are: April-February, April-March, April-September, August-February, December-July, February-March, February-September, January-June, March-September

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```

Hypothesis test whether Mean Order is same for all DayName or not.

|   | DayName   | Mean      | Count |
|---|-----------|-----------|-------|
| 0 | Friday    | 63.507812 | 27010 |
| 1 | Monday    | 66.164939 | 27010 |
| 2 | Saturday  | 75.887934 | 26645 |
| 3 | Sunday    | 77.694389 | 26645 |
| 4 | Thursday  | 64.140244 | 27010 |
| 5 | Tuesday   | 65.198001 | 27010 |
| 6 | Wednesday | 65.078563 | 27010 |

=====

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is

different.

| Multiple Comparison of Means - Tukey HSD, FWER=0.05 |           |          |        |          |          |        |
|-----------------------------------------------------|-----------|----------|--------|----------|----------|--------|
| group1                                              | group2    | meandiff | p-adj  | lower    | upper    | reject |
| Friday                                              | Monday    | 2.6571   | 0.0    | 1.8967   | 3.4176   | True   |
| Friday                                              | Saturday  | 12.3801  | 0.0    | 11.6171  | 13.1431  | True   |
| Friday                                              | Sunday    | 14.1866  | 0.0    | 13.4236  | 14.9496  | True   |
| Friday                                              | Thursday  | 0.6324   | 0.1772 | -0.128   | 1.3929   | False  |
| Friday                                              | Tuesday   | 1.6902   | 0.0    | 0.9298   | 2.4506   | True   |
| Friday                                              | Wednesday | 1.5708   | 0.0    | 0.8103   | 2.3312   | True   |
| Monday                                              | Saturday  | 9.723    | 0.0    | 8.96     | 10.486   | True   |
| Monday                                              | Sunday    | 11.5295  | 0.0    | 10.7664  | 12.2925  | True   |
| Monday                                              | Thursday  | -2.0247  | 0.0    | -2.7851  | -1.2643  | True   |
| Monday                                              | Tuesday   | -0.9669  | 0.0034 | -1.7274  | -0.2065  | True   |
| Monday                                              | Wednesday | -1.0864  | 0.0005 | -1.8468  | -0.326   | True   |
| Saturday                                            | Sunday    | 1.8065   | 0.0    | 1.0408   | 2.5721   | True   |
| Saturday                                            | Thursday  | -11.7477 | 0.0    | -12.5107 | -10.9847 | True   |
| Saturday                                            | Tuesday   | -10.6899 | 0.0    | -11.453  | -9.9269  | True   |
| Saturday                                            | Wednesday | -10.8094 | 0.0    | -11.5724 | -10.0463 | True   |
| Sunday                                              | Thursday  | -13.5541 | 0.0    | -14.3172 | -12.7911 | True   |
| Sunday                                              | Tuesday   | -12.4964 | 0.0    | -13.2594 | -11.7334 | True   |
| Sunday                                              | Wednesday | -12.6158 | 0.0    | -13.3788 | -11.8528 | True   |
| Thursday                                            | Tuesday   | 1.0578   | 0.0008 | 0.2973   | 1.8182   | True   |
| Thursday                                            | Wednesday | 0.9383   | 0.0051 | 0.1779   | 1.6987   | True   |
| Tuesday                                             | Wednesday | -0.1194  | 0.9993 | -0.8799  | 0.641    | False  |

Pairs having different Order mean are: Friday-Monday, Friday-Saturday, Friday-Sunday, Friday-Tuesday, Friday-Wednesday, Monday-Saturday, Monday-Sunday, Monday-Thursday, Monday-Tuesday, Monday-Wednesday, Saturday-Sunday, Saturday-Thursday, Saturday-Tuesday, Saturday-Wednesday, Sunday-Thursday, Sunday-Tuesday, Sunday-Wednesday, Thursday-Tuesday, Thursday-Wednesday

Pairs having same Order mean are: Friday-Thursday, Tuesday-Wednesday

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Hypothesis test whether Mean Sales is same for all DayName or not.

| DayName | Mean | Count |
|---------|------|-------|
|---------|------|-------|

```

0    Friday  39701.020376  27010
1    Monday  42291.175854  27010
2    Saturday 46729.798143  26645
3    Sunday  49044.051947  26645
4    Thursday 40231.985963  27010
5    Tuesday  40802.966220  27010
6    Wednesday 40827.205395  27010

```

```
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```

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

```
=====
```

Multiple Comparison of Means - Tukey HSD, FWER=0.05

```
=====
```

| group1   | group2    | meandiff   | p-adj  | lower      | upper      | reject |
|----------|-----------|------------|--------|------------|------------|--------|
| Friday   | Monday    | 2590.1555  | 0.0    | 2129.6495  | 3050.6614  | True   |
| Friday   | Saturday  | 7028.7778  | 0.0    | 6566.6975  | 7490.8581  | True   |
| Friday   | Sunday    | 9343.0316  | 0.0    | 8880.9513  | 9805.1119  | True   |
| Friday   | Thursday  | 530.9656   | 0.012  | 70.4597    | 991.4715   | True   |
| Friday   | Tuesday   | 1101.9458  | 0.0    | 641.4399   | 1562.4518  | True   |
| Friday   | Wednesday | 1126.185   | 0.0    | 665.6791   | 1586.691   | True   |
| Monday   | Saturday  | 4438.6223  | 0.0    | 3976.542   | 4900.7026  | True   |
| Monday   | Sunday    | 6752.8761  | 0.0    | 6290.7958  | 7214.9564  | True   |
| Monday   | Thursday  | -2059.1899 | 0.0    | -2519.6958 | -1598.684  | True   |
| Monday   | Tuesday   | -1488.2096 | 0.0    | -1948.7156 | -1027.7037 | True   |
| Monday   | Wednesday | -1463.9705 | 0.0    | -1924.4764 | -1003.4645 | True   |
| Saturday | Sunday    | 2314.2538  | 0.0    | 1850.6045  | 2777.9032  | True   |
| Saturday | Thursday  | -6497.8122 | 0.0    | -6959.8925 | -6035.7319 | True   |
| Saturday | Tuesday   | -5926.8319 | 0.0    | -6388.9122 | -5464.7516 | True   |
| Saturday | Wednesday | -5902.5927 | 0.0    | -6364.6731 | -5440.5124 | True   |
| Sunday   | Thursday  | -8812.066  | 0.0    | -9274.1463 | -8349.9857 | True   |
| Sunday   | Tuesday   | -8241.0857 | 0.0    | -8703.166  | -7779.0054 | True   |
| Sunday   | Wednesday | -8216.8466 | 0.0    | -8678.9269 | -7754.7662 | True   |
| Thursday | Tuesday   | 570.9803   | 0.0048 | 110.4743   | 1031.4862  | True   |
| Thursday | Wednesday | 595.2194   | 0.0026 | 134.7135   | 1055.7254  | True   |
| Tuesday  | Wednesday | 24.2392    | 1.0    | -436.2668  | 484.7451   | False  |

```
-----
```

Pairs having different Sales mean are: Friday-Monday, Friday-Saturday, Friday-Sunday, Friday-Thursday, Friday-Tuesday, Friday-Wednesday, Monday-Saturday, Monday-Sunday, Monday-Thursday, Monday-Tuesday, Monday-Wednesday, Saturday-Sunday, Saturday-Thursday, Saturday-Tuesday, Saturday-Wednesday, Sunday-Thursday, Sunday-Tuesday, Sunday-Wednesday, Thursday-Tuesday, Thursday-Wednesday

Pairs having same Sales mean are: Tuesday-Wednesday

```
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```

## 1.6 6. Data Preperation for modeling

```
[35]: # Data Preperation for modeling
# Data for Sales forecastig model training
overall_sales = train.groupby(level=0).agg({'Sales': 'sum'})
id_wise_sales = pd.crosstab(index=train.index, columns=train.Store_id, values=
    ↪train.Sales, aggfunc='sum')
store_type_wise_sales = pd.crosstab(index=train.index, columns=train.
    ↪Store_Type, values =train.Sales, aggfunc='sum')
location_wise_sales = pd.crosstab(index=train.index, columns=train.
    ↪Location_Type, values =train.Sales, aggfunc='sum')
region_wise_sales = pd.crosstab(index=train.index, columns=train.Region_Code,
    ↪values =train.Sales, aggfunc='sum')

# Data for Order forecastig model training
overall_order = train.groupby(level=0).agg({'Order': 'sum'})
id_wise_order = pd.crosstab(index=train.index, columns=train.Store_id, values=
    ↪train.Order, aggfunc='sum')
store_type_wise_order = pd.crosstab(index=train.index, columns=train.
    ↪Store_Type, values =train.Order, aggfunc='sum')
location_wise_order = pd.crosstab(index=train.index, columns=train.
    ↪Location_Type, values =train.Order, aggfunc='sum')
region_wise_order = pd.crosstab(index=train.index, columns=train.Region_Code,
    ↪values =train.Order, aggfunc='sum')

# Create a Single DataFrame for Sales and Order
train_sales = pd.concat([overall_sales, id_wise_sales, store_type_wise_sales,
    ↪location_wise_sales, region_wise_sales], axis=1)
train_order = pd.concat([overall_order, id_wise_order, store_type_wise_order,
    ↪location_wise_order, region_wise_order], axis=1)

exog_train_holiday = train.groupby(train.index).mean('Holiday')['Holiday']
exog_test_holiday = test.groupby(test.index).mean('Holiday')['Holiday']
```



```
[36]: train_sales.sample(5)
```

```
[36]:
```

|            | Sales       | 1       | 2       | 3         | 4       | 5       | \ |
|------------|-------------|---------|---------|-----------|---------|---------|---|
| 2018-09-23 | 15356484.00 | 50787.0 | 45009.0 | 79581.00  | 37530.0 | 56091.0 |   |
| 2018-04-01 | 18166922.52 | 54228.3 | 63533.4 | 66489.96  | 49104.0 | 42486.0 |   |
| 2018-07-06 | 19560669.00 | 55365.0 | 75336.0 | 100575.00 | 55824.0 | 54261.0 |   |
| 2019-03-12 | 15125649.00 | 17169.0 | 48828.0 | 41235.00  | 40383.0 | 31425.0 |   |
| 2019-04-22 | 14214354.00 | 49641.0 | 37809.0 | 62280.00  | 33180.0 | 51990.0 |   |

|            | 6        | 7        | 8        | 9       | ... | S4        | L1        | \ |
|------------|----------|----------|----------|---------|-----|-----------|-----------|---|
| 2018-09-23 | 22146.00 | 33870.00 | 61662.00 | 26868.0 | ... | 5362617.0 | 6643680.0 |   |
| 2018-04-01 | 51044.82 | 46874.04 | 68442.75 | 37654.2 | ... | 6153951.6 | 7935110.1 |   |
| 2018-07-06 | 62088.00 | 60111.00 | 32301.00 | 60669.0 | ... | 6868077.0 | 8374755.0 |   |
| 2019-03-12 | 44379.00 | 44469.00 | 30996.00 | 40953.0 | ... | 4962132.0 | 6785559.0 |   |
| 2019-04-22 | 18630.00 | 29235.00 | 47628.00 | 42177.0 | ... | 5095695.0 | 6166440.0 |   |

|            | L2         | L3         | L4       | L5        | R1         | \ |
|------------|------------|------------|----------|-----------|------------|---|
| 2018-09-23 | 5646750.00 | 1900068.00 | 549048.0 | 616938.00 | 5640360.00 |   |
| 2018-04-01 | 6379018.11 | 2287515.24 | 763146.0 | 802133.07 | 6791009.28 |   |
| 2018-07-06 | 7179198.00 | 2455737.00 | 701085.0 | 849894.00 | 7496133.00 |   |
| 2019-03-12 | 5155902.00 | 1847976.00 | 635424.0 | 700788.00 | 5659689.00 |   |
| 2019-04-22 | 5201874.00 | 1783437.00 | 514428.0 | 548175.00 | 5423253.00 |   |

|            | R2        | R3         | R4         |
|------------|-----------|------------|------------|
| 2018-09-23 | 4184151.0 | 3560130.00 | 1971843.00 |
| 2018-04-01 | 5011791.9 | 4137095.07 | 2227026.27 |
| 2018-07-06 | 4778820.0 | 4823478.00 | 2462238.00 |
| 2019-03-12 | 4096827.0 | 3458814.00 | 1910319.00 |
| 2019-04-22 | 3758352.0 | 3272553.00 | 1760196.00 |

[5 rows x 379 columns]

## 1.7 7. Time series plots

```
[37]: # Function to plot the data
def plot_sales(data, code):
    fig = go.Figure()
    fig.add_trace(go.Scatter(x=data.index, y=data[code], mode='lines', name=code))
    fig.add_trace(go.Bar(x=data.index, y=exog_train_holiday, name='campaign',
    ↪yaxis='y2', opacity=1))
    fig.update_layout(title=f'Timeseries for {code}', showlegend=False, title_x=0.
    ↪12,
        yaxis=dict(title='Sales Amount'),
        yaxis2=dict(overlying='y', showline=False, showgrid=False,
    ↪showticklabels=False, side='right'))
    return fig
```

```
def plot_order(data, code):
    fig = go.Figure()
    fig.add_trace(go.Scatter(x=data.index, y=data[code], mode='lines', name=code))
    fig.add_trace(go.Bar(x=data.index, y=exog_train_holiday, name='campaign',
↪yaxis='y2', opacity=1))
    fig.update_layout(title=f'Timeseries for {code}', showlegend=False, title_x=0.
↪12,
                      yaxis=dict(title='Order Volume'),
                      yaxis2=dict(overlying='y', showline=False, showgrid=False,
↪showticklabels=False, side='right'))
    return fig
```

```
[38]: fig = make_subplots(rows=2, cols=1, specs=[[{"secondary_y": True}],
↪[{"secondary_y": True}]]
for trace in plot_order(overall_order, 'Order').data:
    secondary_y = "yaxis" in trace and trace["yaxis"] == "y2"
    fig.add_trace(trace, row=1, col=1)
for trace in plot_sales(overall_sales, 'Sales').data:
    secondary_y = "yaxis" in trace and trace["yaxis"] == "y2"
    fig.add_trace(trace, row=2, col=1)
fig.show()
```

```
[39]: df_order = region_wise_order
df_sales = region_wise_sales
for code in df_order.columns:
    plot_order(df_order, code).show()
    plot_sales(df_sales, code).show()
```

```
[40]: df_order = location_wise_order
df_sales = location_wise_sales
for code in df_order.columns:
    plot_order(df_order, code).show()
    plot_sales(df_sales, code).show()
```

```
[41]: df_order = store_type_wise_order
df_sales = store_type_wise_sales
for code in df_order.columns:
    plot_order(df_order, code).show()
    plot_sales(df_sales, code).show()
```

## 2 B. Stationarity, decomposition, detrending, ACF, and PACF

### 2.1 8. Stationarity test and decomposition

Most of timeseries model (like **AR**, **MA**, **ARIMA**) works on assumption of Stationarity, which makes it easier to predict future values, estimate model parameters, and perform statistical tests.

By transforming non-stationary data into a stationary form, analysts can apply a broader range of statistical tools and achieve more reliable results.

To check stationarity of timeseries we will use Augmented Dickey-Fuller test with 5% significance level as threshold.

```
[42]: # Import ACF/PACF plotting modules
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf

# Import Dickey-Fuller test
from statsmodels.tsa.stattools import adfuller

[43]: # Print Dickey-Fuller test insights
def adf_test(dataset):
    print(f'Results of Dickey-Fuller Test:')
    for column in dataset.columns:
        pvalue = adfuller(dataset[column])[1]
        if pvalue <= 0.05:
            print(f'\033[32mTimeseries for "{column}" is stationary', end='.\t')
        else:
            print(f'\033[31mTimeseries for "{column}" is not stationary', end='.')
        print(f'\t p-value is {pvalue}\033[0m')

[44]: adf_test(train_order)
adf_test(train_sales)
```

```
Results of Dickey-Fuller Test:
Timeseries for "Order" is stationary.          p-value is
0.00019001472288566557
Timeseries for "1" is stationary.              p-value is
3.3930512375433676e-07
Timeseries for "2" is stationary.              p-value is
3.487864501563372e-05
Timeseries for "3" is stationary.              p-value is
0.0026307597340207416
Timeseries for "4" is stationary.              p-value is
2.1803807823009623e-12
Timeseries for "5" is stationary.              p-value is
0.0001419446382003186
Timeseries for "6" is stationary.              p-value is
0.00205035109867991
Timeseries for "7" is stationary.              p-value is
0.00013323300549812953
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| Timeseries for "8" is stationary.  | p-value is |
| 2.2959953942007774e-07             |            |
| Timeseries for "9" is stationary.  | p-value is |
| 3.2347862976079523e-17             |            |
| Timeseries for "10" is stationary. | p-value is |
| 7.441225128758886e-06              |            |
| Timeseries for "11" is stationary. | p-value is |
| 3.628125417229516e-05              |            |
| Timeseries for "12" is stationary. | p-value is |
| 0.0013883312595671436              |            |
| Timeseries for "13" is stationary. | p-value is |
| 0.013189837370918795               |            |
| Timeseries for "14" is stationary. | p-value is |
| 0.00013405682296692347             |            |
| Timeseries for "15" is stationary. | p-value is |
| 5.111294828052101e-05              |            |
| Timeseries for "16" is stationary. | p-value is |
| 0.0009199590224398585              |            |
| Timeseries for "17" is stationary. | p-value is |
| 1.0711379964565977e-06             |            |
| Timeseries for "18" is stationary. | p-value is |
| 0.00012238000145299083             |            |
| Timeseries for "19" is stationary. | p-value is |
| 2.1112891772215627e-06             |            |
| Timeseries for "20" is stationary. | p-value is |
| 0.02374224801394575                |            |
| Timeseries for "21" is stationary. | p-value is |
| 0.00023624055901910664             |            |
| Timeseries for "22" is stationary. | p-value is |
| 3.8756263276873324e-05             |            |
| Timeseries for "23" is stationary. | p-value is |
| 0.0008614546829018442              |            |
| Timeseries for "24" is stationary. | p-value is |
| 0.0008344652715878641              |            |
| Timeseries for "25" is stationary. | p-value is |
| 1.1717640571394116e-24             |            |

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| Timeseries for "26" is stationary. | p-value is |
| 3.895907782815797e-07              |            |
| Timeseries for "27" is stationary. | p-value is |
| 4.21062260155192e-06               |            |
| Timeseries for "28" is stationary. | p-value is |
| 3.401045038842587e-05              |            |
| Timeseries for "29" is stationary. | p-value is |
| 8.314714296307071e-07              |            |
| Timeseries for "30" is stationary. | p-value is |
| 3.6441956726965804e-05             |            |
| Timeseries for "31" is stationary. | p-value is |
| 0.004680006836468052               |            |
| Timeseries for "32" is stationary. | p-value is |
| 7.348732211260025e-07              |            |
| Timeseries for "33" is stationary. | p-value is |
| 7.890619917291206e-13              |            |
| Timeseries for "34" is stationary. | p-value is |
| 4.512693454886711e-06              |            |
| Timeseries for "35" is stationary. | p-value is |
| 5.309425335125379e-07              |            |
| Timeseries for "36" is stationary. | p-value is |
| 2.1693219921700006e-05             |            |
| Timeseries for "37" is stationary. | p-value is |
| 2.8247390142701275e-11             |            |
| Timeseries for "38" is stationary. | p-value is |
| 0.010751046397342333               |            |
| Timeseries for "39" is stationary. | p-value is |
| 1.9876552667426326e-09             |            |
| Timeseries for "40" is stationary. | p-value is |
| 8.119240331224733e-05              |            |
| Timeseries for "41" is stationary. | p-value is |
| 1.580021909188928e-05              |            |
| Timeseries for "42" is stationary. | p-value is |
| 0.0005572886373698547              |            |
| Timeseries for "43" is stationary. | p-value is |
| 1.2638437278931261e-06             |            |

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| Timeseries for "44" is stationary.     | p-value is |
| 1.8030462937170134e-06                 |            |
| Timeseries for "45" is stationary.     | p-value is |
| 3.8124949892148184e-05                 |            |
| Timeseries for "46" is not stationary. | p-value is |
| 0.05535856530253811                    |            |
| Timeseries for "47" is stationary.     | p-value is |
| 1.8108070324666628e-06                 |            |
| Timeseries for "48" is stationary.     | p-value is |
| 2.5546797099157627e-06                 |            |
| Timeseries for "49" is stationary.     | p-value is |
| 0.0001435214955483385                  |            |
| Timeseries for "50" is stationary.     | p-value is |
| 5.993430215771944e-05                  |            |
| Timeseries for "51" is stationary.     | p-value is |
| 9.894957738616657e-06                  |            |
| Timeseries for "52" is stationary.     | p-value is |
| 7.393797204959565e-05                  |            |
| Timeseries for "53" is stationary.     | p-value is |
| 0.0007221302732318259                  |            |
| Timeseries for "54" is stationary.     | p-value is |
| 8.5513366100919e-06                    |            |
| Timeseries for "55" is stationary.     | p-value is |
| 2.5123285495137178e-05                 |            |
| Timeseries for "56" is stationary.     | p-value is |
| 1.4953534519962917e-06                 |            |
| Timeseries for "57" is stationary.     | p-value is |
| 1.2041706531829316e-06                 |            |
| Timeseries for "58" is not stationary. | p-value is |
| 0.09093201528108513                    |            |
| Timeseries for "59" is stationary.     | p-value is |
| 5.998154721746872e-05                  |            |
| Timeseries for "60" is stationary.     | p-value is |
| 1.698930370119066e-09                  |            |
| Timeseries for "61" is stationary.     | p-value is |
| 2.4968497740175623e-06                 |            |

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| Timeseries for "62" is stationary.     | p-value is |
| 1.497010164466012e-07                  |            |
| Timeseries for "63" is stationary.     | p-value is |
| 0.0013646209488178507                  |            |
| Timeseries for "64" is stationary.     | p-value is |
| 6.460736779407831e-05                  |            |
| Timeseries for "65" is not stationary. | p-value is |
| 0.5386965878127822                     |            |
| Timeseries for "66" is stationary.     | p-value is |
| 0.0002364189250287246                  |            |
| Timeseries for "67" is stationary.     | p-value is |
| 6.013978922957296e-06                  |            |
| Timeseries for "68" is stationary.     | p-value is |
| 1.6717487828797033e-13                 |            |
| Timeseries for "69" is stationary.     | p-value is |
| 1.3551035044719921e-05                 |            |
| Timeseries for "70" is stationary.     | p-value is |
| 0.007720591150134667                   |            |
| Timeseries for "71" is stationary.     | p-value is |
| 1.4830684877403486e-05                 |            |
| Timeseries for "72" is stationary.     | p-value is |
| 4.6820858273089173e-08                 |            |
| Timeseries for "73" is stationary.     | p-value is |
| 1.5741391779406382e-06                 |            |
| Timeseries for "74" is stationary.     | p-value is |
| 0.0043133262978212565                  |            |
| Timeseries for "75" is stationary.     | p-value is |
| 2.697111660497253e-05                  |            |
| Timeseries for "76" is stationary.     | p-value is |
| 2.5708528258692893e-06                 |            |
| Timeseries for "77" is stationary.     | p-value is |
| 3.8155980754113376e-05                 |            |
| Timeseries for "78" is stationary.     | p-value is |
| 0.00016147255591651057                 |            |
| Timeseries for "79" is stationary.     | p-value is |
| 2.605161896558134e-05                  |            |

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| Timeseries for "80" is stationary. | p-value is |
| 4.83481290686305e-05               |            |
| Timeseries for "81" is stationary. | p-value is |
| 3.737655970894863e-05              |            |
| Timeseries for "82" is stationary. | p-value is |
| 0.001993493594374998               |            |
| Timeseries for "83" is stationary. | p-value is |
| 7.004283797447677e-15              |            |
| Timeseries for "84" is stationary. | p-value is |
| 5.571904889755887e-05              |            |
| Timeseries for "85" is stationary. | p-value is |
| 0.0021295531650791922              |            |
| Timeseries for "86" is stationary. | p-value is |
| 4.372334149494939e-06              |            |
| Timeseries for "87" is stationary. | p-value is |
| 1.4046418027945153e-06             |            |
| Timeseries for "88" is stationary. | p-value is |
| 0.038354241685291696               |            |
| Timeseries for "89" is stationary. | p-value is |
| 0.002571840765244099               |            |
| Timeseries for "90" is stationary. | p-value is |
| 9.538544858757939e-05              |            |
| Timeseries for "91" is stationary. | p-value is |
| 0.000336206416799257               |            |
| Timeseries for "92" is stationary. | p-value is |
| 0.0017260076252782856              |            |
| Timeseries for "93" is stationary. | p-value is |
| 0.001474124682377123               |            |
| Timeseries for "94" is stationary. | p-value is |
| 4.575949601838265e-07              |            |
| Timeseries for "95" is stationary. | p-value is |
| 0.001317343984144627               |            |
| Timeseries for "96" is stationary. | p-value is |
| 0.0006942335774146915              |            |
| Timeseries for "97" is stationary. | p-value is |
| 0.00012180161288027802             |            |



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| Timeseries for "98" is stationary.  | p-value is |
| 8.74848672780359e-08                |            |
| Timeseries for "99" is stationary.  | p-value is |
| 3.955645993497474e-06               |            |
| Timeseries for "100" is stationary. | p-value is |
| 0.0006469654542312705               |            |
| Timeseries for "101" is stationary. | p-value is |
| 2.0153101703932955e-07              |            |
| Timeseries for "102" is stationary. | p-value is |
| 9.487147439371601e-11               |            |
| Timeseries for "103" is stationary. | p-value is |
| 6.565326305306632e-07               |            |
| Timeseries for "104" is stationary. | p-value is |
| 3.6991285343036747e-07              |            |
| Timeseries for "105" is stationary. | p-value is |
| 0.011071898631391009                |            |
| Timeseries for "106" is stationary. | p-value is |
| 3.155230372582543e-05               |            |
| Timeseries for "107" is stationary. | p-value is |
| 0.00026624851390524433              |            |
| Timeseries for "108" is stationary. | p-value is |
| 1.853967025189231e-10               |            |
| Timeseries for "109" is stationary. | p-value is |
| 8.749008795477004e-05               |            |
| Timeseries for "110" is stationary. | p-value is |
| 3.149313591033713e-06               |            |
| Timeseries for "111" is stationary. | p-value is |
| 1.0091425117159596e-05              |            |
| Timeseries for "112" is stationary. | p-value is |
| 6.520659064953944e-05               |            |
| Timeseries for "113" is stationary. | p-value is |
| 1.7865455026889918e-10              |            |
| Timeseries for "114" is stationary. | p-value is |
| 8.301087012248881e-12               |            |
| Timeseries for "115" is stationary. | p-value is |
| 0.00012583256779253316              |            |

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| Timeseries for "116" is stationary. | p-value is |
| 1.1834075230958227e-10              |            |
| Timeseries for "117" is stationary. | p-value is |
| 1.9718918986153662e-06              |            |
| Timeseries for "118" is stationary. | p-value is |
| 1.0933309998271666e-10              |            |
| Timeseries for "119" is stationary. | p-value is |
| 0.00014708357883481274              |            |
| Timeseries for "120" is stationary. | p-value is |
| 9.913511150912327e-06               |            |
| Timeseries for "121" is stationary. | p-value is |
| 2.723225101853458e-06               |            |
| Timeseries for "122" is stationary. | p-value is |
| 1.1752964130149005e-05              |            |
| Timeseries for "123" is stationary. | p-value is |
| 2.139101441311718e-05               |            |
| Timeseries for "124" is stationary. | p-value is |
| 7.896420187636915e-07               |            |
| Timeseries for "125" is stationary. | p-value is |
| 0.00011947851846840942              |            |
| Timeseries for "126" is stationary. | p-value is |
| 3.8620535186139247e-07              |            |
| Timeseries for "127" is stationary. | p-value is |
| 3.5670950681081125e-07              |            |
| Timeseries for "128" is stationary. | p-value is |
| 0.010633702829589706                |            |
| Timeseries for "129" is stationary. | p-value is |
| 5.203292864137039e-07               |            |
| Timeseries for "130" is stationary. | p-value is |
| 1.8908153585059535e-06              |            |
| Timeseries for "131" is stationary. | p-value is |
| 0.0007262619422735948               |            |
| Timeseries for "132" is stationary. | p-value is |
| 8.333259467777589e-07               |            |
| Timeseries for "133" is stationary. | p-value is |
| 6.789011652574819e-05               |            |

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| Timeseries for "134" is stationary. | p-value is |
| 2.076297711073456e-07               |            |
| Timeseries for "135" is stationary. | p-value is |
| 3.2544088194635824e-06              |            |
| Timeseries for "136" is stationary. | p-value is |
| 0.0016451747085213385               |            |
| Timeseries for "137" is stationary. | p-value is |
| 2.0090805067845517e-06              |            |
| Timeseries for "138" is stationary. | p-value is |
| 4.270008858444917e-14               |            |
| Timeseries for "139" is stationary. | p-value is |
| 1.6747504360262133e-05              |            |
| Timeseries for "140" is stationary. | p-value is |
| 1.7306650304429188e-07              |            |
| Timeseries for "141" is stationary. | p-value is |
| 2.916748711073959e-05               |            |
| Timeseries for "142" is stationary. | p-value is |
| 3.1496676944661386e-08              |            |
| Timeseries for "143" is stationary. | p-value is |
| 2.3086234268581383e-06              |            |
| Timeseries for "144" is stationary. | p-value is |
| 1.5799794695725325e-11              |            |
| Timeseries for "145" is stationary. | p-value is |
| 4.299464534141279e-06               |            |
| Timeseries for "146" is stationary. | p-value is |
| 0.002468515341846608                |            |
| Timeseries for "147" is stationary. | p-value is |
| 0.00016865675111165732              |            |
| Timeseries for "148" is stationary. | p-value is |
| 4.5403535839328955e-05              |            |
| Timeseries for "149" is stationary. | p-value is |
| 8.295417566991276e-05               |            |
| Timeseries for "150" is stationary. | p-value is |
| 1.0767614434951178e-05              |            |
| Timeseries for "151" is stationary. | p-value is |
| 3.969608207812673e-10               |            |

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| Timeseries for "152" is stationary. | p-value is |
| 5.0078497482456014e-08              |            |
| Timeseries for "153" is stationary. | p-value is |
| 8.444282283952105e-05               |            |
| Timeseries for "154" is stationary. | p-value is |
| 3.383442764215231e-07               |            |
| Timeseries for "155" is stationary. | p-value is |
| 0.00017102218547661131              |            |
| Timeseries for "156" is stationary. | p-value is |
| 5.258887943929971e-08               |            |
| Timeseries for "157" is stationary. | p-value is |
| 6.929853876090441e-08               |            |
| Timeseries for "158" is stationary. | p-value is |
| 6.928076436982305e-05               |            |
| Timeseries for "159" is stationary. | p-value is |
| 0.0035456517565745213               |            |
| Timeseries for "160" is stationary. | p-value is |
| 0.0009795640542862624               |            |
| Timeseries for "161" is stationary. | p-value is |
| 7.780640147016751e-06               |            |
| Timeseries for "162" is stationary. | p-value is |
| 1.254621575298791e-07               |            |
| Timeseries for "163" is stationary. | p-value is |
| 2.58094892281611e-12                |            |
| Timeseries for "164" is stationary. | p-value is |
| 0.0004686842928708999               |            |
| Timeseries for "165" is stationary. | p-value is |
| 0.00016959509179191538              |            |
| Timeseries for "166" is stationary. | p-value is |
| 8.785738747623313e-06               |            |
| Timeseries for "167" is stationary. | p-value is |
| 0.0002595137175460508               |            |
| Timeseries for "168" is stationary. | p-value is |
| 7.077563909724307e-12               |            |
| Timeseries for "169" is stationary. | p-value is |
| 2.7700044055212924e-06              |            |

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| Timeseries for "170" is stationary. | p-value is |
| 7.933104481738624e-07               |            |
| Timeseries for "171" is stationary. | p-value is |
| 4.870367624715471e-07               |            |
| Timeseries for "172" is stationary. | p-value is |
| 5.4642657233765346e-05              |            |
| Timeseries for "173" is stationary. | p-value is |
| 1.7146183668627356e-08              |            |
| Timeseries for "174" is stationary. | p-value is |
| 1.4697060127673197e-07              |            |
| Timeseries for "175" is stationary. | p-value is |
| 0.011386226098472138                |            |
| Timeseries for "176" is stationary. | p-value is |
| 9.684310863336179e-08               |            |
| Timeseries for "177" is stationary. | p-value is |
| 4.6954083274973815e-05              |            |
| Timeseries for "178" is stationary. | p-value is |
| 8.344840987786177e-05               |            |
| Timeseries for "179" is stationary. | p-value is |
| 2.444337187103508e-06               |            |
| Timeseries for "180" is stationary. | p-value is |
| 0.024807871541731644                |            |
| Timeseries for "181" is stationary. | p-value is |
| 5.246482640609067e-10               |            |
| Timeseries for "182" is stationary. | p-value is |
| 0.008143302537358305                |            |
| Timeseries for "183" is stationary. | p-value is |
| 1.4470425609233592e-08              |            |
| Timeseries for "184" is stationary. | p-value is |
| 0.00029333044859244315              |            |
| Timeseries for "185" is stationary. | p-value is |
| 5.79664288666121e-05                |            |
| Timeseries for "186" is stationary. | p-value is |
| 1.4051496255533592e-05              |            |
| Timeseries for "187" is stationary. | p-value is |
| 4.418015767340524e-07               |            |

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| Timeseries for "188" is stationary. | p-value is |
| 0.0007513225966590528               |            |
| Timeseries for "189" is stationary. | p-value is |
| 0.00025605639308622487              |            |
| Timeseries for "190" is stationary. | p-value is |
| 1.90552253482218e-11                |            |
| Timeseries for "191" is stationary. | p-value is |
| 2.9336876492075247e-06              |            |
| Timeseries for "192" is stationary. | p-value is |
| 8.765088353742073e-10               |            |
| Timeseries for "193" is stationary. | p-value is |
| 8.055484375320195e-11               |            |
| Timeseries for "194" is stationary. | p-value is |
| 8.901743696472675e-05               |            |
| Timeseries for "195" is stationary. | p-value is |
| 1.260124858225439e-26               |            |
| Timeseries for "196" is stationary. | p-value is |
| 7.910690793339057e-12               |            |
| Timeseries for "197" is stationary. | p-value is |
| 1.2289931875136164e-06              |            |
| Timeseries for "198" is stationary. | p-value is |
| 8.6523959256508e-07                 |            |
| Timeseries for "199" is stationary. | p-value is |
| 2.2316505781938132e-06              |            |
| Timeseries for "200" is stationary. | p-value is |
| 2.0404072737453138e-07              |            |
| Timeseries for "201" is stationary. | p-value is |
| 0.003151423510302445                |            |
| Timeseries for "202" is stationary. | p-value is |
| 4.227563608810947e-05               |            |
| Timeseries for "203" is stationary. | p-value is |
| 4.795911712537781e-09               |            |
| Timeseries for "204" is stationary. | p-value is |
| 4.3890601708509006e-14              |            |
| Timeseries for "205" is stationary. | p-value is |
| 5.856848465711828e-05               |            |

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| Timeseries for "206" is not stationary. | p-value is |
| 0.10946694123579304                     |            |
| Timeseries for "207" is stationary.     | p-value is |
| 2.129647218943059e-06                   |            |
| Timeseries for "208" is stationary.     | p-value is |
| 2.5326725612245584e-06                  |            |
| Timeseries for "209" is stationary.     | p-value is |
| 6.311216582776823e-05                   |            |
| Timeseries for "210" is stationary.     | p-value is |
| 0.0017479461434251858                   |            |
| Timeseries for "211" is stationary.     | p-value is |
| 0.00024956553972248934                  |            |
| Timeseries for "212" is stationary.     | p-value is |
| 6.3276157098852926e-15                  |            |
| Timeseries for "213" is stationary.     | p-value is |
| 3.135286071523618e-05                   |            |
| Timeseries for "214" is stationary.     | p-value is |
| 3.717417906211807e-05                   |            |
| Timeseries for "215" is stationary.     | p-value is |
| 1.3190527302977789e-05                  |            |
| Timeseries for "216" is stationary.     | p-value is |
| 0.00021826854006605113                  |            |
| Timeseries for "217" is stationary.     | p-value is |
| 6.022004410721664e-06                   |            |
| Timeseries for "218" is stationary.     | p-value is |
| 7.364911445760457e-07                   |            |
| Timeseries for "219" is stationary.     | p-value is |
| 0.0001888642065283942                   |            |
| Timeseries for "220" is stationary.     | p-value is |
| 0.0004068319867345256                   |            |
| Timeseries for "221" is stationary.     | p-value is |
| 0.007102411382209182                    |            |
| Timeseries for "222" is stationary.     | p-value is |
| 5.947031939111964e-09                   |            |
| Timeseries for "223" is stationary.     | p-value is |
| 2.439924239963443e-05                   |            |

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| Timeseries for "224" is stationary. | p-value is |
| 0.0030196886119002292               |            |
| Timeseries for "225" is stationary. | p-value is |
| 4.567402188286042e-10               |            |
| Timeseries for "226" is stationary. | p-value is |
| 6.191692893768323e-07               |            |
| Timeseries for "227" is stationary. | p-value is |
| 2.819149099769977e-06               |            |
| Timeseries for "228" is stationary. | p-value is |
| 1.443445471807939e-06               |            |
| Timeseries for "229" is stationary. | p-value is |
| 0.0002227329582254047               |            |
| Timeseries for "230" is stationary. | p-value is |
| 5.9341160057158775e-06              |            |
| Timeseries for "231" is stationary. | p-value is |
| 1.9731989584590604e-06              |            |
| Timeseries for "232" is stationary. | p-value is |
| 4.862555599428091e-07               |            |
| Timeseries for "233" is stationary. | p-value is |
| 0.011116867819018121                |            |
| Timeseries for "234" is stationary. | p-value is |
| 1.2037130383192282e-05              |            |
| Timeseries for "235" is stationary. | p-value is |
| 0.000417775521394403                |            |
| Timeseries for "236" is stationary. | p-value is |
| 1.268816540835271e-06               |            |
| Timeseries for "237" is stationary. | p-value is |
| 3.3672373338658524e-10              |            |
| Timeseries for "238" is stationary. | p-value is |
| 5.658643960415718e-08               |            |
| Timeseries for "239" is stationary. | p-value is |
| 0.00030691128484766124              |            |
| Timeseries for "240" is stationary. | p-value is |
| 0.0025517073586012588               |            |
| Timeseries for "241" is stationary. | p-value is |
| 4.3461070113121813e-05              |            |



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| Timeseries for "242" is stationary.     | p-value is |
| 4.280415364093271e-06                   |            |
| Timeseries for "243" is stationary.     | p-value is |
| 0.00082853608587924                     |            |
| Timeseries for "244" is stationary.     | p-value is |
| 8.59350255222756e-06                    |            |
| Timeseries for "245" is stationary.     | p-value is |
| 4.730780677154208e-06                   |            |
| Timeseries for "246" is stationary.     | p-value is |
| 1.2161075846856997e-06                  |            |
| Timeseries for "247" is stationary.     | p-value is |
| 0.000131212453389353                    |            |
| Timeseries for "248" is stationary.     | p-value is |
| 1.7918944997759566e-07                  |            |
| Timeseries for "249" is stationary.     | p-value is |
| 0.00036607129773350347                  |            |
| Timeseries for "250" is stationary.     | p-value is |
| 1.681901006718479e-05                   |            |
| Timeseries for "251" is stationary.     | p-value is |
| 3.16610699463011e-07                    |            |
| Timeseries for "252" is stationary.     | p-value is |
| 3.9917513298946077e-05                  |            |
| Timeseries for "253" is not stationary. | p-value is |
| 0.06421249505051625                     |            |
| Timeseries for "254" is stationary.     | p-value is |
| 1.0883878110193443e-07                  |            |
| Timeseries for "255" is stationary.     | p-value is |
| 1.2025255429467576e-10                  |            |
| Timeseries for "256" is stationary.     | p-value is |
| 1.47893177255516e-05                    |            |
| Timeseries for "257" is stationary.     | p-value is |
| 1.4119363821673375e-12                  |            |
| Timeseries for "258" is stationary.     | p-value is |
| 4.992812079165035e-12                   |            |
| Timeseries for "259" is stationary.     | p-value is |
| 2.7924333928363728e-06                  |            |

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| Timeseries for "260" is stationary.     | p-value is |
| 4.262313061592368e-05                   |            |
| Timeseries for "261" is stationary.     | p-value is |
| 0.0006518111638001428                   |            |
| Timeseries for "262" is stationary.     | p-value is |
| 2.1527522559680643e-06                  |            |
| Timeseries for "263" is stationary.     | p-value is |
| 7.46919653800032e-08                    |            |
| Timeseries for "264" is stationary.     | p-value is |
| 1.961118300271593e-06                   |            |
| Timeseries for "265" is not stationary. | p-value is |
| 0.1747960816443197                      |            |
| Timeseries for "266" is not stationary. | p-value is |
| 0.058133744122539535                    |            |
| Timeseries for "267" is not stationary. | p-value is |
| 0.22647562713131197                     |            |
| Timeseries for "268" is stationary.     | p-value is |
| 0.00020972166741867673                  |            |
| Timeseries for "269" is stationary.     | p-value is |
| 0.018873041818966534                    |            |
| Timeseries for "270" is stationary.     | p-value is |
| 0.000327202401245754                    |            |
| Timeseries for "271" is stationary.     | p-value is |
| 0.00015498715561106764                  |            |
| Timeseries for "272" is stationary.     | p-value is |
| 1.6026841135698594e-05                  |            |
| Timeseries for "273" is stationary.     | p-value is |
| 1.777096064991541e-05                   |            |
| Timeseries for "274" is stationary.     | p-value is |
| 4.891416538817896e-06                   |            |
| Timeseries for "275" is stationary.     | p-value is |
| 3.6676556111398138e-28                  |            |
| Timeseries for "276" is stationary.     | p-value is |
| 2.4324285363767784e-06                  |            |
| Timeseries for "277" is stationary.     | p-value is |
| 0.00027601745945045623                  |            |

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| Timeseries for "278" is stationary. | p-value is |
| 0.000337388402361705                |            |
| Timeseries for "279" is stationary. | p-value is |
| 3.904208654283419e-05               |            |
| Timeseries for "280" is stationary. | p-value is |
| 0.00013857330387773327              |            |
| Timeseries for "281" is stationary. | p-value is |
| 7.932930575163268e-10               |            |
| Timeseries for "282" is stationary. | p-value is |
| 1.047579127750594e-05               |            |
| Timeseries for "283" is stationary. | p-value is |
| 0.0005137027537466457               |            |
| Timeseries for "284" is stationary. | p-value is |
| 0.0008325047934977306               |            |
| Timeseries for "285" is stationary. | p-value is |
| 8.313392586855961e-05               |            |
| Timeseries for "286" is stationary. | p-value is |
| 4.556157778610793e-05               |            |
| Timeseries for "287" is stationary. | p-value is |
| 7.263260514975754e-07               |            |
| Timeseries for "288" is stationary. | p-value is |
| 0.00011650204650465217              |            |
| Timeseries for "289" is stationary. | p-value is |
| 1.4920622861657612e-05              |            |
| Timeseries for "290" is stationary. | p-value is |
| 5.074459555452562e-05               |            |
| Timeseries for "291" is stationary. | p-value is |
| 0.005381741594836949                |            |
| Timeseries for "292" is stationary. | p-value is |
| 6.874333642198158e-05               |            |
| Timeseries for "293" is stationary. | p-value is |
| 0.00011136058526701835              |            |
| Timeseries for "294" is stationary. | p-value is |
| 0.0002833971345018345               |            |
| Timeseries for "295" is stationary. | p-value is |
| 1.1453974485699648e-06              |            |

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| Timeseries for "296" is stationary.     | p-value is |
| 0.028491948965722713                    |            |
| Timeseries for "297" is stationary.     | p-value is |
| 4.2705561064375764e-05                  |            |
| Timeseries for "298" is stationary.     | p-value is |
| 9.480148443769051e-08                   |            |
| Timeseries for "299" is stationary.     | p-value is |
| 1.0146305387454682e-07                  |            |
| Timeseries for "300" is not stationary. | p-value is |
| 0.18630095937928448                     |            |
| Timeseries for "301" is stationary.     | p-value is |
| 3.2775535933734434e-07                  |            |
| Timeseries for "302" is stationary.     | p-value is |
| 5.261582469974119e-06                   |            |
| Timeseries for "303" is stationary.     | p-value is |
| 0.005420856557244605                    |            |
| Timeseries for "304" is stationary.     | p-value is |
| 0.006520182864179445                    |            |
| Timeseries for "305" is stationary.     | p-value is |
| 8.500317481400646e-06                   |            |
| Timeseries for "306" is stationary.     | p-value is |
| 5.760695095601388e-14                   |            |
| Timeseries for "307" is stationary.     | p-value is |
| 3.6096933501381394e-05                  |            |
| Timeseries for "308" is stationary.     | p-value is |
| 4.449914013860301e-05                   |            |
| Timeseries for "309" is stationary.     | p-value is |
| 0.0004323393777942778                   |            |
| Timeseries for "310" is stationary.     | p-value is |
| 0.004787697776453726                    |            |
| Timeseries for "311" is stationary.     | p-value is |
| 0.0002560641465854551                   |            |
| Timeseries for "312" is stationary.     | p-value is |
| 0.0005534276875624203                   |            |
| Timeseries for "313" is stationary.     | p-value is |
| 1.8485663934821887e-06                  |            |

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| Timeseries for "314" is stationary. | p-value is |
| 0.0003996736239977625               |            |
| Timeseries for "315" is stationary. | p-value is |
| 0.049945737852137115                |            |
| Timeseries for "316" is stationary. | p-value is |
| 5.580870911314861e-10               |            |
| Timeseries for "317" is stationary. | p-value is |
| 1.9995511777153038e-24              |            |
| Timeseries for "318" is stationary. | p-value is |
| 4.330003152273656e-05               |            |
| Timeseries for "319" is stationary. | p-value is |
| 0.00026576526709938883              |            |
| Timeseries for "320" is stationary. | p-value is |
| 0.0005206065180896851               |            |
| Timeseries for "321" is stationary. | p-value is |
| 0.0018378495059394606               |            |
| Timeseries for "322" is stationary. | p-value is |
| 0.0027337126834068334               |            |
| Timeseries for "323" is stationary. | p-value is |
| 0.00025392437959206166              |            |
| Timeseries for "324" is stationary. | p-value is |
| 0.000347430239172436                |            |
| Timeseries for "325" is stationary. | p-value is |
| 0.017294976083193546                |            |
| Timeseries for "326" is stationary. | p-value is |
| 7.976834333173641e-06               |            |
| Timeseries for "327" is stationary. | p-value is |
| 0.0018461029029841654               |            |
| Timeseries for "328" is stationary. | p-value is |
| 0.0004832099037848997               |            |
| Timeseries for "329" is stationary. | p-value is |
| 3.960684881695652e-05               |            |
| Timeseries for "330" is stationary. | p-value is |
| 0.0033753156780492117               |            |
| Timeseries for "331" is stationary. | p-value is |
| 3.992483857195217e-07               |            |

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| Timeseries for "332" is stationary. | p-value is |
| 1.304637100924014e-06               |            |
| Timeseries for "333" is stationary. | p-value is |
| 4.323510712103889e-07               |            |
| Timeseries for "334" is stationary. | p-value is |
| 1.062355460743779e-05               |            |
| Timeseries for "335" is stationary. | p-value is |
| 0.00907332173138183                 |            |
| Timeseries for "336" is stationary. | p-value is |
| 0.00011682094299079566              |            |
| Timeseries for "337" is stationary. | p-value is |
| 2.5499577221748048e-05              |            |
| Timeseries for "338" is stationary. | p-value is |
| 1.0902150461238297e-05              |            |
| Timeseries for "339" is stationary. | p-value is |
| 0.011717640533577376                |            |
| Timeseries for "340" is stationary. | p-value is |
| 5.511231332364279e-06               |            |
| Timeseries for "341" is stationary. | p-value is |
| 7.241594054128154e-06               |            |
| Timeseries for "342" is stationary. | p-value is |
| 6.888647997770799e-07               |            |
| Timeseries for "343" is stationary. | p-value is |
| 8.800446125133676e-05               |            |
| Timeseries for "344" is stationary. | p-value is |
| 3.073854857697815e-08               |            |
| Timeseries for "345" is stationary. | p-value is |
| 1.5548309912031497e-25              |            |
| Timeseries for "346" is stationary. | p-value is |
| 1.9026313860071634e-05              |            |
| Timeseries for "347" is stationary. | p-value is |
| 1.8563510927320425e-06              |            |
| Timeseries for "348" is stationary. | p-value is |
| 4.410469136597884e-05               |            |
| Timeseries for "349" is stationary. | p-value is |
| 3.3725610944696004e-06              |            |

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| Timeseries for "350" is stationary. | p-value is |
| 0.00048950590573241                 |            |
| Timeseries for "351" is stationary. | p-value is |
| 1.3554110180357414e-05              |            |
| Timeseries for "352" is stationary. | p-value is |
| 0.03502712286435989                 |            |
| Timeseries for "353" is stationary. | p-value is |
| 4.438801287468647e-06               |            |
| Timeseries for "354" is stationary. | p-value is |
| 8.730174857855914e-08               |            |
| Timeseries for "355" is stationary. | p-value is |
| 2.321036507600439e-05               |            |
| Timeseries for "356" is stationary. | p-value is |
| 0.0003218863348237397               |            |
| Timeseries for "357" is stationary. | p-value is |
| 0.010030744366767177                |            |
| Timeseries for "358" is stationary. | p-value is |
| 2.8263736825744944e-06              |            |
| Timeseries for "359" is stationary. | p-value is |
| 0.0008662720360079804               |            |
| Timeseries for "360" is stationary. | p-value is |
| 8.98195210246438e-08                |            |
| Timeseries for "361" is stationary. | p-value is |
| 8.809429002921898e-06               |            |
| Timeseries for "362" is stationary. | p-value is |
| 0.000663340062058788                |            |
| Timeseries for "363" is stationary. | p-value is |
| 0.0010172862630813118               |            |
| Timeseries for "364" is stationary. | p-value is |
| 2.4175579825030357e-06              |            |
| Timeseries for "365" is stationary. | p-value is |
| 0.0021034988056674894               |            |
| Timeseries for "S1" is stationary.  | p-value is |
| 7.793448064208875e-05               |            |
| Timeseries for "S2" is stationary.  | p-value is |
| 3.19465531365585e-05                |            |

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| Timeseries for "S3" is stationary.    | p-value is |
| 0.0004455172797190973                 |            |
| Timeseries for "S4" is stationary.    | p-value is |
| 0.0005447205594067498                 |            |
| Timeseries for "L1" is stationary.    | p-value is |
| 0.00014331514294486087                |            |
| Timeseries for "L2" is stationary.    | p-value is |
| 0.00044985543030531615                |            |
| Timeseries for "L3" is stationary.    | p-value is |
| 6.657730739788191e-05                 |            |
| Timeseries for "L4" is stationary.    | p-value is |
| 5.520188415032601e-06                 |            |
| Timeseries for "L5" is stationary.    | p-value is |
| 2.446372236792949e-05                 |            |
| Timeseries for "R1" is stationary.    | p-value is |
| 0.0004224908491593281                 |            |
| Timeseries for "R2" is stationary.    | p-value is |
| 4.5432256312175485e-05                |            |
| Timeseries for "R3" is stationary.    | p-value is |
| 0.00017724010576170132                |            |
| Timeseries for "R4" is stationary.    | p-value is |
| 0.00017453874458951745                |            |
| <b>Results of Dickey-Fuller Test:</b> |            |
| Timeseries for "Sales" is stationary. | p-value is |
| 0.007386718711362291                  |            |
| Timeseries for "1" is stationary.     | p-value is |
| 0.0010072301346594694                 |            |
| Timeseries for "2" is stationary.     | p-value is |
| 0.00031561292823509697                |            |
| Timeseries for "3" is stationary.     | p-value is |
| 0.008991511921083089                  |            |
| Timeseries for "4" is stationary.     | p-value is |
| 0.0002737671033380586                 |            |
| Timeseries for "5" is stationary.     | p-value is |
| 0.005051306139498418                  |            |
| Timeseries for "6" is stationary.     | p-value is |
| 0.013888862311180786                  |            |



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| Timeseries for "7" is stationary.  | p-value is |
| 0.008717157545251193               |            |
| Timeseries for "8" is stationary.  | p-value is |
| 0.00013217108310095338             |            |
| Timeseries for "9" is stationary.  | p-value is |
| 2.9868967309125026e-21             |            |
| Timeseries for "10" is stationary. | p-value is |
| 9.122877817511299e-05              |            |
| Timeseries for "11" is stationary. | p-value is |
| 0.00023967290176901514             |            |
| Timeseries for "12" is stationary. | p-value is |
| 0.009512150715144845               |            |
| Timeseries for "13" is stationary. | p-value is |
| 0.022684796879694213               |            |
| Timeseries for "14" is stationary. | p-value is |
| 0.0001438788771060245              |            |
| Timeseries for "15" is stationary. | p-value is |
| 0.0005642453559567487              |            |
| Timeseries for "16" is stationary. | p-value is |
| 0.0008708998374719632              |            |
| Timeseries for "17" is stationary. | p-value is |
| 0.00015253072153556218             |            |
| Timeseries for "18" is stationary. | p-value is |
| 0.002310062738161719               |            |
| Timeseries for "19" is stationary. | p-value is |
| 0.0002075112312322143              |            |
| Timeseries for "20" is stationary. | p-value is |
| 0.013183196680306977               |            |
| Timeseries for "21" is stationary. | p-value is |
| 0.0013863982414371134              |            |
| Timeseries for "22" is stationary. | p-value is |
| 0.0006521497642114568              |            |
| Timeseries for "23" is stationary. | p-value is |
| 0.005768868464092041               |            |
| Timeseries for "24" is stationary. | p-value is |
| 0.016916048119491083               |            |

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| Timeseries for "25" is stationary. | p-value is |
| 3.558101260958532e-24              |            |
| Timeseries for "26" is stationary. | p-value is |
| 0.00017876734181824014             |            |
| Timeseries for "27" is stationary. | p-value is |
| 0.0003157634407573397              |            |
| Timeseries for "28" is stationary. | p-value is |
| 0.0010849474336122329              |            |
| Timeseries for "29" is stationary. | p-value is |
| 2.2234749436377456e-05             |            |
| Timeseries for "30" is stationary. | p-value is |
| 0.0005491655112836941              |            |
| Timeseries for "31" is stationary. | p-value is |
| 0.0074353945297359406              |            |
| Timeseries for "32" is stationary. | p-value is |
| 0.0023147416981024642              |            |
| Timeseries for "33" is stationary. | p-value is |
| 0.0002011310512751143              |            |
| Timeseries for "34" is stationary. | p-value is |
| 7.249322540028292e-05              |            |
| Timeseries for "35" is stationary. | p-value is |
| 0.0003736584947946565              |            |
| Timeseries for "36" is stationary. | p-value is |
| 0.0003777959298406816              |            |
| Timeseries for "37" is stationary. | p-value is |
| 1.393012778080807e-11              |            |
| Timeseries for "38" is stationary. | p-value is |
| 0.022930015602661512               |            |
| Timeseries for "39" is stationary. | p-value is |
| 9.569520115462759e-07              |            |
| Timeseries for "40" is stationary. | p-value is |
| 0.001904343486754834               |            |
| Timeseries for "41" is stationary. | p-value is |
| 0.0001738481437417984              |            |
| Timeseries for "42" is stationary. | p-value is |
| 0.007219768463646842               |            |

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| Timeseries for "43" is stationary.     | p-value is |
| 2.7440674341048e-10                    |            |
| Timeseries for "44" is stationary.     | p-value is |
| 2.8660386173796303e-05                 |            |
| Timeseries for "45" is stationary.     | p-value is |
| 0.0015535020882591192                  |            |
| Timeseries for "46" is stationary.     | p-value is |
| 0.029745293195268505                   |            |
| Timeseries for "47" is stationary.     | p-value is |
| 0.0005264761742407543                  |            |
| Timeseries for "48" is stationary.     | p-value is |
| 0.0009533733239574719                  |            |
| Timeseries for "49" is stationary.     | p-value is |
| 0.00018768351929052625                 |            |
| Timeseries for "50" is stationary.     | p-value is |
| 0.001821013315630373                   |            |
| Timeseries for "51" is stationary.     | p-value is |
| 9.709833091280135e-06                  |            |
| Timeseries for "52" is stationary.     | p-value is |
| 0.00010669142753664644                 |            |
| Timeseries for "53" is stationary.     | p-value is |
| 0.016944351315085673                   |            |
| Timeseries for "54" is stationary.     | p-value is |
| 0.00039906920191827295                 |            |
| Timeseries for "55" is stationary.     | p-value is |
| 0.0004199617709412446                  |            |
| Timeseries for "56" is stationary.     | p-value is |
| 0.0006155764926102539                  |            |
| Timeseries for "57" is stationary.     | p-value is |
| 0.0031306500293198517                  |            |
| Timeseries for "58" is not stationary. | p-value is |
| 0.05599412739299651                    |            |
| Timeseries for "59" is stationary.     | p-value is |
| 0.0005049044323103629                  |            |
| Timeseries for "60" is stationary.     | p-value is |
| 5.958124430320324e-06                  |            |

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| Timeseries for "61" is stationary.     | p-value is |
| 3.718347132257486e-05                  |            |
| Timeseries for "62" is stationary.     | p-value is |
| 0.0006939322440744843                  |            |
| Timeseries for "63" is stationary.     | p-value is |
| 0.005152732990119278                   |            |
| Timeseries for "64" is stationary.     | p-value is |
| 0.0041408112601858576                  |            |
| Timeseries for "65" is not stationary. | p-value is |
| 0.18483372921324598                    |            |
| Timeseries for "66" is stationary.     | p-value is |
| 0.0110642570537213                     |            |
| Timeseries for "67" is stationary.     | p-value is |
| 0.0001858253429276891                  |            |
| Timeseries for "68" is stationary.     | p-value is |
| 0.00021692105928102737                 |            |
| Timeseries for "69" is stationary.     | p-value is |
| 0.0002476726160297314                  |            |
| Timeseries for "70" is stationary.     | p-value is |
| 0.01610110687786486                    |            |
| Timeseries for "71" is stationary.     | p-value is |
| 0.0011138623056447929                  |            |
| Timeseries for "72" is stationary.     | p-value is |
| 0.0002259581081959068                  |            |
| Timeseries for "73" is stationary.     | p-value is |
| 0.00010750310980277186                 |            |
| Timeseries for "74" is stationary.     | p-value is |
| 0.028771409803396188                   |            |
| Timeseries for "75" is stationary.     | p-value is |
| 0.0008917292983730971                  |            |
| Timeseries for "76" is stationary.     | p-value is |
| 5.2358450002276005e-05                 |            |
| Timeseries for "77" is stationary.     | p-value is |
| 2.9809608530756844e-05                 |            |
| Timeseries for "78" is stationary.     | p-value is |
| 0.0009624697563829815                  |            |

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| Timeseries for "79" is stationary. | p-value is |
| 0.00016455991284978206             |            |
| Timeseries for "80" is stationary. | p-value is |
| 8.778855813241938e-05              |            |
| Timeseries for "81" is stationary. | p-value is |
| 0.00028144423489681505             |            |
| Timeseries for "82" is stationary. | p-value is |
| 0.005831163927923531               |            |
| Timeseries for "83" is stationary. | p-value is |
| 5.130846582256076e-05              |            |
| Timeseries for "84" is stationary. | p-value is |
| 0.0010651714308486657              |            |
| Timeseries for "85" is stationary. | p-value is |
| 2.363522318342324e-20              |            |
| Timeseries for "86" is stationary. | p-value is |
| 2.213457504886807e-05              |            |
| Timeseries for "87" is stationary. | p-value is |
| 5.4862893774895915e-05             |            |
| Timeseries for "88" is stationary. | p-value is |
| 0.04143993154659144                |            |
| Timeseries for "89" is stationary. | p-value is |
| 0.015928260812085347               |            |
| Timeseries for "90" is stationary. | p-value is |
| 0.00023417991573657947             |            |
| Timeseries for "91" is stationary. | p-value is |
| 0.001730456899608241               |            |
| Timeseries for "92" is stationary. | p-value is |
| 0.003953046849771409               |            |
| Timeseries for "93" is stationary. | p-value is |
| 3.525918966730799e-09              |            |
| Timeseries for "94" is stationary. | p-value is |
| 0.002427024960420313               |            |
| Timeseries for "95" is stationary. | p-value is |
| 2.376101389913979e-05              |            |
| Timeseries for "96" is stationary. | p-value is |
| 0.003137381413218535               |            |

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| Timeseries for "97" is stationary.  | p-value is |
| 0.00107602356931371                 |            |
| Timeseries for "98" is stationary.  | p-value is |
| 0.0004866827000706573               |            |
| Timeseries for "99" is stationary.  | p-value is |
| 1.082660925284785e-05               |            |
| Timeseries for "100" is stationary. | p-value is |
| 0.001790434955505629                |            |
| Timeseries for "101" is stationary. | p-value is |
| 0.00012110899978042064              |            |
| Timeseries for "102" is stationary. | p-value is |
| 0.0010391184787552944               |            |
| Timeseries for "103" is stationary. | p-value is |
| 2.0553471181387548e-05              |            |
| Timeseries for "104" is stationary. | p-value is |
| 2.9894270303828405e-05              |            |
| Timeseries for "105" is stationary. | p-value is |
| 0.033011775202366186                |            |
| Timeseries for "106" is stationary. | p-value is |
| 0.0006272473174448875               |            |
| Timeseries for "107" is stationary. | p-value is |
| 0.007526035876384321                |            |
| Timeseries for "108" is stationary. | p-value is |
| 4.568705663622652e-10               |            |
| Timeseries for "109" is stationary. | p-value is |
| 0.0009411371765543806               |            |
| Timeseries for "110" is stationary. | p-value is |
| 6.564392374203068e-05               |            |
| Timeseries for "111" is stationary. | p-value is |
| 0.0001936772455416642               |            |
| Timeseries for "112" is stationary. | p-value is |
| 0.00042618085530415407              |            |
| Timeseries for "113" is stationary. | p-value is |
| 0.00040523942375613343              |            |
| Timeseries for "114" is stationary. | p-value is |
| 0.0018411896874280392               |            |

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| Timeseries for "115" is stationary. | p-value is |
| 0.00025459123912125473              |            |
| Timeseries for "116" is stationary. | p-value is |
| 6.718188975618646e-09               |            |
| Timeseries for "117" is stationary. | p-value is |
| 8.361888003537213e-05               |            |
| Timeseries for "118" is stationary. | p-value is |
| 3.940266672700867e-05               |            |
| Timeseries for "119" is stationary. | p-value is |
| 0.0016617027675708542               |            |
| Timeseries for "120" is stationary. | p-value is |
| 0.00048028169836101647              |            |
| Timeseries for "121" is stationary. | p-value is |
| 3.854991998881068e-05               |            |
| Timeseries for "122" is stationary. | p-value is |
| 0.0004979907744716396               |            |
| Timeseries for "123" is stationary. | p-value is |
| 0.0014677193942636392               |            |
| Timeseries for "124" is stationary. | p-value is |
| 5.194863134877565e-05               |            |
| Timeseries for "125" is stationary. | p-value is |
| 0.0040296816181112916               |            |
| Timeseries for "126" is stationary. | p-value is |
| 3.3447916782392196e-05              |            |
| Timeseries for "127" is stationary. | p-value is |
| 0.0008367289602497126               |            |
| Timeseries for "128" is stationary. | p-value is |
| 0.020410203453832387                |            |
| Timeseries for "129" is stationary. | p-value is |
| 2.0264426392745064e-05              |            |
| Timeseries for "130" is stationary. | p-value is |
| 0.0018858058564864026               |            |
| Timeseries for "131" is stationary. | p-value is |
| 0.0046206644375212675               |            |
| Timeseries for "132" is stationary. | p-value is |
| 0.0003563715598358019               |            |

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| Timeseries for "133" is stationary. | p-value is |
| 0.005435325827521715                |            |
| Timeseries for "134" is stationary. | p-value is |
| 5.342157715564607e-06               |            |
| Timeseries for "135" is stationary. | p-value is |
| 0.00014829951342225866              |            |
| Timeseries for "136" is stationary. | p-value is |
| 0.004012635832407312                |            |
| Timeseries for "137" is stationary. | p-value is |
| 5.242918624304251e-05               |            |
| Timeseries for "138" is stationary. | p-value is |
| 1.6197594623572468e-05              |            |
| Timeseries for "139" is stationary. | p-value is |
| 0.00024690079368640434              |            |
| Timeseries for "140" is stationary. | p-value is |
| 6.0552756376033996e-05              |            |
| Timeseries for "141" is stationary. | p-value is |
| 1.3940381999497495e-05              |            |
| Timeseries for "142" is stationary. | p-value is |
| 3.1771690956939645e-05              |            |
| Timeseries for "143" is stationary. | p-value is |
| 0.0013764220384307369               |            |
| Timeseries for "144" is stationary. | p-value is |
| 0.0011179628381382566               |            |
| Timeseries for "145" is stationary. | p-value is |
| 6.816240842177759e-05               |            |
| Timeseries for "146" is stationary. | p-value is |
| 0.0024038829584976484               |            |
| Timeseries for "147" is stationary. | p-value is |
| 0.0004342759107233961               |            |
| Timeseries for "148" is stationary. | p-value is |
| 0.0003721526304682833               |            |
| Timeseries for "149" is stationary. | p-value is |
| 0.00033353783438898934              |            |
| Timeseries for "150" is stationary. | p-value is |
| 0.001320918604322212                |            |



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| Timeseries for "151" is stationary. | p-value is |
| 1.3941164437570472e-23              |            |
| Timeseries for "152" is stationary. | p-value is |
| 1.3245681031290174e-05              |            |
| Timeseries for "153" is stationary. | p-value is |
| 0.00045288873118110175              |            |
| Timeseries for "154" is stationary. | p-value is |
| 2.971020683912829e-05               |            |
| Timeseries for "155" is stationary. | p-value is |
| 0.0006735608962806927               |            |
| Timeseries for "156" is stationary. | p-value is |
| 6.066785295908553e-06               |            |
| Timeseries for "157" is stationary. | p-value is |
| 0.00285220447419756                 |            |
| Timeseries for "158" is stationary. | p-value is |
| 2.474079904845501e-06               |            |
| Timeseries for "159" is stationary. | p-value is |
| 0.0023826624953484387               |            |
| Timeseries for "160" is stationary. | p-value is |
| 0.0010601568081331778               |            |
| Timeseries for "161" is stationary. | p-value is |
| 0.0009006657928950012               |            |
| Timeseries for "162" is stationary. | p-value is |
| 0.00010029404247567932              |            |
| Timeseries for "163" is stationary. | p-value is |
| 0.00014355492991076837              |            |
| Timeseries for "164" is stationary. | p-value is |
| 0.001044396002093798                |            |
| Timeseries for "165" is stationary. | p-value is |
| 0.001030960509203344                |            |
| Timeseries for "166" is stationary. | p-value is |
| 3.2511195999710264e-05              |            |
| Timeseries for "167" is stationary. | p-value is |
| 0.0008504456432767575               |            |
| Timeseries for "168" is stationary. | p-value is |
| 1.7328311146079027e-11              |            |

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| Timeseries for "169" is stationary.     | p-value is |
| 2.767696645833784e-05                   |            |
| Timeseries for "170" is stationary.     | p-value is |
| 2.52699783654674e-05                    |            |
| Timeseries for "171" is stationary.     | p-value is |
| 1.7115680935026434e-05                  |            |
| Timeseries for "172" is stationary.     | p-value is |
| 0.002854645341767548                    |            |
| Timeseries for "173" is stationary.     | p-value is |
| 0.00037183650634175                     |            |
| Timeseries for "174" is stationary.     | p-value is |
| 0.0002977941654444389                   |            |
| Timeseries for "175" is stationary.     | p-value is |
| 0.02952885424160673                     |            |
| Timeseries for "176" is stationary.     | p-value is |
| 1.8652537044153936e-05                  |            |
| Timeseries for "177" is stationary.     | p-value is |
| 1.547311263471623e-05                   |            |
| Timeseries for "178" is stationary.     | p-value is |
| 2.3314004656250497e-05                  |            |
| Timeseries for "179" is stationary.     | p-value is |
| 5.050030649808855e-05                   |            |
| Timeseries for "180" is not stationary. | p-value is |
| 0.0704381670914891                      |            |
| Timeseries for "181" is stationary.     | p-value is |
| 4.945394454609212e-07                   |            |
| Timeseries for "182" is stationary.     | p-value is |
| 0.003012509403693294                    |            |
| Timeseries for "183" is stationary.     | p-value is |
| 2.3972410694476644e-06                  |            |
| Timeseries for "184" is stationary.     | p-value is |
| 0.0017036132869262238                   |            |
| Timeseries for "185" is stationary.     | p-value is |
| 0.003141264862993032                    |            |
| Timeseries for "186" is stationary.     | p-value is |
| 0.0008272973123651762                   |            |

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| Timeseries for "187" is stationary. | p-value is |
| 4.708091770182434e-05               |            |
| Timeseries for "188" is stationary. | p-value is |
| 0.0006248862296784562               |            |
| Timeseries for "189" is stationary. | p-value is |
| 0.0004549796057056625               |            |
| Timeseries for "190" is stationary. | p-value is |
| 5.330849934641119e-10               |            |
| Timeseries for "191" is stationary. | p-value is |
| 0.004964974511928851                |            |
| Timeseries for "192" is stationary. | p-value is |
| 9.930872498345495e-05               |            |
| Timeseries for "193" is stationary. | p-value is |
| 0.0012670189977772334               |            |
| Timeseries for "194" is stationary. | p-value is |
| 0.00024337166072774857              |            |
| Timeseries for "195" is stationary. | p-value is |
| 1.7231655740755665e-23              |            |
| Timeseries for "196" is stationary. | p-value is |
| 0.002368185711247773                |            |
| Timeseries for "197" is stationary. | p-value is |
| 0.00017823194694497425              |            |
| Timeseries for "198" is stationary. | p-value is |
| 0.00010982930721878995              |            |
| Timeseries for "199" is stationary. | p-value is |
| 0.00023593185533639865              |            |
| Timeseries for "200" is stationary. | p-value is |
| 1.0567546809902824e-05              |            |
| Timeseries for "201" is stationary. | p-value is |
| 0.006998287872963017                |            |
| Timeseries for "202" is stationary. | p-value is |
| 0.0005080831505495583               |            |
| Timeseries for "203" is stationary. | p-value is |
| 6.398004977933699e-05               |            |
| Timeseries for "204" is stationary. | p-value is |
| 9.457535216944182e-14               |            |

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| Timeseries for "205" is stationary.     | p-value is |
| 0.0002576764452714263                   |            |
| Timeseries for "206" is not stationary. | p-value is |
| 0.11490127651432774                     |            |
| Timeseries for "207" is stationary.     | p-value is |
| 0.0001155650001373095                   |            |
| Timeseries for "208" is stationary.     | p-value is |
| 2.1900987700222402e-05                  |            |
| Timeseries for "209" is stationary.     | p-value is |
| 0.00027185106615009943                  |            |
| Timeseries for "210" is stationary.     | p-value is |
| 0.006298983612997602                    |            |
| Timeseries for "211" is stationary.     | p-value is |
| 0.0030994427336336968                   |            |
| Timeseries for "212" is stationary.     | p-value is |
| 1.8384467255317023e-08                  |            |
| Timeseries for "213" is stationary.     | p-value is |
| 0.008280798571854726                    |            |
| Timeseries for "214" is stationary.     | p-value is |
| 0.0004324746095029078                   |            |
| Timeseries for "215" is stationary.     | p-value is |
| 3.011969529994633e-05                   |            |
| Timeseries for "216" is stationary.     | p-value is |
| 0.00034023366659356166                  |            |
| Timeseries for "217" is stationary.     | p-value is |
| 1.0426360674689158e-13                  |            |
| Timeseries for "218" is stationary.     | p-value is |
| 0.0002038366445523663                   |            |
| Timeseries for "219" is stationary.     | p-value is |
| 0.0014283352492701015                   |            |
| Timeseries for "220" is stationary.     | p-value is |
| 0.0004235424962425248                   |            |
| Timeseries for "221" is stationary.     | p-value is |
| 0.012636122090964205                    |            |
| Timeseries for "222" is stationary.     | p-value is |
| 2.7145152599663654e-05                  |            |

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| Timeseries for "223" is stationary. | p-value is |
| 0.00027199637367506587              |            |
| Timeseries for "224" is stationary. | p-value is |
| 0.002366804395631395                |            |
| Timeseries for "225" is stationary. | p-value is |
| 9.301170925790265e-06               |            |
| Timeseries for "226" is stationary. | p-value is |
| 3.774615392240189e-05               |            |
| Timeseries for "227" is stationary. | p-value is |
| 0.0003031420987914876               |            |
| Timeseries for "228" is stationary. | p-value is |
| 1.0055917243420243e-05              |            |
| Timeseries for "229" is stationary. | p-value is |
| 0.001197972329319524                |            |
| Timeseries for "230" is stationary. | p-value is |
| 0.0010340078587901392               |            |
| Timeseries for "231" is stationary. | p-value is |
| 1.7913763569179506e-05              |            |
| Timeseries for "232" is stationary. | p-value is |
| 6.014281109071207e-06               |            |
| Timeseries for "233" is stationary. | p-value is |
| 0.010232386336641242                |            |
| Timeseries for "234" is stationary. | p-value is |
| 3.519016261255216e-05               |            |
| Timeseries for "235" is stationary. | p-value is |
| 0.011869727260044585                |            |
| Timeseries for "236" is stationary. | p-value is |
| 6.156473227097317e-05               |            |
| Timeseries for "237" is stationary. | p-value is |
| 0.00036215914799563465              |            |
| Timeseries for "238" is stationary. | p-value is |
| 0.00010138689453172003              |            |
| Timeseries for "239" is stationary. | p-value is |
| 0.004431032640689593                |            |
| Timeseries for "240" is stationary. | p-value is |
| 0.01071496275530863                 |            |

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| Timeseries for "241" is stationary.     | p-value is |
| 0.00036218095880287697                  |            |
| Timeseries for "242" is stationary.     | p-value is |
| 1.1734247111458108e-05                  |            |
| Timeseries for "243" is stationary.     | p-value is |
| 0.00027508538682600276                  |            |
| Timeseries for "244" is stationary.     | p-value is |
| 0.0004002338454727453                   |            |
| Timeseries for "245" is stationary.     | p-value is |
| 9.233905576736461e-05                   |            |
| Timeseries for "246" is stationary.     | p-value is |
| 0.0002848468706414233                   |            |
| Timeseries for "247" is stationary.     | p-value is |
| 0.0005428265295455665                   |            |
| Timeseries for "248" is stationary.     | p-value is |
| 6.21331919358916e-05                    |            |
| Timeseries for "249" is stationary.     | p-value is |
| 0.0031294865525661013                   |            |
| Timeseries for "250" is stationary.     | p-value is |
| 0.00011577524298764726                  |            |
| Timeseries for "251" is stationary.     | p-value is |
| 6.502472970219795e-06                   |            |
| Timeseries for "252" is stationary.     | p-value is |
| 0.00297014133205754                     |            |
| Timeseries for "253" is not stationary. | p-value is |
| 0.06608166489018202                     |            |
| Timeseries for "254" is stationary.     | p-value is |
| 2.1890747666875984e-05                  |            |
| Timeseries for "255" is stationary.     | p-value is |
| 2.939232253840054e-10                   |            |
| Timeseries for "256" is stationary.     | p-value is |
| 0.00017599749674439765                  |            |
| Timeseries for "257" is stationary.     | p-value is |
| 1.6436838320565628e-12                  |            |
| Timeseries for "258" is stationary.     | p-value is |
| 0.0009504319588403772                   |            |

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| Timeseries for "259" is stationary.     | p-value is |
| 0.0016216262832032798                   |            |
| Timeseries for "260" is stationary.     | p-value is |
| 0.0011722661783458478                   |            |
| Timeseries for "261" is stationary.     | p-value is |
| 0.0005235278577295648                   |            |
| Timeseries for "262" is stationary.     | p-value is |
| 1.0318144047496912e-05                  |            |
| Timeseries for "263" is stationary.     | p-value is |
| 4.400555566004078e-05                   |            |
| Timeseries for "264" is stationary.     | p-value is |
| 3.108065694738563e-05                   |            |
| Timeseries for "265" is not stationary. | p-value is |
| 0.08932256866593069                     |            |
| Timeseries for "266" is stationary.     | p-value is |
| 0.006060811129853634                    |            |
| Timeseries for "267" is not stationary. | p-value is |
| 0.21304952243086084                     |            |
| Timeseries for "268" is stationary.     | p-value is |
| 0.0003218253261987438                   |            |
| Timeseries for "269" is stationary.     | p-value is |
| 0.00896151731908972                     |            |
| Timeseries for "270" is stationary.     | p-value is |
| 0.0068005208411403536                   |            |
| Timeseries for "271" is stationary.     | p-value is |
| 0.0006382871948541686                   |            |
| Timeseries for "272" is stationary.     | p-value is |
| 2.9372764717430668e-05                  |            |
| Timeseries for "273" is stationary.     | p-value is |
| 0.0004842498602359248                   |            |
| Timeseries for "274" is stationary.     | p-value is |
| 2.5258729215995463e-05                  |            |
| Timeseries for "275" is stationary.     | p-value is |
| 5.9645714026137255e-25                  |            |
| Timeseries for "276" is stationary.     | p-value is |
| 6.5745443216935096e-06                  |            |

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| Timeseries for "277" is stationary.     | p-value is |
| 0.00206096963439632                     |            |
| Timeseries for "278" is stationary.     | p-value is |
| 0.0013725775393979439                   |            |
| Timeseries for "279" is stationary.     | p-value is |
| 0.0019025742504396872                   |            |
| Timeseries for "280" is stationary.     | p-value is |
| 0.000842249239911077                    |            |
| Timeseries for "281" is stationary.     | p-value is |
| 7.884684312223885e-05                   |            |
| Timeseries for "282" is stationary.     | p-value is |
| 0.0003244246637642427                   |            |
| Timeseries for "283" is stationary.     | p-value is |
| 0.0010257519898195966                   |            |
| Timeseries for "284" is stationary.     | p-value is |
| 0.006683033168869181                    |            |
| Timeseries for "285" is stationary.     | p-value is |
| 0.00035279633702756287                  |            |
| Timeseries for "286" is stationary.     | p-value is |
| 0.00011239460818445546                  |            |
| Timeseries for "287" is stationary.     | p-value is |
| 2.6020055037444134e-05                  |            |
| Timeseries for "288" is stationary.     | p-value is |
| 0.00010793626885476344                  |            |
| Timeseries for "289" is stationary.     | p-value is |
| 0.000494607978341371                    |            |
| Timeseries for "290" is stationary.     | p-value is |
| 0.002578818632838419                    |            |
| Timeseries for "291" is not stationary. | p-value is |
| 0.05660839298732183                     |            |
| Timeseries for "292" is stationary.     | p-value is |
| 0.00138631804295186                     |            |
| Timeseries for "293" is stationary.     | p-value is |
| 9.227170846012794e-05                   |            |
| Timeseries for "294" is stationary.     | p-value is |
| 0.0019322849111849656                   |            |



|                                         |            |
|-----------------------------------------|------------|
| Timeseries for "295" is stationary.     | p-value is |
| 0.0003483226840811138                   |            |
| Timeseries for "296" is not stationary. | p-value is |
| 0.08522175424013323                     |            |
| Timeseries for "297" is stationary.     | p-value is |
| 0.0009513523148761597                   |            |
| Timeseries for "298" is stationary.     | p-value is |
| 2.3154900772002134e-07                  |            |
| Timeseries for "299" is stationary.     | p-value is |
| 8.198964138962852e-05                   |            |
| Timeseries for "300" is stationary.     | p-value is |
| 0.02960701081753662                     |            |
| Timeseries for "301" is stationary.     | p-value is |
| 0.0008024291068340855                   |            |
| Timeseries for "302" is stationary.     | p-value is |
| 8.288561721439884e-05                   |            |
| Timeseries for "303" is stationary.     | p-value is |
| 0.007511206148330425                    |            |
| Timeseries for "304" is stationary.     | p-value is |
| 0.016506561303227273                    |            |
| Timeseries for "305" is stationary.     | p-value is |
| 0.0004695374483105809                   |            |
| Timeseries for "306" is stationary.     | p-value is |
| 9.10652662005277e-14                    |            |
| Timeseries for "307" is stationary.     | p-value is |
| 0.0003212892838848065                   |            |
| Timeseries for "308" is stationary.     | p-value is |
| 0.0003516318904385247                   |            |
| Timeseries for "309" is stationary.     | p-value is |
| 8.144569755515096e-26                   |            |
| Timeseries for "310" is stationary.     | p-value is |
| 0.023236368768485848                    |            |
| Timeseries for "311" is stationary.     | p-value is |
| 0.001849704106143876                    |            |
| Timeseries for "312" is stationary.     | p-value is |
| 0.0031234616557759996                   |            |

|                                         |            |
|-----------------------------------------|------------|
| Timeseries for "313" is stationary.     | p-value is |
| 6.769873735967843e-05                   |            |
| Timeseries for "314" is stationary.     | p-value is |
| 0.00242119827219045                     |            |
| Timeseries for "315" is not stationary. | p-value is |
| 0.07098414793954455                     |            |
| Timeseries for "316" is stationary.     | p-value is |
| 0.00032883048073315533                  |            |
| Timeseries for "317" is stationary.     | p-value is |
| 0.008526634021654383                    |            |
| Timeseries for "318" is stationary.     | p-value is |
| 0.004451253636279219                    |            |
| Timeseries for "319" is stationary.     | p-value is |
| 0.0019990276271246873                   |            |
| Timeseries for "320" is stationary.     | p-value is |
| 0.002321073375819277                    |            |
| Timeseries for "321" is stationary.     | p-value is |
| 0.0043801553799993845                   |            |
| Timeseries for "322" is stationary.     | p-value is |
| 0.0029190152014397946                   |            |
| Timeseries for "323" is stationary.     | p-value is |
| 0.0055571501156199046                   |            |
| Timeseries for "324" is stationary.     | p-value is |
| 0.00407112225375758                     |            |
| Timeseries for "325" is not stationary. | p-value is |
| 0.05424739627652914                     |            |
| Timeseries for "326" is stationary.     | p-value is |
| 0.0001318294963165366                   |            |
| Timeseries for "327" is stationary.     | p-value is |
| 0.0040422211288417345                   |            |
| Timeseries for "328" is stationary.     | p-value is |
| 0.0005944383550889401                   |            |
| Timeseries for "329" is stationary.     | p-value is |
| 0.00027879216831228304                  |            |
| Timeseries for "330" is stationary.     | p-value is |
| 0.000998860758398374                    |            |

|                                     |            |
|-------------------------------------|------------|
| Timeseries for "331" is stationary. | p-value is |
| 1.3350525607786505e-05              |            |
| Timeseries for "332" is stationary. | p-value is |
| 5.378603187944803e-05               |            |
| Timeseries for "333" is stationary. | p-value is |
| 0.0006380804496381146               |            |
| Timeseries for "334" is stationary. | p-value is |
| 2.896472891471825e-05               |            |
| Timeseries for "335" is stationary. | p-value is |
| 0.017967412288814648                |            |
| Timeseries for "336" is stationary. | p-value is |
| 0.0006222975405897576               |            |
| Timeseries for "337" is stationary. | p-value is |
| 0.0006886776027446046               |            |
| Timeseries for "338" is stationary. | p-value is |
| 0.0003975014114795488               |            |
| Timeseries for "339" is stationary. | p-value is |
| 0.007551842387699304                |            |
| Timeseries for "340" is stationary. | p-value is |
| 5.8278185854456127e-05              |            |
| Timeseries for "341" is stationary. | p-value is |
| 0.024458939513174457                |            |
| Timeseries for "342" is stationary. | p-value is |
| 8.80299947584453e-22                |            |
| Timeseries for "343" is stationary. | p-value is |
| 0.0025455537863433918               |            |
| Timeseries for "344" is stationary. | p-value is |
| 0.000171545237044495                |            |
| Timeseries for "345" is stationary. | p-value is |
| 0.0004347580821028395               |            |
| Timeseries for "346" is stationary. | p-value is |
| 4.027542336281311e-05               |            |
| Timeseries for "347" is stationary. | p-value is |
| 9.323362886751891e-05               |            |
| Timeseries for "348" is stationary. | p-value is |
| 0.001596161922824127                |            |

|                                     |            |
|-------------------------------------|------------|
| Timeseries for "349" is stationary. | p-value is |
| 2.599161815081659e-05               |            |
| Timeseries for "350" is stationary. | p-value is |
| 0.002818972880596073                |            |
| Timeseries for "351" is stationary. | p-value is |
| 0.00013922679432018566              |            |
| Timeseries for "352" is stationary. | p-value is |
| 0.04481384730031847                 |            |
| Timeseries for "353" is stationary. | p-value is |
| 6.203586391737858e-05               |            |
| Timeseries for "354" is stationary. | p-value is |
| 0.0018002150858307112               |            |
| Timeseries for "355" is stationary. | p-value is |
| 0.003388497575288476                |            |
| Timeseries for "356" is stationary. | p-value is |
| 0.0019667757787619963               |            |
| Timeseries for "357" is stationary. | p-value is |
| 0.00254489802701704                 |            |
| Timeseries for "358" is stationary. | p-value is |
| 0.0021694578498596675               |            |
| Timeseries for "359" is stationary. | p-value is |
| 0.0007575061228127756               |            |
| Timeseries for "360" is stationary. | p-value is |
| 0.00021343745292771302              |            |
| Timeseries for "361" is stationary. | p-value is |
| 5.7338625887903014e-05              |            |
| Timeseries for "362" is stationary. | p-value is |
| 0.005608341846038478                |            |
| Timeseries for "363" is stationary. | p-value is |
| 0.0014778227742358158               |            |
| Timeseries for "364" is stationary. | p-value is |
| 0.00035559780959084524              |            |
| Timeseries for "365" is stationary. | p-value is |
| 0.012319364620433915                |            |
| Timeseries for "S1" is stationary.  | p-value is |
| 0.0056604416023610755               |            |

```

Timeseries for "S2" is stationary.      p-value is
0.003571295858539642
Timeseries for "S3" is stationary.      p-value is
0.011274338394491178
Timeseries for "S4" is stationary.      p-value is
0.009377000210500017
Timeseries for "L1" is stationary.      p-value is
0.007358214508015907
Timeseries for "L2" is stationary.      p-value is
0.009166726145432423
Timeseries for "L3" is stationary.      p-value is
0.004101073644607693
Timeseries for "L4" is stationary.      p-value is
0.0028948095280306304
Timeseries for "L5" is stationary.      p-value is
0.004235997270914649
Timeseries for "R1" is stationary.      p-value is
0.008887459005395964
Timeseries for "R2" is stationary.      p-value is
0.006066321673956619
Timeseries for "R3" is stationary.      p-value is
0.0059852511474317895
Timeseries for "R4" is stationary.      p-value is
0.0057033709981046225

```

## 2.2 9. ACF/PACF Charts

```

[45]: # ACF v/s PACF Plot
def acf_pacf_plot(series_sales:pd.Series,series_order:pd.Series)->None:
    fig, (ax1, ax2, ax3, ax4) = plt.subplots(1, 4, figsize=(13, 5))
    # Plot Sales ACF in first cell
    plot_acf(series_sales, ax=ax1)
    ax1.set_title(f'ACF for {series_sales.name} Sales')
    # Plot Sales PACF in second cell
    plot_pacf(series_sales, ax=ax2)
    ax2.set_title(f'PACF for {series_sales.name} Sales')

    # Plot Sales ACF in first cell
    plot_acf(series_order, ax=ax3)
    ax3.set_title(f'ACF for {series_sales.name} Order')

```

```

# Plot Sales PACF in second cell
plot_pacf(series_order, ax=ax4)
ax4.set_title(f'PACF for {series_sales.name} Order')

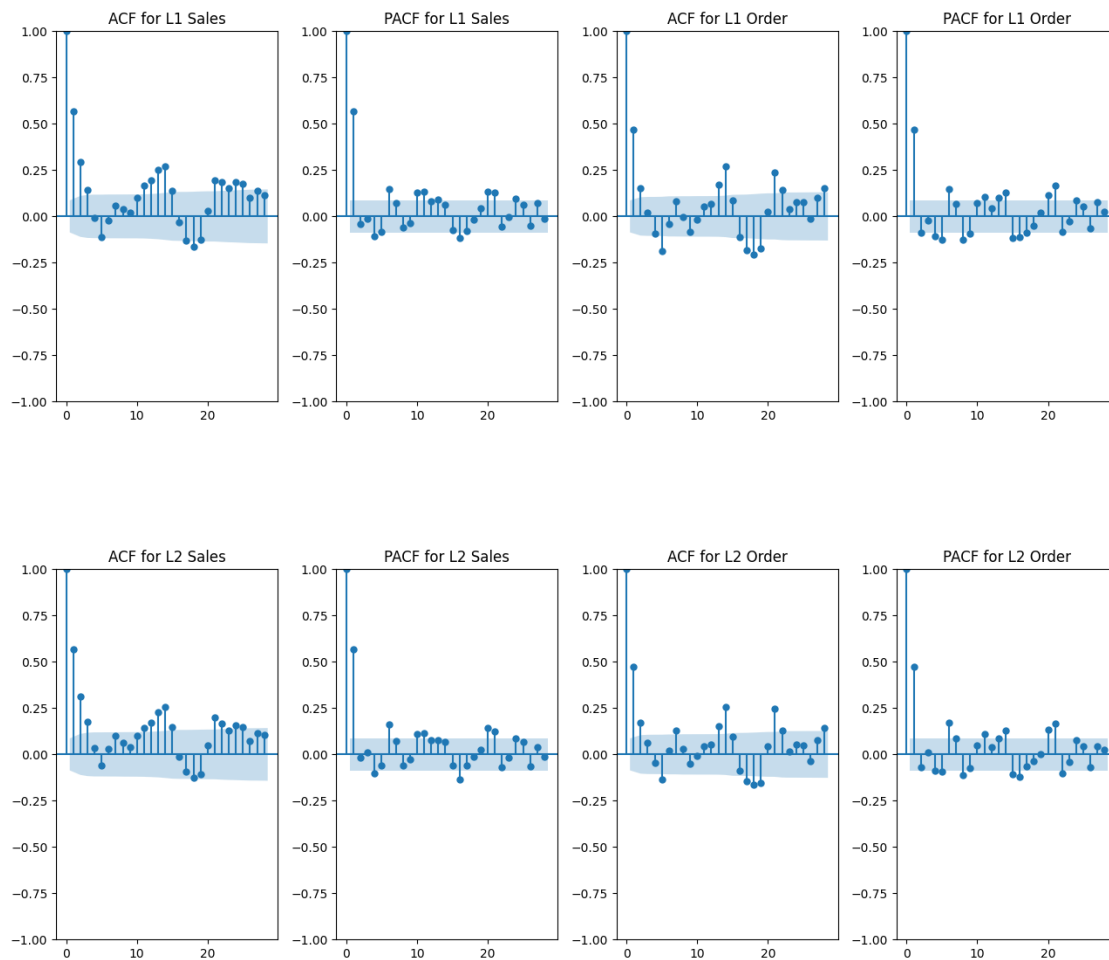
# Adjust layout
plt.tight_layout()
plt.show()

```

```

[46]: # Location Wise Sales and Order ACF/PACF Plot
data_sales = location_wise_sales
data_order = location_wise_order
for column in data_sales.columns:
    acf_pacf_plot(data_sales[column], data_order[column])

```



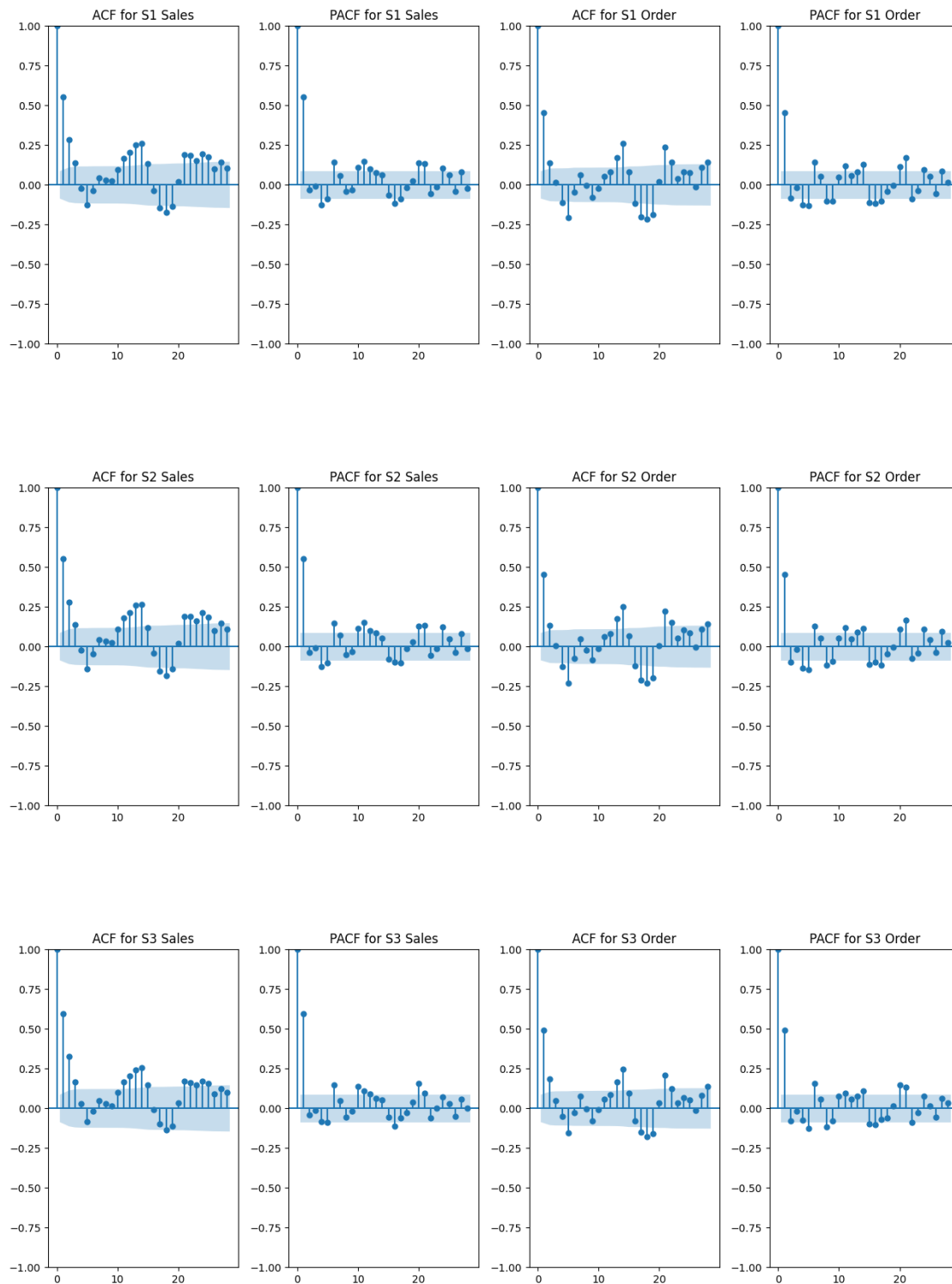


```
[47]: # Store type Wise Sales and Order ACF/PACF Plot
data_sales = store_type_wise_sales
```

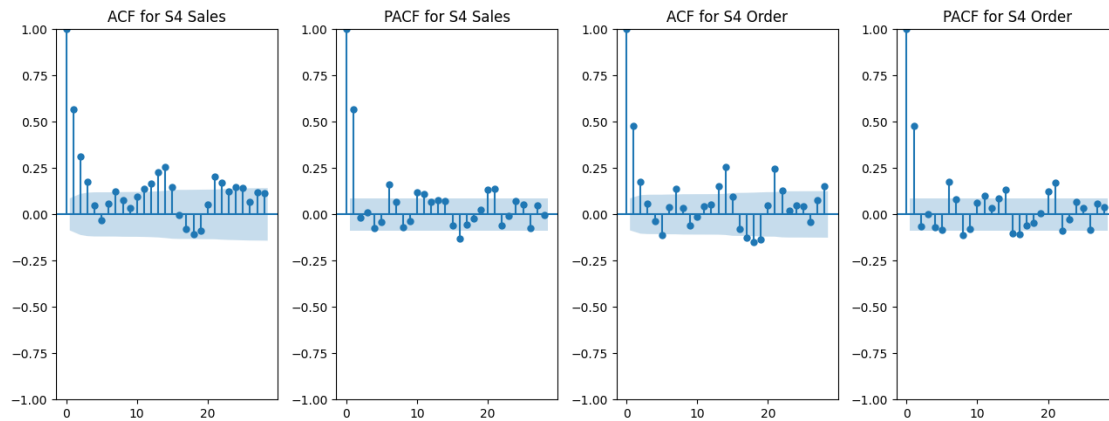
```

data_order = store_type_wise_order
for column in data_sales.columns:
    acf_pacf_plot(data_sales[column], data_order[column])

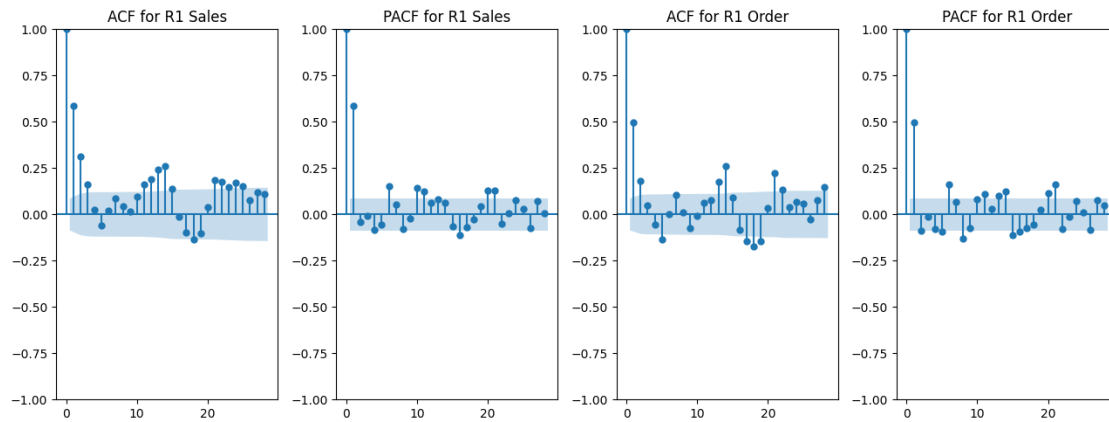
```

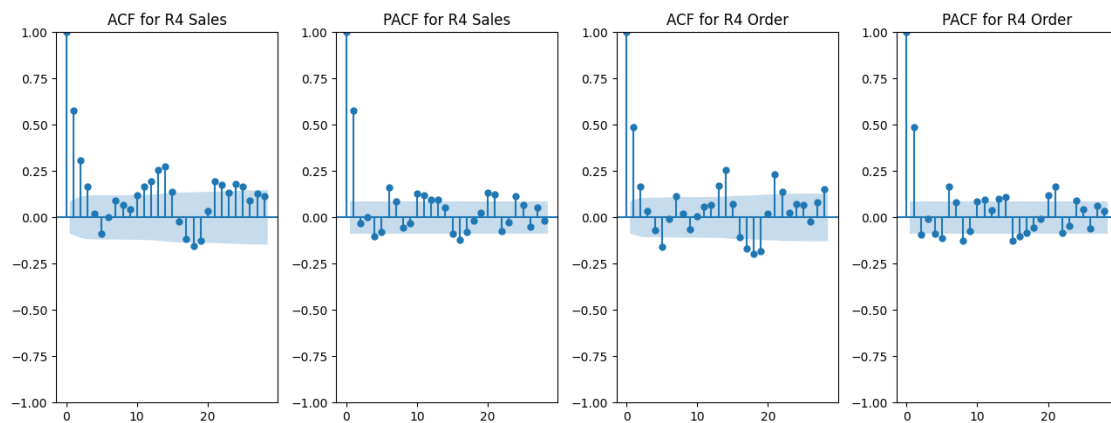
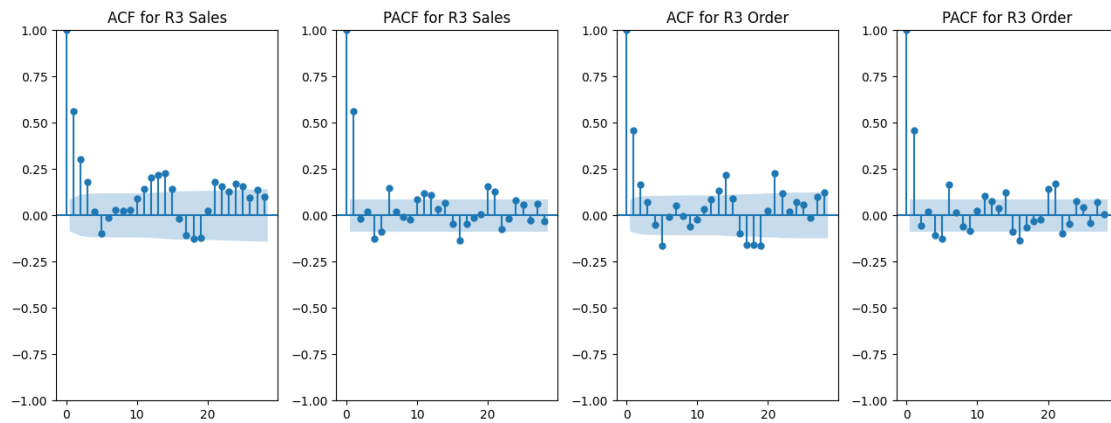
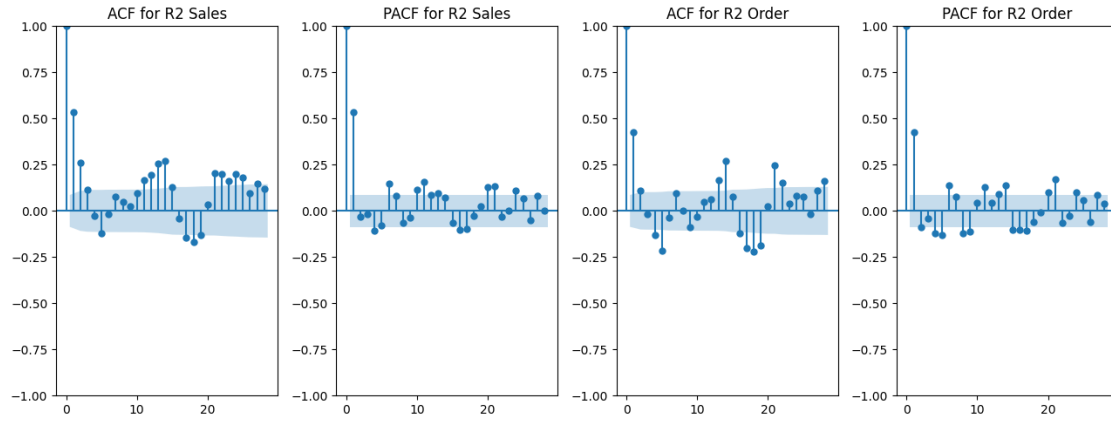






```
[48]: # Region Wise Sales and Order ACF/PACF Plot
data_sales = region_wise_sales
data_order = region_wise_order
for column in data_sales.columns:
    acf_pacf_plot(data_sales[column], data_order[column])
```





## 2.3 10. Seasonality Charts

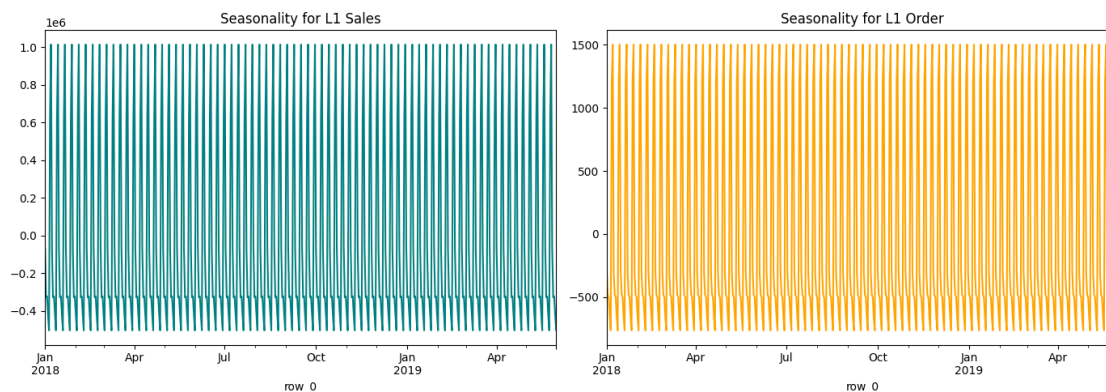
```
[49]: # Seasonality Charts function
from statsmodels.tsa.seasonal import seasonal_decompose

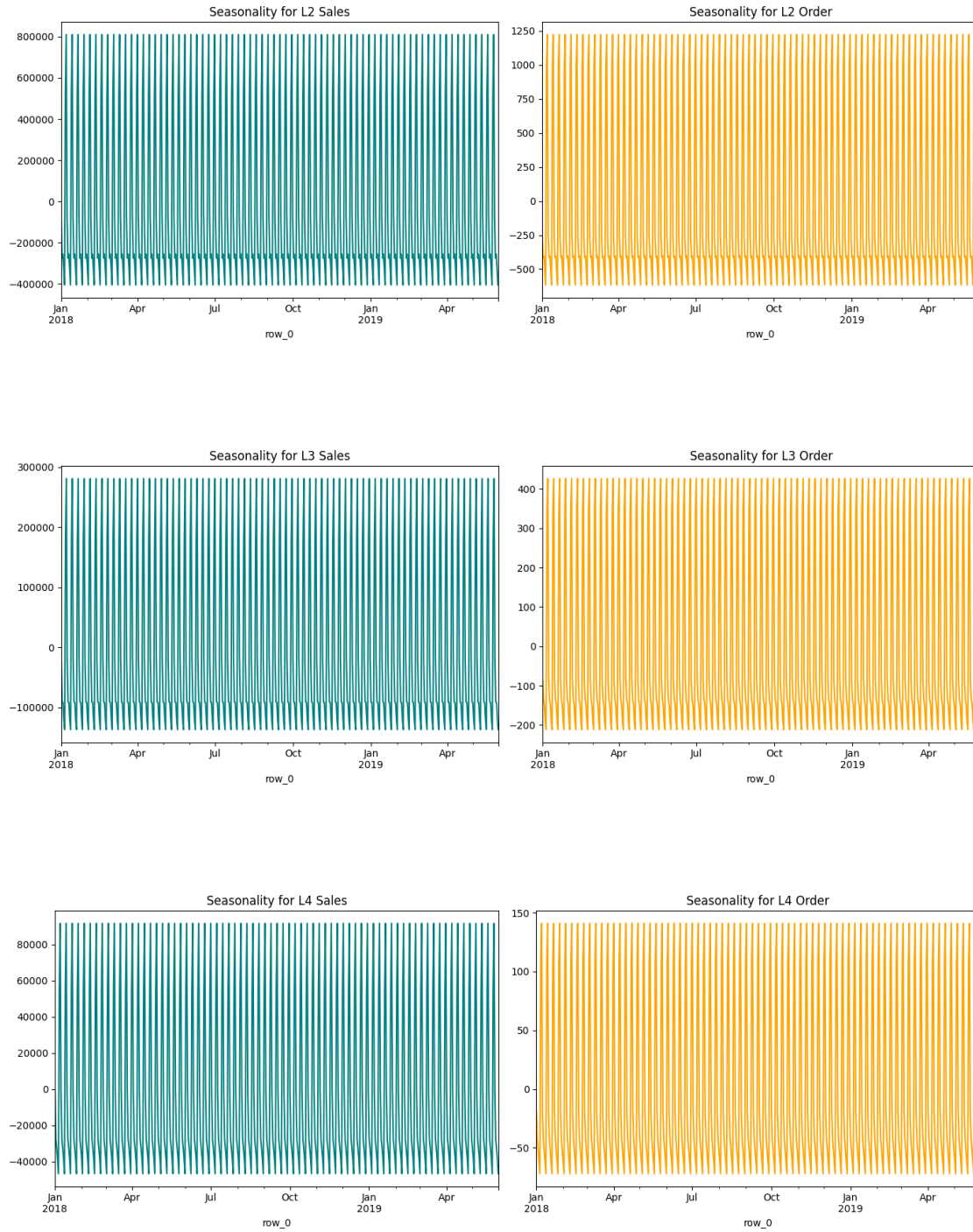
def seasonal_chart(series_sales, series_order):

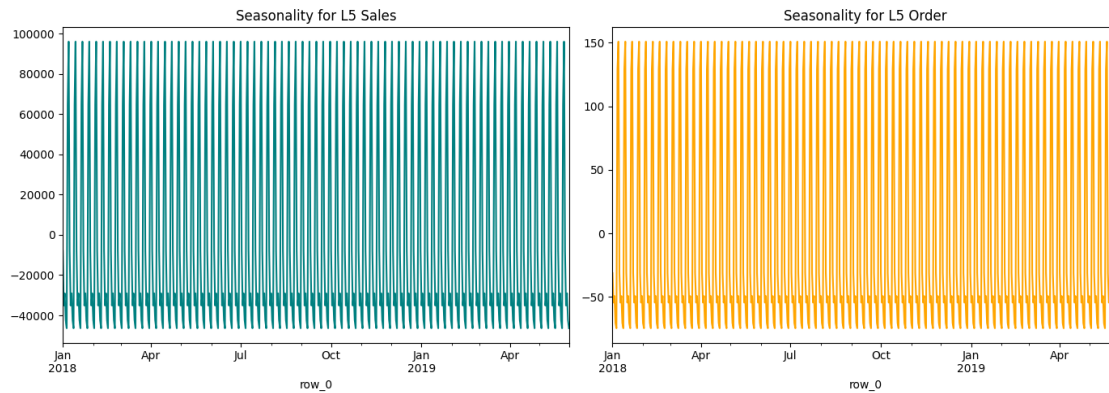
    fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(14, 5))
    # Plot Sales Seasonality in first cell
    result = seasonal_decompose(series_sales, model='additive', period=None)
    result.seasonal.plot(ax=ax1, color='teal')
    ax1.set_title(f'Seasonality for {series_sales.name} Sales')
    # Plot Order Seasonality in second cell
    result = seasonal_decompose(series_order, model='additive', period=None)
    result.seasonal.plot(ax=ax2, color='Orange')
    ax2.set_title(f'Seasonality for {series_order.name} Order')

    # Adjust layout
    plt.tight_layout()
    plt.show()
```

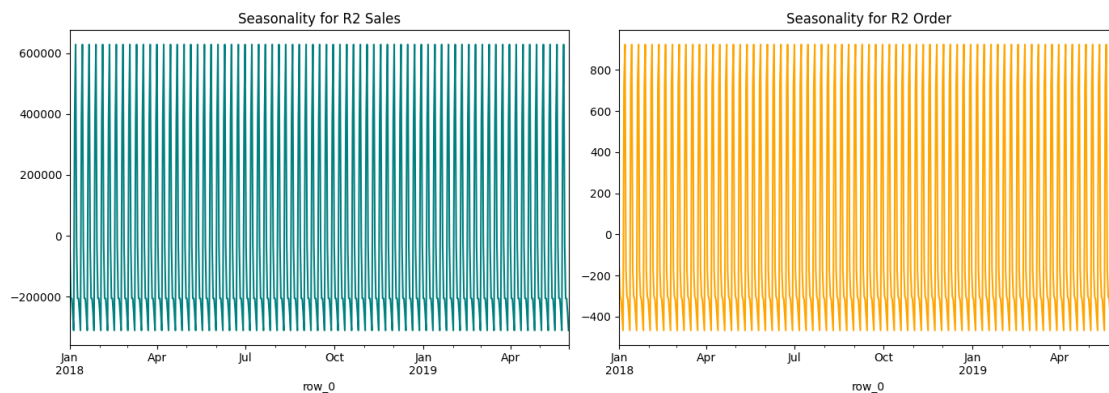
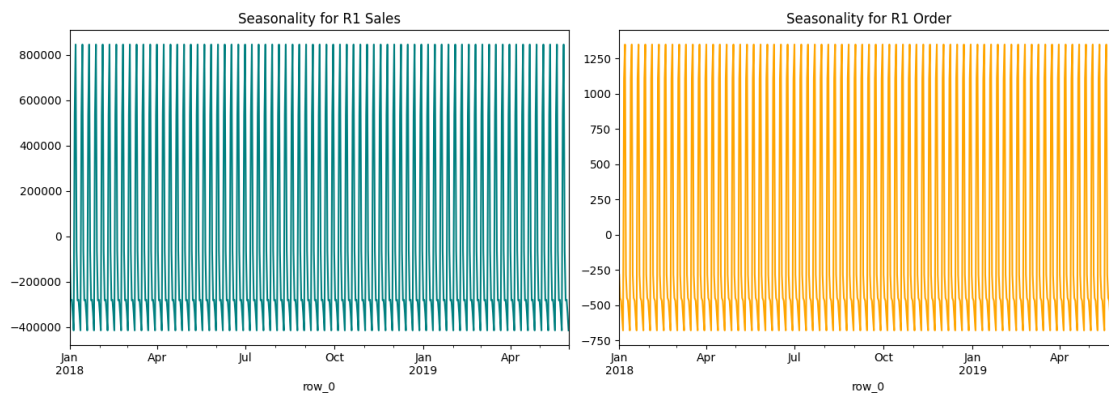
```
[50]: # Location Wise Sales and Order Seasonality Plot
data_sales = location_wise_sales
data_order = location_wise_order
for column in data_sales.columns:
    seasonal_chart(data_sales[column], data_order[column])
```

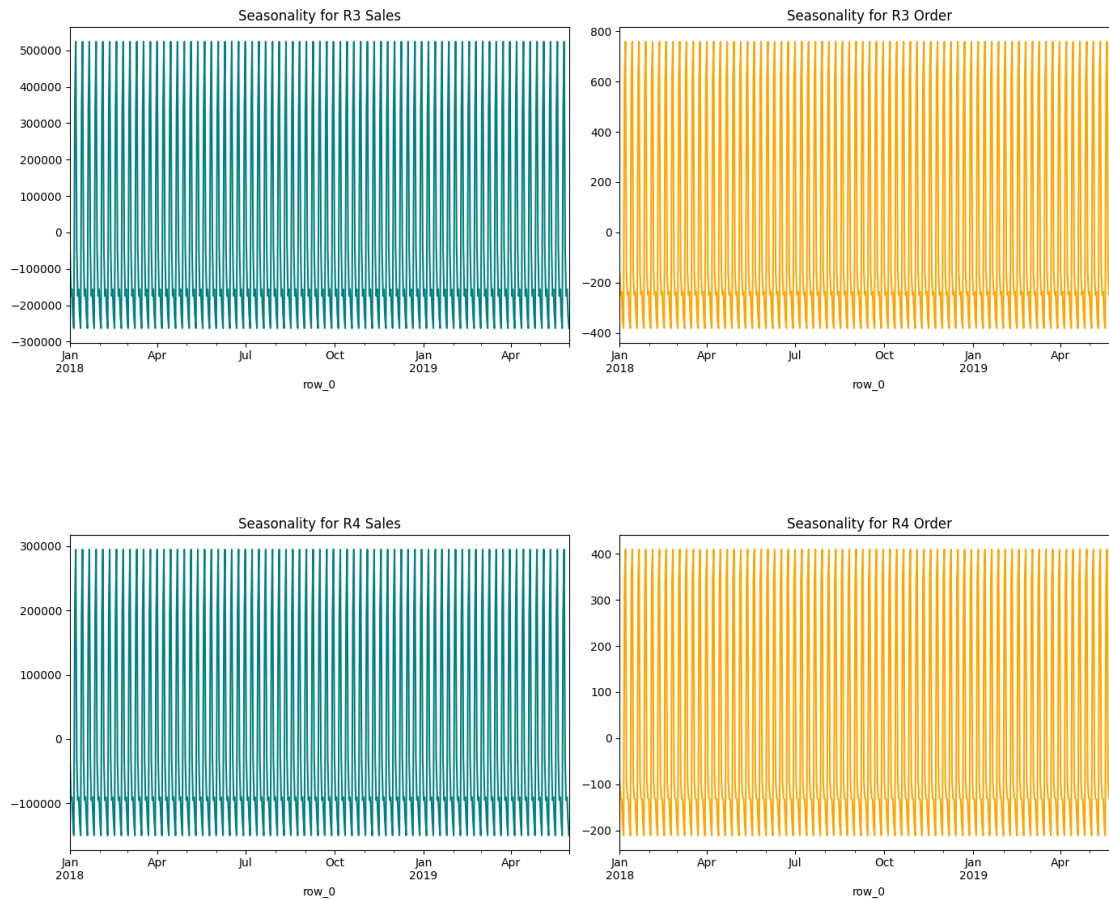




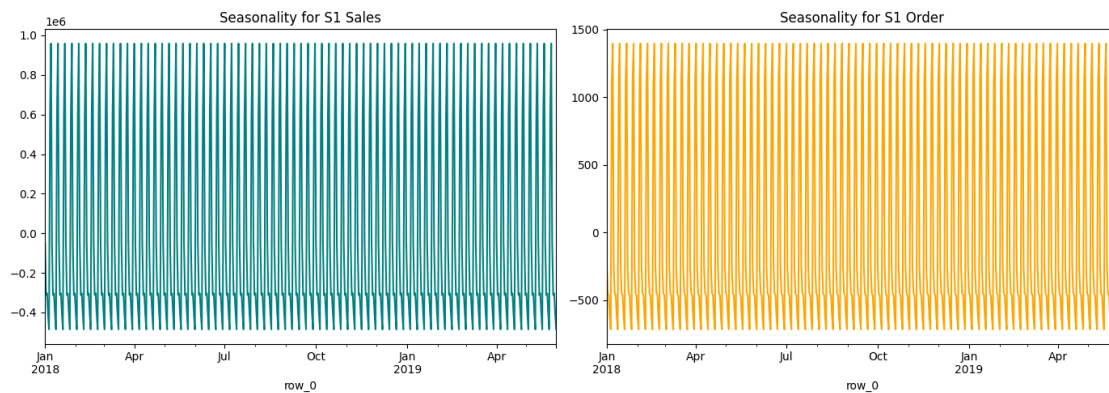


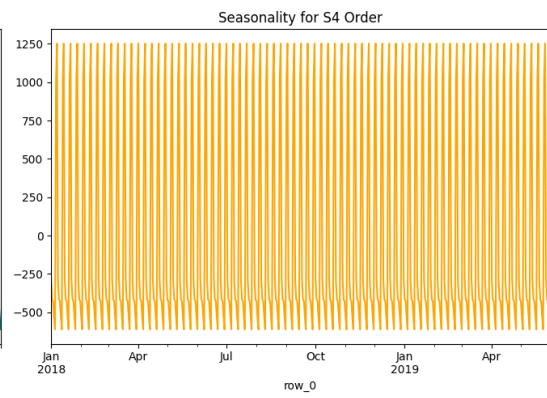
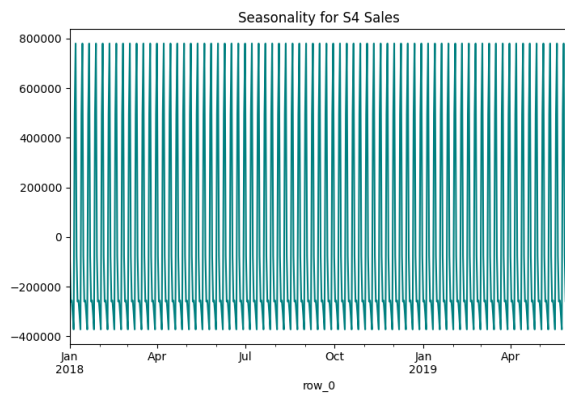
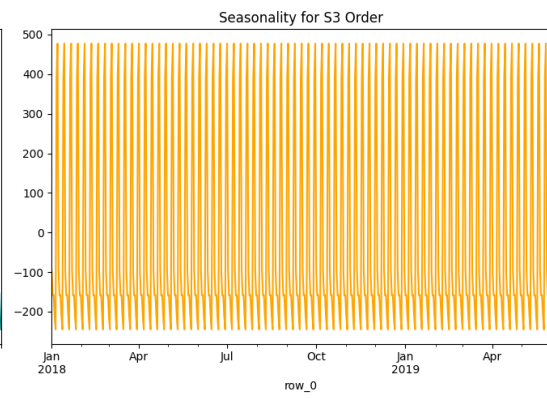
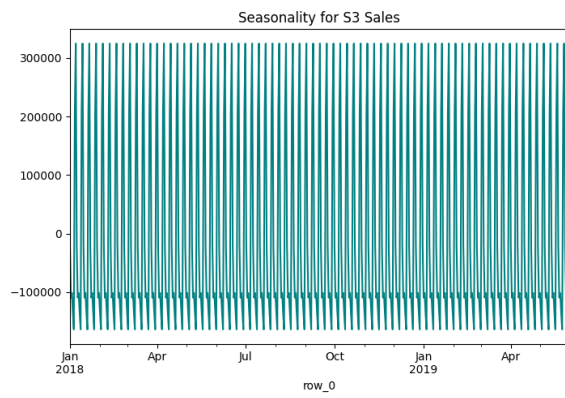
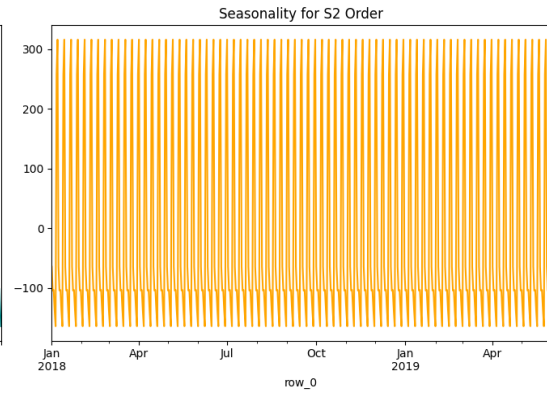
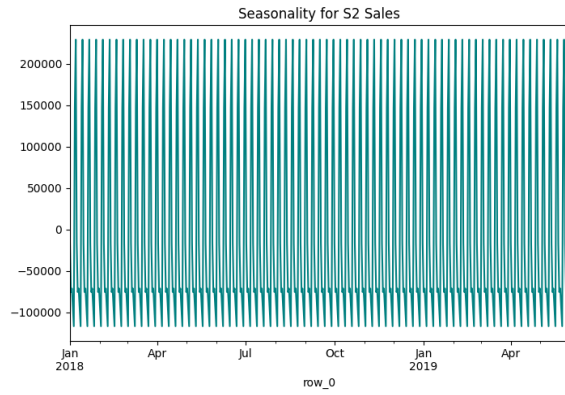
```
[51]: # RRegion Wise Sales and Order Seasonality Plot
data_sales = region_wise_sales
data_order = region_wise_order
for column in data_sales.columns:
    seasonal_chart(data_sales[column], data_order[column])
```





```
[52]: # StoreType Wise Sales and Order Seasonality Plot
data_sales = store_type_wise_sales
data_order = store_type_wise_order
for column in data_sales.columns:
    seasonal_chart(data_sales[column], data_order[column])
```





## 3 C. Model building and Evaluation

### 3.1 10. Data splitting

To build a model we will split data into 80:20 ratio. First 80% rows will be train data whereas remaining 20% will be test data.

```
[53]: # Train/Test splitting stage of pipeline
from sklearn.base import BaseEstimator, TransformerMixin

class TimeSeriesSplitter(BaseEstimator, TransformerMixin):
    def __init__(self, test_size=0.2):
        self.test_size = test_size
        self.train_data, self.test_data = None, None

    def fit(self, X, y=None):
        """No fitting required; just for compatibility."""
        return self

    def transform(self, X, y=None):
        """Split the single-column time series into train and test sets."""
        n_rows = len(X)
        split_index = int(n_rows * (1 - self.test_size))
        self.train_data = X.iloc[:split_index].asfreq('D')
        self.test_data = X.iloc[split_index:].asfreq('D')
        return self.train_data, self.test_data
```

### 3.2 11. SARIMAX Model Training

To have better accuracy in forecasting we will use exogenous variable

#### 3.2.1 Model building preparation

```
[54]: # Seasonality Factor function
def get_seasonal_factor_fft(data:pd.Series)->int:
    """
    Automatically detects seasonality using FFT.
    Args:
        data (pd.Series): Time series data.
    Returns:
        int: Seasonal factor (dominant period).
    """
    fft = np.fft.fft(data - np.mean(data)) # Remove mean for better results
    freqs = np.fft.fftfreq(len(data))
    magnitudes = np.abs(fft)
    dominant_freq = freqs[np.argmax(magnitudes[1:])] + 1 # Ignore zero
    ↪ frequency
```



```

    seasonal_period = int(round(1 / dominant_freq)) if dominant_freq != 0 else_
↪None
    return abs(seasonal_period)

```

```

[55]: for column in train_sales.columns:
        seasonal_factor_fft = get_seasonal_factor_fft(train_sales[column])
        print(f"Detected seasonal factor (FFT) {column}: {seasonal_factor_fft}")

```

```

Detected seasonal factor (FFT) Sales: 12
Detected seasonal factor (FFT) 1: 6
Detected seasonal factor (FFT) 2: 12
Detected seasonal factor (FFT) 3: 172
Detected seasonal factor (FFT) 4: 12
Detected seasonal factor (FFT) 5: 7
Detected seasonal factor (FFT) 6: 13
Detected seasonal factor (FFT) 7: 172
Detected seasonal factor (FFT) 8: 7
Detected seasonal factor (FFT) 9: 12
Detected seasonal factor (FFT) 10: 12
Detected seasonal factor (FFT) 11: 12
Detected seasonal factor (FFT) 12: 12
Detected seasonal factor (FFT) 13: 12
Detected seasonal factor (FFT) 14: 12
Detected seasonal factor (FFT) 15: 7
Detected seasonal factor (FFT) 16: 12
Detected seasonal factor (FFT) 17: 12
Detected seasonal factor (FFT) 18: 7
Detected seasonal factor (FFT) 19: 12
Detected seasonal factor (FFT) 20: 12
Detected seasonal factor (FFT) 21: 172
Detected seasonal factor (FFT) 22: 172
Detected seasonal factor (FFT) 23: 12
Detected seasonal factor (FFT) 24: 3
Detected seasonal factor (FFT) 25: 172
Detected seasonal factor (FFT) 26: 172
Detected seasonal factor (FFT) 27: 12
Detected seasonal factor (FFT) 28: 12
Detected seasonal factor (FFT) 29: 12
Detected seasonal factor (FFT) 30: 12
Detected seasonal factor (FFT) 31: 12
Detected seasonal factor (FFT) 32: 172
Detected seasonal factor (FFT) 33: 12
Detected seasonal factor (FFT) 34: 12
Detected seasonal factor (FFT) 35: 7
Detected seasonal factor (FFT) 36: 13
Detected seasonal factor (FFT) 37: 12
Detected seasonal factor (FFT) 38: 12

```

Detected seasonal factor (FFT) 39: 13  
 Detected seasonal factor (FFT) 40: 12  
 Detected seasonal factor (FFT) 41: 12  
 Detected seasonal factor (FFT) 42: 172  
 Detected seasonal factor (FFT) 43: 12  
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 Detected seasonal factor (FFT) 45: 13  
 Detected seasonal factor (FFT) 46: 12  
 Detected seasonal factor (FFT) 47: 12  
 Detected seasonal factor (FFT) 48: 12  
 Detected seasonal factor (FFT) 49: 7  
 Detected seasonal factor (FFT) 50: 12  
 Detected seasonal factor (FFT) 51: 12  
 Detected seasonal factor (FFT) 52: 12  
 Detected seasonal factor (FFT) 53: 3  
 Detected seasonal factor (FFT) 54: 12  
 Detected seasonal factor (FFT) 55: 12  
 Detected seasonal factor (FFT) 56: 12  
 Detected seasonal factor (FFT) 57: 103  
 Detected seasonal factor (FFT) 58: 516  
 Detected seasonal factor (FFT) 59: 12  
 Detected seasonal factor (FFT) 60: 3  
 Detected seasonal factor (FFT) 61: 12  
 Detected seasonal factor (FFT) 62: 12  
 Detected seasonal factor (FFT) 63: 12  
 Detected seasonal factor (FFT) 64: 7  
 Detected seasonal factor (FFT) 65: 516  
 Detected seasonal factor (FFT) 66: 13  
 Detected seasonal factor (FFT) 67: 13  
 Detected seasonal factor (FFT) 68: 12  
 Detected seasonal factor (FFT) 69: 7  
 Detected seasonal factor (FFT) 70: 7  
 Detected seasonal factor (FFT) 71: 12  
 Detected seasonal factor (FFT) 72: 12  
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 Detected seasonal factor (FFT) 74: 13  
 Detected seasonal factor (FFT) 75: 12  
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 Detected seasonal factor (FFT) 78: 13  
 Detected seasonal factor (FFT) 79: 13  
 Detected seasonal factor (FFT) 80: 12  
 Detected seasonal factor (FFT) 81: 12  
 Detected seasonal factor (FFT) 82: 172  
 Detected seasonal factor (FFT) 83: 12  
 Detected seasonal factor (FFT) 84: 12  
 Detected seasonal factor (FFT) 85: 12  
 Detected seasonal factor (FFT) 86: 7

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Detected seasonal factor (FFT) 88: 516  
Detected seasonal factor (FFT) 89: 172  
Detected seasonal factor (FFT) 90: 13  
Detected seasonal factor (FFT) 91: 12  
Detected seasonal factor (FFT) 92: 7  
Detected seasonal factor (FFT) 93: 172  
Detected seasonal factor (FFT) 94: 12  
Detected seasonal factor (FFT) 95: 12  
Detected seasonal factor (FFT) 96: 172  
Detected seasonal factor (FFT) 97: 7  
Detected seasonal factor (FFT) 98: 172  
Detected seasonal factor (FFT) 99: 12  
Detected seasonal factor (FFT) 100: 12  
Detected seasonal factor (FFT) 101: 12  
Detected seasonal factor (FFT) 102: 12  
Detected seasonal factor (FFT) 103: 12  
Detected seasonal factor (FFT) 104: 12  
Detected seasonal factor (FFT) 105: 172  
Detected seasonal factor (FFT) 106: 12  
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Detected seasonal factor (FFT) S3: 12  
Detected seasonal factor (FFT) S4: 12  
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Detected seasonal factor (FFT) L2: 12  
Detected seasonal factor (FFT) L3: 12  
Detected seasonal factor (FFT) L4: 12  
Detected seasonal factor (FFT) L5: 12



```

Detected seasonal factor (FFT) R1: 12
Detected seasonal factor (FFT) R2: 12
Detected seasonal factor (FFT) R3: 12
Detected seasonal factor (FFT) R4: 12

```

```

[56]: # Model training stage
from statsmodels.tsa.statespace.sarimax import SARIMAX
from sklearn.base import BaseEstimator
from sklearn.metrics import (make_scorer, mean_squared_error as mse,
    ↪ mean_absolute_error as mae, mean_absolute_percentage_error as mape)
import mlflow.statsmodels # Import mlflow.statsmodels

class SARIMAXEstimator(BaseEstimator):
    def __init__(self, order=(1,0,1), seasonal_order = (1,0,1,12)):
        self.order = order
        self.seasonal_order = seasonal_order
        self.model_ = None

    def fit(self, X, exog=None):
        self.exog_train=exog
        try:
            if isinstance(self.exog_train, pd.Series):
                self.model_ = SARIMAX(X, exog=self.exog_train, order=self.order,
    ↪ seasonal_order=self.seasonal_order).fit(dispatch=False)
            else:
                self.model_ = SARIMAX(X, order=self.order, seasonal_order=self.
    ↪ seasonal_order).fit(dispatch=False)
        except Exception as e:
            print(f"Skipping: order={self.order}, seasonal_order={self.
    ↪ seasonal_order}. Error: {e}")
            self.model_ = None
        return self

    def predict(self, n_steps, exog=None):
        if self.model_ is None:
            return np.full(n_steps, 1E-10)
        try:
            if not isinstance(self.exog_train, pd.Series):
                return self.model_.forecast(steps=n_steps)
            elif isinstance(exog, pd.Series):
                return self.model_.forecast(steps=n_steps, exog=exog[:n_steps])
            else:
                raise ValueError('No exog data provided')
        except Exception as e:
            print(e)
        return None

```

```

def score(self, X, exog=None):
    n_steps = len(X)
    predictions = self.predict(n_steps, exog)
    return mape(X, predictions)

```

```

[57]: #@title Define the parameter grid
from itertools import product
p,d,q = range(1,2), [1], range(1, 2)
order = list(product(p, d, q))

# seasonal_parameters P, D, Q, S
P, D, Q, S = range(1, 2), [0], range(1, 2), [7]
seasonal_order = list(product(P, D, Q, S))

param_grid = list(product(order, seasonal_order))

```

### 3.2.2 Model Training with MLFlow

```

[58]: # Model training for sales forecasting with MLFlow
import cloudpickle
import tempfile
import os

mlflow.set_experiment("Sore ID Sales Forecasting-1.1.0")
for column in train_sales.columns[0:1]:
    splitter = TimeSeriesSplitter()
    X_train, X_test = splitter.fit_transform(train_sales[column])
    X_train_exog, X_test_exog = splitter.fit_transform(exog_train_holiday)
    for order, seasonal in param_grid:
        with mlflow.start_run():
            sarimax_estimator = SARIMAXEstimator(order=order, seasonal_order=seasonal)
            sarimax_estimator.fit(X=X_train, exog=X_train_exog)

            if sarimax_estimator.model_ is not None:
                model_score = sarimax_estimator.score(X=X_test, exog=X_test_exog)
                mlflow.set_tag('data', column)
                mlflow.log_params({'order': order, 'seasonal_order': seasonal})
                mlflow.log_metric('mape', model_score)

# Manually save the model as a pickle file and log it as an artifact
                with tempfile.TemporaryDirectory() as tmpdir:
                    model_path = os.path.join(tmpdir, "model.pkl")
                    with open(model_path, "wb") as f:
                        cloudpickle.dump(sarimax_estimator.model_, f)
                    # Log the model.pkl directly at the root of the artifacts
                    mlflow.log_artifact(model_path)

```

```
else:
    print(f"Model fitting failed for column {column} with order={order},␣
↳seasonal_order={seasonal}. Skipping logging of model artifact.")
```

```
2025/12/23 16:45:03 INFO mlflow.store.db.utils: Creating initial MLflow database
tables...
2025/12/23 16:45:03 INFO mlflow.store.db.utils: Updating database tables
2025/12/23 16:45:03 INFO alembic.runtime.migration: Context impl SQLiteImpl.
2025/12/23 16:45:03 INFO alembic.runtime.migration: Will assume non-
transactional DDL.
2025/12/23 16:45:03 INFO alembic.runtime.migration: Running upgrade ->
451aebb31d03, add metric step
2025/12/23 16:45:03 INFO alembic.runtime.migration: Running upgrade 451aebb31d03
-> 90e64c465722, migrate user column to tags
2025/12/23 16:45:03 INFO alembic.runtime.migration: Running upgrade 90e64c465722
-> 181f10493468, allow nulls for metric values
2025/12/23 16:45:03 INFO alembic.runtime.migration: Running upgrade 181f10493468
-> df50e92ffc5e, Add Experiment Tags Table
2025/12/23 16:45:03 INFO alembic.runtime.migration: Running upgrade df50e92ffc5e
-> 7ac759974ad8, Update run tags with larger limit
2025/12/23 16:45:03 INFO alembic.runtime.migration: Running upgrade 7ac759974ad8
-> 89d4b8295536, create latest metrics table
2025/12/23 16:45:03 INFO alembic.runtime.migration: Running upgrade 89d4b8295536
-> 2b4d017a5e9b, add model registry tables to db
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 2b4d017a5e9b
-> cfd24bdc0731, Update run status constraint with killed
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade cfd24bdc0731
-> 0a8213491aaa, drop_duplicate_killed_constraint
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 0a8213491aaa
-> 728d730b5ebd, add registered model tags table
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 728d730b5ebd
-> 27a6a02d2cf1, add model version tags table
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 27a6a02d2cf1
-> 84291f40a231, add run_link to model_version
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 84291f40a231
-> a8c4a736bde6, allow nulls for run_id
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade a8c4a736bde6
-> 39d1c3be5f05, add_is_nan_constraint_for_metrics_tables_if_necessary
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 39d1c3be5f05
-> c48cb773bb87, reset_default_value_for_is_nan_in_metrics_table_for_mysql
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade c48cb773bb87
-> bd07f7e963c5, create index on run_uuid
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade bd07f7e963c5
-> 0c779009ac13, add deleted_time field to runs table
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 0c779009ac13
-> cc1f77228345, change param value length to 500
2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade cc1f77228345
```

-> 97727af70f4d, Add creation\_time and last\_update\_time to experiments table  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 97727af70f4d  
 -> 3500859a5d39, Add Model Aliases table  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 3500859a5d39  
 -> 7f2a7d5fae7d, add datasets inputs input\_tags tables  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 7f2a7d5fae7d  
 -> 2d6e25af4d3e, increase max param val length from 500 to 8000  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 2d6e25af4d3e  
 -> acf3f17fdcc7, add storage location field to model versions  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade acf3f17fdcc7  
 -> 867495a8f9d4, add trace tables  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 867495a8f9d4  
 -> 5b0e9adcef9c, add cascade deletion to trace tables foreign keys  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 5b0e9adcef9c  
 -> 4465047574b1, increase max dataset schema size  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 4465047574b1  
 -> f5a4f2784254, increase run tag value limit to 8000  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade f5a4f2784254  
 -> 0584bdc529eb, add cascading deletion to datasets from experiments  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 0584bdc529eb  
 -> 400f98739977, add logged model tables  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 400f98739977  
 -> 6953534de441, add step to inputs table  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 6953534de441  
 -> bda7b8c39065, increase\_model\_version\_tag\_value\_limit  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade bda7b8c39065  
 -> cbc13b556ace, add V3 trace schema columns  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade cbc13b556ace  
 -> 770bee3ae1dd, add assessments table  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 770bee3ae1dd  
 -> a1b2c3d4e5f6, add spans table  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade a1b2c3d4e5f6  
 -> de4033877273, create entity\_associations table  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade de4033877273  
 -> 1a0cddfcaa16, Add webhooks and webhook\_events tables  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 1a0cddfcaa16  
 -> 534353b11cbc, add scorer tables  
 2025/12/23 16:45:04 INFO alembic.runtime.migration: Running upgrade 534353b11cbc  
 -> 71994744cf8e, add evaluation datasets  
 2025/12/23 16:45:05 INFO alembic.runtime.migration: Running upgrade 71994744cf8e  
 -> 3da73c924c2f, add outputs to dataset record  
 2025/12/23 16:45:05 INFO alembic.runtime.migration: Running upgrade 3da73c924c2f  
 -> bf29a5ff90ea, add jobs table  
 2025/12/23 16:45:05 INFO alembic.runtime.migration: Running upgrade bf29a5ff90ea  
 -> 1bd49d398cd23, add secrets tables  
 2025/12/23 16:45:05 INFO alembic.runtime.migration: Context impl SQLiteImpl.  
 2025/12/23 16:45:05 INFO alembic.runtime.migration: Will assume non-  
 transactional DDL.

2025/12/23 16:45:05 INFO mlflow.tracking.fluent: Experiment with name 'Sore ID Sales Forecasting-1.1.0' does not exist. Creating a new experiment.

```
[59]: # Model training for order forecasting with MLFlow
import cloudpickle
import tempfile
import os

mlflow.set_experiment("Sore ID Order Forecasting-1.1.0")
for column in train_order.columns[0:1]:
    splitter = TimeSeriesSplitter()
    X_train, X_test = splitter.fit_transform(train_order[column])
    X_train_exog, X_test_exog = splitter.fit_transform(exog_train_holiday)
    for order, seasonal in param_grid:
        with mlflow.start_run():
            sarimax_estimator = SARIMAXEstimator(order=order, seasonal_order=seasonal)
            sarimax_estimator.fit(X=X_train, exog=X_train_exog)

            if sarimax_estimator.model_ is not None:
                model_score = sarimax_estimator.score(X=X_test, exog=X_test_exog)
                mlflow.set_tag('data', column)
                mlflow.log_params({'order': order, 'seasonal_order': seasonal})
                mlflow.log_metric('mape', model_score)

                # Manually save the model as a pickle file and log it as an artifact
                with tempfile.TemporaryDirectory() as tmpdir:
                    model_path = os.path.join(tmpdir, "model.pkl")
                    with open(model_path, "wb") as f:
                        cloudpickle.dump(sarimax_estimator.model_, f)
                    # Log the model.pkl directly at the root of the artifacts
                    mlflow.log_artifact(model_path)

            else:
                print(f"Model fitting failed for column {column} with order={order}, seasonal_order={seasonal}. Skipping logging of model artifact.")
```

2025/12/23 16:45:06 INFO mlflow.tracking.fluent: Experiment with name 'Sore ID Order Forecasting-1.1.0' does not exist. Creating a new experiment.

## 4 D. Forecasting Example

```
[60]: import mlflow
import pandas as pd
import shutil
import os
import cloudpickle # Import cloudpickle for loading
```

```

# Create 'models' directory if it's not exist
if not os.path.exists('models'):
    os.makedirs('models')

# Get the MLflow client
client = mlflow.tracking.MlflowClient()

# Get the experiment by name for Order Forecasting
order_experiment = client.get_experiment_by_name("Sore ID Order Forecasting-1.1.
↳0")

if order_experiment is None:
    print("MLflow experiment 'Sore ID Order Forecasting-1.1.0' not found.␣
↳Please ensure the model training step was executed.")
else:
    order_exp_id = order_experiment.experiment_id

    # Search for runs within this experiment, ordered by MAPE ascending
    # Assuming 'Order' is the column name for the overall order forecasting
    runs = client.search_runs(
        experiment_ids=[order_exp_id],
        filter_string="tags.data = 'Order'", # Filter for the specific 'Order'␣
↳data tag
        order_by=["metrics.mape ASC"], # Order by MAPE to find the best model
        max_results=1 # We only need the best one
    )

    if runs:
        best_run = runs[0]
        run_id = best_run.info.run_id
        data_tag = best_run.data.tags.get('data') # This should be 'Order'

        print(f"Found best run for '{data_tag}' forecasting: Run ID {run_id},␣
↳MAPE {best_run.data.metrics.get('mape')}")

        # Define a temporary path to download artifacts for this run
        temp_download_dir = os.path.join('mlflow_temp_artifacts', run_id)
        os.makedirs(temp_download_dir, exist_ok=True)

        # Download the 'model.pkl' artifact (logged directly at root)
        artifact_uri_to_download = client.get_run(run_id).info.artifact_uri + '/'
↳model.pkl'
        mlflow.artifacts.
↳download_artifacts(artifact_uri=artifact_uri_to_download,␣
↳dst_path=temp_download_dir)

```

```

    # The actual model file is now at temp_download_dir/model.pkl
    source_model_path = os.path.join(temp_download_dir, 'model.pkl')
    destination_filename = os.path.join('models', f'{data_tag.
↳lower()}_order.pkl')

    # Move the model.pkl to its final destination
    shutil.move(source_model_path, destination_filename)
    print(f"Model for '{data_tag}' saved to {destination_filename}")

    # Clean up the temporary download directory
    shutil.rmtree(temp_download_dir)

else:
    print("No runs found for 'Order' in 'Sore ID Order Forecasting-1.1.0'↳
↳experiment. Cannot save model.")

```

Found best run for 'Order' forecasting: Run ID 73d81e6dbd01429aa5b060f8e6de65f2, MAPE 0.15094690023597634

Downloading artifacts: 0%| | 0/1 [00:00<?, ?it/s]

Model for 'Order' saved to models/order\_order.pkl

```

[61]: import mlflow
import pandas as pd
import shutil
import os
import cloudpickle

# Get the MLflow client
client = mlflow.tracking.MlflowClient()

# Get the experiment by name for Sales Forecasting
sales_experiment = client.get_experiment_by_name("Sore ID Sales Forecasting-1.1.
↳0")

if sales_experiment is None:
    print("MLflow experiment 'Sore ID Sales Forecasting-1.1.0' not found.↳
↳Please ensure the model training step was executed.")
else:
    sales_exp_id = sales_experiment.experiment_id

    # Search for runs within this experiment, ordered by MAPE ascending
    # Assuming 'Sales' is the column name for the overall sales forecasting
    runs = client.search_runs(
        experiment_ids=[sales_exp_id],
        filter_string="tags.data = 'Sales'", # Filter for the specific 'Sales'↳
↳data tag

```

```

        order_by=["metrics.mape ASC"], # Order by MAPE to find the best model
        max_results=1 # We only need the best one
    )

    if runs:
        best_run = runs[0]
        run_id = best_run.info.run_id
        data_tag = best_run.data.tags.get('data') # This should be 'Sales'

        print(f"Found best run for '{data_tag}' forecasting: Run ID {run_id},  

↳MAPE {best_run.data.metrics.get('mape')}")

        # Define a temporary path to download artifacts for this run
        temp_download_dir = os.path.join('mlflow_temp_artifacts', run_id)
        os.makedirs(temp_download_dir, exist_ok=True)

        # Download the 'model.pkl' artifact (logged directly at root)
        artifact_uri_to_download = client.get_run(run_id).info.artifact_uri + '/  

↳model.pkl'
        mlflow.artifacts.  

↳download_artifacts(artifact_uri=artifact_uri_to_download,  

↳dst_path=temp_download_dir)

        # The actual model file is now at temp_download_dir/model.pkl
        source_model_path = os.path.join(temp_download_dir, 'model.pkl')
        destination_filename = os.path.join('models', f'{data_tag}.  

↳lower()}_sales.pkl')

        # Move the model.pkl to its final destination
        shutil.move(source_model_path, destination_filename)
        print(f"Model for '{data_tag}' saved to {destination_filename}")

        # Clean up the temporary download directory
        shutil.rmtree(temp_download_dir)

    else:
        print("No runs found for 'Sales' in 'Sore ID Sales Forecasting-1.1.0'  

↳experiment. Cannot save model.")

```

Found best run for 'Sales' forecasting: Run ID 4c5193f3575947ccb13eb8f9aef568a9,  
MAPE 0.19729424250763192

Downloading artifacts: 0%| | 0/1 [00:00<?, ?it/s]

Model for 'Sales' saved to models/sales\_sales.pkl

```

[62]: import cloudpickle as pickle
      with open('models/sales_sales.pkl', 'rb') as file:

```



```
model = pickle.load(file)
model.summary()
```

[62]:

|                         |                               |                          |           |
|-------------------------|-------------------------------|--------------------------|-----------|
| <b>Dep. Variable:</b>   | Sales                         | <b>No. Observations:</b> | 412       |
| <b>Model:</b>           | SARIMAX(1, 1, 1)x(1, 0, 1, 7) | <b>Log Likelihood</b>    | -6643.432 |
| <b>Date:</b>            | Tue, 23 Dec 2025              | <b>AIC</b>               | 13298.864 |
| <b>Time:</b>            | 16:45:06                      | <b>BIC</b>               | 13322.975 |
| <b>Sample:</b>          | 01-01-2018<br>- 02-16-2019    | <b>HQIC</b>              | 13308.402 |
| <b>Covariance Type:</b> | opg                           |                          |           |

|                | coef       | std err  | z         | P>  z | [0.025    | 0.975]    |
|----------------|------------|----------|-----------|-------|-----------|-----------|
| <b>Holiday</b> | -2.225e+06 | 1.32e-09 | -1.68e+15 | 0.000 | -2.23e+06 | -2.23e+06 |
| <b>ar.L1</b>   | 0.5814     | 0.042    | 13.805    | 0.000 | 0.499     | 0.664     |
| <b>ma.L1</b>   | -0.9989    | 0.021    | -46.864   | 0.000 | -1.041    | -0.957    |
| <b>ar.S.L7</b> | 0.9963     | 0.013    | 74.994    | 0.000 | 0.970     | 1.022     |
| <b>ma.S.L7</b> | -0.9707    | 0.056    | -17.266   | 0.000 | -1.081    | -0.860    |
| <b>sigma2</b>  | 8.338e+12  | 3.67e-15 | 2.27e+27  | 0.000 | 8.34e+12  | 8.34e+12  |

|                                |      |                          |        |
|--------------------------------|------|--------------------------|--------|
| <b>Ljung-Box (L1) (Q):</b>     | 0.55 | <b>Jarque-Bera (JB):</b> | 507.31 |
| <b>Prob(Q):</b>                | 0.46 | <b>Prob(JB):</b>         | 0.00   |
| <b>Heteroskedasticity (H):</b> | 0.85 | <b>Skew:</b>             | -0.65  |
| <b>Prob(H) (two-sided):</b>    | 0.34 | <b>Kurtosis:</b>         | 8.29   |

Warnings:

- [1] Covariance matrix calculated using the outer product of gradients (complex-step).
- [2] Covariance matrix is singular or near-singular, with condition number 5.91e+41. Standard errors may be unstable.

[63]:

```
# Forecasting values
# Define the number of days to forecast
n = 50

# Re-run splitter to get consistent train/test sets for 'Sales'
# This ensures that X_train_sales, X_test_sales, and X_test_exog_sales align
# with how the model was trained and evaluated.
splitter = TimeSeriesSplitter()
X_train_sales, X_test_sales = splitter.fit_transform(overall_sales['Sales'])
_, X_test_exog_sales = splitter.fit_transform(exog_train_holiday) # Only need
# the test part of exog_train_holiday

# Prepare data for plotting
df_plot = X_train_sales
test_plot = X_test_sales.iloc[:n] # Take the first 'n' days of the actual test
# data
exog_for_pred = X_test_exog_sales.iloc[:n] # Exogenous variables for the
# prediction period
```

```

# Generate predictions using the loaded model
test_plot['pred'] = model.forecast(steps=n, exog=exog_for_pred)

# Create and display the plot
fig = go.Figure()
fig.add_trace(go.Scatter(x=df_plot.index, y=df_plot, mode='lines', name='Train_
↪values', line=dict(color='green'))))
fig.add_trace(go.Scatter(x=test_plot.index, y=test_plot, mode='lines',
↪name='Test values', line=dict(color='orange'))))
fig.add_trace(go.Scatter(x=test_plot.index, y=test_plot['pred'], mode='lines',
↪name='Forecasting', line=dict(color='red'))))
fig.update_layout(title_text='Forecasting of overall Sales', # Updated title_
↪for clarity
                    title_x=0.5, title_y=0.85,
                    legend_x=0)
fig.show()

```

```

[64]: import cloudpickle as pickle
with open('models/sales_sales.pkl', 'rb') as file:
    model = pickle.load(file)
model.summary()

```

```

[64]:

```

|                         |                               |                          |           |
|-------------------------|-------------------------------|--------------------------|-----------|
| <b>Dep. Variable:</b>   | Sales                         | <b>No. Observations:</b> | 412       |
| <b>Model:</b>           | SARIMAX(1, 1, 1)x(1, 0, 1, 7) | <b>Log Likelihood</b>    | -6643.432 |
| <b>Date:</b>            | Tue, 23 Dec 2025              | <b>AIC</b>               | 13298.864 |
| <b>Time:</b>            | 16:45:07                      | <b>BIC</b>               | 13322.975 |
| <b>Sample:</b>          | 01-01-2018                    | <b>HQIC</b>              | 13308.402 |
|                         | - 02-16-2019                  |                          |           |
| <b>Covariance Type:</b> | opg                           |                          |           |

|                | coef       | std err  | z         | P>  z | [0.025    | 0.975]    |
|----------------|------------|----------|-----------|-------|-----------|-----------|
| <b>Holiday</b> | -2.225e+06 | 1.32e-09 | -1.68e+15 | 0.000 | -2.23e+06 | -2.23e+06 |
| <b>ar.L1</b>   | 0.5814     | 0.042    | 13.805    | 0.000 | 0.499     | 0.664     |
| <b>ma.L1</b>   | -0.9989    | 0.021    | -46.864   | 0.000 | -1.041    | -0.957    |
| <b>ar.S.L7</b> | 0.9963     | 0.013    | 74.994    | 0.000 | 0.970     | 1.022     |
| <b>ma.S.L7</b> | -0.9707    | 0.056    | -17.266   | 0.000 | -1.081    | -0.860    |
| <b>sigma2</b>  | 8.338e+12  | 3.67e-15 | 2.27e+27  | 0.000 | 8.34e+12  | 8.34e+12  |

|                                |      |                          |        |
|--------------------------------|------|--------------------------|--------|
| <b>Ljung-Box (L1) (Q):</b>     | 0.55 | <b>Jarque-Bera (JB):</b> | 507.31 |
| <b>Prob(Q):</b>                | 0.46 | <b>Prob(JB):</b>         | 0.00   |
| <b>Heteroskedasticity (H):</b> | 0.85 | <b>Skew:</b>             | -0.65  |
| <b>Prob(H) (two-sided):</b>    | 0.34 | <b>Kurtosis:</b>         | 8.29   |

Warnings:

- [1] Covariance matrix calculated using the outer product of gradients (complex-step).
- [2] Covariance matrix is singular or near-singular, with condition number 5.91e+41. Standard errors may be unstable.

```
[65]: sub_to_forecast = 'Sales' # Changed to 'Sales' to match the loaded overall
      ↪ sales model
n = 50 # Number of days

# Create splitter instance
splitter = TimeSeriesSplitter()

# Split the overall sales data and the exogenous holiday data for the overall
      ↪ sales model
X_train_data, X_test_data = splitter.
      ↪ fit_transform(overall_sales[sub_to_forecast])
_, X_test_exog_data = splitter.fit_transform(exog_train_holiday)

# Use the 'n' variable to define the length of the test data for plotting and
      ↪ forecasting
test_plot_data = X_test_data.iloc[:n] # Actual test values for the first 'n'
      ↪ days
exog_for_forecast = X_test_exog_data.iloc[:n] # Exogenous variables for the
      ↪ forecast period

# The model 'model' is already loaded from 'models/sales_sales.pkl' in cell
      ↪ PYOujvumwZaw

# Generate predictions using the loaded model
test_plot_data['pred'] = model.forecast(steps=n, exog=exog_for_forecast)

fig = go.Figure()
fig.add_trace(go.Scatter(x=X_train_data.index, y=X_train_data, mode='lines',
      ↪ name='Train values', line=dict(color='green'))))
fig.add_trace(go.Scatter(x=test_plot_data.index, y=test_plot_data,
      ↪ mode='lines', name='Test values', line=dict(color='orange'))))
fig.add_trace(go.Scatter(x=test_plot_data.index, y=test_plot_data['pred'],
      ↪ mode='lines', name='Forecasting', line=dict(color='red'))))
fig.update_layout(title_text=f'Forecasting of {sub_to_forecast}',
                  title_x=0.5, title_y=0.85,
                  legend_x=0)
fig.show()
```

```
[66]: import cloudpickle as pickle
      with open('models/order_order.pkl', 'rb') as file:
          model = pickle.load(file)
      model.summary()
```

[66]:

|                         |                               |                          |           |
|-------------------------|-------------------------------|--------------------------|-----------|
| <b>Dep. Variable:</b>   | Order                         | <b>No. Observations:</b> | 412       |
| <b>Model:</b>           | SARIMAX(1, 1, 1)x(1, 0, 1, 7) | <b>Log Likelihood</b>    | -3938.587 |
| <b>Date:</b>            | Tue, 23 Dec 2025              | <b>AIC</b>               | 7889.174  |
| <b>Time:</b>            | 16:45:07                      | <b>BIC</b>               | 7913.286  |
| <b>Sample:</b>          | 01-01-2018<br>- 02-16-2019    | <b>HQIC</b>              | 7898.713  |
| <b>Covariance Type:</b> | opg                           |                          |           |

|                | coef       | std err | z        | P>  z | [0.025    | 0.975]    |
|----------------|------------|---------|----------|-------|-----------|-----------|
| <b>Holiday</b> | -3412.0755 | 640.458 | -5.328   | 0.000 | -4667.350 | -2156.801 |
| <b>ar.L1</b>   | 0.5009     | 0.041   | 12.166   | 0.000 | 0.420     | 0.582     |
| <b>ma.L1</b>   | -0.9982    | 0.011   | -91.624  | 0.000 | -1.020    | -0.977    |
| <b>ar.S.L7</b> | 0.9961     | 0.013   | 79.606   | 0.000 | 0.972     | 1.021     |
| <b>ma.S.L7</b> | -0.9644    | 0.059   | -16.368  | 0.000 | -1.080    | -0.849    |
| <b>sigma2</b>  | 1.711e+07  | 0.094   | 1.83e+08 | 0.000 | 1.71e+07  | 1.71e+07  |

|                                |      |                          |        |
|--------------------------------|------|--------------------------|--------|
| <b>Ljung-Box (L1) (Q):</b>     | 0.25 | <b>Jarque-Bera (JB):</b> | 908.66 |
| <b>Prob(Q):</b>                | 0.62 | <b>Prob(JB):</b>         | 0.00   |
| <b>Heteroskedasticity (H):</b> | 0.77 | <b>Skew:</b>             | -0.99  |
| <b>Prob(H) (two-sided):</b>    | 0.12 | <b>Kurtosis:</b>         | 10.01  |

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

[2] Covariance matrix is singular or near-singular, with condition number 8.16e+24. Standard errors may be unstable.

```
[67]: # Forecasting values
sub_to_forecast = 'Order' # Changed to 'Order' to match the loaded overall_order model
n = 50 # Number of days

# Create splitter instance
splitter = TimeSeriesSplitter()

# Split the overall order data and the exogenous holiday data for the overall_order model
X_train_data_order, X_test_data_order = splitter.fit_transform(overall_order[sub_to_forecast], X_test_exog_data_order = splitter.fit_transform(exog_train_holiday) # Only need the test part of exog_train_holiday

# Use the 'n' variable to define the length of the test data for plotting and forecasting
test_plot_data_order = X_test_data_order.iloc[:n] # Actual test values for the first 'n' days
exog_for_forecast_order = X_test_exog_data_order.iloc[:n] # Exogenous variables for the forecast period
```

```

# The model 'model' is already loaded from 'models/order_order.pkl' in cell
↳ hnZfqILrwZaw

# Generate predictions using the loaded model
test_plot_data_order['pred'] = model.forecast(steps=n,
↳ exog=exog_for_forecast_order)

fig = go.Figure()
fig.add_trace(go.Scatter(x=X_train_data_order.index, y=X_train_data_order,
↳ mode='lines', name='Train values', line=dict(color='green'))))
fig.add_trace(go.Scatter(x=test_plot_data_order.index, y=test_plot_data_order,
↳ mode='lines', name='Test values', line=dict(color='orange'))))
fig.add_trace(go.Scatter(x=test_plot_data_order.index,
↳ y=test_plot_data_order['pred'], mode='lines', name='Forecasting',
↳ line=dict(color='red'))))
fig.update_layout(title_text=f'Forecasting of overall {sub_to_forecast}', #
↳ Updated title for clarity
                    title_x=0.5, title_y=0.85,
                    legend_x=0)
fig.show()

```

## 4.1 Observations

- Sales and Orders move together, when orders increase, sales also increase.
- Discounts lead to higher customer activity compared to non-discount days.
- Sales and orders drop noticeably on holidays.
- Performance varies significantly across Store Type, Location Type, and Region.
- Clear seasonal patterns exist across months and days of the week.
- Time-series statistical tests show the data is suitable for forecasting.

## 4.2 Key Insights

- **Discounts are effective** : They significantly boost both sales and order volume.
- **Holidays negatively impact business** : Lower sales and fewer orders are recorded during holidays.
- **Store characteristics matter** : Store Type, Region, and Location strongly influence performance.
- **Strong seasonality exists** : Sales follow predictable monthly and weekly patterns.
- **Reliable forecasting potential** : Data supports accurate time-series forecasting.

[69]: