

# Product\_Sales\_Forecasting

December 23, 2025

## 1 Product Sales Forecasting

### Project Objective

Need and Use of Product Sales Forecasting Effective sales forecasting is fundamental for multiple aspects of retail management and operation, including:

1. **Inventory Management:** Accurate sales forecasts help ensure that stores maintain optimal inventory levels—enough to meet customer demand without overstocking, which can lead to increased costs or waste, especially in the case of perishable goods.
2. **Financial Planning:** Forecasting sales allows businesses to estimate future revenue and manage budgets more effectively. This is crucial for allocating resources to areas such as marketing, staffing, and capital investments.
3. **Marketing and Promotions:** Understanding when sales peaks and troughs are likely to occur enables retailers to plan effective marketing campaigns and promotional offers to boost revenue or manage customer flow.
4. **Supply Chain Optimization:** Sales forecasts inform production schedules, logistics, and distribution plans, ensuring that products are available where and when they are needed, thereby reducing transportation and storage costs.
5. **Strategic Decision Making:** Long-term sales forecasting supports broader business strategies, including store expansions, market entry, and other capital expenditures.

### 1.1 1. Dataset Loading

```
[80]: # Import Basic libraries
import pandas as pd
import numpy as np

# Import Visualization libraries
import plotly.graph_objs as go
import plotly.express as px
import plotly.io as pio
from plotly.subplots import make_subplots
import matplotlib.pyplot as plt
import seaborn as sns
import warnings
warnings.filterwarnings('ignore')
```

```

# Install MLflow
!pip install mlflow

# Import MLFlow libraries
import mlflow

# Suppress the specific ConvergenceWarning
from statsmodels.tools.sm_exceptions import ConvergenceWarning
warnings.simplefilter("ignore", ConvergenceWarning)

```

```

Requirement already satisfied: mlflow in /usr/local/lib/python3.12/dist-packages
(3.8.0)
Requirement already satisfied: mlflow-skinny==3.8.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (3.8.0)
Requirement already satisfied: mlflow-tracing==3.8.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (3.8.0)
Requirement already satisfied: Flask-CORS<7 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (6.0.2)
Requirement already satisfied: Flask<4 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (3.1.2)
Requirement already satisfied: alembic!=1.10.0,<2 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (1.17.2)
Requirement already satisfied: cryptography<47,>=43.0.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (43.0.3)
Requirement already satisfied: docker<8,>=4.0.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (7.1.0)
Requirement already satisfied: graphene<4 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (3.4.3)
Requirement already satisfied: gunicorn<24 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (23.0.0)
Requirement already satisfied: huey<3,>=2.5.0 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (2.5.5)
Requirement already satisfied: matplotlib<4 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (3.10.0)
Requirement already satisfied: numpy<3 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (2.0.2)
Requirement already satisfied: pandas<3 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (2.2.2)
Requirement already satisfied: pyarrow<23,>=4.0.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (18.1.0)
Requirement already satisfied: scikit-learn<2 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (1.6.1)
Requirement already satisfied: scipy<2 in /usr/local/lib/python3.12/dist-
packages (from mlflow) (1.16.3)
Requirement already satisfied: sqlalchemy<3,>=1.4.0 in
/usr/local/lib/python3.12/dist-packages (from mlflow) (2.0.45)

```

Requirement already satisfied: cachetools<7,>=5.0.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (6.2.4)

Requirement already satisfied: click<9,>=7.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (8.3.1)

Requirement already satisfied: cloudpickle<4 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (3.1.2)

Requirement already satisfied: databricks-sdk<1,>=0.20.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (0.76.0)

Requirement already satisfied: fastapi<1 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (0.123.10)

Requirement already satisfied: gitpython<4,>=3.1.9 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (3.1.45)

Requirement already satisfied: importlib\_metadata!=4.7.0,<9,>=3.7.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (8.7.0)

Requirement already satisfied: opentelemetry-api<3,>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.37.0)

Requirement already satisfied: opentelemetry-proto<3,>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.37.0)

Requirement already satisfied: opentelemetry-sdk<3,>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.37.0)

Requirement already satisfied: packaging<26 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (25.0)

Requirement already satisfied: protobuf<7,>=3.12.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (5.29.5)

Requirement already satisfied: pydantic<3,>=2.0.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (2.12.3)

Requirement already satisfied: python-dotenv<2,>=0.19.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (1.2.1)

Requirement already satisfied: pyyaml<7,>=5.1 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (6.0.3)

Requirement already satisfied: requests<3,>=2.17.3 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (2.32.4)

Requirement already satisfied: sqlparse<1,>=0.4.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (0.5.4)

Requirement already satisfied: typing-extensions<5,>=4.0.0 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow)

(4.15.0)

Requirement already satisfied: uvicorn<1 in /usr/local/lib/python3.12/dist-packages (from mlflow-skinny==3.8.0->mlflow) (0.38.0)

Requirement already satisfied: Mako in /usr/local/lib/python3.12/dist-packages (from alembic!=1.10.0,<2->mlflow) (1.3.10)

Requirement already satisfied: cffi>=1.12 in /usr/local/lib/python3.12/dist-packages (from cryptography<47,>=43.0.0->mlflow) (2.0.0)

Requirement already satisfied: urllib3>=1.26.0 in /usr/local/lib/python3.12/dist-packages (from docker<8,>=4.0.0->mlflow) (2.5.0)

Requirement already satisfied: blinker>=1.9.0 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (1.9.0)

Requirement already satisfied: itsdangerous>=2.2.0 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (2.2.0)

Requirement already satisfied: jinja2>=3.1.2 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (3.1.6)

Requirement already satisfied: markupsafe>=2.1.1 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (3.0.3)

Requirement already satisfied: werkzeug>=3.1.0 in /usr/local/lib/python3.12/dist-packages (from Flask<4->mlflow) (3.1.4)

Requirement already satisfied: graphql-core<3.3,>=3.1 in /usr/local/lib/python3.12/dist-packages (from graphene<4->mlflow) (3.2.7)

Requirement already satisfied: graphql-relay<3.3,>=3.1 in /usr/local/lib/python3.12/dist-packages (from graphene<4->mlflow) (3.2.0)

Requirement already satisfied: python-dateutil<3,>=2.7.0 in /usr/local/lib/python3.12/dist-packages (from graphene<4->mlflow) (2.9.0.post0)

Requirement already satisfied: contourpy>=1.0.1 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (1.3.3)

Requirement already satisfied: cycycler>=0.10 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (0.12.1)

Requirement already satisfied: fonttools>=4.22.0 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (4.61.1)

Requirement already satisfied: kiwisolver>=1.3.1 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (1.4.9)

Requirement already satisfied: pillow>=8 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (11.3.0)

Requirement already satisfied: pyparsing>=2.3.1 in /usr/local/lib/python3.12/dist-packages (from matplotlib<4->mlflow) (3.2.5)

Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.12/dist-packages (from pandas<3->mlflow) (2025.2)

Requirement already satisfied: tzdata>=2022.7 in /usr/local/lib/python3.12/dist-packages (from pandas<3->mlflow) (2025.3)

Requirement already satisfied: joblib>=1.2.0 in /usr/local/lib/python3.12/dist-packages (from scikit-learn<2->mlflow) (1.5.3)

Requirement already satisfied: threadpoolctl>=3.1.0 in /usr/local/lib/python3.12/dist-packages (from scikit-learn<2->mlflow) (3.6.0)

Requirement already satisfied: greenlet>=1 in /usr/local/lib/python3.12/dist-packages (from sqlalchemy<3,>=1.4.0->mlflow) (3.3.0)

Requirement already satisfied: pycparser in /usr/local/lib/python3.12/dist-

packages (from cffi>=1.12->cryptography<47,>=43.0.0->mlflow) (2.23)  
 Requirement already satisfied: google-auth~=2.0 in  
 /usr/local/lib/python3.12/dist-packages (from databricks-sdk<1,>=0.20.0->mlflow-  
 skinny==3.8.0->mlflow) (2.43.0)  
 Requirement already satisfied: starlette<0.51.0,>=0.40.0 in  
 /usr/local/lib/python3.12/dist-packages (from fastapi<1->mlflow-  
 skinny==3.8.0->mlflow) (0.50.0)  
 Requirement already satisfied: annotated-doc>=0.0.2 in  
 /usr/local/lib/python3.12/dist-packages (from fastapi<1->mlflow-  
 skinny==3.8.0->mlflow) (0.0.4)  
 Requirement already satisfied: gitdb<5,>=4.0.1 in  
 /usr/local/lib/python3.12/dist-packages (from gitpython<4,>=3.1.9->mlflow-  
 skinny==3.8.0->mlflow) (4.0.12)  
 Requirement already satisfied: zipp>=3.20 in /usr/local/lib/python3.12/dist-  
 packages (from importlib\_metadata!=4.7.0,<9,>=3.7.0->mlflow-  
 skinny==3.8.0->mlflow) (3.23.0)  
 Requirement already satisfied: opentelemetry-semantic-conventions==0.58b0 in  
 /usr/local/lib/python3.12/dist-packages (from opentelemetry-  
 sdk<3,>=1.9.0->mlflow-skinny==3.8.0->mlflow) (0.58b0)  
 Requirement already satisfied: annotated-types>=0.6.0 in  
 /usr/local/lib/python3.12/dist-packages (from pydantic<3,>=2.0.0->mlflow-  
 skinny==3.8.0->mlflow) (0.7.0)  
 Requirement already satisfied: pydantic-core==2.41.4 in  
 /usr/local/lib/python3.12/dist-packages (from pydantic<3,>=2.0.0->mlflow-  
 skinny==3.8.0->mlflow) (2.41.4)  
 Requirement already satisfied: typing-inspection>=0.4.2 in  
 /usr/local/lib/python3.12/dist-packages (from pydantic<3,>=2.0.0->mlflow-  
 skinny==3.8.0->mlflow) (0.4.2)  
 Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.12/dist-  
 packages (from python-dateutil<3,>=2.7.0->graphene<4->mlflow) (1.17.0)  
 Requirement already satisfied: charset\_normalizer<4,>=2 in  
 /usr/local/lib/python3.12/dist-packages (from requests<3,>=2.17.3->mlflow-  
 skinny==3.8.0->mlflow) (3.4.4)  
 Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.12/dist-  
 packages (from requests<3,>=2.17.3->mlflow-skinny==3.8.0->mlflow) (3.11)  
 Requirement already satisfied: certifi>=2017.4.17 in  
 /usr/local/lib/python3.12/dist-packages (from requests<3,>=2.17.3->mlflow-  
 skinny==3.8.0->mlflow) (2025.11.12)  
 Requirement already satisfied: h11>=0.8 in /usr/local/lib/python3.12/dist-  
 packages (from uvicorn<1->mlflow-skinny==3.8.0->mlflow) (0.16.0)  
 Requirement already satisfied: smmap<6,>=3.0.1 in  
 /usr/local/lib/python3.12/dist-packages (from  
 gitdb<5,>=4.0.1->gitpython<4,>=3.1.9->mlflow-skinny==3.8.0->mlflow) (5.0.2)  
 Requirement already satisfied: pyasn1-modules>=0.2.1 in  
 /usr/local/lib/python3.12/dist-packages (from google-auth~=2.0->databricks-  
 sdk<1,>=0.20.0->mlflow-skinny==3.8.0->mlflow) (0.4.2)  
 Requirement already satisfied: rsa<5,>=3.1.4 in /usr/local/lib/python3.12/dist-  
 packages (from google-auth~=2.0->databricks-sdk<1,>=0.20.0->mlflow-

```
skinny==3.8.0->mlflow) (4.9.1)
Requirement already satisfied: anyio<5,>=3.6.2 in
/usr/local/lib/python3.12/dist-packages (from
starlette<0.51.0,>=0.40.0->fastapi<1->mlflow-skinny==3.8.0->mlflow) (4.12.0)
Requirement already satisfied: pyasn1<0.7.0,>=0.6.1 in
/usr/local/lib/python3.12/dist-packages (from pyasn1-modules>=0.2.1->google-
auth~2.0->databricks-sdk<1,>=0.20.0->mlflow-skinny==3.8.0->mlflow) (0.6.1)
```

```
[81]: # Read
train = pd.read_csv('/content/TRAIN.csv')
test = pd.read_csv('/content/TEST.csv')
```

```
[82]: train.sample(5)
```

```
[82]:
```

	ID	Store_id	Store_Type	Location_Type	Region_Code	Date	\
89253	T1089254	28	S3	L2	R3	2018-09-02	
116479	T1116480	335	S1	L1	R3	2018-11-16	
3532	T1003533	164	S1	L1	R3	2018-01-10	
25050	T1025051	56	S2	L5	R3	2018-03-10	
147425	T1147426	107	S1	L3	R3	2019-02-08	

	Holiday	Discount	#Order	Sales
89253	0	Yes	84	58263.0
116479	0	No	51	28374.0
3532	0	No	46	36276.0
25050	0	No	38	22947.0
147425	0	Yes	96	59616.0

```
[83]: test.sample(5)
```

```
[83]:
```

	ID	Store_id	Store_Type	Location_Type	Region_Code	Date	\
11027	T1199368	251	S2	L3	R1	2019-07-01	
15538	T1203879	163	S1	L2	R3	2019-07-13	
12518	T1200859	344	S1	L5	R1	2019-07-05	
18241	T1206582	265	S2	L4	R2	2019-07-20	
15393	T1203734	233	S1	L3	R3	2019-07-13	

	Holiday	Discount
11027	0	Yes
15538	0	Yes
12518	0	Yes
18241	0	Yes
15393	0	No

## 1.2 2. Observations on Data

```
[84]: train.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 188340 entries, 0 to 188339
Data columns (total 10 columns):
#   Column          Non-Null Count  Dtype
---  -
0   ID              188340 non-null object
1   Store_id        188340 non-null int64
2   Store_Type      188340 non-null object
3   Location_Type   188340 non-null object
4   Region_Code     188340 non-null object
5   Date            188340 non-null object
6   Holiday         188340 non-null int64
7   Discount        188340 non-null object
8   #Order          188340 non-null int64
9   Sales           188340 non-null float64
dtypes: float64(1), int64(3), object(6)
memory usage: 14.4+ MB
```

```
[85]: test.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 22265 entries, 0 to 22264
Data columns (total 8 columns):
#   Column          Non-Null Count  Dtype
---  -
0   ID              22265 non-null object
1   Store_id        22265 non-null int64
2   Store_Type      22265 non-null object
3   Location_Type   22265 non-null object
4   Region_Code     22265 non-null object
5   Date            22265 non-null object
6   Holiday         22265 non-null int64
7   Discount        22265 non-null object
dtypes: int64(2), object(6)
memory usage: 1.4+ MB
```

```
[86]: train.Date = pd.to_datetime(train.Date)
      test.Date = pd.to_datetime(test.Date)
```

```
[87]: train.describe().T
```

```
[87]:
```

	count	mean	min	\
Store_id	188340.0	183.0	1.0	
Date	188340	2018-09-15 12:00:00.000000256	2018-01-01 00:00:00	

Holiday	188340.0	0.131783	0.0
#Order	188340.0	68.205692	0.0
Sales	188340.0	42784.327982	0.0

	25%	50%	75% \
Store_id	92.0	183.0	274.0
Date	2018-05-09 18:00:00	2018-09-15 12:00:00	2019-01-22 06:00:00
Holiday	0.0	0.0	0.0
#Order	48.0	63.0	82.0
Sales	30426.0	39678.0	51909.0

	max	std
Store_id	365.0	105.366308
Date	2019-05-31 00:00:00	NaN
Holiday	1.0	0.338256
#Order	371.0	30.467415
Sales	247215.0	18456.708302

```
[88]: test.describe().T
```

```
[88]:
```

	count	mean	min \
Store_id	22265.0	183.0	1.0
Date	22265	2019-06-30 23:59:59.999999744	2019-06-01 00:00:00
Holiday	22265.0	0.032787	0.0

	25%	50%	75% \
Store_id	92.0	183.0	274.0
Date	2019-06-16 00:00:00	2019-07-01 00:00:00	2019-07-16 00:00:00
Holiday	0.0	0.0	0.0

	max	std
Store_id	365.0	105.368395
Date	2019-07-31 00:00:00	NaN
Holiday	1.0	0.178082

### 1.3 3. Handling missing values and Preprocessing

```
[89]: train_null = train.isna().sum().sum()
test_null = test.isna().sum().sum()
print(f'There are {train_null} nulls in train dataset and {test_null} nulls in_
↳test dataset.')
```

There are 0 nulls in train dataset and 0 nulls in test dataset.

```
[90]: # Define dataset type in separate column for train and test
train['Train'] = True
test['Train'] = False
```



```
[91]: def decorator(func):
    def wrapper(*args, **kwargs):
        print('='*50)
        result = func(*args, **kwargs)
        print('='*50)
        return result
    return wrapper

@decorator
def df_size(df, typ):
    size = df.memory_usage().sum()/(1024**2)
    print(f'Size of {typ} data is: {size:.2f} MB')
    return size
```

```
[92]: # Combine both the dataset into single dataframe
data = pd.concat([train, test])
raw_size = df_size(data, 'Non-Converted')
data.reset_index(drop=True, inplace=True)
# Change Datatypes to optimize sizes
# Store_id as unsigned integer 16 (Range is 1 to 371)
data.Store_id = data.Store_id.astype('uint16')
# Store_Type, Location_Type, Region_Code as categorical
data.Store_Type = data.Store_Type.astype('category')
data.Location_Type = data.Location_Type.astype('category')
data.Region_Code = data.Region_Code.astype('category')
# Holiday and Discount as Boolean
data.Holiday = data.Holiday.astype('bool')
data.replace({'Discount':{'Yes':True, 'No':False}}, inplace=True)
# Drop unnecessary column Transaction ID
data.pop('ID')
data.set_index('Date', inplace=True)
processed_size = df_size(data, 'Converted')
reduction = 100*(raw_size - processed_size)/raw_size
print(f'Reduction in size after processing is: {reduction:.2f}%')
print('='*50)
```

```
=====
Size of Non-Converted data is: 17.88 MB
=====
Size of Converted data is: 6.43 MB
=====
Reduction in size after processing is: 64.04%
=====
```

```
[93]: data.info()
```

```
<class 'pandas.core.frame.DataFrame'>
```

DatetimeIndex: 210605 entries, 2018-01-01 to 2019-07-31

Data columns (total 9 columns):

#	Column	Non-Null Count	Dtype
0	Store_id	210605 non-null	uint16
1	Store_Type	210605 non-null	category
2	Location_Type	210605 non-null	category
3	Region_Code	210605 non-null	category
4	Holiday	210605 non-null	bool
5	Discount	210605 non-null	bool
6	#Order	188340 non-null	float64
7	Sales	188340 non-null	float64
8	Train	210605 non-null	bool

dtypes: bool(3), category(3), float64(2), uint16(1)

memory usage: 6.4 MB

```
[94]: data.describe()
```

```
[94]:
```

	Store_id	#Order	Sales
count	210605.000000	188340.000000	188340.000000
mean	183.000000	68.205692	42784.327982
std	105.366279	30.467415	18456.708302
min	1.000000	0.000000	0.000000
25%	92.000000	48.000000	30426.000000
50%	183.000000	63.000000	39678.000000
75%	274.000000	82.000000	51909.000000
max	365.000000	371.000000	247215.000000

```
[95]: # Rename #Order column name for ease of use
data.rename(columns={'#Order':'Order'}, inplace=True)
```

```
[96]: # Assign index to Exogenous variable dataframe
exog_holiday = data.Holiday
exog_discount = data.Discount
exog = pd.concat([exog_holiday, exog_discount, data.Train], axis=1)
exog_train = exog[exog.Train == True][['Holiday','Discount']]
exog_test = exog[exog.Train == False][['Holiday','Discount']]
```

## 1.4 4. Feature Engineering

```
[97]: # Developing Features from date
data['Year'] = data.index.year
data['Quarter'] = data.index.quarter
data['Month'] = data.index.month
data['MonthName'] = data.index.month_name()
data['Day'] = data.index.day
data['Week'] = data.index.isocalendar().week
```

```
data['Weekday'] = data.index.weekday
data['DayName'] = data.index.day_name()
data['Weekend'] = data.Weekday.apply(lambda x: 'Weekend' if x in [
    ↪ ['Saturday', 'Sunday'] else 'Weekday')
```

```
[98]: # Additional features
data['S/O'] = round(data.Sales/data.Order,2)
```

```
[99]: data.sample(5)
```

```
[99]:
```

	Store_id	Store_Type	Location_Type	Region_Code	Holiday	Discount	\
Date							
2019-03-02	244	S2	L5	R4	False	True	
2018-06-18	238	S1	L1	R2	False	True	
2018-06-22	234	S2	L4	R2	False	False	
2019-05-17	190	S3	L3	R1	False	False	
2018-11-17	145	S1	L3	R1	False	False	

	Order	Sales	Train	Year	Quarter	Month	MonthName	Day	Week	\
Date										
2019-03-02	57.0	34365.0	True	2019	1	3	March	2	9	
2018-06-18	46.0	37695.0	True	2018	2	6	June	18	25	
2018-06-22	31.0	23778.0	True	2018	2	6	June	22	25	
2019-05-17	92.0	54867.0	True	2019	2	5	May	17	20	
2018-11-17	71.0	35820.0	True	2018	4	11	November	17	46	

	Weekday	DayName	Weekend	S/O
Date				
2019-03-02	5	Saturday	Weekday	602.89
2018-06-18	0	Monday	Weekday	819.46
2018-06-22	4	Friday	Weekday	767.03
2019-05-17	4	Friday	Weekday	596.38
2018-11-17	5	Saturday	Weekday	504.51

```
[100]: # Split the data into train and test before proceeding further
train = data[data.Train == True]
test = data[data.Train == False]
```

## 1.5 5. EDA

```
[101]: # **Univariate Analysis: Distribution of numerical data**
fig = make_subplots(rows=1, cols=3, subplot_titles=('Order', 'Sales', 'Sales per_
    ↪ Order'))
fig.add_trace(go.Histogram(x=train.Order, marker_color='teal'), row=1, col=1)
fig.add_trace(go.Histogram(x=train.Sales, marker_color='orange'), row=1, col=2)
fig.add_trace(go.Histogram(x=train['S/O'], marker_color='purple'), row=1, col=3)
```

```
fig.update_layout(title='Distribution of target parameters', showlegend=False,
    ↪title_x=0.5, title_y=0.1)
fig.show()
```

```
[102]: # **Bivariate Analysis: Bar Charts**
order_color = 'darkgreen'
sales_color = 'teal'
fig = make_subplots(rows=2, cols=4)
grouped = train.groupby('Store_Type').agg({'Order': 'sum', 'Sales': 'sum'})
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Order,
    ↪marker=dict(color=order_color)), row=1, col=1)
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=1)
grouped = train.groupby('Location_Type').agg({'Order': 'sum', 'Sales': 'sum'})
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Order,
    ↪marker=dict(color=order_color)), row=1, col=2)
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=2)
grouped = train.groupby('Region_Code').agg({'Order': 'sum', 'Sales': 'sum'})
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Order,
    ↪marker=dict(color=order_color)), row=1, col=3)
fig.add_trace(go.Bar(x=grouped.index, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=3)
grouped = train.groupby(['Weekday', 'DayName']).agg({'Order': 'sum', 'Sales':
    ↪'sum'}).reset_index()
fig.add_trace(go.Bar(x=grouped.DayName, y=grouped.Order,
    ↪marker=dict(color=order_color)), row=1, col=4)
fig.add_trace(go.Bar(x=grouped.DayName, y=grouped.Sales,
    ↪marker=dict(color=sales_color)), row=2, col=4)
fig.update_layout(title='Order, Sales and Sales/Order distribution',
    ↪showlegend=False, title_x=0.5, title_y=0.85)

fig.update_yaxes(title='Order Volume', row=1, col=1)
fig.update_yaxes(title='Sales Amount', row=2, col=1)

fig.update_xaxes(title='Store Type', row=2, col=1)
fig.update_xaxes(title='Location Type', row=2, col=2)
fig.update_xaxes(title='Region Code', row=2, col=3)

fig.show()
```

```
[103]: # **Top/Bottom 10s**
fig = make_subplots(rows=2, cols=1, subplot_titles=('Top/Bottom 10 Store IDs',
    ↪'))
top_order = train.groupby('Store_id').agg({'Order': 'sum'}).sort_values('Order',
    ↪ascending=False).head(10)
```

```

top_sales = train.groupby('Store_id').agg({'Sales': 'sum'}).sort_values('Sales',
    ↪ascending=False).head(10)
bottom_order = train.groupby('Store_id').agg({'Order': 'sum'}).
    ↪sort_values('Order', ascending=False).tail(10)
bottom_sales = train.groupby('Store_id').agg({'Sales': 'sum'}).
    ↪sort_values('Sales', ascending=False).tail(10)
tb_order = pd.concat([top_order, bottom_order])
tb_sales = pd.concat([top_sales, bottom_sales])
fig.add_trace(go.Bar(x=tb_order.index, y=tb_order.Order, name='Order',
    ↪marker=dict(color=order_color)), row=1, col=1)
fig.add_trace(go.Bar(x=tb_sales.index, y=tb_sales.Sales, name='Sales',
    ↪marker=dict(color=sales_color)), row=2, col=1)
fig.update_layout(xaxis=dict(type='category'),
    xaxis2=dict(type='category'),
    yaxis=dict(title='Order Volume'),
    yaxis2=dict(title='Sales Amount'),
    showlegend=False, width=500)
fig.show()

```

```

[104]: # **Bi-variate Analysis: Order/Sales Scatter Plots**
def scatter_plots(df, column):
    categories = df[column].astype('category').unique().sort_values()
    fig = make_subplots(rows=1, cols=len(categories), subplot_titles=[str(c) for
    ↪c in categories])
    for i, category in enumerate(categories):
        fig.add_trace(go.Scatter(x=df[df[column] == category]['Order'],
    ↪y=df[df[column] == category]['Sales'],
        mode='markers', marker=dict(size=2),
    ↪name=category, row=1, col=i+1)
        fig.update_xaxes(range = [0,300], row=1, col=i+1)
        fig.update_yaxes(range = [0,250000], row=1, col=i+1)
    fig.update_layout(title=f'{column} wise Order v/s Sales Scatter Plot', height
    ↪= 400, showlegend=False, title_x=0.5)
    fig.show()

def scatter_save(df, column):
    categories = df[column].unique().sort_values()
    for category in categories:
        fig = go.Figure()
        fig.add_trace(go.Scatter(x=df[df[column] == category]['Order'],
    ↪y=df[df[column] == category]['Sales'],
        mode='markers', marker=dict(size=2),
    ↪name=category,))
        fig.update_xaxes(range = [0,300])
        fig.update_yaxes(range = [0,250000])

```

```
fig.update_layout(title=f'{column} wise Order v/s Sales Scatter Plot',
title_x=0.5, showlegend=False,
axis_title='Order Volume', yaxis_title='Sales Amount')
pio.write_html(fig, f'{column}_{category}_scatter.html', full_html=False)
```

```
[105]: ignore = True
if not ignore:
    scatter_plots(train, 'Store_Type')
    scatter_plots(train, 'Region_Code')
    scatter_plots(train, 'Location_Type')
    scatter_plots(train, 'Holiday')
    scatter_plots(train, 'Discount')
```

```
[106]: ignore = True
if not ignore:
    scatter_save(train, 'Store_Type')
    scatter_save(train, 'Region_Code')
    scatter_save(train, 'Location_Type')
    scatter_save(train, 'Holiday')
    scatter_save(train, 'Discount')
```

### 1.5.1 Hypothesis Testing

```
[107]: # **Chi-Square test for dependency**
from scipy.stats import chi2_contingency

@decorator
def chi2test(data, category1, category2, alpha=0.05):
    data = data.groupby(by=[category1, category2]).agg({'Order': 'sum', 'Sales':
    'sum'}).reset_index()
    test = chi2_contingency(data.
    pivot(index=category1, columns=category2, values='Order').fillna(0))
    order_dependency = test.pvalue < alpha
    if order_dependency:
        print(f'Reject the Null Hypothesis. For Order volume, {category1} and
    {category2} are dependent', end=" | ")
    else:
        print(f'Fail to reject the Null Hypothesis. For Order volume, {category1}
    and {category2} are independent', end=" | ")
    print(f'Test statistics:{test.statistic},\tp-value:{test.pvalue}')

    test = chi2_contingency(data.
    pivot(index=category1, columns=category2, values='Sales').fillna(0))
    sales_dependency = test.pvalue < alpha
    if sales_dependency:
```

```

    print(f'Reject the Null Hypothesis. For Sales amount, {category1} and
    ↪{category2} are dependent', end=" | ")
    else:
        print(f'Fail to reject the Null Hypothesis. For Sales amount, {category1}
    ↪and {category2} are independent', end=" | ")
    print(f'Test statistics:{test.statistic},\tp-value:{test.pvalue}')

    return {'C1':category1, 'C2':category2,'Order': order_dependency, 'Sales':
    ↪sales_dependency}

```

```

[108]: from itertools import permutations
columns = ['Store_Type', 'Location_Type', 'Region_Code', 'Holiday', 'Discount',
    ↪'MonthName', 'DayName']
dependency_summary = pd.DataFrame([chi2test(train,c1,c2) for c1,c2 in
    ↪list(permutations(columns,2))])

```

```

=====
Reject the Null Hypothesis. For Order volume, Store_Type and Location_Type are
dependent | Test statistics:8560447.197307907,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, Store_Type and Location_Type are
dependent | Test statistics:5347008627.585614,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and Region_Code are
dependent | Test statistics:2063286.1134297573,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, Store_Type and Region_Code are
dependent | Test statistics:1263592484.9694943,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and Holiday are
dependent | Test statistics:27.94049935419796, p-value:3.7379941858049926e-06
Reject the Null Hypothesis. For Sales amount, Store_Type and Holiday are
dependent | Test statistics:21093.7298558246,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and Discount are
dependent | Test statistics:321.25338064274575,
p-value:2.497032993795113e-69
Reject the Null Hypothesis. For Sales amount, Store_Type and Discount are
dependent | Test statistics:329382.9310341213,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and MonthName are
dependent | Test statistics:767.6808790550784,
p-value:4.541885984630596e-140
Reject the Null Hypothesis. For Sales amount, Store_Type and MonthName are
dependent | Test statistics:554539.2424337461,    p-value:0.0

```

```

=====
=====
Reject the Null Hypothesis. For Order volume, Store_Type and DayName are
dependent | Test statistics:75.9649544550106, p-value:4.312391037787697e-09
Reject the Null Hypothesis. For Sales amount, Store_Type and DayName are
dependent | Test statistics:52319.79147868339, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Store_Type are
dependent | Test statistics:8560447.197307909, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Location_Type and Store_Type are
dependent | Test statistics:5347008627.585613, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Region_Code are
dependent | Test statistics:373016.05851354415, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Location_Type and Region_Code are
dependent | Test statistics:228540888.13728154, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Holiday are
dependent | Test statistics:21.222613057623803,
p-value:0.00028605478639954726
Reject the Null Hypothesis. For Sales amount, Location_Type and Holiday are
dependent | Test statistics:21296.647804881504, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and Discount are
dependent | Test statistics:1260.3760430857506,
p-value:1.2971148482759126e-271
Reject the Null Hypothesis. For Sales amount, Location_Type and Discount are
dependent | Test statistics:724101.2360874555, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and MonthName are
dependent | Test statistics:439.16646867455864, p-value:1.3959817749676116e-66
Reject the Null Hypothesis. For Sales amount, Location_Type and MonthName are
dependent | Test statistics:307715.5842903906, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Location_Type and DayName are
dependent | Test statistics:50.63707711934928,
p-value:0.0011740360390016633
Reject the Null Hypothesis. For Sales amount, Location_Type and DayName are
dependent | Test statistics:38344.05165385948, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and Store_Type are

```



```

dependent | Test statistics:2063286.1134297573,    p-value:0.0
Reject the Null Hypothesis. For Sales amount, Region_Code and Store_Type are
dependent | Test statistics:1263592484.9694943,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and Location_Type are
dependent | Test statistics:373016.05851354403, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Region_Code and Location_Type are
dependent | Test statistics:228540888.13728154, p-value:0.0
=====
=====
Fail to reject the Null Hypothesis. For Order volume, Region_Code and Holiday
are independent | Test statistics:5.22312907474964,
p-value:0.15616892563963025
Reject the Null Hypothesis. For Sales amount, Region_Code and Holiday are
dependent | Test statistics:4415.458954381414,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and Discount are
dependent | Test statistics:726.5818658215513,
p-value:3.6135273295344166e-157
Reject the Null Hypothesis. For Sales amount, Region_Code and Discount are
dependent | Test statistics:567114.1191712606,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and MonthName are
dependent | Test statistics:852.9791229987399,
p-value:6.956453417684306e-158
Reject the Null Hypothesis. For Sales amount, Region_Code and MonthName are
dependent | Test statistics:669584.5488212734,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Region_Code and DayName are
dependent | Test statistics:30.149954668791192,
p-value:0.03601386919680342
Reject the Null Hypothesis. For Sales amount, Region_Code and DayName are
dependent | Test statistics:29839.71437344468,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Holiday and Store_Type are
dependent | Test statistics:27.94049935419796, p-value:3.7379941858049926e-06
Reject the Null Hypothesis. For Sales amount, Holiday and Store_Type are
dependent | Test statistics:21093.729855824597,    p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Holiday and Location_Type are
dependent | Test statistics:21.2226130576238,
p-value:0.0002860547863995476

```

Reject the Null Hypothesis. For Sales amount, Holiday and Location\_Type are dependent | Test statistics:21296.647804881504, p-value:0.0  
=====

Fail to reject the Null Hypothesis. For Order volume, Holiday and Region\_Code are independent | Test statistics:5.2231290747496395, p-value:0.15616892563963033

Reject the Null Hypothesis. For Sales amount, Holiday and Region\_Code are dependent | Test statistics:4415.458954381414, p-value:0.0  
=====

Reject the Null Hypothesis. For Order volume, Holiday and Discount are dependent | Test statistics:1531.4534101037711, p-value:0.0

Reject the Null Hypothesis. For Sales amount, Holiday and Discount are dependent | Test statistics:569983.2461383714, p-value:0.0  
=====

Reject the Null Hypothesis. For Order volume, Holiday and MonthName are dependent | Test statistics:329278.4500446775, p-value:0.0

Reject the Null Hypothesis. For Sales amount, Holiday and MonthName are dependent | Test statistics:206015674.04294717, p-value:0.0  
=====

Reject the Null Hypothesis. For Order volume, Holiday and DayName are dependent | Test statistics:70922.4490624049, p-value:0.0

Reject the Null Hypothesis. For Sales amount, Holiday and DayName are dependent | Test statistics:40319768.89511568, p-value:0.0  
=====

Reject the Null Hypothesis. For Order volume, Discount and Store\_Type are dependent | Test statistics:321.2533806427457, p-value:2.4970329937951835e-69

Reject the Null Hypothesis. For Sales amount, Discount and Store\_Type are dependent | Test statistics:329382.9310341213, p-value:0.0  
=====

Reject the Null Hypothesis. For Order volume, Discount and Location\_Type are dependent | Test statistics:1260.3760430857506, p-value:1.2971148482759126e-271

Reject the Null Hypothesis. For Sales amount, Discount and Location\_Type are dependent | Test statistics:724101.2360874556, p-value:0.0  
=====

Reject the Null Hypothesis. For Order volume, Discount and Region\_Code are dependent | Test statistics:726.5818658215514, p-value:3.61352732953421e-157

Reject the Null Hypothesis. For Sales amount, Discount and Region\_Code are dependent | Test statistics:567114.1191712606, p-value:0.0

```

=====
=====
Reject the Null Hypothesis. For Order volume, Discount and Holiday are dependent
| Test statistics:1531.4534101037711, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Discount and Holiday are dependent
| Test statistics:569983.2461383714, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and MonthName are
dependent | Test statistics:97104.88049468104, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Discount and MonthName are
dependent | Test statistics:59894831.49811946, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, Discount and DayName are dependent
| Test statistics:14454.702562989041, p-value:0.0
Reject the Null Hypothesis. For Sales amount, Discount and DayName are dependent
| Test statistics:9301326.292060012, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Store_Type are
dependent | Test statistics:767.6808790550785,
p-value:4.541885984630337e-140
Reject the Null Hypothesis. For Sales amount, MonthName and Store_Type are
dependent | Test statistics:554539.2424337475, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Location_Type are
dependent | Test statistics:439.1664686745586, p-value:1.3959817749676514e-66
Reject the Null Hypothesis. For Sales amount, MonthName and Location_Type are
dependent | Test statistics:307715.5842903907, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Region_Code are
dependent | Test statistics:852.97912299874,
p-value:6.956453417683911e-158
Reject the Null Hypothesis. For Sales amount, MonthName and Region_Code are
dependent | Test statistics:669584.5488212737, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Holiday are
dependent | Test statistics:329278.4500446775, p-value:0.0
Reject the Null Hypothesis. For Sales amount, MonthName and Holiday are
dependent | Test statistics:206015674.04294714, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and Discount are
dependent | Test statistics:97104.88049468104, p-value:0.0

```

```

Reject the Null Hypothesis. For Sales amount, MonthName and Discount are
dependent | Test statistics:59894831.4981195, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, MonthName and DayName are
dependent | Test statistics:115360.52602159233, p-value:0.0
Reject the Null Hypothesis. For Sales amount, MonthName and DayName are
dependent | Test statistics:77573972.75065999, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Store_Type are
dependent | Test statistics:75.96495445501058, p-value:4.312391037787728e-09
Reject the Null Hypothesis. For Sales amount, DayName and Store_Type are
dependent | Test statistics:52319.79147868339, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Location_Type are
dependent | Test statistics:50.637077119349286,
p-value:0.0011740360390016587
Reject the Null Hypothesis. For Sales amount, DayName and Location_Type are
dependent | Test statistics:38344.05165385942, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Region_Code are
dependent | Test statistics:30.149954668791196,
p-value:0.036013869196803355
Reject the Null Hypothesis. For Sales amount, DayName and Region_Code are
dependent | Test statistics:29839.71437344464, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Holiday are dependent
| Test statistics:70922.4490624049, p-value:0.0
Reject the Null Hypothesis. For Sales amount, DayName and Holiday are dependent
| Test statistics:40319768.89511567, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and Discount are dependent
| Test statistics:14454.70256298904, p-value:0.0
Reject the Null Hypothesis. For Sales amount, DayName and Discount are dependent
| Test statistics:9301326.292059988, p-value:0.0
=====
=====
Reject the Null Hypothesis. For Order volume, DayName and MonthName are
dependent | Test statistics:115360.52602159233, p-value:0.0
Reject the Null Hypothesis. For Sales amount, DayName and MonthName are
dependent | Test statistics:77573972.75065999, p-value:0.0
=====

```

```
[109]: pd.crosstab(dependancy_summary.C1, dependancy_summary.C2, dependancy_summary.
↳Order, aggfunc='max')
```

```
[109]: C2          DayName Discount Holiday Location_Type MonthName Region_Code \
C1
DayName          NaN      True      True          True      True      True
Discount          True      NaN      True          True      True      True
Holiday           True      True      NaN          True      True      False
Location_Type     True      True      True          NaN      True      True
MonthName          True      True      True          True      NaN      True
Region_Code        True      True      False         True      True      NaN
Store_Type         True      True      True          True      True      True

C2          Store_Type
C1
DayName          True
Discount          True
Holiday           True
Location_Type     True
MonthName          True
Region_Code        True
Store_Type         NaN
```

```
[110]: pd.crosstab(dependancy_summary.C1, dependancy_summary.C2, dependancy_summary.
↳Sales, aggfunc='max').fillna(0)
```

```
[110]: C2          DayName Discount Holiday Location_Type MonthName Region_Code \
C1
DayName          0      True      True          True      True      True
Discount          True      0      True          True      True      True
Holiday           True      True      0          True      True      True
Location_Type     True      True      True          0      True      True
MonthName          True      True      True          True      0      True
Region_Code        True      True      True          True      True      0
Store_Type         True      True      True          True      True      True

C2          Store_Type
C1
DayName          True
Discount          True
Holiday           True
Location_Type     True
MonthName          True
Region_Code        True
Store_Type         0
```

```

[111]: # **Mean similarity test**
from scipy.stats import f_oneway, kruskal, anderson, levene
from statsmodels.stats.multicomp import pairwise_tukeyhsd
from itertools import combinations

def decorator(func):
    def wrapper(*args, **kwargs):
        print('~'*100)
        print('~'*100)
        result = func(*args, **kwargs)
        print('~'*100)
        print('~'*100)
        return result
    return wrapper

@decorator
def variance_test(data, category, target, alpha=0.05):
    d = data.groupby(by=category).agg(Mean=(target, 'mean'), Count=(target, 'size')).reset_index()
    print(f'Hypothesis test whether Mean {target} is same for all {category} or not.\n')
    print(d)
    print('='*53)
    cats = sorted(data[category].unique())
    groups = {}
    for cat in cats:
        groups[cat] = data[data[category] == cat][target]

    # Check for Normality test of all categories
    normality_test = True
    print('Criteria check for ANOVA')
    for cat, group in groups.items():
        if not anderson(group).fit_result.success:
            normality_test = False
            print(f'\033[31m \u274C Group {cat} is not normally distributed.\033[0m')
            break
    if normality_test:
        print(f'\033[32m \u2705 All groups are normally distributed.\033[0m')
    # Check for levene test
    levene_test = True
    _, p_levene = levene(*groups.values())
    if p_levene < alpha:
        levene_test = False
        print(f'\033[31m \u274C Variance of all groups are not same.\033[0m')
    else:
        print(f'\033[32m \u2705 Variance of all groups are same.\033[0m')

```

```

# Perform One-way ANOVA if criteria meets otherwise perform Kruskal
if normality_test and levene_test:
    print('One-Way ANOVA will be performed.')
    _, p_value = f_oneway(*groups.values())
else:
    print('All criterias not met for ANOVA. Kruskal test will be performed.')
    _, p_value = kruskal(*groups.values())

# Proceed for ttest_ind if one group has different mean
if p_value > alpha:
    print(f'p-Value is {p_value} > {alpha} Significance level.\nWe dont have_
    ↪ enough evidence to reject the Null Hypothesis. All means are same.')
    print('='*53)
    return None
else:
    print(f'p-Value is {p_value} < {alpha} Significance level.\nWe have enough_
    ↪ evidence to reject the Null Hypothesis and at least one mean is different.')
    print('='*53)

tukey = pairwise_tukeyhsd(endog=data[target], groups=data[category], alpha=0.
    ↪ 05)
print(tukey)
# Extract group1 and group2 using the Tukey object attributes
group1 = tukey.groupsunique[tukey._multicomp.pairindices[0]]
group2 = tukey.groupsunique[tukey._multicomp.pairindices[1]]
pair = [f'{a}-{b}' for a,b in list(zip(group1, group2))]
reject = tukey.reject

# Combine group1 and group2 into a DataFrame
group_pairs = pd.DataFrame({'pair': pair, 'reject': reject})
same_mean_pairs = group_pairs[group_pairs['reject'] == False]['pair']
different_mean_pairs = group_pairs[group_pairs['reject'] == True]['pair']
print(f'\033[34mPairs having different {target} mean are: {"",".
    ↪ join(different_mean_pairs.values)}')
print(f'\033[35mPairs having same {target} mean are: {"",".
    ↪ join(same_mean_pairs.values)}\033[0m')

return None

```

```

[112]: from itertools import product
for category, target in product(columns, ['Order', 'Sales']):
    variance_test(train, category, target)

```

```

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```

Hypothesis test whether Mean Order is same for all Store\_Type or not.

	Store_Type	Mean	Count
0	S1	58.022095	88752
1	S2	40.472799	28896
2	S3	73.663396	24768
3	S4	102.392779	45924

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is  $0.0 < 0.05$  Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

Multiple Comparison of Means - Tukey HSD, FWER=0.05

group1	group2	meandiff	p-adj	lower	upper	reject
S1	S2	-17.5493	0.0	-17.9275	-17.1711	True
S1	S3	15.6413	0.0	15.24	16.0426	True
S1	S4	44.3707	0.0	44.0497	44.6917	True
S2	S3	33.1906	0.0	32.707	33.6742	True
S2	S4	61.92	0.0	61.5007	62.3393	True
S3	S4	28.7294	0.0	28.2891	29.1696	True

Pairs having different Order mean are: S1-S2,S1-S3,S1-S4,S2-S3,S2-S4,S3-S4

Pairs having same Order mean are:

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Hypothesis test whether Mean Sales is same for all Store\_Type or not.

|   | Store_Type | Mean         | Count |
|---|------------|--------------|-------|
| 0 | S1         | 37676.511694 | 88752 |
| 1 | S2         | 27530.828222 | 28896 |
| 2 | S3         | 47063.068209 | 24768 |
| 3 | S4         | 59945.685926 | 45924 |

Criteria check for ANOVA

All groups are normally distributed.



Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

```
=====
Multiple Comparison of Means - Tukey HSD, FWER=0.05
=====
```

| group1 | group2 | meandiff    | p-adj | lower       | upper      | reject |
|--------|--------|-------------|-------|-------------|------------|--------|
| S1     | S2     | -10145.6835 | 0.0   | -10402.8539 | -9888.513  | True   |
| S1     | S3     | 9386.5565   | 0.0   | 9113.6974   | 9659.4156  | True   |
| S1     | S4     | 22269.1742  | 0.0   | 22050.9148  | 22487.4336 | True   |
| S2     | S3     | 19532.24    | 0.0   | 19203.4535  | 19861.0265 | True   |
| S2     | S4     | 32414.8577  | 0.0   | 32129.7514  | 32699.9641 | True   |
| S3     | S4     | 12882.6177  | 0.0   | 12583.2834  | 13181.9521 | True   |

```
-----
```

Pairs having different Sales mean are: S1-S2,S1-S3,S1-S4,S2-S3,S2-S4,S3-S4

Pairs having same Sales mean are:

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```

Hypothesis test whether Mean Order is same for all Location\_Type or not.

|   | Location_Type | Mean      | Count |
|---|---------------|-----------|-------|
| 0 | L1            | 65.265938 | 85140 |
| 1 | L2            | 94.851456 | 48504 |
| 2 | L3            | 53.156943 | 29928 |
| 3 | L4            | 47.386028 | 10836 |
| 4 | L5            | 41.924131 | 13932 |

```
=====
Criteria check for ANOVA
```

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

```
=====
Multiple Comparison of Means - Tukey HSD, FWER=0.05
=====
```

| group1 | group2 | meandiff | p-adj | lower | upper | reject |
|--------|--------|----------|-------|-------|-------|--------|
|--------|--------|----------|-------|-------|-------|--------|

|    |    |          |     |          |          |      |
|----|----|----------|-----|----------|----------|------|
| L1 | L2 | 29.5855  | 0.0 | 29.1962  | 29.9749  | True |
| L1 | L3 | -12.109  | 0.0 | -12.5689 | -11.6491 | True |
| L1 | L4 | -17.8799 | 0.0 | -18.578  | -17.1819 | True |
| L1 | L5 | -23.3418 | 0.0 | -23.9673 | -22.7163 | True |
| L2 | L3 | -41.6945 | 0.0 | -42.1976 | -41.1914 | True |
| L2 | L4 | -47.4654 | 0.0 | -48.1926 | -46.7382 | True |
| L2 | L5 | -52.9273 | 0.0 | -53.5852 | -52.2695 | True |
| L3 | L4 | -5.7709  | 0.0 | -6.5382  | -5.0036  | True |
| L3 | L5 | -11.2328 | 0.0 | -11.9347 | -10.5309 | True |
| L4 | L5 | -5.4619  | 0.0 | -6.3385  | -4.5853  | True |

Pairs having different Order mean are:

L1-L2,L1-L3,L1-L4,L1-L5,L2-L3,L2-L4,L2-L5,L3-L4,L3-L5,L4-L5

Pairs having same Order mean are:

[illegible]

Hypothesis test whether Mean Sales is same for all Location\_Type or not.

|   | Location_Type | Mean         | Count |
|---|---------------|--------------|-------|
| 0 | L1            | 41453.597889 | 85140 |
| 1 | L2            | 59231.480373 | 48504 |
| 2 | L3            | 33072.257756 | 29928 |
| 3 | L4            | 29067.414313 | 10836 |
| 4 | L5            | 25187.787261 | 13932 |

### Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is  $0.0 < 0.05$  Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

=====

Multiple Comparison of Means - Tukey HSD, FWER=0.05

| group1 | group2 | meandiff   | p-adj | lower      | upper      | reject |
|--------|--------|------------|-------|------------|------------|--------|
| L1     | L2     | 17777.8825 | 0.0   | 17546.9501 | 18008.8149 | True   |
| L1     | L3     | -8381.3401 | 0.0   | -8654.1357 | -8108.5446 | True   |

|    |    |             |     |             |             |      |
|----|----|-------------|-----|-------------|-------------|------|
| L1 | L4 | -12386.1836 | 0.0 | -12800.2268 | -11972.1403 | True |
| L1 | L5 | -16265.8106 | 0.0 | -16636.8052 | -15894.816  | True |
| L2 | L3 | -26159.2226 | 0.0 | -26457.6129 | -25860.8323 | True |
| L2 | L4 | -30164.0661 | 0.0 | -30595.4025 | -29732.7296 | True |
| L2 | L5 | -34043.6931 | 0.0 | -34433.8935 | -33653.4927 | True |
| L3 | L4 | -4004.8434  | 0.0 | -4459.9685  | -3549.7184  | True |
| L3 | L5 | -7884.4705  | 0.0 | -8300.8165  | -7468.1245  | True |
| L4 | L5 | -3879.6271  | 0.0 | -4399.5871  | -3359.667   | True |

-----

Pairs having different Sales mean are:

L1-L2,L1-L3,L1-L4,L1-L5,L2-L3,L2-L4,L2-L5,L3-L4,L3-L5,L4-L5

Pairs having same Sales mean are:

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Hypothesis test whether Mean Order is same for all Region\_Code or not.

|   | Region_Code | Mean      | Count |
|---|-------------|-----------|-------|
| 0 | R1          | 79.626063 | 63984 |
| 1 | R2          | 62.798616 | 54180 |
| 2 | R3          | 63.882436 | 44376 |
| 3 | R4          | 58.674031 | 25800 |

=====

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

=====

Multiple Comparison of Means - Tukey HSD, FWER=0.05

=====

| group1 | group2 | meandiff | p-adj | lower | upper | reject |
|--------|--------|----------|-------|-------|-------|--------|
|--------|--------|----------|-------|-------|-------|--------|

-----

|    |    |          |     |          |          |      |
|----|----|----------|-----|----------|----------|------|
| R1 | R2 | -16.8274 | 0.0 | -17.267  | -16.3879 | True |
| R1 | R3 | -15.7436 | 0.0 | -16.2087 | -15.2786 | True |
| R1 | R4 | -20.952  | 0.0 | -21.5072 | -20.3968 | True |
| R2 | R3 | 1.0838   | 0.0 | 0.6018   | 1.5658   | True |
| R2 | R4 | -4.1246  | 0.0 | -4.694   | -3.5551  | True |
| R3 | R4 | -5.2084  | 0.0 | -5.7978  | -4.619   | True |





```
=====
group1 group2 meandiff p-adj lower upper reject
-----
False True -8445.4101 0.0 -8688.8675 -8201.9526 True
-----
```

Pairs having different Sales mean are: False-True

Pairs having same Sales mean are:

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```

Hypothesis test whether Mean Order is same for all Discount or not.

|   | Discount | Mean      | Count  |
|---|----------|-----------|--------|
| 0 | False    | 61.806153 | 104051 |
| 1 | True     | 76.105637 | 84289  |

```
=====
Criteria check for ANOVA
```

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

```
=====
Multiple Comparison of Means - Tukey HSD, FWER=0.05
=====
```

```
group1 group2 meandiff p-adj lower upper reject
-----
False True 14.2995 0.0 14.0304 14.5686 True
-----
```

Pairs having different Order mean are: False-True

Pairs having same Order mean are:

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```

Hypothesis test whether Mean Sales is same for all Discount or not.

|   | Discount | Mean         | Count  |
|---|----------|--------------|--------|
| 0 | False    | 37403.679678 | 104051 |
| 1 | True     | 49426.497620 | 84289  |

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

Multiple Comparison of Means - Tukey HSD, FWER=0.05

| group1 | group2 | meandiff   | p-adj | lower      | upper      | reject |
|--------|--------|------------|-------|------------|------------|--------|
| False  | True   | 12022.8179 | 0.0   | 11864.2197 | 12181.4162 | True   |

Pairs having different Sales mean are: False-True

Pairs having same Sales mean are:

Hypothesis test whether Mean Order is same for all MonthName or not.

|    | MonthName | Mean      | Count |
|----|-----------|-----------|-------|
| 0  | April     | 68.212968 | 21900 |
| 1  | August    | 67.128502 | 11315 |
| 2  | December  | 69.479806 | 11315 |
| 3  | February  | 67.453474 | 20440 |
| 4  | January   | 66.933672 | 22630 |
| 5  | July      | 76.048873 | 11315 |
| 6  | June      | 66.174155 | 10950 |
| 7  | March     | 67.761688 | 22630 |
| 8  | May       | 71.100044 | 22630 |
| 9  | November  | 63.416438 | 10950 |
| 10 | October   | 65.460009 | 11315 |
| 11 | September | 68.509954 | 10950 |

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 1.7657332953564353e-282 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

=====

Multiple Comparison of Means - Tukey HSD, FWER=0.05

=====

| group1   | group2    | meandiff | p-adj  | lower   | upper   | reject |
|----------|-----------|----------|--------|---------|---------|--------|
| -----    |           |          |        |         |         |        |
| April    | August    | -1.0845  | 0.0855 | -2.2328 | 0.0639  | False  |
| April    | December  | 1.2668   | 0.0163 | 0.1185  | 2.4152  | True   |
| April    | February  | -0.7595  | 0.295  | -1.7241 | 0.2051  | False  |
| April    | January   | -1.2793  | 0.0005 | -2.2195 | -0.3391 | True   |
| April    | July      | 7.8359   | 0.0    | 6.6876  | 8.9842  | True   |
| April    | June      | -2.0388  | 0.0    | -3.1997 | -0.8779 | True   |
| April    | March     | -0.4513  | 0.9204 | -1.3915 | 0.4889  | False  |
| April    | May       | 2.8871   | 0.0    | 1.9469  | 3.8272  | True   |
| April    | November  | -4.7965  | 0.0    | -5.9574 | -3.6357 | True   |
| April    | October   | -2.753   | 0.0    | -3.9013 | -1.6046 | True   |
| April    | September | 0.297    | 0.9996 | -0.8639 | 1.4579  | False  |
| August   | December  | 2.3513   | 0.0    | 1.0326  | 3.67    | True   |
| August   | February  | 0.325    | 0.999  | -0.8372 | 1.4872  | False  |
| August   | January   | -0.1948  | 1.0    | -1.3368 | 0.9472  | False  |
| August   | July      | 8.9204   | 0.0    | 7.6017  | 10.239  | True   |
| August   | June      | -0.9543  | 0.4438 | -2.2839 | 0.3753  | False  |
| August   | March     | 0.6332   | 0.8118 | -0.5088 | 1.7752  | False  |
| August   | May       | 3.9715   | 0.0    | 2.8296  | 5.1135  | True   |
| August   | November  | -3.7121  | 0.0    | -5.0417 | -2.3825 | True   |
| August   | October   | -1.6685  | 0.0021 | -2.9872 | -0.3498 | True   |
| August   | September | 1.3815   | 0.0334 | 0.0519  | 2.7111  | True   |
| December | February  | -2.0263  | 0.0    | -3.1885 | -0.8641 | True   |
| December | January   | -2.5461  | 0.0    | -3.6881 | -1.4041 | True   |
| December | July      | 6.5691   | 0.0    | 5.2504  | 7.8877  | True   |
| December | June      | -3.3057  | 0.0    | -4.6353 | -1.976  | True   |
| December | March     | -1.7181  | 0.0001 | -2.8601 | -0.5761 | True   |
| December | May       | 1.6202   | 0.0002 | 0.4782  | 2.7622  | True   |
| December | November  | -6.0634  | 0.0    | -7.393  | -4.7338 | True   |
| December | October   | -4.0198  | 0.0    | -5.3385 | -2.7011 | True   |
| December | September | -0.9699  | 0.417  | -2.2995 | 0.3598  | False  |
| February | January   | -0.5198  | 0.8319 | -1.4769 | 0.4373  | False  |
| February | July      | 8.5954   | 0.0    | 7.4332  | 9.7576  | True   |
| February | June      | -1.2793  | 0.0192 | -2.4539 | -0.1047 | True   |
| February | March     | 0.3082   | 0.9964 | -0.6489 | 1.2653  | False  |
| February | May       | 3.6466   | 0.0    | 2.6895  | 4.6037  | True   |
| February | November  | -4.037   | 0.0    | -5.2116 | -2.8624 | True   |
| February | October   | -1.9935  | 0.0    | -3.1557 | -0.8313 | True   |
| February | September | 1.0565   | 0.1272 | -0.1181 | 2.2311  | False  |



|          |           |          |        |          |          |       |
|----------|-----------|----------|--------|----------|----------|-------|
| January  | July      | 9.1152   | 0.0    | 7.9732   | 10.2572  | True  |
| January  | June      | -0.7595  | 0.5865 | -1.9141  | 0.3951   | False |
| January  | March     | 0.828    | 0.14   | -0.1044  | 1.7604   | False |
| January  | May       | 4.1664   | 0.0    | 3.2339   | 5.0988   | True  |
| January  | November  | -3.5172  | 0.0    | -4.6718  | -2.3626  | True  |
| January  | October   | -1.4737  | 0.0015 | -2.6157  | -0.3317  | True  |
| January  | September | 1.5763   | 0.0005 | 0.4217   | 2.7309   | True  |
| July     | June      | -9.8747  | 0.0    | -11.2043 | -8.5451  | True  |
| July     | March     | -8.2872  | 0.0    | -9.4292  | -7.1452  | True  |
| July     | May       | -4.9488  | 0.0    | -6.0908  | -3.8068  | True  |
| July     | November  | -12.6324 | 0.0    | -13.962  | -11.3028 | True  |
| July     | October   | -10.5889 | 0.0    | -11.9075 | -9.2702  | True  |
| July     | September | -7.5389  | 0.0    | -8.8685  | -6.2093  | True  |
| June     | March     | 1.5875   | 0.0004 | 0.4329   | 2.7421   | True  |
| June     | May       | 4.9259   | 0.0    | 3.7713   | 6.0805   | True  |
| June     | November  | -2.7577  | 0.0    | -4.0982  | -1.4173  | True  |
| June     | October   | -0.7141  | 0.8421 | -2.0437  | 0.6155   | False |
| June     | September | 2.3358   | 0.0    | 0.9953   | 3.6763   | True  |
| March    | May       | 3.3384   | 0.0    | 2.4059   | 4.2708   | True  |
| March    | November  | -4.3452  | 0.0    | -5.4999  | -3.1906  | True  |
| March    | October   | -2.3017  | 0.0    | -3.4437  | -1.1597  | True  |
| March    | September | 0.7483   | 0.6098 | -0.4063  | 1.9029   | False |
| May      | November  | -7.6836  | 0.0    | -8.8382  | -6.529   | True  |
| May      | October   | -5.64    | 0.0    | -6.782   | -4.498   | True  |
| May      | September | -2.5901  | 0.0    | -3.7447  | -1.4355  | True  |
| November | October   | 2.0436   | 0.0    | 0.714    | 3.3732   | True  |
| November | September | 5.0935   | 0.0    | 3.7531   | 6.434    | True  |
| October  | September | 3.0499   | 0.0    | 1.7203   | 4.3795   | True  |

---

Pairs having different Order mean are: April-December, April-January, April-July, April-June, April-May, April-November, April-October, August-December, August-July, August-May, August-November, August-October, August-September, December-February, December-January, December-July, December-June, December-March, December-May, December-November, December-October, February-July, February-June, February-May, February-November, February-October, January-July, January-May, January-November, January-October, January-September, July-June, July-March, July-May, July-November, July-October, July-September, June-March, June-May, June-November, June-September, March-May, March-November, March-October, May-November, May-October, May-September, November-October, November-September, October-September

Pairs having same Order mean are: April-August, April-February, April-March, April-September, August-February, August-January, August-June, August-March, December-September, February-January, February-March, February-September, January-June, January-March, June-October, March-September

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Hypothesis test whether Mean Sales is same for all MonthName or not.

|    | MonthName | Mean         | Count |
|----|-----------|--------------|-------|
| 0  | April     | 40773.681352 | 21900 |
| 1  | August    | 40020.368869 | 11315 |
| 2  | December  | 46477.110199 | 11315 |
| 3  | February  | 40424.350645 | 20440 |
| 4  | January   | 44979.147732 | 22630 |
| 5  | July      | 46585.406232 | 11315 |
| 6  | June      | 44705.726389 | 10950 |
| 7  | March     | 40979.577286 | 22630 |
| 8  | May       | 48115.830407 | 22630 |
| 9  | November  | 38160.962496 | 10950 |
| 10 | October   | 38988.407398 | 11315 |
| 11 | September | 41123.184822 | 10950 |

=====

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is  $0.0 < 0.05$  Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

| =====                                               |           |            |        |            |            |        |
|-----------------------------------------------------|-----------|------------|--------|------------|------------|--------|
| Multiple Comparison of Means - Tukey HSD, FWER=0.05 |           |            |        |            |            |        |
| =====                                               |           |            |        |            |            |        |
| group1                                              | group2    | meandiff   | p-adj  | lower      | upper      | reject |
| -----                                               |           |            |        |            |            |        |
| April                                               | August    | -753.3125  | 0.018  | -1441.2331 | -65.3918   | True   |
| April                                               | December  | 5703.4288  | 0.0    | 5015.5082  | 6391.3495  | True   |
| April                                               | February  | -349.3307  | 0.7103 | -927.2051  | 228.5437   | False  |
| April                                               | January   | 4205.4664  | 0.0    | 3642.2406  | 4768.6922  | True   |
| April                                               | July      | 5811.7249  | 0.0    | 5123.8042  | 6499.6455  | True   |
| April                                               | June      | 3932.045   | 0.0    | 3236.6059  | 4627.4842  | True   |
| April                                               | March     | 205.8959   | 0.9895 | -357.3299  | 769.1218   | False  |
| April                                               | May       | 7342.1491  | 0.0    | 6778.9232  | 7905.3749  | True   |
| April                                               | November  | -2612.7189 | 0.0    | -3308.158  | -1917.2797 | True   |
| April                                               | October   | -1785.274  | 0.0    | -2473.1946 | -1097.3533 | True   |
| April                                               | September | 349.5035   | 0.8934 | -345.9356  | 1044.9426  | False  |
| August                                              | December  | 6456.7413  | 0.0    | 5666.7756  | 7246.7071  | True   |
| August                                              | February  | 403.9818   | 0.762  | -292.2581  | 1100.2216  | False  |
| August                                              | January   | 4958.7789  | 0.0    | 4274.6485  | 5642.9093  | True   |
| August                                              | July      | 6565.0374  | 0.0    | 5775.0716  | 7355.0031  | True   |
| August                                              | June      | 4685.3575  | 0.0    | 3888.8359  | 5481.8791  | True   |
| August                                              | March     | 959.2084   | 0.0003 | 275.078    | 1643.3388  | True   |
| August                                              | May       | 8095.4615  | 0.0    | 7411.3311  | 8779.5919  | True   |
| August                                              | November  | -1859.4064 | 0.0    | -2655.928  | -1062.8848 | True   |
| August                                              | October   | -1031.9615 | 0.0012 | -1821.9272 | -241.9957  | True   |
| August                                              | September | 1102.816   | 0.0004 | 306.2944   | 1899.3376  | True   |
| December                                            | February  | -6052.7596 | 0.0    | -6748.9994 | -5356.5197 | True   |
| December                                            | January   | -1497.9625 | 0.0    | -2182.0929 | -813.8321  | True   |
| December                                            | July      | 108.296    | 1.0    | -681.6697  | 898.2618   | False  |
| December                                            | June      | -1771.3838 | 0.0    | -2567.9054 | -974.8622  | True   |
| December                                            | March     | -5497.5329 | 0.0    | -6181.6633 | -4813.4025 | True   |
| December                                            | May       | 1638.7202  | 0.0    | 954.5898   | 2322.8506  | True   |
| December                                            | November  | -8316.1477 | 0.0    | -9112.6693 | -7519.6261 | True   |
| December                                            | October   | -7488.7028 | 0.0    | -8278.6686 | -6698.737  | True   |
| December                                            | September | -5353.9254 | 0.0    | -6150.447  | -4557.4038 | True   |
| February                                            | January   | 4554.7971  | 0.0    | 3981.4399  | 5128.1543  | True   |
| February                                            | July      | 6161.0556  | 0.0    | 5464.8157  | 6857.2954  | True   |
| February                                            | June      | 4281.3757  | 0.0    | 3577.7063  | 4985.0452  | True   |
| February                                            | March     | 555.2266   | 0.0682 | -18.1305   | 1128.5838  | False  |
| February                                            | May       | 7691.4798  | 0.0    | 7118.1226  | 8264.8369  | True   |
| February                                            | November  | -2263.3881 | 0.0    | -2967.0576 | -1559.7187 | True   |
| February                                            | October   | -1435.9432 | 0.0    | -2132.1831 | -739.7034  | True   |
| February                                            | September | 698.8342   | 0.0536 | -4.8353    | 1402.5036  | False  |
| January                                             | July      | 1606.2585  | 0.0    | 922.1281   | 2290.3889  | True   |

|          |           |            |        |            |            |       |
|----------|-----------|------------|--------|------------|------------|-------|
| January  | June      | -273.4213  | 0.9803 | -965.1114  | 418.2687   | False |
| January  | March     | -3999.5704 | 0.0    | -4558.1606 | -3440.9803 | True  |
| January  | May       | 3136.6827  | 0.0    | 2578.0925  | 3695.2728  | True  |
| January  | November  | -6818.1852 | 0.0    | -7509.8753 | -6126.4951 | True  |
| January  | October   | -5990.7403 | 0.0    | -6674.8707 | -5306.6099 | True  |
| January  | September | -3855.9629 | 0.0    | -4547.653  | -3164.2728 | True  |
| July     | June      | -1879.6798 | 0.0    | -2676.2014 | -1083.1582 | True  |
| July     | March     | -5605.8289 | 0.0    | -6289.9594 | -4921.6985 | True  |
| July     | May       | 1530.4242  | 0.0    | 846.2938   | 2214.5546  | True  |
| July     | November  | -8424.4437 | 0.0    | -9220.9653 | -7627.9221 | True  |
| July     | October   | -7596.9988 | 0.0    | -8386.9646 | -6807.0331 | True  |
| July     | September | -5462.2214 | 0.0    | -6258.743  | -4665.6998 | True  |
| June     | March     | -3726.1491 | 0.0    | -4417.8392 | -3034.459  | True  |
| June     | May       | 3410.104   | 0.0    | 2718.4139  | 4101.7941  | True  |
| June     | November  | -6544.7639 | 0.0    | -7347.7878 | -5741.74   | True  |
| June     | October   | -5717.319  | 0.0    | -6513.8406 | -4920.7974 | True  |
| June     | September | -3582.5416 | 0.0    | -4385.5655 | -2779.5176 | True  |
| March    | May       | 7136.2531  | 0.0    | 6577.663   | 7694.8433  | True  |
| March    | November  | -2818.6148 | 0.0    | -3510.3049 | -2126.9247 | True  |
| March    | October   | -1991.1699 | 0.0    | -2675.3003 | -1307.0395 | True  |
| March    | September | 143.6075   | 0.9999 | -548.0826  | 835.2976   | False |
| May      | November  | -9954.8679 | 0.0    | -10646.558 | -9263.1778 | True  |
| May      | October   | -9127.423  | 0.0    | -9811.5534 | -8443.2926 | True  |
| May      | September | -6992.6456 | 0.0    | -7684.3357 | -6300.9555 | True  |
| November | October   | 827.4449   | 0.0334 | 30.9233    | 1623.9665  | True  |
| November | September | 2962.2223  | 0.0    | 2159.1984  | 3765.2462  | True  |
| October  | September | 2134.7774  | 0.0    | 1338.2558  | 2931.299   | True  |

---

Pairs having different Sales mean are: April-August, April-December, April-January, April-July, April-June, April-May, April-November, April-October, August-December, August-January, August-July, August-June, August-March, August-May, August-November, August-October, August-September, December-February, December-January, December-June, December-March, December-May, December-November, December-October, December-September, February-January, February-July, February-June, February-May, February-November, February-October, January-July, January-March, January-May, January-November, January-October, January-September, July-June, July-March, July-May, July-November, July-October, July-September, June-March, June-May, June-November, June-October, June-September, March-May, March-November, March-October, May-November, May-October, May-September, November-October, November-September, October-September

Pairs having same Sales mean are: April-February, April-March, April-September, August-February, December-July, February-March, February-September, January-June, March-September

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```

Hypothesis test whether Mean Order is same for all DayName or not.

|   | DayName   | Mean      | Count |
|---|-----------|-----------|-------|
| 0 | Friday    | 63.507812 | 27010 |
| 1 | Monday    | 66.164939 | 27010 |
| 2 | Saturday  | 75.887934 | 26645 |
| 3 | Sunday    | 77.694389 | 26645 |
| 4 | Thursday  | 64.140244 | 27010 |
| 5 | Tuesday   | 65.198001 | 27010 |
| 6 | Wednesday | 65.078563 | 27010 |

=====

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is

different.

| Multiple Comparison of Means - Tukey HSD, FWER=0.05 |           |          |        |          |          |        |
|-----------------------------------------------------|-----------|----------|--------|----------|----------|--------|
| group1                                              | group2    | meandiff | p-adj  | lower    | upper    | reject |
| Friday                                              | Monday    | 2.6571   | 0.0    | 1.8967   | 3.4176   | True   |
| Friday                                              | Saturday  | 12.3801  | 0.0    | 11.6171  | 13.1431  | True   |
| Friday                                              | Sunday    | 14.1866  | 0.0    | 13.4236  | 14.9496  | True   |
| Friday                                              | Thursday  | 0.6324   | 0.1772 | -0.128   | 1.3929   | False  |
| Friday                                              | Tuesday   | 1.6902   | 0.0    | 0.9298   | 2.4506   | True   |
| Friday                                              | Wednesday | 1.5708   | 0.0    | 0.8103   | 2.3312   | True   |
| Monday                                              | Saturday  | 9.723    | 0.0    | 8.96     | 10.486   | True   |
| Monday                                              | Sunday    | 11.5295  | 0.0    | 10.7664  | 12.2925  | True   |
| Monday                                              | Thursday  | -2.0247  | 0.0    | -2.7851  | -1.2643  | True   |
| Monday                                              | Tuesday   | -0.9669  | 0.0034 | -1.7274  | -0.2065  | True   |
| Monday                                              | Wednesday | -1.0864  | 0.0005 | -1.8468  | -0.326   | True   |
| Saturday                                            | Sunday    | 1.8065   | 0.0    | 1.0408   | 2.5721   | True   |
| Saturday                                            | Thursday  | -11.7477 | 0.0    | -12.5107 | -10.9847 | True   |
| Saturday                                            | Tuesday   | -10.6899 | 0.0    | -11.453  | -9.9269  | True   |
| Saturday                                            | Wednesday | -10.8094 | 0.0    | -11.5724 | -10.0463 | True   |
| Sunday                                              | Thursday  | -13.5541 | 0.0    | -14.3172 | -12.7911 | True   |
| Sunday                                              | Tuesday   | -12.4964 | 0.0    | -13.2594 | -11.7334 | True   |
| Sunday                                              | Wednesday | -12.6158 | 0.0    | -13.3788 | -11.8528 | True   |
| Thursday                                            | Tuesday   | 1.0578   | 0.0008 | 0.2973   | 1.8182   | True   |
| Thursday                                            | Wednesday | 0.9383   | 0.0051 | 0.1779   | 1.6987   | True   |
| Tuesday                                             | Wednesday | -0.1194  | 0.9993 | -0.8799  | 0.641    | False  |

Pairs having different Order mean are: Friday-Monday, Friday-Saturday, Friday-Sunday, Friday-Tuesday, Friday-Wednesday, Monday-Saturday, Monday-Sunday, Monday-Thursday, Monday-Tuesday, Monday-Wednesday, Saturday-Sunday, Saturday-Thursday, Saturday-Tuesday, Saturday-Wednesday, Sunday-Thursday, Sunday-Tuesday, Sunday-Wednesday, Thursday-Tuesday, Thursday-Wednesday

Pairs having same Order mean are: Friday-Thursday, Tuesday-Wednesday

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Hypothesis test whether Mean Sales is same for all DayName or not.

|         |      |       |
|---------|------|-------|
| DayName | Mean | Count |
|---------|------|-------|

```

0    Friday  39701.020376  27010
1    Monday  42291.175854  27010
2    Saturday 46729.798143  26645
3    Sunday  49044.051947  26645
4    Thursday 40231.985963  27010
5    Tuesday  40802.966220  27010
6    Wednesday 40827.205395  27010

```

```
=====
```

Criteria check for ANOVA

All groups are normally distributed.

Variance of all groups are not same.

All criterias not met for ANOVA. Kruskal test will be performed.

p-Value is 0.0 < 0.05 Significance level.

We have enough evidence to reject the Null Hypothesis and at least one mean is different.

```
=====
```

Multiple Comparison of Means - Tukey HSD, FWER=0.05

```
=====
```

| group1   | group2    | meandiff   | p-adj  | lower      | upper      | reject |
|----------|-----------|------------|--------|------------|------------|--------|
| Friday   | Monday    | 2590.1555  | 0.0    | 2129.6495  | 3050.6614  | True   |
| Friday   | Saturday  | 7028.7778  | 0.0    | 6566.6975  | 7490.8581  | True   |
| Friday   | Sunday    | 9343.0316  | 0.0    | 8880.9513  | 9805.1119  | True   |
| Friday   | Thursday  | 530.9656   | 0.012  | 70.4597    | 991.4715   | True   |
| Friday   | Tuesday   | 1101.9458  | 0.0    | 641.4399   | 1562.4518  | True   |
| Friday   | Wednesday | 1126.185   | 0.0    | 665.6791   | 1586.691   | True   |
| Monday   | Saturday  | 4438.6223  | 0.0    | 3976.542   | 4900.7026  | True   |
| Monday   | Sunday    | 6752.8761  | 0.0    | 6290.7958  | 7214.9564  | True   |
| Monday   | Thursday  | -2059.1899 | 0.0    | -2519.6958 | -1598.684  | True   |
| Monday   | Tuesday   | -1488.2096 | 0.0    | -1948.7156 | -1027.7037 | True   |
| Monday   | Wednesday | -1463.9705 | 0.0    | -1924.4764 | -1003.4645 | True   |
| Saturday | Sunday    | 2314.2538  | 0.0    | 1850.6045  | 2777.9032  | True   |
| Saturday | Thursday  | -6497.8122 | 0.0    | -6959.8925 | -6035.7319 | True   |
| Saturday | Tuesday   | -5926.8319 | 0.0    | -6388.9122 | -5464.7516 | True   |
| Saturday | Wednesday | -5902.5927 | 0.0    | -6364.6731 | -5440.5124 | True   |
| Sunday   | Thursday  | -8812.066  | 0.0    | -9274.1463 | -8349.9857 | True   |
| Sunday   | Tuesday   | -8241.0857 | 0.0    | -8703.166  | -7779.0054 | True   |
| Sunday   | Wednesday | -8216.8466 | 0.0    | -8678.9269 | -7754.7662 | True   |
| Thursday | Tuesday   | 570.9803   | 0.0048 | 110.4743   | 1031.4862  | True   |
| Thursday | Wednesday | 595.2194   | 0.0026 | 134.7135   | 1055.7254  | True   |
| Tuesday  | Wednesday | 24.2392    | 1.0    | -436.2668  | 484.7451   | False  |

```
-----
```

Pairs having different Sales mean are: Friday-Monday, Friday-Saturday, Friday-Sunday, Friday-Thursday, Friday-Tuesday, Friday-Wednesday, Monday-Saturday, Monday-Sunday, Monday-Thursday, Monday-Tuesday, Monday-Wednesday, Saturday-Sunday, Saturday-Thursday, Saturday-Tuesday, Saturday-Wednesday, Sunday-Thursday, Sunday-Tuesday, Sunday-Wednesday, Thursday-Tuesday, Thursday-Wednesday

Pairs having same Sales mean are: Tuesday-Wednesday

```
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```

## 1.6 6. Data Preperation for modeling

```
[113]: # Data Preperation for modeling
# Data for Sales forecastig model training
overall_sales = train.groupby(level=0).agg({'Sales': 'sum'})
id_wise_sales = pd.crosstab(index=train.index, columns=train.Store_id, values=
    ↪ train.Sales, aggfunc='sum')
store_type_wise_sales = pd.crosstab(index=train.index, columns=train.
    ↪ Store_Type, values =train.Sales, aggfunc='sum')
location_wise_sales = pd.crosstab(index=train.index, columns=train.
    ↪ Location_Type, values =train.Sales, aggfunc='sum')
region_wise_sales = pd.crosstab(index=train.index, columns=train.Region_Code,
    ↪ values =train.Sales, aggfunc='sum')

# Data for Order forecastig model training
overall_order = train.groupby(level=0).agg({'Order': 'sum'})
id_wise_order = pd.crosstab(index=train.index, columns=train.Store_id, values=
    ↪ train.Order, aggfunc='sum')
store_type_wise_order = pd.crosstab(index=train.index, columns=train.
    ↪ Store_Type, values =train.Order, aggfunc='sum')
location_wise_order = pd.crosstab(index=train.index, columns=train.
    ↪ Location_Type, values =train.Order, aggfunc='sum')
region_wise_order = pd.crosstab(index=train.index, columns=train.Region_Code,
    ↪ values =train.Order, aggfunc='sum')

# Create a Single DataFrame for Sales and Order
train_sales = pd.concat([overall_sales, id_wise_sales, store_type_wise_sales,
    ↪ location_wise_sales, region_wise_sales], axis=1)
train_order = pd.concat([overall_order, id_wise_order, store_type_wise_order,
    ↪ location_wise_order, region_wise_order], axis=1)

exog_train_holiday = train.groupby(train.index).mean('Holiday')['Holiday']
exog_test_holiday = test.groupby(test.index).mean('Holiday')['Holiday']
```



```
[114]: train_sales.sample(5)
```

```
[114]:
```

|            | Sales      | 1       | 2       | 3       | 4       | 5       | 6       | \ |
|------------|------------|---------|---------|---------|---------|---------|---------|---|
| 2018-02-17 | 14310783.0 | 20640.0 | 35442.0 | 45831.0 | 28461.0 | 47409.0 | 21192.0 |   |
| 2018-04-18 | 12723330.0 | 28029.0 | 22452.0 | 53787.0 | 21336.0 | 37323.0 | 34947.0 |   |
| 2018-09-22 | 15541707.0 | 45441.0 | 28767.0 | 71805.0 | 26781.0 | 43773.0 | 77217.0 |   |
| 2018-12-26 | 16289970.0 | 35292.0 | 52809.0 | 68925.0 | 45357.0 | 40401.0 | 22173.0 |   |
| 2018-04-20 | 14895594.0 | 30237.0 | 43641.0 | 51180.0 | 36099.0 | 46542.0 | 47790.0 |   |

|            | 7       | 8       | 9       | ... | S4        | L1        | L2        | \ |
|------------|---------|---------|---------|-----|-----------|-----------|-----------|---|
| 2018-02-17 | 34725.0 | 37458.0 | 33012.0 | ... | 4836258.0 | 6366114.0 | 5215773.0 |   |
| 2018-04-18 | 39132.0 | 33228.0 | 33969.0 | ... | 4302309.0 | 5592231.0 | 4615056.0 |   |
| 2018-09-22 | 64896.0 | 69903.0 | 29778.0 | ... | 5452764.0 | 6900450.0 | 5614299.0 |   |
| 2018-12-26 | 31599.0 | 66489.0 | 39738.0 | ... | 5594970.0 | 7072977.0 | 5837862.0 |   |
| 2018-04-20 | 50487.0 | 60261.0 | 35535.0 | ... | 4952796.0 | 6550737.0 | 5223570.0 |   |

|            | L3        | L4       | L5       | R1        | R2        | R3        | \ |
|------------|-----------|----------|----------|-----------|-----------|-----------|---|
| 2018-02-17 | 1668222.0 | 516879.0 | 543795.0 | 5198505.0 | 3897471.0 | 3225231.0 |   |
| 2018-04-18 | 1510986.0 | 469251.0 | 535806.0 | 4592550.0 | 3515751.0 | 2911914.0 |   |
| 2018-09-22 | 1832052.0 | 521406.0 | 673500.0 | 5949081.0 | 4231203.0 | 3383079.0 |   |
| 2018-12-26 | 1995621.0 | 631731.0 | 751779.0 | 6023886.0 | 4183356.0 | 3968982.0 |   |
| 2018-04-20 | 1835229.0 | 613557.0 | 672501.0 | 5475228.0 | 4005525.0 | 3480258.0 |   |

|            | R4        |
|------------|-----------|
| 2018-02-17 | 1989576.0 |
| 2018-04-18 | 1703115.0 |
| 2018-09-22 | 1978344.0 |
| 2018-12-26 | 2113746.0 |
| 2018-04-20 | 1934583.0 |

[5 rows x 379 columns]

## 1.7 7. Time series plots

```
[115]: # Function to plot the data
def plot_sales(data, code):
    fig = go.Figure()
    fig.add_trace(go.Scatter(x=data.index, y=data[code], mode='lines', name=code))
    fig.add_trace(go.Bar(x=data.index, y=exog_train_holiday, name='campaign',
    ↪yaxis='y2', opacity=1))
    fig.update_layout(title=f'Timeseries for {code}', showlegend=False, title_x=0.
    ↪12,
        yaxis=dict(title='Sales Amount'),
        yaxis2=dict(overlying='y', showline=False, showgrid=False,
    ↪showticklabels=False, side='right'))
    return fig
```

```
def plot_order(data, code):
    fig = go.Figure()
    fig.add_trace(go.Scatter(x=data.index, y=data[code], mode='lines', name=code))
    fig.add_trace(go.Bar(x=data.index, y=exog_train_holiday, name='campaign',
↪yaxis='y2', opacity=1))
    fig.update_layout(title=f'Timeseries for {code}', showlegend=False, title_x=0.
↪12,
                      yaxis=dict(title='Order Volume'),
                      yaxis2=dict(overlying='y', showline=False, showgrid=False,
↪showticklabels=False, side='right'))
    return fig
```

```
[116]: fig = make_subplots(rows=2, cols=1, specs=[[{"secondary_y": True}],
↪[{"secondary_y": True}]]
for trace in plot_order(overall_order, 'Order').data:
    secondary_y = "yaxis" in trace and trace["yaxis"] == "y2"
    fig.add_trace(trace, row=1, col=1)
for trace in plot_sales(overall_sales, 'Sales').data:
    secondary_y = "yaxis" in trace and trace["yaxis"] == "y2"
    fig.add_trace(trace, row=2, col=1)
fig.show()
```

```
[117]: df_order = region_wise_order
df_sales = region_wise_sales
for code in df_order.columns:
    plot_order(df_order, code).show()
    plot_sales(df_sales, code).show()
```

```
[118]: df_order = location_wise_order
df_sales = location_wise_sales
for code in df_order.columns:
    plot_order(df_order, code).show()
    plot_sales(df_sales, code).show()
```

```
[119]: df_order = store_type_wise_order
df_sales = store_type_wise_sales
for code in df_order.columns:
    plot_order(df_order, code).show()
    plot_sales(df_sales, code).show()
```

## 2 B. Stationarity, decomposition, detrending, ACF, and PACF

### 2.1 8. Stationarity test and decomposition

Most of timeseries model (like **AR**, **MA**, **ARIMA**) works on assumption of Stationarity, which makes it easier to predict future values, estimate model parameters, and perform statistical tests.

By transforming non-stationary data into a stationary form, analysts can apply a broader range of statistical tools and achieve more reliable results.

To check stationarity of timeseries we will use Augmented Dickey-Fuller test with 5% significance level as threshold.

```
[120]: # Import ACF/PACF plotting modules
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf

# Import Dickey-Fuller test
from statsmodels.tsa.stattools import adfuller
```

```
[121]: # Print Dickey-Fuller test insights
def adf_test(dataset):
    print(f'Results of Dickey-Fuller Test:')
    for column in dataset.columns:
        pvalue = adfuller(dataset[column])[1]
        if pvalue <= 0.05:
            print(f'\033[32mTimeseries for "{column}" is stationary', end='.\t')
        else:
            print(f'\033[31mTimeseries for "{column}" is not stationary', end='.')
        print(f'\t p-value is {pvalue}\033[0m')
```

```
[122]: adf_test(train_order)
adf_test(train_sales)
```

Results of Dickey-Fuller Test:

| Timeseries for "Order" is stationary. | p-value is |
|---------------------------------------|------------|
| 0.00019001472288566557                |            |
| Timeseries for "1" is stationary.     | p-value is |
| 3.3930512375433676e-07                |            |
| Timeseries for "2" is stationary.     | p-value is |
| 3.487864501563372e-05                 |            |
| Timeseries for "3" is stationary.     | p-value is |
| 0.0026307597340207416                 |            |
| Timeseries for "4" is stationary.     | p-value is |
| 2.1803807823009623e-12                |            |
| Timeseries for "5" is stationary.     | p-value is |
| 0.0001419446382003186                 |            |
| Timeseries for "6" is stationary.     | p-value is |
| 0.00205035109867991                   |            |
| Timeseries for "7" is stationary.     | p-value is |
| 0.00013323300549812953                |            |

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| Timeseries for "8" is stationary.  | p-value is |
| 2.2959953942007774e-07             |            |
| Timeseries for "9" is stationary.  | p-value is |
| 3.2347862976079523e-17             |            |
| Timeseries for "10" is stationary. | p-value is |
| 7.441225128758886e-06              |            |
| Timeseries for "11" is stationary. | p-value is |
| 3.628125417229516e-05              |            |
| Timeseries for "12" is stationary. | p-value is |
| 0.0013883312595671436              |            |
| Timeseries for "13" is stationary. | p-value is |
| 0.013189837370918795               |            |
| Timeseries for "14" is stationary. | p-value is |
| 0.00013405682296692347             |            |
| Timeseries for "15" is stationary. | p-value is |
| 5.111294828052101e-05              |            |
| Timeseries for "16" is stationary. | p-value is |
| 0.0009199590224398585              |            |
| Timeseries for "17" is stationary. | p-value is |
| 1.0711379964565977e-06             |            |
| Timeseries for "18" is stationary. | p-value is |
| 0.00012238000145299083             |            |
| Timeseries for "19" is stationary. | p-value is |
| 2.1112891772215627e-06             |            |
| Timeseries for "20" is stationary. | p-value is |
| 0.02374224801394575                |            |
| Timeseries for "21" is stationary. | p-value is |
| 0.00023624055901910664             |            |
| Timeseries for "22" is stationary. | p-value is |
| 3.8756263276873324e-05             |            |
| Timeseries for "23" is stationary. | p-value is |
| 0.0008614546829018442              |            |
| Timeseries for "24" is stationary. | p-value is |
| 0.0008344652715878641              |            |
| Timeseries for "25" is stationary. | p-value is |
| 1.1717640571394116e-24             |            |

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| Timeseries for "26" is stationary. | p-value is |
| 3.895907782815797e-07              |            |
| Timeseries for "27" is stationary. | p-value is |
| 4.21062260155192e-06               |            |
| Timeseries for "28" is stationary. | p-value is |
| 3.401045038842587e-05              |            |
| Timeseries for "29" is stationary. | p-value is |
| 8.314714296307071e-07              |            |
| Timeseries for "30" is stationary. | p-value is |
| 3.6441956726965804e-05             |            |
| Timeseries for "31" is stationary. | p-value is |
| 0.004680006836468052               |            |
| Timeseries for "32" is stationary. | p-value is |
| 7.348732211260025e-07              |            |
| Timeseries for "33" is stationary. | p-value is |
| 7.890619917291206e-13              |            |
| Timeseries for "34" is stationary. | p-value is |
| 4.512693454886711e-06              |            |
| Timeseries for "35" is stationary. | p-value is |
| 5.309425335125379e-07              |            |
| Timeseries for "36" is stationary. | p-value is |
| 2.1693219921700006e-05             |            |
| Timeseries for "37" is stationary. | p-value is |
| 2.8247390142701275e-11             |            |
| Timeseries for "38" is stationary. | p-value is |
| 0.010751046397342333               |            |
| Timeseries for "39" is stationary. | p-value is |
| 1.9876552667426326e-09             |            |
| Timeseries for "40" is stationary. | p-value is |
| 8.119240331224733e-05              |            |
| Timeseries for "41" is stationary. | p-value is |
| 1.580021909188928e-05              |            |
| Timeseries for "42" is stationary. | p-value is |
| 0.0005572886373698547              |            |
| Timeseries for "43" is stationary. | p-value is |
| 1.2638437278931261e-06             |            |

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| Timeseries for "44" is stationary.     | p-value is |
| 1.8030462937170134e-06                 |            |
| Timeseries for "45" is stationary.     | p-value is |
| 3.8124949892148184e-05                 |            |
| Timeseries for "46" is not stationary. | p-value is |
| 0.05535856530253811                    |            |
| Timeseries for "47" is stationary.     | p-value is |
| 1.8108070324666628e-06                 |            |
| Timeseries for "48" is stationary.     | p-value is |
| 2.5546797099157627e-06                 |            |
| Timeseries for "49" is stationary.     | p-value is |
| 0.0001435214955483385                  |            |
| Timeseries for "50" is stationary.     | p-value is |
| 5.993430215771944e-05                  |            |
| Timeseries for "51" is stationary.     | p-value is |
| 9.894957738616657e-06                  |            |
| Timeseries for "52" is stationary.     | p-value is |
| 7.393797204959565e-05                  |            |
| Timeseries for "53" is stationary.     | p-value is |
| 0.0007221302732318259                  |            |
| Timeseries for "54" is stationary.     | p-value is |
| 8.5513366100919e-06                    |            |
| Timeseries for "55" is stationary.     | p-value is |
| 2.5123285495137178e-05                 |            |
| Timeseries for "56" is stationary.     | p-value is |
| 1.4953534519962917e-06                 |            |
| Timeseries for "57" is stationary.     | p-value is |
| 1.2041706531829316e-06                 |            |
| Timeseries for "58" is not stationary. | p-value is |
| 0.09093201528108513                    |            |
| Timeseries for "59" is stationary.     | p-value is |
| 5.998154721746872e-05                  |            |
| Timeseries for "60" is stationary.     | p-value is |
| 1.698930370119066e-09                  |            |
| Timeseries for "61" is stationary.     | p-value is |
| 2.4968497740175623e-06                 |            |

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| Timeseries for "62" is stationary.     | p-value is |
| 1.497010164466012e-07                  |            |
| Timeseries for "63" is stationary.     | p-value is |
| 0.0013646209488178507                  |            |
| Timeseries for "64" is stationary.     | p-value is |
| 6.460736779407831e-05                  |            |
| Timeseries for "65" is not stationary. | p-value is |
| 0.5386965878127822                     |            |
| Timeseries for "66" is stationary.     | p-value is |
| 0.0002364189250287246                  |            |
| Timeseries for "67" is stationary.     | p-value is |
| 6.013978922957296e-06                  |            |
| Timeseries for "68" is stationary.     | p-value is |
| 1.6717487828797033e-13                 |            |
| Timeseries for "69" is stationary.     | p-value is |
| 1.3551035044719921e-05                 |            |
| Timeseries for "70" is stationary.     | p-value is |
| 0.007720591150134667                   |            |
| Timeseries for "71" is stationary.     | p-value is |
| 1.4830684877403486e-05                 |            |
| Timeseries for "72" is stationary.     | p-value is |
| 4.6820858273089173e-08                 |            |
| Timeseries for "73" is stationary.     | p-value is |
| 1.5741391779406382e-06                 |            |
| Timeseries for "74" is stationary.     | p-value is |
| 0.0043133262978212565                  |            |
| Timeseries for "75" is stationary.     | p-value is |
| 2.697111660497253e-05                  |            |
| Timeseries for "76" is stationary.     | p-value is |
| 2.5708528258692893e-06                 |            |
| Timeseries for "77" is stationary.     | p-value is |
| 3.8155980754113376e-05                 |            |
| Timeseries for "78" is stationary.     | p-value is |
| 0.00016147255591651057                 |            |
| Timeseries for "79" is stationary.     | p-value is |
| 2.605161896558134e-05                  |            |

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| Timeseries for "80" is stationary. | p-value is |
| 4.83481290686305e-05               |            |
| Timeseries for "81" is stationary. | p-value is |
| 3.737655970894863e-05              |            |
| Timeseries for "82" is stationary. | p-value is |
| 0.001993493594374998               |            |
| Timeseries for "83" is stationary. | p-value is |
| 7.004283797447677e-15              |            |
| Timeseries for "84" is stationary. | p-value is |
| 5.571904889755887e-05              |            |
| Timeseries for "85" is stationary. | p-value is |
| 0.0021295531650791922              |            |
| Timeseries for "86" is stationary. | p-value is |
| 4.372334149494939e-06              |            |
| Timeseries for "87" is stationary. | p-value is |
| 1.4046418027945153e-06             |            |
| Timeseries for "88" is stationary. | p-value is |
| 0.038354241685291696               |            |
| Timeseries for "89" is stationary. | p-value is |
| 0.002571840765244099               |            |
| Timeseries for "90" is stationary. | p-value is |
| 9.538544858757939e-05              |            |
| Timeseries for "91" is stationary. | p-value is |
| 0.000336206416799257               |            |
| Timeseries for "92" is stationary. | p-value is |
| 0.0017260076252782856              |            |
| Timeseries for "93" is stationary. | p-value is |
| 0.001474124682377123               |            |
| Timeseries for "94" is stationary. | p-value is |
| 4.575949601838265e-07              |            |
| Timeseries for "95" is stationary. | p-value is |
| 0.001317343984144627               |            |
| Timeseries for "96" is stationary. | p-value is |
| 0.0006942335774146915              |            |
| Timeseries for "97" is stationary. | p-value is |
| 0.00012180161288027802             |            |



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| Timeseries for "98" is stationary.  | p-value is |
| 8.74848672780359e-08                |            |
| Timeseries for "99" is stationary.  | p-value is |
| 3.955645993497474e-06               |            |
| Timeseries for "100" is stationary. | p-value is |
| 0.0006469654542312705               |            |
| Timeseries for "101" is stationary. | p-value is |
| 2.0153101703932955e-07              |            |
| Timeseries for "102" is stationary. | p-value is |
| 9.487147439371601e-11               |            |
| Timeseries for "103" is stationary. | p-value is |
| 6.565326305306632e-07               |            |
| Timeseries for "104" is stationary. | p-value is |
| 3.6991285343036747e-07              |            |
| Timeseries for "105" is stationary. | p-value is |
| 0.011071898631391009                |            |
| Timeseries for "106" is stationary. | p-value is |
| 3.155230372582543e-05               |            |
| Timeseries for "107" is stationary. | p-value is |
| 0.00026624851390524433              |            |
| Timeseries for "108" is stationary. | p-value is |
| 1.853967025189231e-10               |            |
| Timeseries for "109" is stationary. | p-value is |
| 8.749008795477004e-05               |            |
| Timeseries for "110" is stationary. | p-value is |
| 3.149313591033713e-06               |            |
| Timeseries for "111" is stationary. | p-value is |
| 1.0091425117159596e-05              |            |
| Timeseries for "112" is stationary. | p-value is |
| 6.520659064953944e-05               |            |
| Timeseries for "113" is stationary. | p-value is |
| 1.7865455026889918e-10              |            |
| Timeseries for "114" is stationary. | p-value is |
| 8.301087012248881e-12               |            |
| Timeseries for "115" is stationary. | p-value is |
| 0.00012583256779253316              |            |

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| Timeseries for "116" is stationary. | p-value is |
| 1.1834075230958227e-10              |            |
| Timeseries for "117" is stationary. | p-value is |
| 1.9718918986153662e-06              |            |
| Timeseries for "118" is stationary. | p-value is |
| 1.0933309998271666e-10              |            |
| Timeseries for "119" is stationary. | p-value is |
| 0.00014708357883481274              |            |
| Timeseries for "120" is stationary. | p-value is |
| 9.913511150912327e-06               |            |
| Timeseries for "121" is stationary. | p-value is |
| 2.723225101853458e-06               |            |
| Timeseries for "122" is stationary. | p-value is |
| 1.1752964130149005e-05              |            |
| Timeseries for "123" is stationary. | p-value is |
| 2.139101441311718e-05               |            |
| Timeseries for "124" is stationary. | p-value is |
| 7.896420187636915e-07               |            |
| Timeseries for "125" is stationary. | p-value is |
| 0.00011947851846840942              |            |
| Timeseries for "126" is stationary. | p-value is |
| 3.8620535186139247e-07              |            |
| Timeseries for "127" is stationary. | p-value is |
| 3.5670950681081125e-07              |            |
| Timeseries for "128" is stationary. | p-value is |
| 0.010633702829589706                |            |
| Timeseries for "129" is stationary. | p-value is |
| 5.203292864137039e-07               |            |
| Timeseries for "130" is stationary. | p-value is |
| 1.8908153585059535e-06              |            |
| Timeseries for "131" is stationary. | p-value is |
| 0.0007262619422735948               |            |
| Timeseries for "132" is stationary. | p-value is |
| 8.333259467777589e-07               |            |
| Timeseries for "133" is stationary. | p-value is |
| 6.789011652574819e-05               |            |

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| Timeseries for "134" is stationary. | p-value is |
| 2.076297711073456e-07               |            |
| Timeseries for "135" is stationary. | p-value is |
| 3.2544088194635824e-06              |            |
| Timeseries for "136" is stationary. | p-value is |
| 0.0016451747085213385               |            |
| Timeseries for "137" is stationary. | p-value is |
| 2.0090805067845517e-06              |            |
| Timeseries for "138" is stationary. | p-value is |
| 4.270008858444917e-14               |            |
| Timeseries for "139" is stationary. | p-value is |
| 1.6747504360262133e-05              |            |
| Timeseries for "140" is stationary. | p-value is |
| 1.7306650304429188e-07              |            |
| Timeseries for "141" is stationary. | p-value is |
| 2.916748711073959e-05               |            |
| Timeseries for "142" is stationary. | p-value is |
| 3.1496676944661386e-08              |            |
| Timeseries for "143" is stationary. | p-value is |
| 2.3086234268581383e-06              |            |
| Timeseries for "144" is stationary. | p-value is |
| 1.5799794695725325e-11              |            |
| Timeseries for "145" is stationary. | p-value is |
| 4.299464534141279e-06               |            |
| Timeseries for "146" is stationary. | p-value is |
| 0.002468515341846608                |            |
| Timeseries for "147" is stationary. | p-value is |
| 0.00016865675111165732              |            |
| Timeseries for "148" is stationary. | p-value is |
| 4.5403535839328955e-05              |            |
| Timeseries for "149" is stationary. | p-value is |
| 8.295417566991276e-05               |            |
| Timeseries for "150" is stationary. | p-value is |
| 1.0767614434951178e-05              |            |
| Timeseries for "151" is stationary. | p-value is |
| 3.969608207812673e-10               |            |

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| Timeseries for "152" is stationary. | p-value is |
| 5.0078497482456014e-08              |            |
| Timeseries for "153" is stationary. | p-value is |
| 8.444282283952105e-05               |            |
| Timeseries for "154" is stationary. | p-value is |
| 3.383442764215231e-07               |            |
| Timeseries for "155" is stationary. | p-value is |
| 0.00017102218547661131              |            |
| Timeseries for "156" is stationary. | p-value is |
| 5.258887943929971e-08               |            |
| Timeseries for "157" is stationary. | p-value is |
| 6.929853876090441e-08               |            |
| Timeseries for "158" is stationary. | p-value is |
| 6.928076436982305e-05               |            |
| Timeseries for "159" is stationary. | p-value is |
| 0.0035456517565745213               |            |
| Timeseries for "160" is stationary. | p-value is |
| 0.0009795640542862624               |            |
| Timeseries for "161" is stationary. | p-value is |
| 7.780640147016751e-06               |            |
| Timeseries for "162" is stationary. | p-value is |
| 1.254621575298791e-07               |            |
| Timeseries for "163" is stationary. | p-value is |
| 2.58094892281611e-12                |            |
| Timeseries for "164" is stationary. | p-value is |
| 0.0004686842928708999               |            |
| Timeseries for "165" is stationary. | p-value is |
| 0.00016959509179191538              |            |
| Timeseries for "166" is stationary. | p-value is |
| 8.785738747623313e-06               |            |
| Timeseries for "167" is stationary. | p-value is |
| 0.0002595137175460508               |            |
| Timeseries for "168" is stationary. | p-value is |
| 7.077563909724307e-12               |            |
| Timeseries for "169" is stationary. | p-value is |
| 2.7700044055212924e-06              |            |

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| Timeseries for "170" is stationary. | p-value is |
| 7.933104481738624e-07               |            |
| Timeseries for "171" is stationary. | p-value is |
| 4.870367624715471e-07               |            |
| Timeseries for "172" is stationary. | p-value is |
| 5.4642657233765346e-05              |            |
| Timeseries for "173" is stationary. | p-value is |
| 1.7146183668627356e-08              |            |
| Timeseries for "174" is stationary. | p-value is |
| 1.4697060127673197e-07              |            |
| Timeseries for "175" is stationary. | p-value is |
| 0.011386226098472138                |            |
| Timeseries for "176" is stationary. | p-value is |
| 9.684310863336179e-08               |            |
| Timeseries for "177" is stationary. | p-value is |
| 4.6954083274973815e-05              |            |
| Timeseries for "178" is stationary. | p-value is |
| 8.344840987786177e-05               |            |
| Timeseries for "179" is stationary. | p-value is |
| 2.444337187103508e-06               |            |
| Timeseries for "180" is stationary. | p-value is |
| 0.024807871541731644                |            |
| Timeseries for "181" is stationary. | p-value is |
| 5.246482640609067e-10               |            |
| Timeseries for "182" is stationary. | p-value is |
| 0.008143302537358305                |            |
| Timeseries for "183" is stationary. | p-value is |
| 1.4470425609233592e-08              |            |
| Timeseries for "184" is stationary. | p-value is |
| 0.00029333044859244315              |            |
| Timeseries for "185" is stationary. | p-value is |
| 5.79664288666121e-05                |            |
| Timeseries for "186" is stationary. | p-value is |
| 1.4051496255533592e-05              |            |
| Timeseries for "187" is stationary. | p-value is |
| 4.418015767340524e-07               |            |

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| Timeseries for "188" is stationary. | p-value is |
| 0.0007513225966590528               |            |
| Timeseries for "189" is stationary. | p-value is |
| 0.00025605639308622487              |            |
| Timeseries for "190" is stationary. | p-value is |
| 1.90552253482218e-11                |            |
| Timeseries for "191" is stationary. | p-value is |
| 2.9336876492075247e-06              |            |
| Timeseries for "192" is stationary. | p-value is |
| 8.765088353742073e-10               |            |
| Timeseries for "193" is stationary. | p-value is |
| 8.055484375320195e-11               |            |
| Timeseries for "194" is stationary. | p-value is |
| 8.901743696472675e-05               |            |
| Timeseries for "195" is stationary. | p-value is |
| 1.260124858225439e-26               |            |
| Timeseries for "196" is stationary. | p-value is |
| 7.910690793339057e-12               |            |
| Timeseries for "197" is stationary. | p-value is |
| 1.2289931875136164e-06              |            |
| Timeseries for "198" is stationary. | p-value is |
| 8.6523959256508e-07                 |            |
| Timeseries for "199" is stationary. | p-value is |
| 2.2316505781938132e-06              |            |
| Timeseries for "200" is stationary. | p-value is |
| 2.0404072737453138e-07              |            |
| Timeseries for "201" is stationary. | p-value is |
| 0.003151423510302445                |            |
| Timeseries for "202" is stationary. | p-value is |
| 4.227563608810947e-05               |            |
| Timeseries for "203" is stationary. | p-value is |
| 4.795911712537781e-09               |            |
| Timeseries for "204" is stationary. | p-value is |
| 4.3890601708509006e-14              |            |
| Timeseries for "205" is stationary. | p-value is |
| 5.856848465711828e-05               |            |

|                                         |            |
|-----------------------------------------|------------|
| Timeseries for "206" is not stationary. | p-value is |
| 0.10946694123579304                     |            |
| Timeseries for "207" is stationary.     | p-value is |
| 2.129647218943059e-06                   |            |
| Timeseries for "208" is stationary.     | p-value is |
| 2.5326725612245584e-06                  |            |
| Timeseries for "209" is stationary.     | p-value is |
| 6.311216582776823e-05                   |            |
| Timeseries for "210" is stationary.     | p-value is |
| 0.0017479461434251858                   |            |
| Timeseries for "211" is stationary.     | p-value is |
| 0.00024956553972248934                  |            |
| Timeseries for "212" is stationary.     | p-value is |
| 6.3276157098852926e-15                  |            |
| Timeseries for "213" is stationary.     | p-value is |
| 3.135286071523618e-05                   |            |
| Timeseries for "214" is stationary.     | p-value is |
| 3.717417906211807e-05                   |            |
| Timeseries for "215" is stationary.     | p-value is |
| 1.3190527302977789e-05                  |            |
| Timeseries for "216" is stationary.     | p-value is |
| 0.00021826854006605113                  |            |
| Timeseries for "217" is stationary.     | p-value is |
| 6.022004410721664e-06                   |            |
| Timeseries for "218" is stationary.     | p-value is |
| 7.364911445760457e-07                   |            |
| Timeseries for "219" is stationary.     | p-value is |
| 0.0001888642065283942                   |            |
| Timeseries for "220" is stationary.     | p-value is |
| 0.0004068319867345256                   |            |
| Timeseries for "221" is stationary.     | p-value is |
| 0.007102411382209182                    |            |
| Timeseries for "222" is stationary.     | p-value is |
| 5.947031939111964e-09                   |            |
| Timeseries for "223" is stationary.     | p-value is |
| 2.439924239963443e-05                   |            |

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| Timeseries for "224" is stationary. | p-value is |
| 0.0030196886119002292               |            |
| Timeseries for "225" is stationary. | p-value is |
| 4.567402188286042e-10               |            |
| Timeseries for "226" is stationary. | p-value is |
| 6.191692893768323e-07               |            |
| Timeseries for "227" is stationary. | p-value is |
| 2.819149099769977e-06               |            |
| Timeseries for "228" is stationary. | p-value is |
| 1.443445471807939e-06               |            |
| Timeseries for "229" is stationary. | p-value is |
| 0.0002227329582254047               |            |
| Timeseries for "230" is stationary. | p-value is |
| 5.9341160057158775e-06              |            |
| Timeseries for "231" is stationary. | p-value is |
| 1.9731989584590604e-06              |            |
| Timeseries for "232" is stationary. | p-value is |
| 4.862555599428091e-07               |            |
| Timeseries for "233" is stationary. | p-value is |
| 0.011116867819018121                |            |
| Timeseries for "234" is stationary. | p-value is |
| 1.2037130383192282e-05              |            |
| Timeseries for "235" is stationary. | p-value is |
| 0.000417775521394403                |            |
| Timeseries for "236" is stationary. | p-value is |
| 1.268816540835271e-06               |            |
| Timeseries for "237" is stationary. | p-value is |
| 3.3672373338658524e-10              |            |
| Timeseries for "238" is stationary. | p-value is |
| 5.658643960415718e-08               |            |
| Timeseries for "239" is stationary. | p-value is |
| 0.00030691128484766124              |            |
| Timeseries for "240" is stationary. | p-value is |
| 0.0025517073586012588               |            |
| Timeseries for "241" is stationary. | p-value is |
| 4.3461070113121813e-05              |            |



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| Timeseries for "242" is stationary.     | p-value is |
| 4.280415364093271e-06                   |            |
| Timeseries for "243" is stationary.     | p-value is |
| 0.00082853608587924                     |            |
| Timeseries for "244" is stationary.     | p-value is |
| 8.59350255222756e-06                    |            |
| Timeseries for "245" is stationary.     | p-value is |
| 4.730780677154208e-06                   |            |
| Timeseries for "246" is stationary.     | p-value is |
| 1.2161075846856997e-06                  |            |
| Timeseries for "247" is stationary.     | p-value is |
| 0.000131212453389353                    |            |
| Timeseries for "248" is stationary.     | p-value is |
| 1.7918944997759566e-07                  |            |
| Timeseries for "249" is stationary.     | p-value is |
| 0.00036607129773350347                  |            |
| Timeseries for "250" is stationary.     | p-value is |
| 1.681901006718479e-05                   |            |
| Timeseries for "251" is stationary.     | p-value is |
| 3.16610699463011e-07                    |            |
| Timeseries for "252" is stationary.     | p-value is |
| 3.9917513298946077e-05                  |            |
| Timeseries for "253" is not stationary. | p-value is |
| 0.06421249505051625                     |            |
| Timeseries for "254" is stationary.     | p-value is |
| 1.0883878110193443e-07                  |            |
| Timeseries for "255" is stationary.     | p-value is |
| 1.2025255429467576e-10                  |            |
| Timeseries for "256" is stationary.     | p-value is |
| 1.47893177255516e-05                    |            |
| Timeseries for "257" is stationary.     | p-value is |
| 1.4119363821673375e-12                  |            |
| Timeseries for "258" is stationary.     | p-value is |
| 4.992812079165035e-12                   |            |
| Timeseries for "259" is stationary.     | p-value is |
| 2.7924333928363728e-06                  |            |

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| Timeseries for "260" is stationary.     | p-value is |
| 4.262313061592368e-05                   |            |
| Timeseries for "261" is stationary.     | p-value is |
| 0.0006518111638001428                   |            |
| Timeseries for "262" is stationary.     | p-value is |
| 2.1527522559680643e-06                  |            |
| Timeseries for "263" is stationary.     | p-value is |
| 7.46919653800032e-08                    |            |
| Timeseries for "264" is stationary.     | p-value is |
| 1.961118300271593e-06                   |            |
| Timeseries for "265" is not stationary. | p-value is |
| 0.1747960816443197                      |            |
| Timeseries for "266" is not stationary. | p-value is |
| 0.058133744122539535                    |            |
| Timeseries for "267" is not stationary. | p-value is |
| 0.22647562713131197                     |            |
| Timeseries for "268" is stationary.     | p-value is |
| 0.00020972166741867673                  |            |
| Timeseries for "269" is stationary.     | p-value is |
| 0.018873041818966534                    |            |
| Timeseries for "270" is stationary.     | p-value is |
| 0.000327202401245754                    |            |
| Timeseries for "271" is stationary.     | p-value is |
| 0.00015498715561106764                  |            |
| Timeseries for "272" is stationary.     | p-value is |
| 1.6026841135698594e-05                  |            |
| Timeseries for "273" is stationary.     | p-value is |
| 1.777096064991541e-05                   |            |
| Timeseries for "274" is stationary.     | p-value is |
| 4.891416538817896e-06                   |            |
| Timeseries for "275" is stationary.     | p-value is |
| 3.6676556111398138e-28                  |            |
| Timeseries for "276" is stationary.     | p-value is |
| 2.4324285363767784e-06                  |            |
| Timeseries for "277" is stationary.     | p-value is |
| 0.00027601745945045623                  |            |

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| Timeseries for "278" is stationary. | p-value is |
| 0.000337388402361705                |            |
| Timeseries for "279" is stationary. | p-value is |
| 3.904208654283419e-05               |            |
| Timeseries for "280" is stationary. | p-value is |
| 0.00013857330387773327              |            |
| Timeseries for "281" is stationary. | p-value is |
| 7.932930575163268e-10               |            |
| Timeseries for "282" is stationary. | p-value is |
| 1.047579127750594e-05               |            |
| Timeseries for "283" is stationary. | p-value is |
| 0.0005137027537466457               |            |
| Timeseries for "284" is stationary. | p-value is |
| 0.0008325047934977306               |            |
| Timeseries for "285" is stationary. | p-value is |
| 8.313392586855961e-05               |            |
| Timeseries for "286" is stationary. | p-value is |
| 4.556157778610793e-05               |            |
| Timeseries for "287" is stationary. | p-value is |
| 7.263260514975754e-07               |            |
| Timeseries for "288" is stationary. | p-value is |
| 0.00011650204650465217              |            |
| Timeseries for "289" is stationary. | p-value is |
| 1.4920622861657612e-05              |            |
| Timeseries for "290" is stationary. | p-value is |
| 5.074459555452562e-05               |            |
| Timeseries for "291" is stationary. | p-value is |
| 0.005381741594836949                |            |
| Timeseries for "292" is stationary. | p-value is |
| 6.874333642198158e-05               |            |
| Timeseries for "293" is stationary. | p-value is |
| 0.00011136058526701835              |            |
| Timeseries for "294" is stationary. | p-value is |
| 0.0002833971345018345               |            |
| Timeseries for "295" is stationary. | p-value is |
| 1.1453974485699648e-06              |            |

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| Timeseries for "296" is stationary.     | p-value is |
| 0.028491948965722713                    |            |
| Timeseries for "297" is stationary.     | p-value is |
| 4.2705561064375764e-05                  |            |
| Timeseries for "298" is stationary.     | p-value is |
| 9.480148443769051e-08                   |            |
| Timeseries for "299" is stationary.     | p-value is |
| 1.0146305387454682e-07                  |            |
| Timeseries for "300" is not stationary. | p-value is |
| 0.18630095937928448                     |            |
| Timeseries for "301" is stationary.     | p-value is |
| 3.2775535933734434e-07                  |            |
| Timeseries for "302" is stationary.     | p-value is |
| 5.261582469974119e-06                   |            |
| Timeseries for "303" is stationary.     | p-value is |
| 0.005420856557244605                    |            |
| Timeseries for "304" is stationary.     | p-value is |
| 0.006520182864179445                    |            |
| Timeseries for "305" is stationary.     | p-value is |
| 8.500317481400646e-06                   |            |
| Timeseries for "306" is stationary.     | p-value is |
| 5.760695095601388e-14                   |            |
| Timeseries for "307" is stationary.     | p-value is |
| 3.6096933501381394e-05                  |            |
| Timeseries for "308" is stationary.     | p-value is |
| 4.449914013860301e-05                   |            |
| Timeseries for "309" is stationary.     | p-value is |
| 0.0004323393777942778                   |            |
| Timeseries for "310" is stationary.     | p-value is |
| 0.004787697776453726                    |            |
| Timeseries for "311" is stationary.     | p-value is |
| 0.0002560641465854551                   |            |
| Timeseries for "312" is stationary.     | p-value is |
| 0.0005534276875624203                   |            |
| Timeseries for "313" is stationary.     | p-value is |
| 1.8485663934821887e-06                  |            |

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| Timeseries for "314" is stationary. | p-value is |
| 0.0003996736239977625               |            |
| Timeseries for "315" is stationary. | p-value is |
| 0.049945737852137115                |            |
| Timeseries for "316" is stationary. | p-value is |
| 5.580870911314861e-10               |            |
| Timeseries for "317" is stationary. | p-value is |
| 1.9995511777153038e-24              |            |
| Timeseries for "318" is stationary. | p-value is |
| 4.330003152273656e-05               |            |
| Timeseries for "319" is stationary. | p-value is |
| 0.00026576526709938883              |            |
| Timeseries for "320" is stationary. | p-value is |
| 0.0005206065180896851               |            |
| Timeseries for "321" is stationary. | p-value is |
| 0.0018378495059394606               |            |
| Timeseries for "322" is stationary. | p-value is |
| 0.0027337126834068334               |            |
| Timeseries for "323" is stationary. | p-value is |
| 0.00025392437959206166              |            |
| Timeseries for "324" is stationary. | p-value is |
| 0.000347430239172436                |            |
| Timeseries for "325" is stationary. | p-value is |
| 0.017294976083193546                |            |
| Timeseries for "326" is stationary. | p-value is |
| 7.976834333173641e-06               |            |
| Timeseries for "327" is stationary. | p-value is |
| 0.0018461029029841654               |            |
| Timeseries for "328" is stationary. | p-value is |
| 0.0004832099037848997               |            |
| Timeseries for "329" is stationary. | p-value is |
| 3.960684881695652e-05               |            |
| Timeseries for "330" is stationary. | p-value is |
| 0.0033753156780492117               |            |
| Timeseries for "331" is stationary. | p-value is |
| 3.992483857195217e-07               |            |

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| Timeseries for "332" is stationary. | p-value is |
| 1.304637100924014e-06               |            |
| Timeseries for "333" is stationary. | p-value is |
| 4.323510712103889e-07               |            |
| Timeseries for "334" is stationary. | p-value is |
| 1.062355460743779e-05               |            |
| Timeseries for "335" is stationary. | p-value is |
| 0.00907332173138183                 |            |
| Timeseries for "336" is stationary. | p-value is |
| 0.00011682094299079566              |            |
| Timeseries for "337" is stationary. | p-value is |
| 2.5499577221748048e-05              |            |
| Timeseries for "338" is stationary. | p-value is |
| 1.0902150461238297e-05              |            |
| Timeseries for "339" is stationary. | p-value is |
| 0.011717640533577376                |            |
| Timeseries for "340" is stationary. | p-value is |
| 5.511231332364279e-06               |            |
| Timeseries for "341" is stationary. | p-value is |
| 7.241594054128154e-06               |            |
| Timeseries for "342" is stationary. | p-value is |
| 6.888647997770799e-07               |            |
| Timeseries for "343" is stationary. | p-value is |
| 8.800446125133676e-05               |            |
| Timeseries for "344" is stationary. | p-value is |
| 3.073854857697815e-08               |            |
| Timeseries for "345" is stationary. | p-value is |
| 1.5548309912031497e-25              |            |
| Timeseries for "346" is stationary. | p-value is |
| 1.9026313860071634e-05              |            |
| Timeseries for "347" is stationary. | p-value is |
| 1.8563510927320425e-06              |            |
| Timeseries for "348" is stationary. | p-value is |
| 4.410469136597884e-05               |            |
| Timeseries for "349" is stationary. | p-value is |
| 3.3725610944696004e-06              |            |

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| Timeseries for "350" is stationary. | p-value is |
| 0.00048950590573241                 |            |
| Timeseries for "351" is stationary. | p-value is |
| 1.3554110180357414e-05              |            |
| Timeseries for "352" is stationary. | p-value is |
| 0.03502712286435989                 |            |
| Timeseries for "353" is stationary. | p-value is |
| 4.438801287468647e-06               |            |
| Timeseries for "354" is stationary. | p-value is |
| 8.730174857855914e-08               |            |
| Timeseries for "355" is stationary. | p-value is |
| 2.321036507600439e-05               |            |
| Timeseries for "356" is stationary. | p-value is |
| 0.0003218863348237397               |            |
| Timeseries for "357" is stationary. | p-value is |
| 0.010030744366767177                |            |
| Timeseries for "358" is stationary. | p-value is |
| 2.8263736825744944e-06              |            |
| Timeseries for "359" is stationary. | p-value is |
| 0.0008662720360079804               |            |
| Timeseries for "360" is stationary. | p-value is |
| 8.98195210246438e-08                |            |
| Timeseries for "361" is stationary. | p-value is |
| 8.809429002921898e-06               |            |
| Timeseries for "362" is stationary. | p-value is |
| 0.000663340062058788                |            |
| Timeseries for "363" is stationary. | p-value is |
| 0.0010172862630813118               |            |
| Timeseries for "364" is stationary. | p-value is |
| 2.4175579825030357e-06              |            |
| Timeseries for "365" is stationary. | p-value is |
| 0.0021034988056674894               |            |
| Timeseries for "S1" is stationary.  | p-value is |
| 7.793448064208875e-05               |            |
| Timeseries for "S2" is stationary.  | p-value is |
| 3.19465531365585e-05                |            |

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| Timeseries for "S3" is stationary.    | p-value is |
| 0.0004455172797190973                 |            |
| Timeseries for "S4" is stationary.    | p-value is |
| 0.0005447205594067498                 |            |
| Timeseries for "L1" is stationary.    | p-value is |
| 0.00014331514294486087                |            |
| Timeseries for "L2" is stationary.    | p-value is |
| 0.00044985543030531615                |            |
| Timeseries for "L3" is stationary.    | p-value is |
| 6.657730739788191e-05                 |            |
| Timeseries for "L4" is stationary.    | p-value is |
| 5.520188415032601e-06                 |            |
| Timeseries for "L5" is stationary.    | p-value is |
| 2.446372236792949e-05                 |            |
| Timeseries for "R1" is stationary.    | p-value is |
| 0.0004224908491593281                 |            |
| Timeseries for "R2" is stationary.    | p-value is |
| 4.5432256312175485e-05                |            |
| Timeseries for "R3" is stationary.    | p-value is |
| 0.00017724010576170132                |            |
| Timeseries for "R4" is stationary.    | p-value is |
| 0.00017453874458951745                |            |
| <b>Results of Dickey-Fuller Test:</b> |            |
| Timeseries for "Sales" is stationary. | p-value is |
| 0.007386718711362291                  |            |
| Timeseries for "1" is stationary.     | p-value is |
| 0.0010072301346594694                 |            |
| Timeseries for "2" is stationary.     | p-value is |
| 0.00031561292823509697                |            |
| Timeseries for "3" is stationary.     | p-value is |
| 0.008991511921083089                  |            |
| Timeseries for "4" is stationary.     | p-value is |
| 0.0002737671033380586                 |            |
| Timeseries for "5" is stationary.     | p-value is |
| 0.005051306139498418                  |            |
| Timeseries for "6" is stationary.     | p-value is |
| 0.013888862311180786                  |            |



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| Timeseries for "7" is stationary.  | p-value is |
| 0.008717157545251193               |            |
| Timeseries for "8" is stationary.  | p-value is |
| 0.00013217108310095338             |            |
| Timeseries for "9" is stationary.  | p-value is |
| 2.9868967309125026e-21             |            |
| Timeseries for "10" is stationary. | p-value is |
| 9.122877817511299e-05              |            |
| Timeseries for "11" is stationary. | p-value is |
| 0.00023967290176901514             |            |
| Timeseries for "12" is stationary. | p-value is |
| 0.009512150715144845               |            |
| Timeseries for "13" is stationary. | p-value is |
| 0.022684796879694213               |            |
| Timeseries for "14" is stationary. | p-value is |
| 0.0001438788771060245              |            |
| Timeseries for "15" is stationary. | p-value is |
| 0.0005642453559567487              |            |
| Timeseries for "16" is stationary. | p-value is |
| 0.0008708998374719632              |            |
| Timeseries for "17" is stationary. | p-value is |
| 0.00015253072153556218             |            |
| Timeseries for "18" is stationary. | p-value is |
| 0.002310062738161719               |            |
| Timeseries for "19" is stationary. | p-value is |
| 0.0002075112312322143              |            |
| Timeseries for "20" is stationary. | p-value is |
| 0.013183196680306977               |            |
| Timeseries for "21" is stationary. | p-value is |
| 0.0013863982414371134              |            |
| Timeseries for "22" is stationary. | p-value is |
| 0.0006521497642114568              |            |
| Timeseries for "23" is stationary. | p-value is |
| 0.005768868464092041               |            |
| Timeseries for "24" is stationary. | p-value is |
| 0.016916048119491083               |            |

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| Timeseries for "25" is stationary. | p-value is |
| 3.558101260958532e-24              |            |
| Timeseries for "26" is stationary. | p-value is |
| 0.00017876734181824014             |            |
| Timeseries for "27" is stationary. | p-value is |
| 0.0003157634407573397              |            |
| Timeseries for "28" is stationary. | p-value is |
| 0.0010849474336122329              |            |
| Timeseries for "29" is stationary. | p-value is |
| 2.2234749436377456e-05             |            |
| Timeseries for "30" is stationary. | p-value is |
| 0.0005491655112836941              |            |
| Timeseries for "31" is stationary. | p-value is |
| 0.0074353945297359406              |            |
| Timeseries for "32" is stationary. | p-value is |
| 0.0023147416981024642              |            |
| Timeseries for "33" is stationary. | p-value is |
| 0.0002011310512751143              |            |
| Timeseries for "34" is stationary. | p-value is |
| 7.249322540028292e-05              |            |
| Timeseries for "35" is stationary. | p-value is |
| 0.0003736584947946565              |            |
| Timeseries for "36" is stationary. | p-value is |
| 0.0003777959298406816              |            |
| Timeseries for "37" is stationary. | p-value is |
| 1.393012778080807e-11              |            |
| Timeseries for "38" is stationary. | p-value is |
| 0.022930015602661512               |            |
| Timeseries for "39" is stationary. | p-value is |
| 9.569520115462759e-07              |            |
| Timeseries for "40" is stationary. | p-value is |
| 0.001904343486754834               |            |
| Timeseries for "41" is stationary. | p-value is |
| 0.0001738481437417984              |            |
| Timeseries for "42" is stationary. | p-value is |
| 0.007219768463646842               |            |

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| Timeseries for "43" is stationary.     | p-value is |
| 2.7440674341048e-10                    |            |
| Timeseries for "44" is stationary.     | p-value is |
| 2.8660386173796303e-05                 |            |
| Timeseries for "45" is stationary.     | p-value is |
| 0.0015535020882591192                  |            |
| Timeseries for "46" is stationary.     | p-value is |
| 0.029745293195268505                   |            |
| Timeseries for "47" is stationary.     | p-value is |
| 0.0005264761742407543                  |            |
| Timeseries for "48" is stationary.     | p-value is |
| 0.0009533733239574719                  |            |
| Timeseries for "49" is stationary.     | p-value is |
| 0.00018768351929052625                 |            |
| Timeseries for "50" is stationary.     | p-value is |
| 0.001821013315630373                   |            |
| Timeseries for "51" is stationary.     | p-value is |
| 9.709833091280135e-06                  |            |
| Timeseries for "52" is stationary.     | p-value is |
| 0.00010669142753664644                 |            |
| Timeseries for "53" is stationary.     | p-value is |
| 0.016944351315085673                   |            |
| Timeseries for "54" is stationary.     | p-value is |
| 0.00039906920191827295                 |            |
| Timeseries for "55" is stationary.     | p-value is |
| 0.0004199617709412446                  |            |
| Timeseries for "56" is stationary.     | p-value is |
| 0.0006155764926102539                  |            |
| Timeseries for "57" is stationary.     | p-value is |
| 0.0031306500293198517                  |            |
| Timeseries for "58" is not stationary. | p-value is |
| 0.05599412739299651                    |            |
| Timeseries for "59" is stationary.     | p-value is |
| 0.0005049044323103629                  |            |
| Timeseries for "60" is stationary.     | p-value is |
| 5.958124430320324e-06                  |            |

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| Timeseries for "61" is stationary.     | p-value is |
| 3.718347132257486e-05                  |            |
| Timeseries for "62" is stationary.     | p-value is |
| 0.0006939322440744843                  |            |
| Timeseries for "63" is stationary.     | p-value is |
| 0.005152732990119278                   |            |
| Timeseries for "64" is stationary.     | p-value is |
| 0.0041408112601858576                  |            |
| Timeseries for "65" is not stationary. | p-value is |
| 0.18483372921324598                    |            |
| Timeseries for "66" is stationary.     | p-value is |
| 0.0110642570537213                     |            |
| Timeseries for "67" is stationary.     | p-value is |
| 0.0001858253429276891                  |            |
| Timeseries for "68" is stationary.     | p-value is |
| 0.00021692105928102737                 |            |
| Timeseries for "69" is stationary.     | p-value is |
| 0.0002476726160297314                  |            |
| Timeseries for "70" is stationary.     | p-value is |
| 0.01610110687786486                    |            |
| Timeseries for "71" is stationary.     | p-value is |
| 0.0011138623056447929                  |            |
| Timeseries for "72" is stationary.     | p-value is |
| 0.0002259581081959068                  |            |
| Timeseries for "73" is stationary.     | p-value is |
| 0.00010750310980277186                 |            |
| Timeseries for "74" is stationary.     | p-value is |
| 0.028771409803396188                   |            |
| Timeseries for "75" is stationary.     | p-value is |
| 0.0008917292983730971                  |            |
| Timeseries for "76" is stationary.     | p-value is |
| 5.2358450002276005e-05                 |            |
| Timeseries for "77" is stationary.     | p-value is |
| 2.9809608530756844e-05                 |            |
| Timeseries for "78" is stationary.     | p-value is |
| 0.0009624697563829815                  |            |

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| Timeseries for "79" is stationary. | p-value is |
| 0.00016455991284978206             |            |
| Timeseries for "80" is stationary. | p-value is |
| 8.778855813241938e-05              |            |
| Timeseries for "81" is stationary. | p-value is |
| 0.00028144423489681505             |            |
| Timeseries for "82" is stationary. | p-value is |
| 0.005831163927923531               |            |
| Timeseries for "83" is stationary. | p-value is |
| 5.130846582256076e-05              |            |
| Timeseries for "84" is stationary. | p-value is |
| 0.0010651714308486657              |            |
| Timeseries for "85" is stationary. | p-value is |
| 2.363522318342324e-20              |            |
| Timeseries for "86" is stationary. | p-value is |
| 2.213457504886807e-05              |            |
| Timeseries for "87" is stationary. | p-value is |
| 5.4862893774895915e-05             |            |
| Timeseries for "88" is stationary. | p-value is |
| 0.04143993154659144                |            |
| Timeseries for "89" is stationary. | p-value is |
| 0.015928260812085347               |            |
| Timeseries for "90" is stationary. | p-value is |
| 0.00023417991573657947             |            |
| Timeseries for "91" is stationary. | p-value is |
| 0.001730456899608241               |            |
| Timeseries for "92" is stationary. | p-value is |
| 0.003953046849771409               |            |
| Timeseries for "93" is stationary. | p-value is |
| 3.525918966730799e-09              |            |
| Timeseries for "94" is stationary. | p-value is |
| 0.002427024960420313               |            |
| Timeseries for "95" is stationary. | p-value is |
| 2.376101389913979e-05              |            |
| Timeseries for "96" is stationary. | p-value is |
| 0.003137381413218535               |            |

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| Timeseries for "97" is stationary.  | p-value is |
| 0.00107602356931371                 |            |
| Timeseries for "98" is stationary.  | p-value is |
| 0.0004866827000706573               |            |
| Timeseries for "99" is stationary.  | p-value is |
| 1.082660925284785e-05               |            |
| Timeseries for "100" is stationary. | p-value is |
| 0.001790434955505629                |            |
| Timeseries for "101" is stationary. | p-value is |
| 0.00012110899978042064              |            |
| Timeseries for "102" is stationary. | p-value is |
| 0.0010391184787552944               |            |
| Timeseries for "103" is stationary. | p-value is |
| 2.0553471181387548e-05              |            |
| Timeseries for "104" is stationary. | p-value is |
| 2.9894270303828405e-05              |            |
| Timeseries for "105" is stationary. | p-value is |
| 0.033011775202366186                |            |
| Timeseries for "106" is stationary. | p-value is |
| 0.0006272473174448875               |            |
| Timeseries for "107" is stationary. | p-value is |
| 0.007526035876384321                |            |
| Timeseries for "108" is stationary. | p-value is |
| 4.568705663622652e-10               |            |
| Timeseries for "109" is stationary. | p-value is |
| 0.0009411371765543806               |            |
| Timeseries for "110" is stationary. | p-value is |
| 6.564392374203068e-05               |            |
| Timeseries for "111" is stationary. | p-value is |
| 0.0001936772455416642               |            |
| Timeseries for "112" is stationary. | p-value is |
| 0.00042618085530415407              |            |
| Timeseries for "113" is stationary. | p-value is |
| 0.00040523942375613343              |            |
| Timeseries for "114" is stationary. | p-value is |
| 0.0018411896874280392               |            |

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| Timeseries for "115" is stationary. | p-value is |
| 0.00025459123912125473              |            |
| Timeseries for "116" is stationary. | p-value is |
| 6.718188975618646e-09               |            |
| Timeseries for "117" is stationary. | p-value is |
| 8.361888003537213e-05               |            |
| Timeseries for "118" is stationary. | p-value is |
| 3.940266672700867e-05               |            |
| Timeseries for "119" is stationary. | p-value is |
| 0.0016617027675708542               |            |
| Timeseries for "120" is stationary. | p-value is |
| 0.00048028169836101647              |            |
| Timeseries for "121" is stationary. | p-value is |
| 3.854991998881068e-05               |            |
| Timeseries for "122" is stationary. | p-value is |
| 0.0004979907744716396               |            |
| Timeseries for "123" is stationary. | p-value is |
| 0.0014677193942636392               |            |
| Timeseries for "124" is stationary. | p-value is |
| 5.194863134877565e-05               |            |
| Timeseries for "125" is stationary. | p-value is |
| 0.0040296816181112916               |            |
| Timeseries for "126" is stationary. | p-value is |
| 3.3447916782392196e-05              |            |
| Timeseries for "127" is stationary. | p-value is |
| 0.0008367289602497126               |            |
| Timeseries for "128" is stationary. | p-value is |
| 0.020410203453832387                |            |
| Timeseries for "129" is stationary. | p-value is |
| 2.0264426392745064e-05              |            |
| Timeseries for "130" is stationary. | p-value is |
| 0.0018858058564864026               |            |
| Timeseries for "131" is stationary. | p-value is |
| 0.0046206644375212675               |            |
| Timeseries for "132" is stationary. | p-value is |
| 0.0003563715598358019               |            |

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| Timeseries for "133" is stationary. | p-value is |
| 0.005435325827521715                |            |
| Timeseries for "134" is stationary. | p-value is |
| 5.342157715564607e-06               |            |
| Timeseries for "135" is stationary. | p-value is |
| 0.00014829951342225866              |            |
| Timeseries for "136" is stationary. | p-value is |
| 0.004012635832407312                |            |
| Timeseries for "137" is stationary. | p-value is |
| 5.242918624304251e-05               |            |
| Timeseries for "138" is stationary. | p-value is |
| 1.6197594623572468e-05              |            |
| Timeseries for "139" is stationary. | p-value is |
| 0.00024690079368640434              |            |
| Timeseries for "140" is stationary. | p-value is |
| 6.0552756376033996e-05              |            |
| Timeseries for "141" is stationary. | p-value is |
| 1.3940381999497495e-05              |            |
| Timeseries for "142" is stationary. | p-value is |
| 3.1771690956939645e-05              |            |
| Timeseries for "143" is stationary. | p-value is |
| 0.0013764220384307369               |            |
| Timeseries for "144" is stationary. | p-value is |
| 0.0011179628381382566               |            |
| Timeseries for "145" is stationary. | p-value is |
| 6.816240842177759e-05               |            |
| Timeseries for "146" is stationary. | p-value is |
| 0.0024038829584976484               |            |
| Timeseries for "147" is stationary. | p-value is |
| 0.0004342759107233961               |            |
| Timeseries for "148" is stationary. | p-value is |
| 0.0003721526304682833               |            |
| Timeseries for "149" is stationary. | p-value is |
| 0.00033353783438898934              |            |
| Timeseries for "150" is stationary. | p-value is |
| 0.001320918604322212                |            |



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| Timeseries for "151" is stationary. | p-value is |
| 1.3941164437570472e-23              |            |
| Timeseries for "152" is stationary. | p-value is |
| 1.3245681031290174e-05              |            |
| Timeseries for "153" is stationary. | p-value is |
| 0.00045288873118110175              |            |
| Timeseries for "154" is stationary. | p-value is |
| 2.971020683912829e-05               |            |
| Timeseries for "155" is stationary. | p-value is |
| 0.0006735608962806927               |            |
| Timeseries for "156" is stationary. | p-value is |
| 6.066785295908553e-06               |            |
| Timeseries for "157" is stationary. | p-value is |
| 0.00285220447419756                 |            |
| Timeseries for "158" is stationary. | p-value is |
| 2.474079904845501e-06               |            |
| Timeseries for "159" is stationary. | p-value is |
| 0.0023826624953484387               |            |
| Timeseries for "160" is stationary. | p-value is |
| 0.0010601568081331778               |            |
| Timeseries for "161" is stationary. | p-value is |
| 0.0009006657928950012               |            |
| Timeseries for "162" is stationary. | p-value is |
| 0.00010029404247567932              |            |
| Timeseries for "163" is stationary. | p-value is |
| 0.00014355492991076837              |            |
| Timeseries for "164" is stationary. | p-value is |
| 0.001044396002093798                |            |
| Timeseries for "165" is stationary. | p-value is |
| 0.001030960509203344                |            |
| Timeseries for "166" is stationary. | p-value is |
| 3.2511195999710264e-05              |            |
| Timeseries for "167" is stationary. | p-value is |
| 0.0008504456432767575               |            |
| Timeseries for "168" is stationary. | p-value is |
| 1.7328311146079027e-11              |            |

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| Timeseries for "169" is stationary.     | p-value is |
| 2.767696645833784e-05                   |            |
| Timeseries for "170" is stationary.     | p-value is |
| 2.52699783654674e-05                    |            |
| Timeseries for "171" is stationary.     | p-value is |
| 1.7115680935026434e-05                  |            |
| Timeseries for "172" is stationary.     | p-value is |
| 0.002854645341767548                    |            |
| Timeseries for "173" is stationary.     | p-value is |
| 0.00037183650634175                     |            |
| Timeseries for "174" is stationary.     | p-value is |
| 0.0002977941654444389                   |            |
| Timeseries for "175" is stationary.     | p-value is |
| 0.02952885424160673                     |            |
| Timeseries for "176" is stationary.     | p-value is |
| 1.8652537044153936e-05                  |            |
| Timeseries for "177" is stationary.     | p-value is |
| 1.547311263471623e-05                   |            |
| Timeseries for "178" is stationary.     | p-value is |
| 2.3314004656250497e-05                  |            |
| Timeseries for "179" is stationary.     | p-value is |
| 5.050030649808855e-05                   |            |
| Timeseries for "180" is not stationary. | p-value is |
| 0.0704381670914891                      |            |
| Timeseries for "181" is stationary.     | p-value is |
| 4.945394454609212e-07                   |            |
| Timeseries for "182" is stationary.     | p-value is |
| 0.003012509403693294                    |            |
| Timeseries for "183" is stationary.     | p-value is |
| 2.3972410694476644e-06                  |            |
| Timeseries for "184" is stationary.     | p-value is |
| 0.0017036132869262238                   |            |
| Timeseries for "185" is stationary.     | p-value is |
| 0.003141264862993032                    |            |
| Timeseries for "186" is stationary.     | p-value is |
| 0.0008272973123651762                   |            |

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| Timeseries for "187" is stationary. | p-value is |
| 4.708091770182434e-05               |            |
| Timeseries for "188" is stationary. | p-value is |
| 0.0006248862296784562               |            |
| Timeseries for "189" is stationary. | p-value is |
| 0.0004549796057056625               |            |
| Timeseries for "190" is stationary. | p-value is |
| 5.330849934641119e-10               |            |
| Timeseries for "191" is stationary. | p-value is |
| 0.004964974511928851                |            |
| Timeseries for "192" is stationary. | p-value is |
| 9.930872498345495e-05               |            |
| Timeseries for "193" is stationary. | p-value is |
| 0.0012670189977772334               |            |
| Timeseries for "194" is stationary. | p-value is |
| 0.00024337166072774857              |            |
| Timeseries for "195" is stationary. | p-value is |
| 1.7231655740755665e-23              |            |
| Timeseries for "196" is stationary. | p-value is |
| 0.002368185711247773                |            |
| Timeseries for "197" is stationary. | p-value is |
| 0.00017823194694497425              |            |
| Timeseries for "198" is stationary. | p-value is |
| 0.00010982930721878995              |            |
| Timeseries for "199" is stationary. | p-value is |
| 0.00023593185533639865              |            |
| Timeseries for "200" is stationary. | p-value is |
| 1.0567546809902824e-05              |            |
| Timeseries for "201" is stationary. | p-value is |
| 0.006998287872963017                |            |
| Timeseries for "202" is stationary. | p-value is |
| 0.0005080831505495583               |            |
| Timeseries for "203" is stationary. | p-value is |
| 6.398004977933699e-05               |            |
| Timeseries for "204" is stationary. | p-value is |
| 9.457535216944182e-14               |            |

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| Timeseries for "205" is stationary.     | p-value is |
| 0.0002576764452714263                   |            |
| Timeseries for "206" is not stationary. | p-value is |
| 0.11490127651432774                     |            |
| Timeseries for "207" is stationary.     | p-value is |
| 0.0001155650001373095                   |            |
| Timeseries for "208" is stationary.     | p-value is |
| 2.1900987700222402e-05                  |            |
| Timeseries for "209" is stationary.     | p-value is |
| 0.00027185106615009943                  |            |
| Timeseries for "210" is stationary.     | p-value is |
| 0.006298983612997602                    |            |
| Timeseries for "211" is stationary.     | p-value is |
| 0.0030994427336336968                   |            |
| Timeseries for "212" is stationary.     | p-value is |
| 1.8384467255317023e-08                  |            |
| Timeseries for "213" is stationary.     | p-value is |
| 0.008280798571854726                    |            |
| Timeseries for "214" is stationary.     | p-value is |
| 0.0004324746095029078                   |            |
| Timeseries for "215" is stationary.     | p-value is |
| 3.011969529994633e-05                   |            |
| Timeseries for "216" is stationary.     | p-value is |
| 0.00034023366659356166                  |            |
| Timeseries for "217" is stationary.     | p-value is |
| 1.0426360674689158e-13                  |            |
| Timeseries for "218" is stationary.     | p-value is |
| 0.0002038366445523663                   |            |
| Timeseries for "219" is stationary.     | p-value is |
| 0.0014283352492701015                   |            |
| Timeseries for "220" is stationary.     | p-value is |
| 0.0004235424962425248                   |            |
| Timeseries for "221" is stationary.     | p-value is |
| 0.012636122090964205                    |            |
| Timeseries for "222" is stationary.     | p-value is |
| 2.7145152599663654e-05                  |            |

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| Timeseries for "223" is stationary. | p-value is |
| 0.00027199637367506587              |            |
| Timeseries for "224" is stationary. | p-value is |
| 0.002366804395631395                |            |
| Timeseries for "225" is stationary. | p-value is |
| 9.301170925790265e-06               |            |
| Timeseries for "226" is stationary. | p-value is |
| 3.774615392240189e-05               |            |
| Timeseries for "227" is stationary. | p-value is |
| 0.0003031420987914876               |            |
| Timeseries for "228" is stationary. | p-value is |
| 1.0055917243420243e-05              |            |
| Timeseries for "229" is stationary. | p-value is |
| 0.001197972329319524                |            |
| Timeseries for "230" is stationary. | p-value is |
| 0.0010340078587901392               |            |
| Timeseries for "231" is stationary. | p-value is |
| 1.7913763569179506e-05              |            |
| Timeseries for "232" is stationary. | p-value is |
| 6.014281109071207e-06               |            |
| Timeseries for "233" is stationary. | p-value is |
| 0.010232386336641242                |            |
| Timeseries for "234" is stationary. | p-value is |
| 3.519016261255216e-05               |            |
| Timeseries for "235" is stationary. | p-value is |
| 0.011869727260044585                |            |
| Timeseries for "236" is stationary. | p-value is |
| 6.156473227097317e-05               |            |
| Timeseries for "237" is stationary. | p-value is |
| 0.00036215914799563465              |            |
| Timeseries for "238" is stationary. | p-value is |
| 0.00010138689453172003              |            |
| Timeseries for "239" is stationary. | p-value is |
| 0.004431032640689593                |            |
| Timeseries for "240" is stationary. | p-value is |
| 0.01071496275530863                 |            |

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| Timeseries for "241" is stationary.     | p-value is |
| 0.00036218095880287697                  |            |
| Timeseries for "242" is stationary.     | p-value is |
| 1.1734247111458108e-05                  |            |
| Timeseries for "243" is stationary.     | p-value is |
| 0.00027508538682600276                  |            |
| Timeseries for "244" is stationary.     | p-value is |
| 0.0004002338454727453                   |            |
| Timeseries for "245" is stationary.     | p-value is |
| 9.233905576736461e-05                   |            |
| Timeseries for "246" is stationary.     | p-value is |
| 0.0002848468706414233                   |            |
| Timeseries for "247" is stationary.     | p-value is |
| 0.0005428265295455665                   |            |
| Timeseries for "248" is stationary.     | p-value is |
| 6.21331919358916e-05                    |            |
| Timeseries for "249" is stationary.     | p-value is |
| 0.0031294865525661013                   |            |
| Timeseries for "250" is stationary.     | p-value is |
| 0.00011577524298764726                  |            |
| Timeseries for "251" is stationary.     | p-value is |
| 6.502472970219795e-06                   |            |
| Timeseries for "252" is stationary.     | p-value is |
| 0.00297014133205754                     |            |
| Timeseries for "253" is not stationary. | p-value is |
| 0.06608166489018202                     |            |
| Timeseries for "254" is stationary.     | p-value is |
| 2.1890747666875984e-05                  |            |
| Timeseries for "255" is stationary.     | p-value is |
| 2.939232253840054e-10                   |            |
| Timeseries for "256" is stationary.     | p-value is |
| 0.00017599749674439765                  |            |
| Timeseries for "257" is stationary.     | p-value is |
| 1.6436838320565628e-12                  |            |
| Timeseries for "258" is stationary.     | p-value is |
| 0.0009504319588403772                   |            |

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| Timeseries for "259" is stationary.     | p-value is |
| 0.0016216262832032798                   |            |
| Timeseries for "260" is stationary.     | p-value is |
| 0.0011722661783458478                   |            |
| Timeseries for "261" is stationary.     | p-value is |
| 0.0005235278577295648                   |            |
| Timeseries for "262" is stationary.     | p-value is |
| 1.0318144047496912e-05                  |            |
| Timeseries for "263" is stationary.     | p-value is |
| 4.400555566004078e-05                   |            |
| Timeseries for "264" is stationary.     | p-value is |
| 3.108065694738563e-05                   |            |
| Timeseries for "265" is not stationary. | p-value is |
| 0.08932256866593069                     |            |
| Timeseries for "266" is stationary.     | p-value is |
| 0.006060811129853634                    |            |
| Timeseries for "267" is not stationary. | p-value is |
| 0.21304952243086084                     |            |
| Timeseries for "268" is stationary.     | p-value is |
| 0.0003218253261987438                   |            |
| Timeseries for "269" is stationary.     | p-value is |
| 0.00896151731908972                     |            |
| Timeseries for "270" is stationary.     | p-value is |
| 0.0068005208411403536                   |            |
| Timeseries for "271" is stationary.     | p-value is |
| 0.0006382871948541686                   |            |
| Timeseries for "272" is stationary.     | p-value is |
| 2.9372764717430668e-05                  |            |
| Timeseries for "273" is stationary.     | p-value is |
| 0.0004842498602359248                   |            |
| Timeseries for "274" is stationary.     | p-value is |
| 2.5258729215995463e-05                  |            |
| Timeseries for "275" is stationary.     | p-value is |
| 5.9645714026137255e-25                  |            |
| Timeseries for "276" is stationary.     | p-value is |
| 6.5745443216935096e-06                  |            |

|                                         |            |
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| Timeseries for "277" is stationary.     | p-value is |
| 0.00206096963439632                     |            |
| Timeseries for "278" is stationary.     | p-value is |
| 0.0013725775393979439                   |            |
| Timeseries for "279" is stationary.     | p-value is |
| 0.0019025742504396872                   |            |
| Timeseries for "280" is stationary.     | p-value is |
| 0.000842249239911077                    |            |
| Timeseries for "281" is stationary.     | p-value is |
| 7.884684312223885e-05                   |            |
| Timeseries for "282" is stationary.     | p-value is |
| 0.0003244246637642427                   |            |
| Timeseries for "283" is stationary.     | p-value is |
| 0.0010257519898195966                   |            |
| Timeseries for "284" is stationary.     | p-value is |
| 0.006683033168869181                    |            |
| Timeseries for "285" is stationary.     | p-value is |
| 0.00035279633702756287                  |            |
| Timeseries for "286" is stationary.     | p-value is |
| 0.00011239460818445546                  |            |
| Timeseries for "287" is stationary.     | p-value is |
| 2.6020055037444134e-05                  |            |
| Timeseries for "288" is stationary.     | p-value is |
| 0.00010793626885476344                  |            |
| Timeseries for "289" is stationary.     | p-value is |
| 0.000494607978341371                    |            |
| Timeseries for "290" is stationary.     | p-value is |
| 0.002578818632838419                    |            |
| Timeseries for "291" is not stationary. | p-value is |
| 0.05660839298732183                     |            |
| Timeseries for "292" is stationary.     | p-value is |
| 0.00138631804295186                     |            |
| Timeseries for "293" is stationary.     | p-value is |
| 9.227170846012794e-05                   |            |
| Timeseries for "294" is stationary.     | p-value is |
| 0.0019322849111849656                   |            |



|                                         |            |
|-----------------------------------------|------------|
| Timeseries for "295" is stationary.     | p-value is |
| 0.0003483226840811138                   |            |
| Timeseries for "296" is not stationary. | p-value is |
| 0.08522175424013323                     |            |
| Timeseries for "297" is stationary.     | p-value is |
| 0.0009513523148761597                   |            |
| Timeseries for "298" is stationary.     | p-value is |
| 2.3154900772002134e-07                  |            |
| Timeseries for "299" is stationary.     | p-value is |
| 8.198964138962852e-05                   |            |
| Timeseries for "300" is stationary.     | p-value is |
| 0.02960701081753662                     |            |
| Timeseries for "301" is stationary.     | p-value is |
| 0.0008024291068340855                   |            |
| Timeseries for "302" is stationary.     | p-value is |
| 8.288561721439884e-05                   |            |
| Timeseries for "303" is stationary.     | p-value is |
| 0.007511206148330425                    |            |
| Timeseries for "304" is stationary.     | p-value is |
| 0.016506561303227273                    |            |
| Timeseries for "305" is stationary.     | p-value is |
| 0.0004695374483105809                   |            |
| Timeseries for "306" is stationary.     | p-value is |
| 9.10652662005277e-14                    |            |
| Timeseries for "307" is stationary.     | p-value is |
| 0.0003212892838848065                   |            |
| Timeseries for "308" is stationary.     | p-value is |
| 0.0003516318904385247                   |            |
| Timeseries for "309" is stationary.     | p-value is |
| 8.144569755515096e-26                   |            |
| Timeseries for "310" is stationary.     | p-value is |
| 0.023236368768485848                    |            |
| Timeseries for "311" is stationary.     | p-value is |
| 0.001849704106143876                    |            |
| Timeseries for "312" is stationary.     | p-value is |
| 0.0031234616557759996                   |            |

|                                         |            |
|-----------------------------------------|------------|
| Timeseries for "313" is stationary.     | p-value is |
| 6.769873735967843e-05                   |            |
| Timeseries for "314" is stationary.     | p-value is |
| 0.00242119827219045                     |            |
| Timeseries for "315" is not stationary. | p-value is |
| 0.07098414793954455                     |            |
| Timeseries for "316" is stationary.     | p-value is |
| 0.00032883048073315533                  |            |
| Timeseries for "317" is stationary.     | p-value is |
| 0.008526634021654383                    |            |
| Timeseries for "318" is stationary.     | p-value is |
| 0.004451253636279219                    |            |
| Timeseries for "319" is stationary.     | p-value is |
| 0.0019990276271246873                   |            |
| Timeseries for "320" is stationary.     | p-value is |
| 0.002321073375819277                    |            |
| Timeseries for "321" is stationary.     | p-value is |
| 0.0043801553799993845                   |            |
| Timeseries for "322" is stationary.     | p-value is |
| 0.0029190152014397946                   |            |
| Timeseries for "323" is stationary.     | p-value is |
| 0.0055571501156199046                   |            |
| Timeseries for "324" is stationary.     | p-value is |
| 0.00407112225375758                     |            |
| Timeseries for "325" is not stationary. | p-value is |
| 0.05424739627652914                     |            |
| Timeseries for "326" is stationary.     | p-value is |
| 0.0001318294963165366                   |            |
| Timeseries for "327" is stationary.     | p-value is |
| 0.0040422211288417345                   |            |
| Timeseries for "328" is stationary.     | p-value is |
| 0.0005944383550889401                   |            |
| Timeseries for "329" is stationary.     | p-value is |
| 0.00027879216831228304                  |            |
| Timeseries for "330" is stationary.     | p-value is |
| 0.000998860758398374                    |            |

|                                     |            |
|-------------------------------------|------------|
| Timeseries for "331" is stationary. | p-value is |
| 1.3350525607786505e-05              |            |
| Timeseries for "332" is stationary. | p-value is |
| 5.378603187944803e-05               |            |
| Timeseries for "333" is stationary. | p-value is |
| 0.0006380804496381146               |            |
| Timeseries for "334" is stationary. | p-value is |
| 2.896472891471825e-05               |            |
| Timeseries for "335" is stationary. | p-value is |
| 0.017967412288814648                |            |
| Timeseries for "336" is stationary. | p-value is |
| 0.0006222975405897576               |            |
| Timeseries for "337" is stationary. | p-value is |
| 0.0006886776027446046               |            |
| Timeseries for "338" is stationary. | p-value is |
| 0.0003975014114795488               |            |
| Timeseries for "339" is stationary. | p-value is |
| 0.007551842387699304                |            |
| Timeseries for "340" is stationary. | p-value is |
| 5.8278185854456127e-05              |            |
| Timeseries for "341" is stationary. | p-value is |
| 0.024458939513174457                |            |
| Timeseries for "342" is stationary. | p-value is |
| 8.80299947584453e-22                |            |
| Timeseries for "343" is stationary. | p-value is |
| 0.0025455537863433918               |            |
| Timeseries for "344" is stationary. | p-value is |
| 0.000171545237044495                |            |
| Timeseries for "345" is stationary. | p-value is |
| 0.0004347580821028395               |            |
| Timeseries for "346" is stationary. | p-value is |
| 4.027542336281311e-05               |            |
| Timeseries for "347" is stationary. | p-value is |
| 9.323362886751891e-05               |            |
| Timeseries for "348" is stationary. | p-value is |
| 0.001596161922824127                |            |

|                                     |            |
|-------------------------------------|------------|
| Timeseries for "349" is stationary. | p-value is |
| 2.599161815081659e-05               |            |
| Timeseries for "350" is stationary. | p-value is |
| 0.002818972880596073                |            |
| Timeseries for "351" is stationary. | p-value is |
| 0.00013922679432018566              |            |
| Timeseries for "352" is stationary. | p-value is |
| 0.04481384730031847                 |            |
| Timeseries for "353" is stationary. | p-value is |
| 6.203586391737858e-05               |            |
| Timeseries for "354" is stationary. | p-value is |
| 0.0018002150858307112               |            |
| Timeseries for "355" is stationary. | p-value is |
| 0.003388497575288476                |            |
| Timeseries for "356" is stationary. | p-value is |
| 0.0019667757787619963               |            |
| Timeseries for "357" is stationary. | p-value is |
| 0.00254489802701704                 |            |
| Timeseries for "358" is stationary. | p-value is |
| 0.0021694578498596675               |            |
| Timeseries for "359" is stationary. | p-value is |
| 0.0007575061228127756               |            |
| Timeseries for "360" is stationary. | p-value is |
| 0.00021343745292771302              |            |
| Timeseries for "361" is stationary. | p-value is |
| 5.7338625887903014e-05              |            |
| Timeseries for "362" is stationary. | p-value is |
| 0.005608341846038478                |            |
| Timeseries for "363" is stationary. | p-value is |
| 0.0014778227742358158               |            |
| Timeseries for "364" is stationary. | p-value is |
| 0.00035559780959084524              |            |
| Timeseries for "365" is stationary. | p-value is |
| 0.012319364620433915                |            |
| Timeseries for "S1" is stationary.  | p-value is |
| 0.0056604416023610755               |            |

```

Timeseries for "S2" is stationary.      p-value is
0.003571295858539642
Timeseries for "S3" is stationary.      p-value is
0.011274338394491178
Timeseries for "S4" is stationary.      p-value is
0.009377000210500017
Timeseries for "L1" is stationary.      p-value is
0.007358214508015907
Timeseries for "L2" is stationary.      p-value is
0.009166726145432423
Timeseries for "L3" is stationary.      p-value is
0.004101073644607693
Timeseries for "L4" is stationary.      p-value is
0.0028948095280306304
Timeseries for "L5" is stationary.      p-value is
0.004235997270914649
Timeseries for "R1" is stationary.      p-value is
0.008887459005395964
Timeseries for "R2" is stationary.      p-value is
0.006066321673956619
Timeseries for "R3" is stationary.      p-value is
0.0059852511474317895
Timeseries for "R4" is stationary.      p-value is
0.0057033709981046225

```

## 2.2 9. ACF/PACF Charts

```

[148]: # ACF v/s PACF Plot
def acf_pacf_plot(series_sales:pd.Series,series_order:pd.Series)->None:
    fig, (ax1, ax2, ax3, ax4) = plt.subplots(1, 4, figsize=(13, 5))
    # Plot Sales ACF in first cell
    plot_acf(series_sales, ax=ax1)
    ax1.set_title(f'ACF for {series_sales.name} Sales')
    # Plot Sales PACF in second cell
    plot_pacf(series_sales, ax=ax2)
    ax2.set_title(f'PACF for {series_sales.name} Sales')

    # Plot Sales ACF in first cell
    plot_acf(series_order, ax=ax3)
    ax3.set_title(f'ACF for {series_sales.name} Order')

```

```

# Plot Sales PACF in second cell
plot_pacf(series_order, ax=ax4)
ax4.set_title(f'PACF for {series_sales.name} Order')

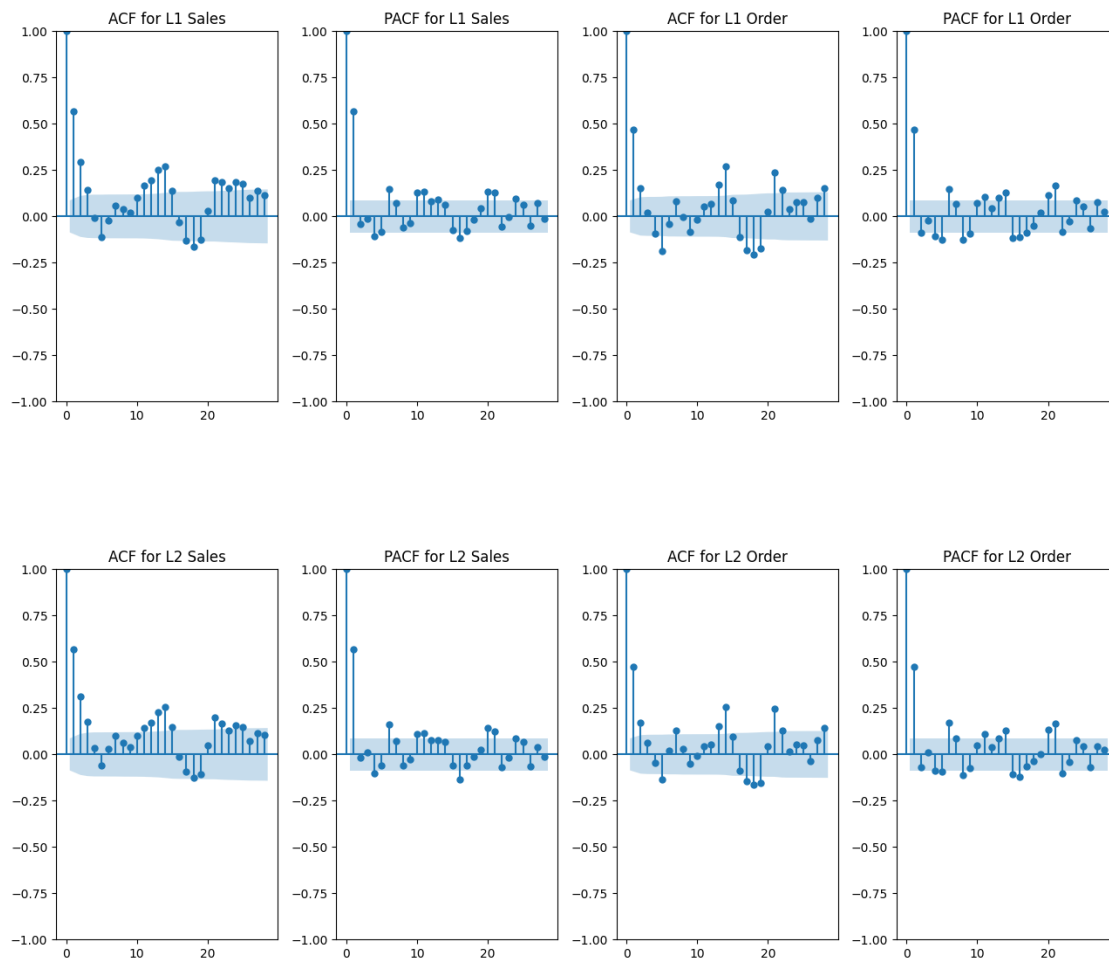
# Adjust layout
plt.tight_layout()
plt.show()

```

```

[149]: # Location Wise Sales and Order ACF/PACF Plot
data_sales = location_wise_sales
data_order = location_wise_order
for column in data_sales.columns:
    acf_pacf_plot(data_sales[column], data_order[column])

```





```
[150]: # Store type Wise Sales and Order ACF/PACF Plot
data_sales = store_type_wise_sales
```

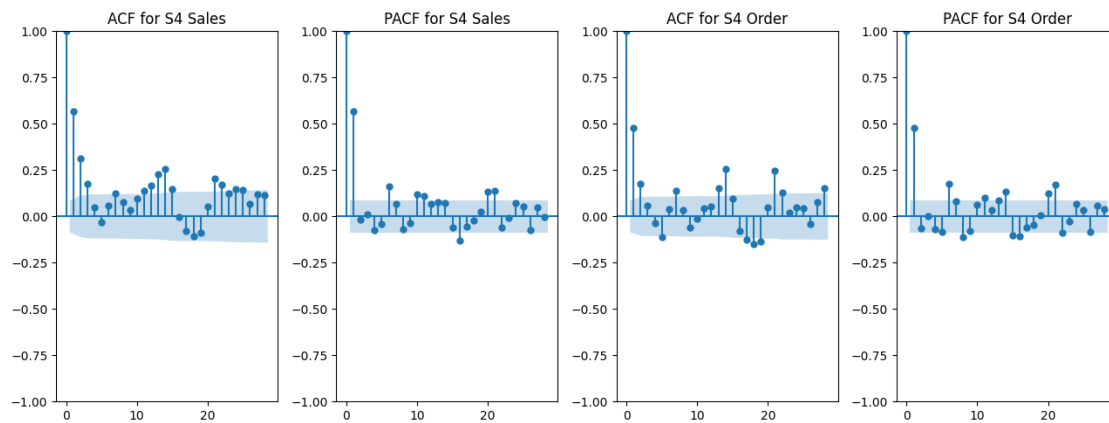
```

data_order = store_type_wise_order
for column in data_sales.columns:
    acf_pacf_plot(data_sales[column], data_order[column])

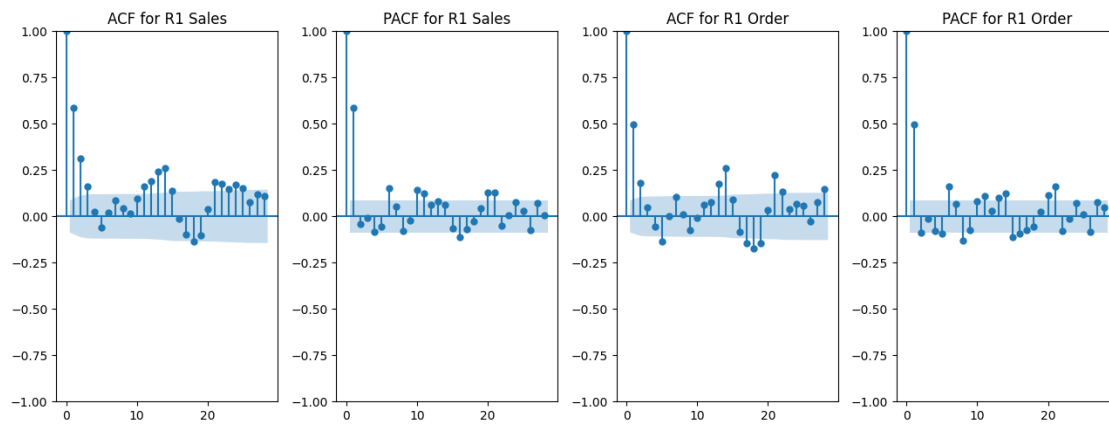
```

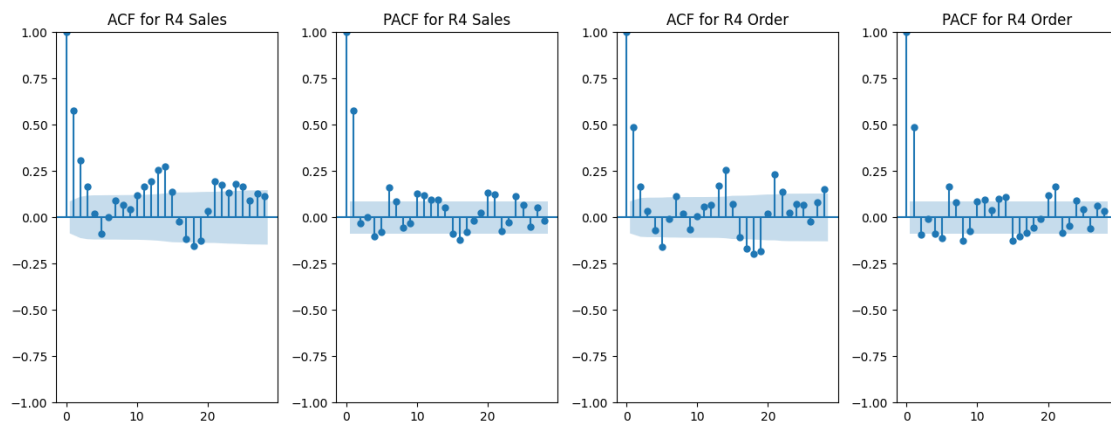
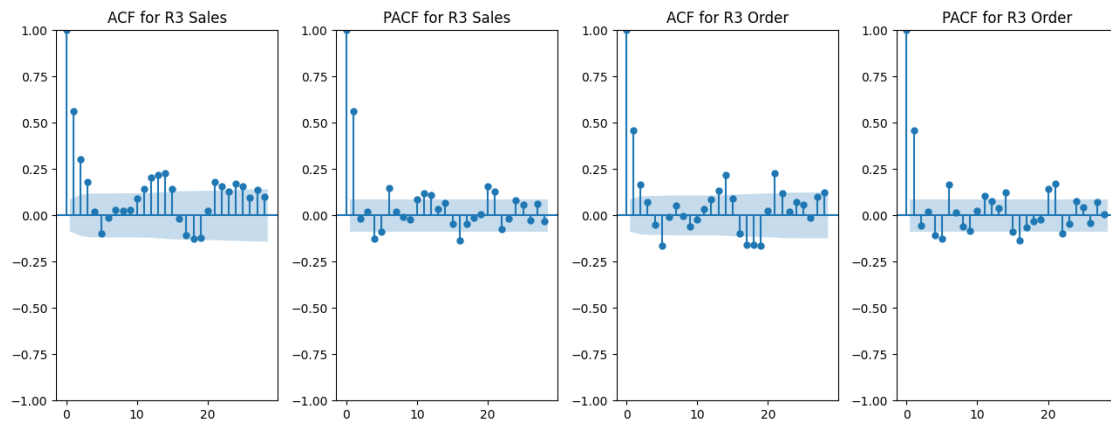
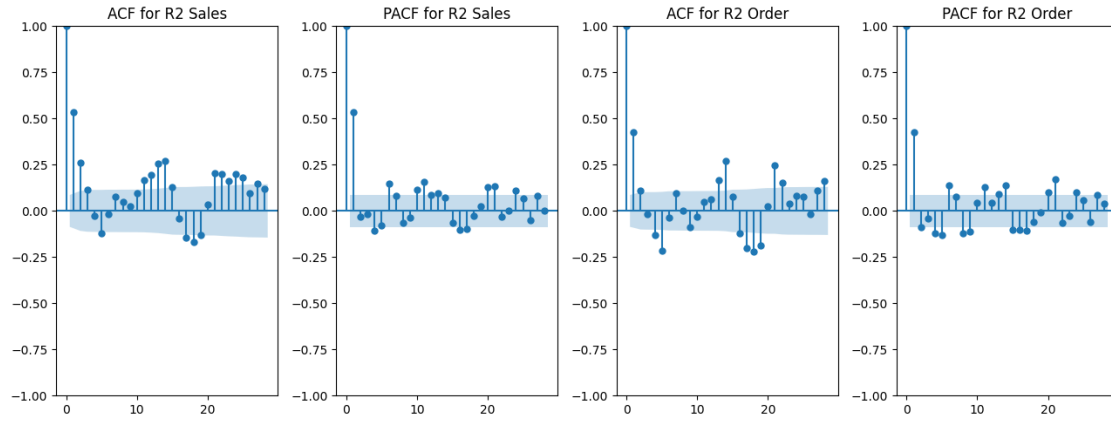






```
[151]: # Region Wise Sales and Order ACF/PACF Plot
data_sales = region_wise_sales
data_order = region_wise_order
for column in data_sales.columns:
    acf_pacf_plot(data_sales[column], data_order[column])
```





## 2.3 10. Seasonality Charts

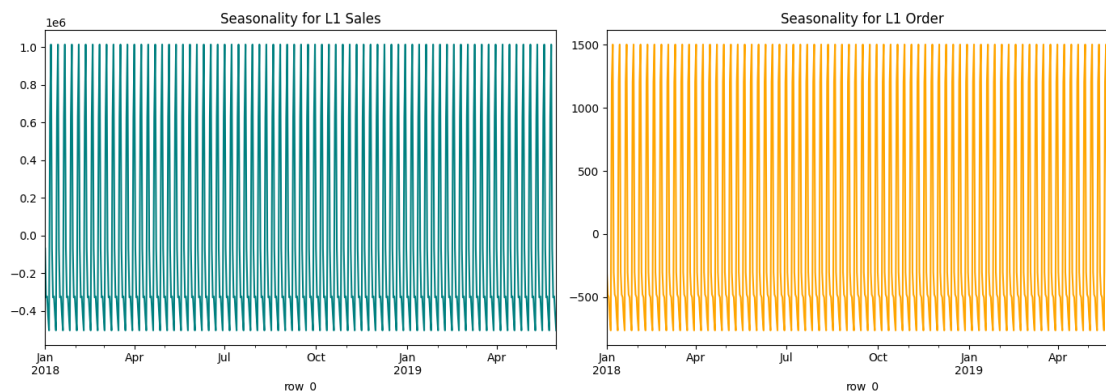
```
[152]: # Seasonality Charts function
from statsmodels.tsa.seasonal import seasonal_decompose

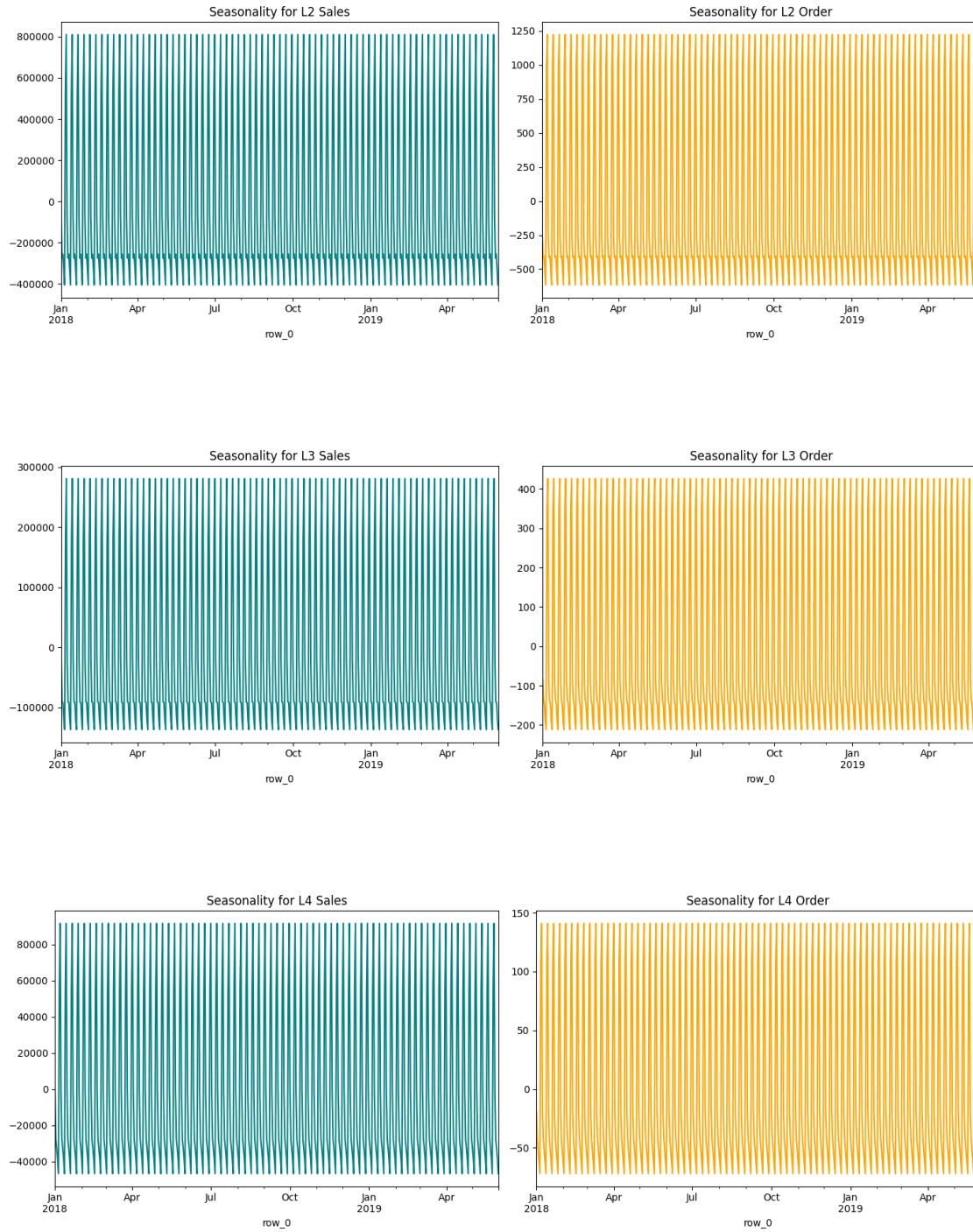
def seasonal_chart(series_sales, series_order):

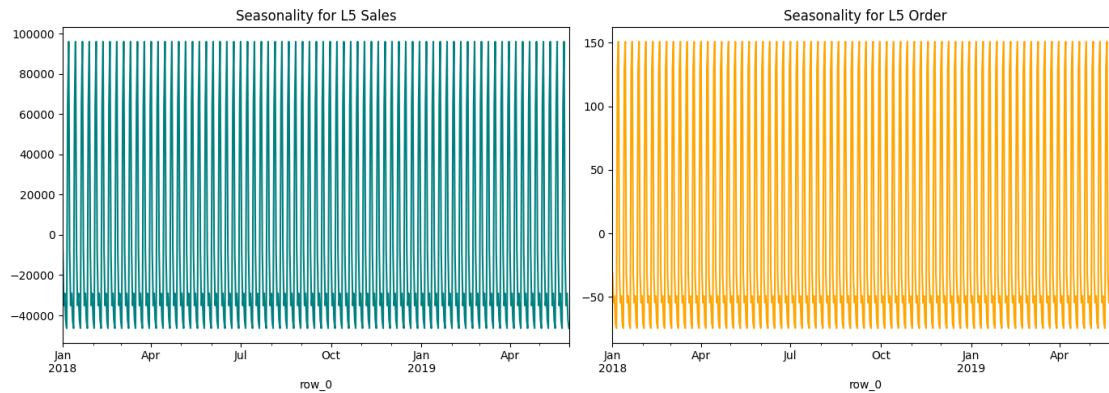
    fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(14, 5))
    # Plot Sales Seasonality in first cell
    result = seasonal_decompose(series_sales, model='additive', period=None)
    result.seasonal.plot(ax=ax1, color='teal')
    ax1.set_title(f'Seasonality for {series_sales.name} Sales')
    # Plot Order Seasonality in second cell
    result = seasonal_decompose(series_order, model='additive', period=None)
    result.seasonal.plot(ax=ax2, color='Orange')
    ax2.set_title(f'Seasonality for {series_order.name} Order')

    # Adjust layout
    plt.tight_layout()
    plt.show()
```

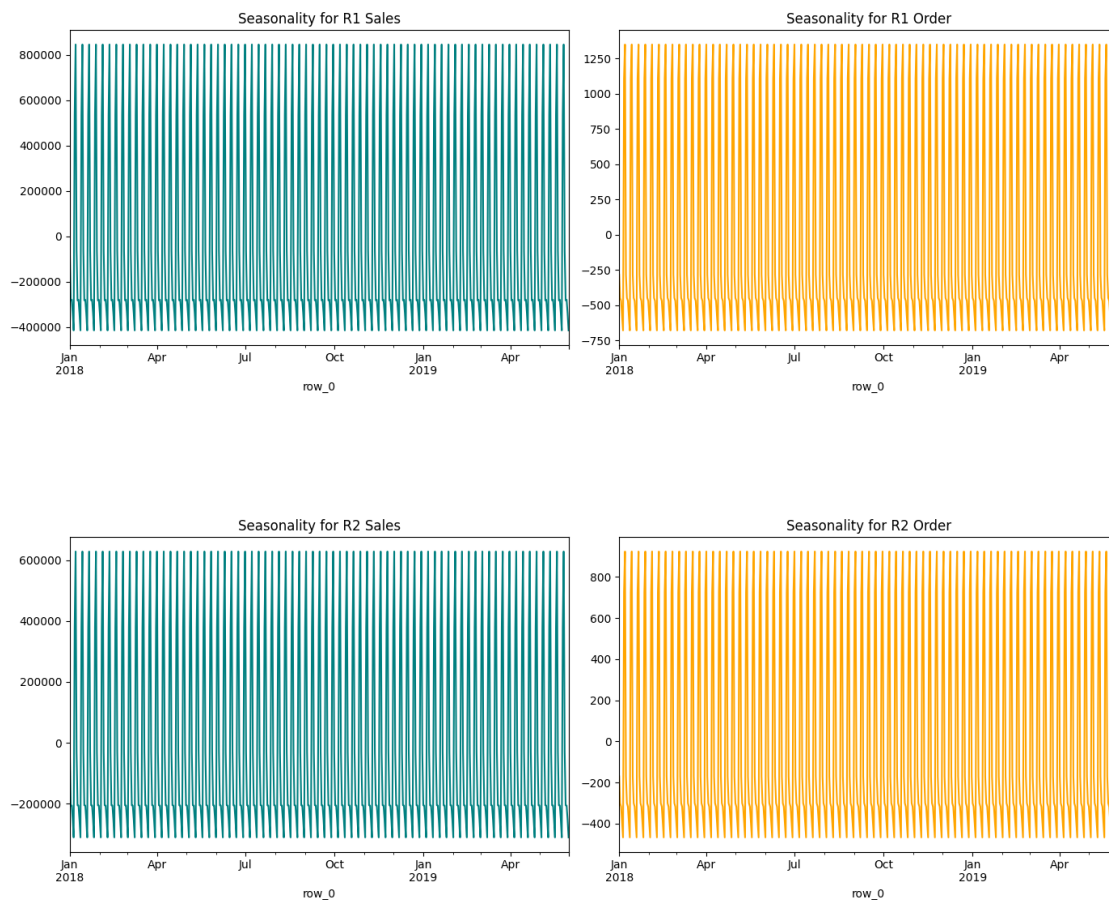
```
[153]: # Location Wise Sales and Order Seasonality Plot
data_sales = location_wise_sales
data_order = location_wise_order
for column in data_sales.columns:
    seasonal_chart(data_sales[column], data_order[column])
```

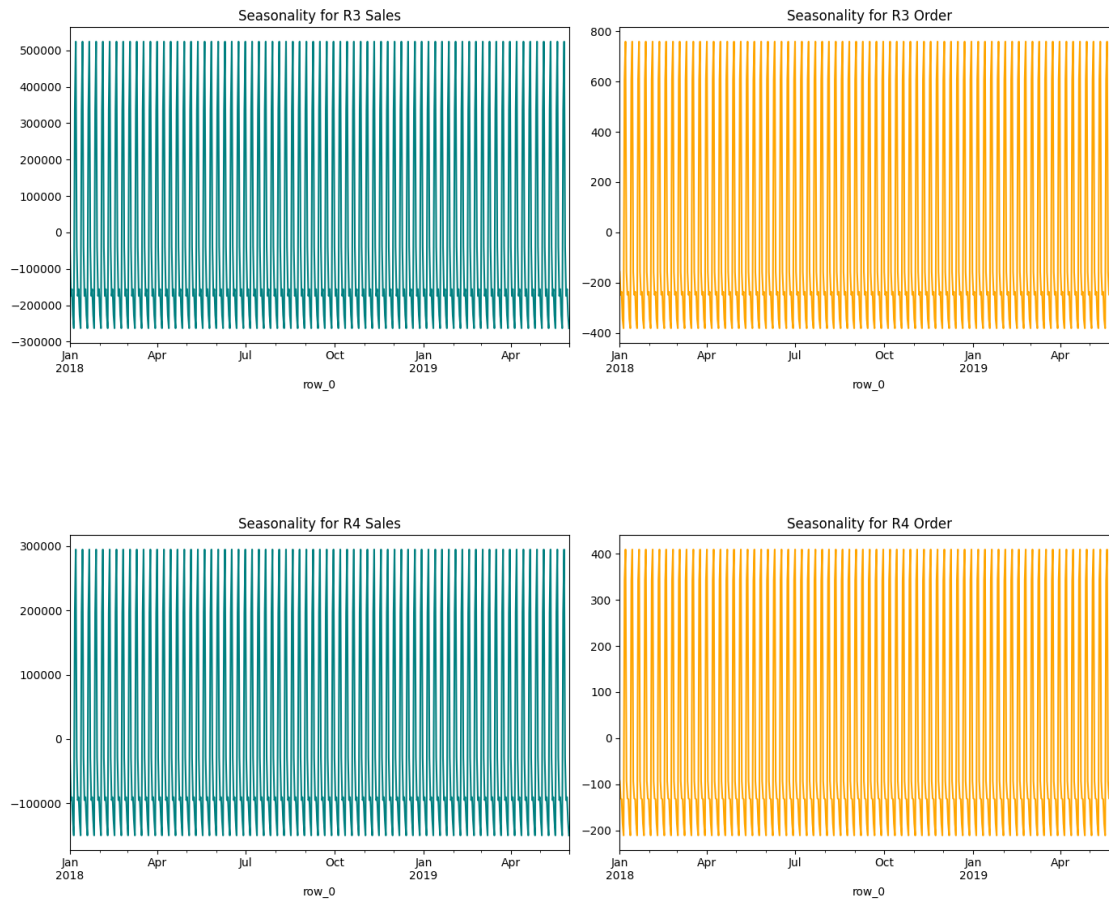




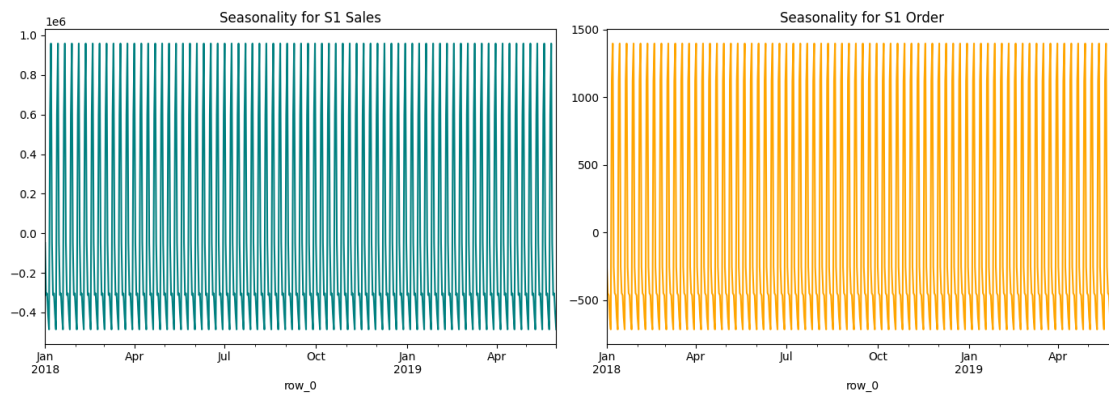


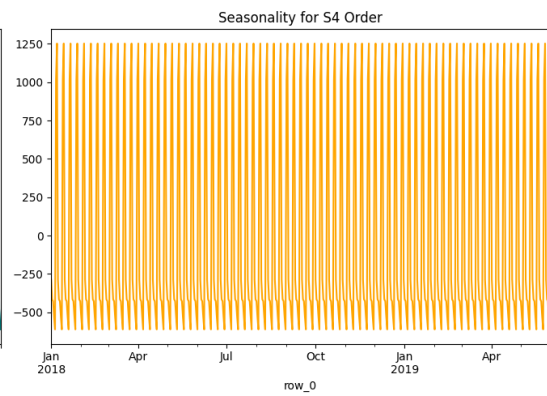
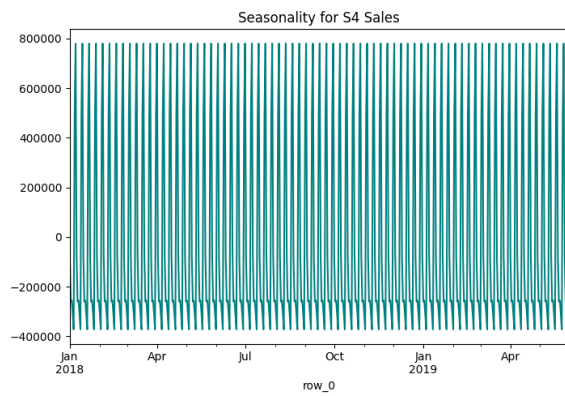
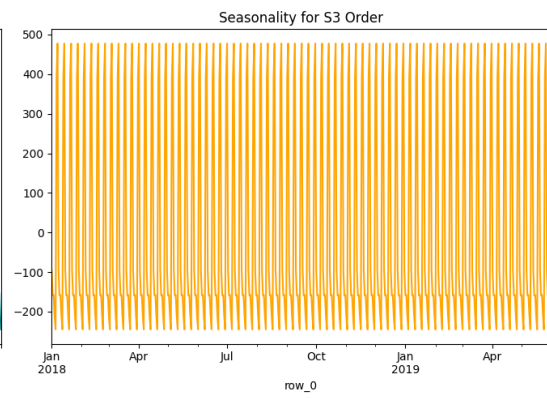
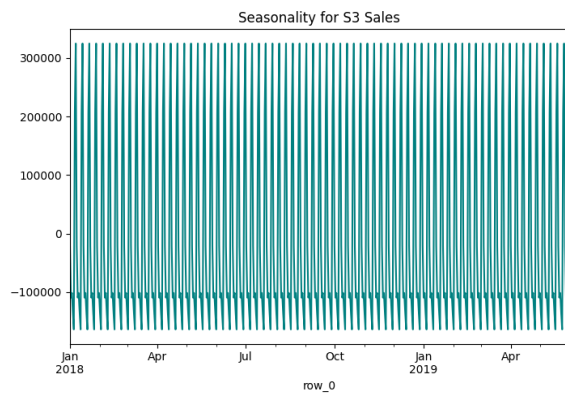
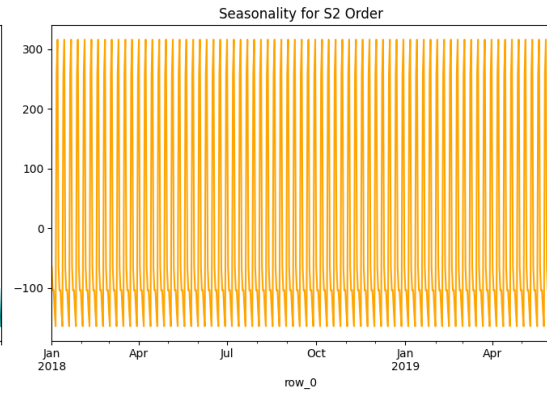
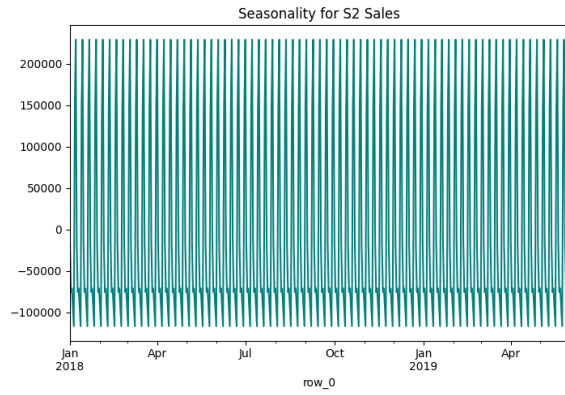
```
[154]: # RRegion Wise Sales and Order Seasonality Plot
data_sales = region_wise_sales
data_order = region_wise_order
for column in data_sales.columns:
    seasonal_chart(data_sales[column], data_order[column])
```





```
[155]: # StoreType Wise Sales and Order Seasonality Plot
data_sales = store_type_wise_sales
data_order = store_type_wise_order
for column in data_sales.columns:
    seasonal_chart(data_sales[column], data_order[column])
```





## 3 C. Model building and Evaluation

### 3.1 10. Data splitting

To build a model we will split data into 80:20 ratio. First 80% rows will be train data whereas remaining 20% will be test data.

```
[156]: # Train/Test splitting stage of pipeline
from sklearn.base import BaseEstimator, TransformerMixin

class TimeSeriesSplitter(BaseEstimator, TransformerMixin):
    def __init__(self, test_size=0.2):
        self.test_size = test_size
        self.train_data, self.test_data = None, None

    def fit(self, X, y=None):
        """No fitting required; just for compatibility."""
        return self

    def transform(self, X, y=None):
        """Split the single-column time series into train and test sets."""
        n_rows = len(X)
        split_index = int(n_rows * (1 - self.test_size))
        self.train_data = X.iloc[:split_index].asfreq('D')
        self.test_data = X.iloc[split_index:].asfreq('D')
        return self.train_data, self.test_data
```

### 3.2 11. SARIMAX Model Training

To have better accuracy in forecasting we will use exogenous variable

#### 3.2.1 Model building preparation

```
[132]: # Seasonality Factor function
def get_seasonal_factor_fft(data:pd.Series)->int:
    """
    Automatically detects seasonality using FFT.
    Args:
        data (pd.Series): Time series data.
    Returns:
        int: Seasonal factor (dominant period).
    """
    fft = np.fft.fft(data - np.mean(data)) # Remove mean for better results
    freqs = np.fft.fftfreq(len(data))
    magnitudes = np.abs(fft)
    dominant_freq = freqs[np.argmax(magnitudes[1:])] + 1 # Ignore zero
    ↪frequency
```



```

    seasonal_period = int(round(1 / dominant_freq)) if dominant_freq != 0 else_
↪None
    return abs(seasonal_period)

```

```

[133]: for column in train_sales.columns:
        seasonal_factor_fft = get_seasonal_factor_fft(train_sales[column])
        print(f"Detected seasonal factor (FFT) {column}: {seasonal_factor_fft}")

```

```

Detected seasonal factor (FFT) Sales: 12
Detected seasonal factor (FFT) 1: 6
Detected seasonal factor (FFT) 2: 12
Detected seasonal factor (FFT) 3: 172
Detected seasonal factor (FFT) 4: 12
Detected seasonal factor (FFT) 5: 7
Detected seasonal factor (FFT) 6: 13
Detected seasonal factor (FFT) 7: 172
Detected seasonal factor (FFT) 8: 7
Detected seasonal factor (FFT) 9: 12
Detected seasonal factor (FFT) 10: 12
Detected seasonal factor (FFT) 11: 12
Detected seasonal factor (FFT) 12: 12
Detected seasonal factor (FFT) 13: 12
Detected seasonal factor (FFT) 14: 12
Detected seasonal factor (FFT) 15: 7
Detected seasonal factor (FFT) 16: 12
Detected seasonal factor (FFT) 17: 12
Detected seasonal factor (FFT) 18: 7
Detected seasonal factor (FFT) 19: 12
Detected seasonal factor (FFT) 20: 12
Detected seasonal factor (FFT) 21: 172
Detected seasonal factor (FFT) 22: 172
Detected seasonal factor (FFT) 23: 12
Detected seasonal factor (FFT) 24: 3
Detected seasonal factor (FFT) 25: 172
Detected seasonal factor (FFT) 26: 172
Detected seasonal factor (FFT) 27: 12
Detected seasonal factor (FFT) 28: 12
Detected seasonal factor (FFT) 29: 12
Detected seasonal factor (FFT) 30: 12
Detected seasonal factor (FFT) 31: 12
Detected seasonal factor (FFT) 32: 172
Detected seasonal factor (FFT) 33: 12
Detected seasonal factor (FFT) 34: 12
Detected seasonal factor (FFT) 35: 7
Detected seasonal factor (FFT) 36: 13
Detected seasonal factor (FFT) 37: 12
Detected seasonal factor (FFT) 38: 12

```

Detected seasonal factor (FFT) 39: 13  
 Detected seasonal factor (FFT) 40: 12  
 Detected seasonal factor (FFT) 41: 12  
 Detected seasonal factor (FFT) 42: 172  
 Detected seasonal factor (FFT) 43: 12  
 Detected seasonal factor (FFT) 44: 12  
 Detected seasonal factor (FFT) 45: 13  
 Detected seasonal factor (FFT) 46: 12  
 Detected seasonal factor (FFT) 47: 12  
 Detected seasonal factor (FFT) 48: 12  
 Detected seasonal factor (FFT) 49: 7  
 Detected seasonal factor (FFT) 50: 12  
 Detected seasonal factor (FFT) 51: 12  
 Detected seasonal factor (FFT) 52: 12  
 Detected seasonal factor (FFT) 53: 3  
 Detected seasonal factor (FFT) 54: 12  
 Detected seasonal factor (FFT) 55: 12  
 Detected seasonal factor (FFT) 56: 12  
 Detected seasonal factor (FFT) 57: 103  
 Detected seasonal factor (FFT) 58: 516  
 Detected seasonal factor (FFT) 59: 12  
 Detected seasonal factor (FFT) 60: 3  
 Detected seasonal factor (FFT) 61: 12  
 Detected seasonal factor (FFT) 62: 12  
 Detected seasonal factor (FFT) 63: 12  
 Detected seasonal factor (FFT) 64: 7  
 Detected seasonal factor (FFT) 65: 516  
 Detected seasonal factor (FFT) 66: 13  
 Detected seasonal factor (FFT) 67: 13  
 Detected seasonal factor (FFT) 68: 12  
 Detected seasonal factor (FFT) 69: 7  
 Detected seasonal factor (FFT) 70: 7  
 Detected seasonal factor (FFT) 71: 12  
 Detected seasonal factor (FFT) 72: 12  
 Detected seasonal factor (FFT) 73: 12  
 Detected seasonal factor (FFT) 74: 13  
 Detected seasonal factor (FFT) 75: 12  
 Detected seasonal factor (FFT) 76: 12  
 Detected seasonal factor (FFT) 77: 12  
 Detected seasonal factor (FFT) 78: 13  
 Detected seasonal factor (FFT) 79: 13  
 Detected seasonal factor (FFT) 80: 12  
 Detected seasonal factor (FFT) 81: 12  
 Detected seasonal factor (FFT) 82: 172  
 Detected seasonal factor (FFT) 83: 12  
 Detected seasonal factor (FFT) 84: 12  
 Detected seasonal factor (FFT) 85: 12  
 Detected seasonal factor (FFT) 86: 7

Detected seasonal factor (FFT) 87: 12  
Detected seasonal factor (FFT) 88: 516  
Detected seasonal factor (FFT) 89: 172  
Detected seasonal factor (FFT) 90: 13  
Detected seasonal factor (FFT) 91: 12  
Detected seasonal factor (FFT) 92: 7  
Detected seasonal factor (FFT) 93: 172  
Detected seasonal factor (FFT) 94: 12  
Detected seasonal factor (FFT) 95: 12  
Detected seasonal factor (FFT) 96: 172  
Detected seasonal factor (FFT) 97: 7  
Detected seasonal factor (FFT) 98: 172  
Detected seasonal factor (FFT) 99: 12  
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 Detected seasonal factor (FFT) L2: 12  
 Detected seasonal factor (FFT) L3: 12  
 Detected seasonal factor (FFT) L4: 12  
 Detected seasonal factor (FFT) L5: 12



```

Detected seasonal factor (FFT) R1: 12
Detected seasonal factor (FFT) R2: 12
Detected seasonal factor (FFT) R3: 12
Detected seasonal factor (FFT) R4: 12

```

```

[134]: # Model training stage
from statsmodels.tsa.statespace.sarimax import SARIMAX
from sklearn.base import BaseEstimator
from sklearn.metrics import (make_scorer, mean_squared_error as mse,
    ↪ mean_absolute_error as mae, mean_absolute_percentage_error as mape)
import mlflow.statsmodels # Import mlflow.statsmodels

class SARIMAXEstimator(BaseEstimator):
    def __init__(self, order=(1,0,1), seasonal_order = (1,0,1,12)):
        self.order = order
        self.seasonal_order = seasonal_order
        self.model_ = None

    def fit(self, X, exog=None):
        self.exog_train=exog
        try:
            if isinstance(self.exog_train, pd.Series):
                self.model_ = SARIMAX(X, exog=self.exog_train, order=self.order,
    ↪ seasonal_order=self.seasonal_order).fit(dispatch=False)
            else:
                self.model_ = SARIMAX(X, order=self.order, seasonal_order=self.
    ↪ seasonal_order).fit(dispatch=False)
        except Exception as e:
            print(f"Skipping: order={self.order}, seasonal_order={self.
    ↪ seasonal_order}. Error: {e}")
            self.model_ = None
        return self

    def predict(self, n_steps, exog=None):
        if self.model_ is None:
            return np.full(n_steps, 1E-10)
        try:
            if not isinstance(self.exog_train, pd.Series):
                return self.model_.forecast(steps=n_steps)
            elif isinstance(exog, pd.Series):
                return self.model_.forecast(steps=n_steps, exog=exog[:n_steps])
            else:
                raise ValueError('No exog data provided')
        except Exception as e:
            print(e)
        return None

```

```

def score(self, X, exog=None):
    n_steps = len(X)
    predictions = self.predict(n_steps, exog)
    return mape(X, predictions)

```

```

[135]: #@title Define the parameter grid
from itertools import product
p,d,q = range(1,2), [1], range(1, 2)
order = list(product(p, d, q))

# seasonal_parameters P, D, Q, S
P, D, Q, S = range(1, 2), [0], range(1, 2), [7]
seasonal_order = list(product(P, D, Q, S))

param_grid = list(product(order, seasonal_order))

```

### 3.2.2 Model Training with MLFlow

```

[136]: # Model training for sales forecasting with MLFlow
import cloudpickle
import tempfile
import os

mlflow.set_experiment("Sore ID Sales Forecasting-1.1.0")
for column in train_sales.columns[0:1]:
    splitter = TimeSeriesSplitter()
    X_train, X_test = splitter.fit_transform(train_sales[column])
    X_train_exog, X_test_exog = splitter.fit_transform(exog_train_holiday)
    for order, seasonal in param_grid:
        with mlflow.start_run():
            sarimax_estimator = SARIMAXEstimator(order=order, seasonal_order=seasonal)
            sarimax_estimator.fit(X=X_train, exog=X_train_exog)

            if sarimax_estimator.model_ is not None:
                model_score = sarimax_estimator.score(X=X_test, exog=X_test_exog)
                mlflow.set_tag('data', column)
                mlflow.log_params({'order': order, 'seasonal_order': seasonal})
                mlflow.log_metric('mape', model_score)

# Manually save the model as a pickle file and log it as an artifact
                with tempfile.TemporaryDirectory() as tmpdir:
                    model_path = os.path.join(tmpdir, "model.pkl")
                    with open(model_path, "wb") as f:
                        cloudpickle.dump(sarimax_estimator.model_, f)
                    # Log the model.pkl directly at the root of the artifacts
                    mlflow.log_artifact(model_path)

```

```

else:
    print(f"Model fitting failed for column {column} with order={order},␣
↪seasonal_order={seasonal}. Skipping logging of model artifact.")

```

```

[137]: # Model training for order forecasting with MLFlow
import cloudpickle
import tempfile
import os

mlflow.set_experiment("Sore ID Order Forecasting-1.1.0")
for column in train_order.columns[0:1]:
    splitter = TimeSeriesSplitter()
    X_train, X_test = splitter.fit_transform(train_order[column])
    X_train_exog, X_test_exog = splitter.fit_transform(exog_train_holiday)
    for order, seasonal in param_grid:
        with mlflow.start_run():
            sarimax_estimator = SARIMAXEstimator(order=order, seasonal_order=seasonal)
            sarimax_estimator.fit(X=X_train, exog=X_train_exog)

            if sarimax_estimator.model_ is not None:
                model_score = sarimax_estimator.score(X=X_test, exog=X_test_exog)
                mlflow.set_tag('data', column)
                mlflow.log_params({'order': order, 'seasonal_order': seasonal})
                mlflow.log_metric('mape', model_score)

                # Manually save the model as a pickle file and log it as an artifact
                with tempfile.TemporaryDirectory() as tmpdir:
                    model_path = os.path.join(tmpdir, "model.pkl")
                    with open(model_path, "wb") as f:
                        cloudpickle.dump(sarimax_estimator.model_, f)
                    # Log the model.pkl directly at the root of the artifacts
                    mlflow.log_artifact(model_path)

            else:
                print(f"Model fitting failed for column {column} with order={order},␣
↪seasonal_order={seasonal}. Skipping logging of model artifact.")

```

## 4 D. Forecasting Example

```

[138]: import mlflow
import pandas as pd
import shutil
import os
import cloudpickle # Import cloudpickle for loading

# Create 'models' directory if it's not exist

```

```

if not os.path.exists('models'):
    os.makedirs('models')

# Get the MLflow client
client = mlflow.tracking.MlflowClient()

# Get the experiment by name for Order Forecasting
order_experiment = client.get_experiment_by_name("Sore ID Order Forecasting-1.1.
↳0")

if order_experiment is None:
    print("MLflow experiment 'Sore ID Order Forecasting-1.1.0' not found.␣
↳Please ensure the model training step was executed.")
else:
    order_exp_id = order_experiment.experiment_id

    # Search for runs within this experiment, ordered by MAPE ascending
    # Assuming 'Order' is the column name for the overall order forecasting
    runs = client.search_runs(
        experiment_ids=[order_exp_id],
        filter_string="tags.data = 'Order'", # Filter for the specific 'Order'␣
↳data tag
        order_by=["metrics.mape ASC"], # Order by MAPE to find the best model
        max_results=1 # We only need the best one
    )

    if runs:
        best_run = runs[0]
        run_id = best_run.info.run_id
        data_tag = best_run.data.tags.get('data') # This should be 'Order'

        print(f"Found best run for '{data_tag}' forecasting: Run ID {run_id},␣
↳MAPE {best_run.data.metrics.get('mape')}")

        # Define a temporary path to download artifacts for this run
        temp_download_dir = os.path.join('mlflow_temp_artifacts', run_id)
        os.makedirs(temp_download_dir, exist_ok=True)

        # Download the 'model.pkl' artifact (logged directly at root)
        artifact_uri_to_download = client.get_run(run_id).info.artifact_uri + '/'
↳model.pkl'
        mlflow.artifacts.
↳download_artifacts(artifact_uri=artifact_uri_to_download,␣
↳dst_path=temp_download_dir)

        # The actual model file is now at temp_download_dir/model.pkl

```

```

        source_model_path = os.path.join(temp_download_dir, 'model.pkl')
        destination_filename = os.path.join('models', f'{data_tag.
↳lower()}_order.pkl')

        # Move the model.pkl to its final destination
        shutil.move(source_model_path, destination_filename)
        print(f"Model for '{data_tag}' saved to {destination_filename}")

        # Clean up the temporary download directory
        shutil.rmtree(temp_download_dir)

    else:
        print("No runs found for 'Order' in 'Sore ID Order Forecasting-1.1.0'↳
↳experiment. Cannot save model.")

```

Found best run for 'Order' forecasting: Run ID f27d319ed1064e5b9125e81ddba37dda, MAPE 0.15094690023597634

Downloading artifacts: 0%| | 0/1 [00:00<?, ?it/s]

Model for 'Order' saved to models/order\_order.pkl

```

[139]: import mlflow
import pandas as pd
import shutil
import os
import cloudpickle

# Get the MLflow client
client = mlflow.tracking.MlflowClient()

# Get the experiment by name for Sales Forecasting
sales_experiment = client.get_experiment_by_name("Sore ID Sales Forecasting-1.1.
↳0")

if sales_experiment is None:
    print("MLflow experiment 'Sore ID Sales Forecasting-1.1.0' not found.↳
↳Please ensure the model training step was executed.")
else:
    sales_exp_id = sales_experiment.experiment_id

    # Search for runs within this experiment, ordered by MAPE ascending
    # Assuming 'Sales' is the column name for the overall sales forecasting
    runs = client.search_runs(
        experiment_ids=[sales_exp_id],
        filter_string="tags.data = 'Sales'", # Filter for the specific 'Sales'↳
↳data tag
        order_by=["metrics.mape ASC"], # Order by MAPE to find the best model

```

```

        max_results=1 # We only need the best one
    )

    if runs:
        best_run = runs[0]
        run_id = best_run.info.run_id
        data_tag = best_run.data.tags.get('data') # This should be 'Sales'

        print(f"Found best run for '{data_tag}' forecasting: Run ID {run_id},  

↳MAPE {best_run.data.metrics.get('mape')}")

        # Define a temporary path to download artifacts for this run
        temp_download_dir = os.path.join('mlflow_temp_artifacts', run_id)
        os.makedirs(temp_download_dir, exist_ok=True)

        # Download the 'model.pkl' artifact (logged directly at root)
        artifact_uri_to_download = client.get_run(run_id).info.artifact_uri + '/  

↳model.pkl'
        mlflow.artifacts.  

↳download_artifacts(artifact_uri=artifact_uri_to_download,  

↳dst_path=temp_download_dir)

        # The actual model file is now at temp_download_dir/model.pkl
        source_model_path = os.path.join(temp_download_dir, 'model.pkl')
        destination_filename = os.path.join('models', f'{data_tag}.  

↳lower()}_sales.pkl')

        # Move the model.pkl to its final destination
        shutil.move(source_model_path, destination_filename)
        print(f"Model for '{data_tag}' saved to {destination_filename}")

        # Clean up the temporary download directory
        shutil.rmtree(temp_download_dir)

    else:
        print("No runs found for 'Sales' in 'Sore ID Sales Forecasting-1.1.0'  

↳experiment. Cannot save model.")

```

Found best run for 'Sales' forecasting: Run ID 136db9cab66048629500df1d87a5768a,  
MAPE 0.19729424250763192

Downloading artifacts: 0%| | 0/1 [00:00<?, ?it/s]

Model for 'Sales' saved to models/sales\_sales.pkl

```

[140]: import cloudpickle as pickle
with open('models/sales_sales.pkl', 'rb') as file:
    model = pickle.load(file)

```

```
model.summary()
```

[140]:

|                         |                               |                          |           |
|-------------------------|-------------------------------|--------------------------|-----------|
| <b>Dep. Variable:</b>   | Sales                         | <b>No. Observations:</b> | 412       |
| <b>Model:</b>           | SARIMAX(1, 1, 1)x(1, 0, 1, 7) | <b>Log Likelihood</b>    | -6643.432 |
| <b>Date:</b>            | Tue, 23 Dec 2025              | <b>AIC</b>               | 13298.864 |
| <b>Time:</b>            | 11:25:41                      | <b>BIC</b>               | 13322.975 |
| <b>Sample:</b>          | 01-01-2018<br>- 02-16-2019    | <b>HQIC</b>              | 13308.402 |
| <b>Covariance Type:</b> | opg                           |                          |           |

|                | coef       | std err  | z         | P>  z | [0.025    | 0.975]    |
|----------------|------------|----------|-----------|-------|-----------|-----------|
| <b>Holiday</b> | -2.225e+06 | 1.32e-09 | -1.68e+15 | 0.000 | -2.23e+06 | -2.23e+06 |
| <b>ar.L1</b>   | 0.5814     | 0.042    | 13.805    | 0.000 | 0.499     | 0.664     |
| <b>ma.L1</b>   | -0.9989    | 0.021    | -46.864   | 0.000 | -1.041    | -0.957    |
| <b>ar.S.L7</b> | 0.9963     | 0.013    | 74.994    | 0.000 | 0.970     | 1.022     |
| <b>ma.S.L7</b> | -0.9707    | 0.056    | -17.266   | 0.000 | -1.081    | -0.860    |
| <b>sigma2</b>  | 8.338e+12  | 3.67e-15 | 2.27e+27  | 0.000 | 8.34e+12  | 8.34e+12  |

|                                |      |                          |        |
|--------------------------------|------|--------------------------|--------|
| <b>Ljung-Box (L1) (Q):</b>     | 0.55 | <b>Jarque-Bera (JB):</b> | 507.31 |
| <b>Prob(Q):</b>                | 0.46 | <b>Prob(JB):</b>         | 0.00   |
| <b>Heteroskedasticity (H):</b> | 0.85 | <b>Skew:</b>             | -0.65  |
| <b>Prob(H) (two-sided):</b>    | 0.34 | <b>Kurtosis:</b>         | 8.29   |

Warnings:

- [1] Covariance matrix calculated using the outer product of gradients (complex-step).
- [2] Covariance matrix is singular or near-singular, with condition number 5.91e+41. Standard errors may be unstable.

[158]:

```
# Forecasting values
# Define the number of days to forecast
n = 50

# Re-run splitter to get consistent train/test sets for 'Sales'
# This ensures that X_train_sales, X_test_sales, and X_test_exog_sales align
# with how the model was trained and evaluated.
splitter = TimeSeriesSplitter()
X_train_sales, X_test_sales = splitter.fit_transform(overall_sales['Sales'])
_, X_test_exog_sales = splitter.fit_transform(exog_train_holiday) # Only need
# the test part of exog_train_holiday

# Prepare data for plotting
df_plot = X_train_sales
test_plot = X_test_sales.iloc[:n] # Take the first 'n' days of the actual test
# data
exog_for_pred = X_test_exog_sales.iloc[:n] # Exogenous variables for the
# prediction period

# Generate predictions using the loaded model
```

```

test_plot['pred'] = model.forecast(steps=n, exog=exog_for_pred)

# Create and display the plot
fig = go.Figure()
fig.add_trace(go.Scatter(x=df_plot.index, y=df_plot, mode='lines', name='Train_
↪values', line=dict(color='green'))))
fig.add_trace(go.Scatter(x=test_plot.index, y=test_plot, mode='lines',
↪name='Test values', line=dict(color='orange'))))
fig.add_trace(go.Scatter(x=test_plot.index, y=test_plot['pred'], mode='lines',
↪name='Forecasting', line=dict(color='red'))))
fig.update_layout(title_text='Forecasting of overall Sales', # Updated title_
↪for clarity
                    title_x=0.5, title_y=0.85,
                    legend_x=0)
fig.show()

```

```

[142]: import cloudpickle as pickle
with open('models/sales_sales.pkl', 'rb') as file:
    model = pickle.load(file)
model.summary()

```

```

[142]:

```

|                         |                               |                          |           |
|-------------------------|-------------------------------|--------------------------|-----------|
| <b>Dep. Variable:</b>   | Sales                         | <b>No. Observations:</b> | 412       |
| <b>Model:</b>           | SARIMAX(1, 1, 1)x(1, 0, 1, 7) | <b>Log Likelihood</b>    | -6643.432 |
| <b>Date:</b>            | Tue, 23 Dec 2025              | <b>AIC</b>               | 13298.864 |
| <b>Time:</b>            | 11:25:41                      | <b>BIC</b>               | 13322.975 |
| <b>Sample:</b>          | 01-01-2018<br>- 02-16-2019    | <b>HQIC</b>              | 13308.402 |
| <b>Covariance Type:</b> | opg                           |                          |           |

|                | coef       | std err  | z         | P>  z | [0.025    | 0.975]    |
|----------------|------------|----------|-----------|-------|-----------|-----------|
| <b>Holiday</b> | -2.225e+06 | 1.32e-09 | -1.68e+15 | 0.000 | -2.23e+06 | -2.23e+06 |
| <b>ar.L1</b>   | 0.5814     | 0.042    | 13.805    | 0.000 | 0.499     | 0.664     |
| <b>ma.L1</b>   | -0.9989    | 0.021    | -46.864   | 0.000 | -1.041    | -0.957    |
| <b>ar.S.L7</b> | 0.9963     | 0.013    | 74.994    | 0.000 | 0.970     | 1.022     |
| <b>ma.S.L7</b> | -0.9707    | 0.056    | -17.266   | 0.000 | -1.081    | -0.860    |
| <b>sigma2</b>  | 8.338e+12  | 3.67e-15 | 2.27e+27  | 0.000 | 8.34e+12  | 8.34e+12  |

|                                |      |                          |        |
|--------------------------------|------|--------------------------|--------|
| <b>Ljung-Box (L1) (Q):</b>     | 0.55 | <b>Jarque-Bera (JB):</b> | 507.31 |
| <b>Prob(Q):</b>                | 0.46 | <b>Prob(JB):</b>         | 0.00   |
| <b>Heteroskedasticity (H):</b> | 0.85 | <b>Skew:</b>             | -0.65  |
| <b>Prob(H) (two-sided):</b>    | 0.34 | <b>Kurtosis:</b>         | 8.29   |

Warnings:

- [1] Covariance matrix calculated using the outer product of gradients (complex-step).
- [2] Covariance matrix is singular or near-singular, with condition number 5.91e+41. Standard errors may be unstable.



```
[160]: sub_to_forecast = 'Sales' # Changed to 'Sales' to match the loaded overall
      ↪ sales model
n = 50 # Number of days

# Create splitter instance
splitter = TimeSeriesSplitter()

# Split the overall sales data and the exogenous holiday data for the overall
      ↪ sales model
X_train_data, X_test_data = splitter.
      ↪ fit_transform(overall_sales[sub_to_forecast])
_, X_test_exog_data = splitter.fit_transform(exog_train_holiday)

# Use the 'n' variable to define the length of the test data for plotting and
      ↪ forecasting
test_plot_data = X_test_data.iloc[:n] # Actual test values for the first 'n'
      ↪ days
exog_for_forecast = X_test_exog_data.iloc[:n] # Exogenous variables for the
      ↪ forecast period

# The model 'model' is already loaded from 'models/sales_sales.pkl' in cell
      ↪ PYOujvumwZaw

# Generate predictions using the loaded model
test_plot_data['pred'] = model.forecast(steps=n, exog=exog_for_forecast)

fig = go.Figure()
fig.add_trace(go.Scatter(x=X_train_data.index, y=X_train_data, mode='lines',
      ↪ name='Train values', line=dict(color='green'))))
fig.add_trace(go.Scatter(x=test_plot_data.index, y=test_plot_data,
      ↪ mode='lines', name='Test values', line=dict(color='orange'))))
fig.add_trace(go.Scatter(x=test_plot_data.index, y=test_plot_data['pred'],
      ↪ mode='lines', name='Forecasting', line=dict(color='red'))))
fig.update_layout(title_text=f'Forecasting of {sub_to_forecast}',
                  title_x=0.5, title_y=0.85,
                  legend_x=0)
fig.show()
```

```
[144]: import cloudpickle as pickle
      with open('models/order_order.pkl', 'rb') as file:
          model = pickle.load(file)
      model.summary()
```

[144]:

|                         |                               |                          |           |
|-------------------------|-------------------------------|--------------------------|-----------|
| <b>Dep. Variable:</b>   | Order                         | <b>No. Observations:</b> | 412       |
| <b>Model:</b>           | SARIMAX(1, 1, 1)x(1, 0, 1, 7) | <b>Log Likelihood</b>    | -3938.587 |
| <b>Date:</b>            | Tue, 23 Dec 2025              | <b>AIC</b>               | 7889.174  |
| <b>Time:</b>            | 11:25:41                      | <b>BIC</b>               | 7913.286  |
| <b>Sample:</b>          | 01-01-2018<br>- 02-16-2019    | <b>HQIC</b>              | 7898.713  |
| <b>Covariance Type:</b> | opg                           |                          |           |

|                | coef       | std err | z        | P>  z | [0.025    | 0.975]    |
|----------------|------------|---------|----------|-------|-----------|-----------|
| <b>Holiday</b> | -3412.0755 | 640.458 | -5.328   | 0.000 | -4667.350 | -2156.801 |
| <b>ar.L1</b>   | 0.5009     | 0.041   | 12.166   | 0.000 | 0.420     | 0.582     |
| <b>ma.L1</b>   | -0.9982    | 0.011   | -91.624  | 0.000 | -1.020    | -0.977    |
| <b>ar.S.L7</b> | 0.9961     | 0.013   | 79.606   | 0.000 | 0.972     | 1.021     |
| <b>ma.S.L7</b> | -0.9644    | 0.059   | -16.368  | 0.000 | -1.080    | -0.849    |
| <b>sigma2</b>  | 1.711e+07  | 0.094   | 1.83e+08 | 0.000 | 1.71e+07  | 1.71e+07  |

|                                |      |                          |        |
|--------------------------------|------|--------------------------|--------|
| <b>Ljung-Box (L1) (Q):</b>     | 0.25 | <b>Jarque-Bera (JB):</b> | 908.66 |
| <b>Prob(Q):</b>                | 0.62 | <b>Prob(JB):</b>         | 0.00   |
| <b>Heteroskedasticity (H):</b> | 0.77 | <b>Skew:</b>             | -0.99  |
| <b>Prob(H) (two-sided):</b>    | 0.12 | <b>Kurtosis:</b>         | 10.01  |

Warnings:

[1] Covariance matrix calculated using the outer product of gradients (complex-step).

[2] Covariance matrix is singular or near-singular, with condition number 8.16e+24. Standard errors may be unstable.

```
[161]: # Forecasting values
sub_to_forecast = 'Order' # Changed to 'Order' to match the loaded overall_order model
n = 50 # Number of days

# Create splitter instance
splitter = TimeSeriesSplitter()

# Split the overall order data and the exogenous holiday data for the overall_order model
X_train_data_order, X_test_data_order = splitter.fit_transform(overall_order[sub_to_forecast], X_test_exog_data_order = splitter.fit_transform(exog_train_holiday) # Only need the test part of exog_train_holiday

# Use the 'n' variable to define the length of the test data for plotting and forecasting
test_plot_data_order = X_test_data_order.iloc[:n] # Actual test values for the first 'n' days
exog_for_forecast_order = X_test_exog_data_order.iloc[:n] # Exogenous variables for the forecast period
```

```

# The model 'model' is already loaded from 'models/order_order.pkl' in cell
↳ hnZfqILrwZaw

# Generate predictions using the loaded model
test_plot_data_order['pred'] = model.forecast(steps=n,
↳ exog=exog_for_forecast_order)

fig = go.Figure()
fig.add_trace(go.Scatter(x=X_train_data_order.index, y=X_train_data_order,
↳ mode='lines', name='Train values', line=dict(color='green'))))
fig.add_trace(go.Scatter(x=test_plot_data_order.index, y=test_plot_data_order,
↳ mode='lines', name='Test values', line=dict(color='orange'))))
fig.add_trace(go.Scatter(x=test_plot_data_order.index,
↳ y=test_plot_data_order['pred'], mode='lines', name='Forecasting',
↳ line=dict(color='red'))))
fig.update_layout(title_text=f'Forecasting of overall {sub_to_forecast}', #
↳ Updated title for clarity
                    title_x=0.5, title_y=0.85,
                    legend_x=0)
fig.show()

```

## 4.1 Observations

- Sales and Orders move together, when orders increase, sales also increase.
- Discounts lead to higher customer activity compared to non-discount days.
- Sales and orders drop noticeably on holidays.
- Performance varies significantly across Store Type, Location Type, and Region.
- Clear seasonal patterns exist across months and days of the week.
- Time-series statistical tests show the data is suitable for forecasting.

## 4.2 Key Insights

- **Discounts are effective** : They significantly boost both sales and order volume.
- **Holidays negatively impact business** : Lower sales and fewer orders are recorded during holidays.
- **Store characteristics matter** : Store Type, Region, and Location strongly influence performance.
- **Strong seasonality exists** : Sales follow predictable monthly and weekly patterns.
- **Reliable forecasting potential** : Data supports accurate time-series forecasting.

[145]:

[145]:

[145]: