# notebook

May 20, 2020

### IB031 Project

- Source
- Testing csv
- Training csv

In this project we will implement several models to predict credibility of a loan applicant. We will use the Loan Prediction Problem Dataset from Kaggle. The structure of the project is as follows:

- 1. Section ??
- 2. Section ??
- 3. Section ??
- 4. Section ??
- 5. Section ??
- 6. Section ??
- 7. Section ??
- 8. Section ??
- 9. Section ??

### 0.1 1. Exploratory Analysis

The dataset consists of basic information about applicants. There are 13 columns with about 1000 rows. First of all, we will deal with the data types.

```
[3]: import seaborn as sns
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
sns.set()
```

Since pandas loads categorical data types as 'object' dtype by default, we want to convert them back to category after loading the csv. We are also dropping the "Loan\_Status" column, which will later provide labels for classification. Unfortunately, this particular dataset does not contain a set of testing labels, therefore we were forced to split an already sparse training set into 2 parts.

```
[4]: from sklearn.model_selection import train_test_split

#X_test = pd.read_csv("./test_Y3wMUE5_7gLdaTN.csv", index_col="Loan_ID")
```

```
dataset = pd.read_csv("./train_u6lujuX_CVtuZ9i.csv", index_col="Loan_ID")

for col in dataset.columns:
    if dataset[col].dtype == 'object':
        dataset[col] = dataset[col].astype('category')

X, y = dataset.drop(["Loan_Status"], axis=1), dataset["Loan_Status"][:]
    y = y.map({"Y": True, "N": False})

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=.2)
```

## [5]: X.info()

<class 'pandas.core.frame.DataFrame'>
Index: 614 entries, LP001002 to LP002990
Data columns (total 11 columns):

# Column Non-Null Count Dtype -----\_\_\_\_\_ 0 Gender 601 non-null category 1 Married 611 non-null category 2 Dependents 599 non-null category 3 Education 614 non-null category Self\_Employed 582 non-null 4 category 5 ApplicantIncome 614 non-null int64 6 CoapplicantIncome 614 non-null float64 7 float64 LoanAmount 592 non-null

600 non-null

564 non-null

10 Property\_Area 614 non-null category dtypes: category(6), float64(4), int64(1) memory usage: 33.0+ KB

Loan\_Amount\_Term

Credit\_History

We have dropped the 'Loan Status' column, which will provide labels during classification

float64

float64

```
[6]: X.shape
```

[6]: (614, 11)

```
[7]: y.shape
```

[7]: (614,)

The dataset had been split into training and testing subsets in around 1.67:1 ratio.

We can look at the amount of distinct values of selected features.

```
[8]: # value count of just some selected columns

print(X.Gender.value_counts()) # oh yeah boi
```

```
print(X.Married.value_counts())
     print(X.Education.value_counts())
     print(X.Property_Area.value_counts())
    Male
               489
    Female
               112
    Name: Gender, dtype: int64
           398
    Yes
    No
           213
    Name: Married, dtype: int64
    Graduate
                     480
    Not Graduate
                     134
    Name: Education, dtype: int64
    Semiurban
                  233
    Urban
                  202
    Rural
                  179
    Name: Property_Area, dtype: int64
[9]: X.head()
[9]:
              Gender Married Dependents
                                              Education Self_Employed \
     Loan_ID
    LP001002
                Male
                           No
                                       0
                                               Graduate
                                                                    No
    LP001003
                Male
                          Yes
                                       1
                                               Graduate
                                                                    No
     LP001005
                Male
                          Yes
                                       0
                                               Graduate
                                                                   Yes
                Male
                                          Not Graduate
     LP001006
                          Yes
                                       0
                                                                    No
     LP001008
                Male
                           No
                                       0
                                               Graduate
                                                                    No
               ApplicantIncome
                                 CoapplicantIncome LoanAmount Loan_Amount_Term \
    Loan_ID
    LP001002
                           5849
                                                0.0
                                                                             360.0
                                                            {\tt NaN}
    LP001003
                           4583
                                             1508.0
                                                          128.0
                                                                             360.0
    LP001005
                           3000
                                                0.0
                                                           66.0
                                                                             360.0
                                                          120.0
    LP001006
                           2583
                                             2358.0
                                                                             360.0
    LP001008
                           6000
                                                0.0
                                                          141.0
                                                                             360.0
               Credit_History Property_Area
     Loan_ID
     LP001002
                           1.0
                                       Urban
```

# [10]: X.isnull().sum()

LP001003

LP001005

LP001006

LP001008

Rural

Urban

Urban

Urban

1.0

1.0

1.0

1.0

```
[10]: Gender
                            13
      Married
                             3
      Dependents
                            15
      Education
                             0
      Self Employed
                            32
      ApplicantIncome
                             0
      CoapplicantIncome
                             0
      LoanAmount
                            22
      Loan_Amount_Term
                            14
      Credit_History
                            50
      Property_Area
                             0
      dtype: int64
```

As we can see, there are a lot of null values which will need to be imputed. Since there is no column with more missing data than present, we do not need to drop any.

# [11]: X.describe()

50%

75%

max

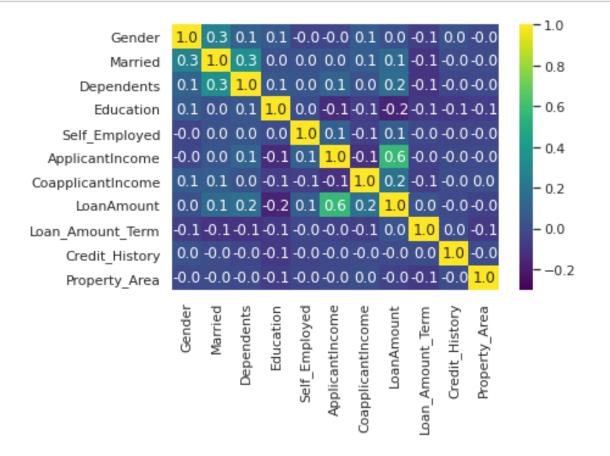
1.000000

1.000000

[11]:		ApplicantIncome	${\tt CoapplicantIncome}$	${\tt LoanAmount}$	Loan_Amount_Term	\
	count	614.000000	614.000000	592.000000	600.00000	
	mean	5403.459283	1621.245798	146.412162	342.00000	
	std	6109.041673	2926.248369	85.587325	65.12041	
	min	150.000000	0.000000	9.000000	12.00000	
	25%	2877.500000	0.000000	100.000000	360.00000	
	50%	3812.500000	1188.500000	128.000000	360.00000	
	75%	5795.000000	2297.250000	168.000000	360.00000	
	max	81000.000000	41667.000000	700.000000	480.00000	
		Credit_History				
	count	564.000000				
	mean	0.842199				
	std	0.364878				
	min	0.000000				
	25%	1.000000				

Here we have some essential statistics about our dataset. For instance, we can see, that the most frequent length of loan term is about 1 year, with maximum being 1.5 year and minimum just 12 days. Furthermore, coapplicants have much lower income than applicants.

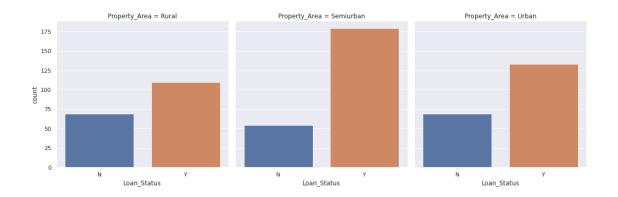
plt.show()

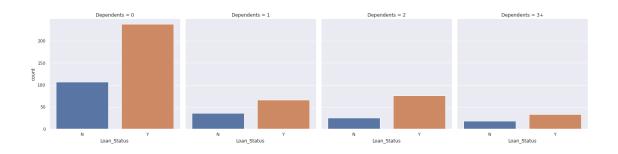


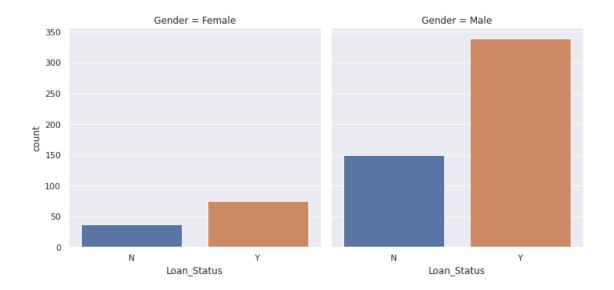
We also computed and plotted correlation matrix of features in the dataset. There is only one pair of features, loan amount and applicant income, which can be considered to be mildly positively correlated. Other features, have nearly no correlation among them. This results is quite suprising, as one would expect higher correlation of features.

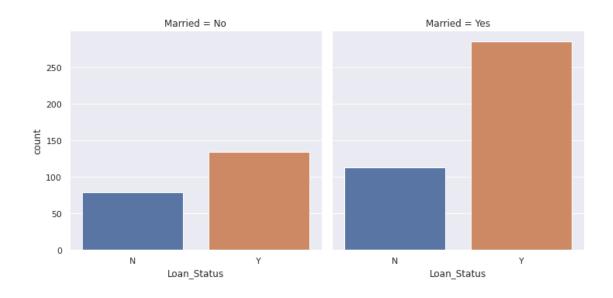
```
[13]: sns.catplot("Loan_Status", col="Property_Area", data=dataset, kind="count")
sns.catplot("Loan_Status", col="Dependents", data=dataset, kind="count")
sns.catplot("Loan_Status", col="Gender", data=dataset, kind="count")
sns.catplot("Loan_Status", col="Married", data=dataset, kind="count")
sns.catplot("Loan_Status", col="Education", data=dataset, kind="count")
```

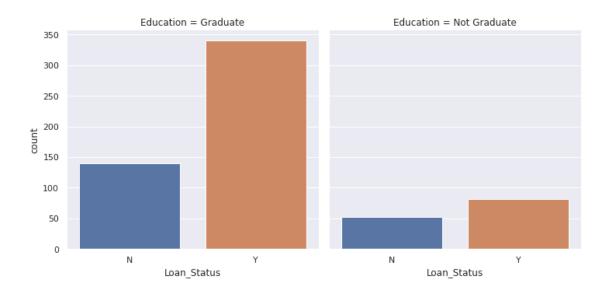
[13]: <seaborn.axisgrid.FacetGrid at 0x7fc01d075978>









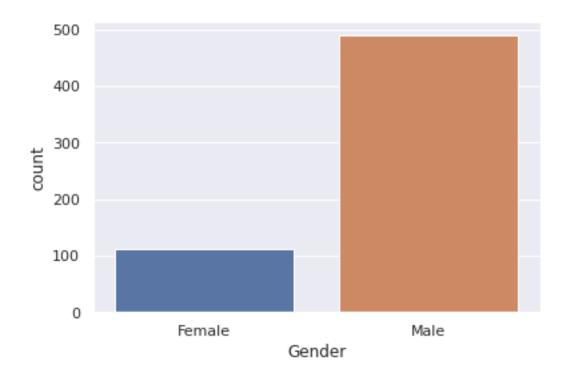


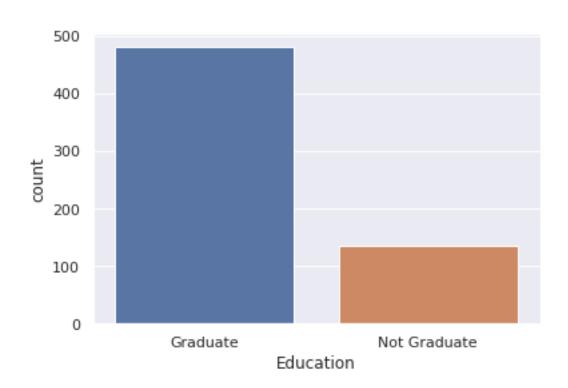
```
[67]: for col in {"Property_Area", "Dependents", "Gender", "Married", "Education",

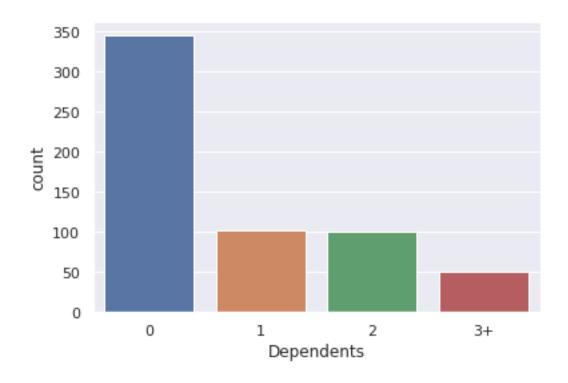
→"Self_Employed"}:
    sns.countplot(X[col])
    plt.show()

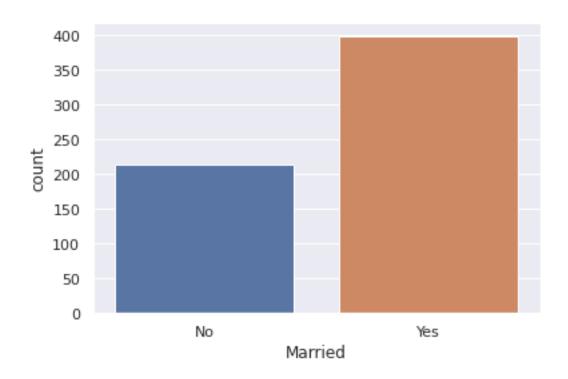
for col in {"ApplicantIncome", "CoapplicantIncome", "Credit_History",

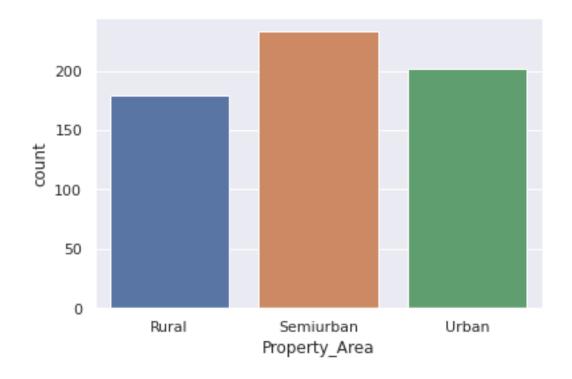
→"LoanAmount", "Loan_Amount_Term"}:
    sns.distplot(X[col])
```

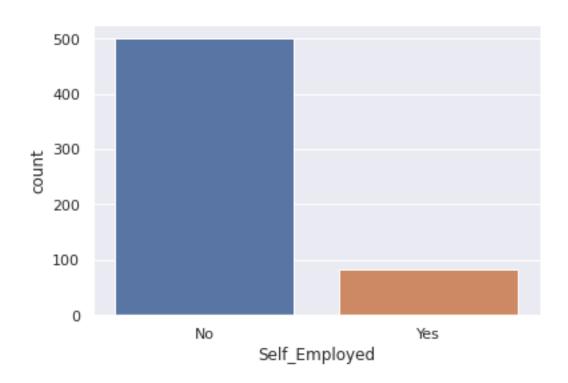


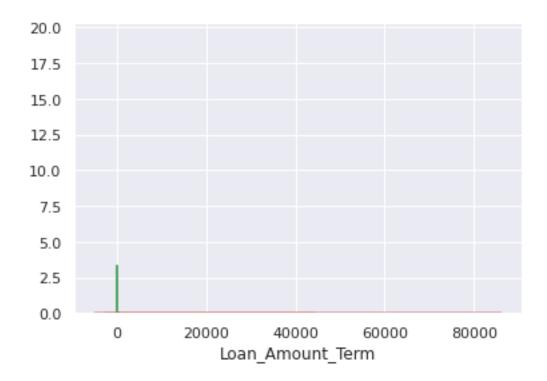












Most of the features are scattered along the x-axis. The only exception is Loan Amount, which roughly follows the Chi-squared distribution.

```
[15]: sns.countplot(y)
```

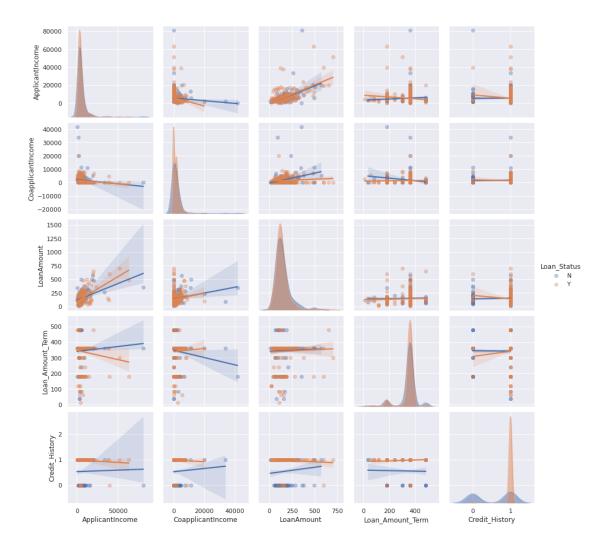
[15]: <matplotlib.axes.\_subplots.AxesSubplot at 0x7fc01cc9c630>



```
[65]: sns.pairplot(dataset, hue="Loan_Status", kind="reg", diag_kws={"alpha": 0.5}, 

→plot_kws={"scatter_kws": {"alpha": 0.35}})
```

[65]: <seaborn.axisgrid.PairGrid at 0x7fbf6a0a8cc0>



Credit history seems to have the highest impact on deciding whether the loan should be approved or not. Clients with low credit score seem more likely to be denied.

There are some cases where ApplicantIncome and CoapplicantIncome are very low, their loan request gets approved, whereas in a few cases the CoapplicantIncome is very high and ApplicantIncome is very low, the request gets denied.

### 0.2 2. Data preprocessing

## [17]: y.isna().sum()

#### [17]: 0

Good, there are no N/A labels. We do not need to drop any rows. Besides that, dropping a significant part of the dataset could have misrepresenting effects.

Firstly, we will impute the missing values with SimpleImputer and strategy most\_frequent. As SimpleImputer returns an array, we will transform it back to a pandas dataframe. Another step

is encoding the categorical features using OneHotEncoder. Lastly, we will scale the features with StandardScaler. Their mean will therefore be 0 and variance 1.

The labels need significantly less preprocessing. Encoding their boolean values is sufficient.

```
[18]: from sklearn.preprocessing import OrdinalEncoder, OneHotEncoder, StandardScaler
      from sklearn.pipeline import make_pipeline
      from sklearn.compose import make_column_transformer
      from sklearn.impute import SimpleImputer
      class NpToDf:
          columns = []
          def __init__(self, columns=None):
              self.columns = columns
          def fit(self, X, *args, **kwargs):
              return X
          def fit_transform(self, X, *args, **kwargs):
              return self.transform(X)
          def transform(self, X, *args, **kwargs):
              return pd.DataFrame(data=X, columns=self.columns)
      pipe_X = make_pipeline(
          SimpleImputer(missing values=np.nan, strategy="most frequent"),
          NpToDf(X train.columns),
          make_column_transformer(
              (OneHotEncoder(), ['Gender', 'Married', 'Education', 'Self_Employed', __
       →'Property_Area', 'Dependents']),
              remainder=StandardScaler()),
          NpToDf(),
      pipe_y = make_pipeline(
          OrdinalEncoder()
```

```
[19]: pipe_X.fit_transform(X_train)
    train_X = pipe_X.transform(X_train)
    test_X = pipe_X.transform(X_test)

train_y = pipe_y.fit_transform(y_train.to_numpy().reshape(-1, 1)).reshape(-1)
    test_y = pipe_y.fit_transform(y_test.to_numpy().reshape(-1, 1)).reshape(-1)
```

Some helper functions for training and evaluation of our models.

```
[20]: from sklearn.metrics import mean squared_error, f1_score
     from sklearn.model_selection import cross_val_score
     import matplotlib.pyplot as plt
     def evaluate(clf, X_test, y_test):
         y_pred = clf.predict(X_test)
         scores = cross_val_score(clf, X_test, y_test, cv=10)
         print(f"RMSE: {mean_squared_error(y_test, y_pred, squared = False):.4f}")
         print(f"Accuracy: {scores.mean():.3f} ± {scores.std() * 2:.3f}")
         print("F1 Score: %.2f" % f1_score(y_test, y_pred, average='weighted'))
[21]: from sklearn.metrics import plot_roc_curve
     def roc(clf, test_X, test_y):
         plot_roc_curve(clf, test_X, test_y)
         plt.plot([0, 1], [0, 1], linestyle='--', lw=2, color='r', label='Chance',
       ⇒alpha=.8)
         plt.legend()
[22]: from sklearn.metrics import plot precision recall curve as pro
     from sklearn.metrics import precision_recall_curve
[23]: from sklearn.metrics import plot_confusion_matrix
     from sklearn.metrics import confusion_matrix
     from sklearn.model_selection import GridSearchCV
     def confusion(clf, X_test, y_test):
         plot_confusion_matrix(clf, X_test, y_test, cmap=plt.cm.Blues)
[24]: def get_gscv(clf, param_grid, verbose=1, **kwargs):
         gs = GridSearchCV(clf, param_grid, verbose=verbose, cv=kwargs.get("cv", 3), u
       gs.fit(train_X, train_y, **kwargs)
         score = gs.score(test_X, test_y)
```

In the following 4 sections, we will always start by running a grid search tuning hyperparameters of our models. There is a wrapper for keras sequential models, which we will use for grid searching. All models will be trained on the same training set. We chose these evaluation metrics - **RMSE** - measures error of the predictions compared to actual values, the lower the better. - **Acurracy** computed with cross validation score - is the proportion of correct predictions (both true positives and true negatives) among the total number of cases examined, the higher the better - **F1 score** - is weighted average of precision and recall, the best value is 1, the worst is 0 - **Receiver Operating Characteristic curve** - measures the ability of a model to distinguish between classes - **Precision** 

print(f"Best parameters: {gs.best\_params\_}, with F1 score of {score:.2f}")

return gs.best\_estimator\_

**Recall curve** - shows the tradeoff between precision and recall for different threshold - **Confusion matrix** - shows the number of True Positive (TP), False Negative (FN), True Negative (TN), False Positive (FP) classifications.

### 0.3 3. Naive baseline model

This is a simple classifier, which chooses the class based on training set class distribution.

It is very basic and is affected by the chosen train/test split a lot.

```
[26]: from sklearn.dummy import DummyClassifier

dummy_clf = DummyClassifier(strategy="stratified")

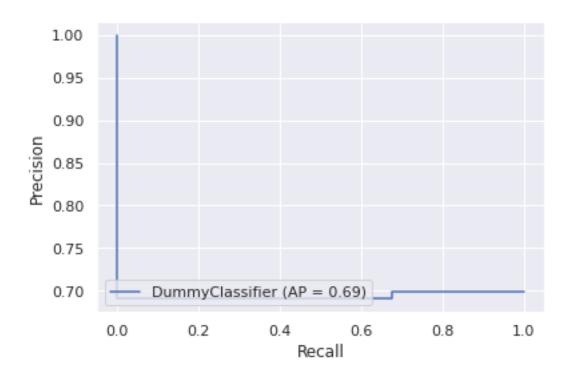
dummy_clf.fit(train_X, train_y)

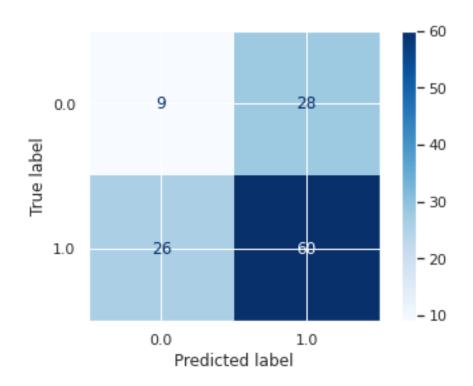
evaluate(dummy_clf, test_X, test_y)
 roc(dummy_clf, test_X, test_y)
 prc(dummy_clf, test_X, test_y)
 confusion(dummy_clf, test_X, test_y)
 plt.show()
```

RMSE: 0.6182

Accuracy:  $0.577 \pm 0.179$ 







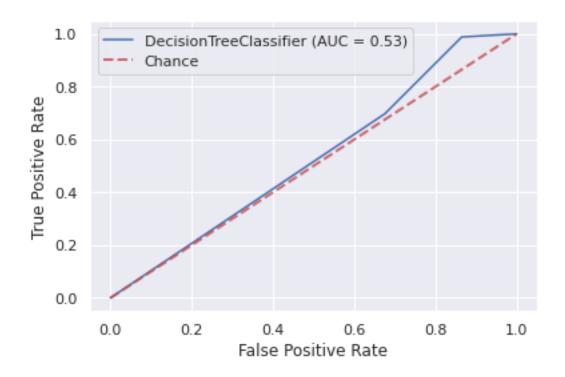
#### 0.4 4. Decision tree classifier

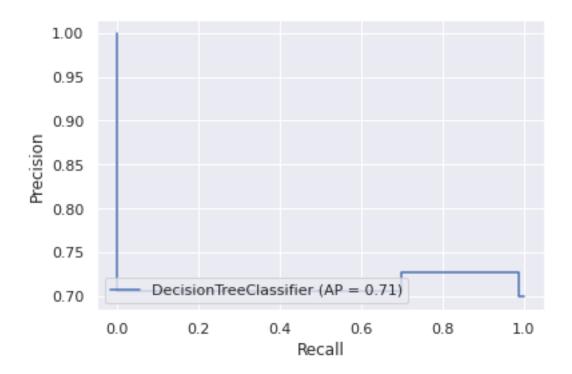
Decision trees are among the most used classification models. They iteratively split the dataset, until a tree conforming to given parameters has been constructed. In leaves they contain class labels. Internal nodes represent kind of a boolean test, usually a value of a sample's feature, according to which the algorithm chooses the respective edge on the way to leaves. The tests can also use entropy and information gain to choose the best edge. There are many to ways to construct a tree, therefore extensive hyperparameter tunning is suitable. Decision trees can also be pruned, etheir during construction of after it.

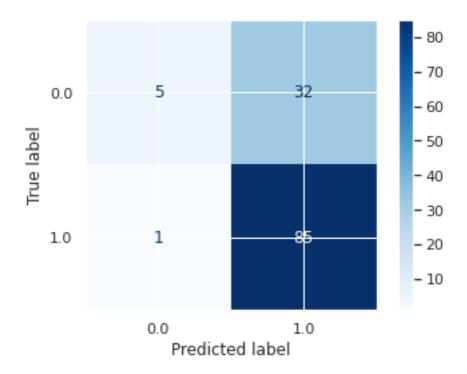
```
[28]: evaluate(tree_clf, test_X, test_y)
   roc(tree_clf, test_X, test_y)
   prc(tree_clf, test_X, test_y)
   confusion(tree_clf, test_X, test_y)
   plt.show()
```

RMSE: 0.5180

Accuracy:  $0.749 \pm 0.245$ 







#### 0.5 5. KNN classifier

Another popular classification algorithm, an example of instace-based learning or lazy learning. This time, all distances from a data point to other points are computed, and k-closest neighbours are chosen. Then, the class memberships of the k-closest members are considered, with the original data point taking a class label from the most occurring one among its k-closest neighbours. For the distance metrics, Euclidean or Hamming distances are usually used. There is a tradeoff in the number of k-closest neighbours. Smaller k, signifies the result of noise on classification, but makes the various classses more distinct and vice versa with higher k.

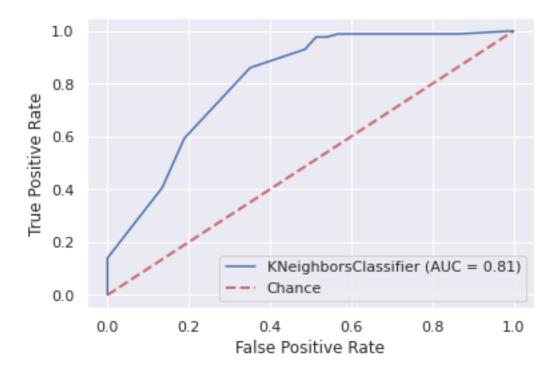
```
Fitting 3 folds for each of 560 candidates, totalling 1680 fits [Parallel(n_jobs=-2)]: Using backend LokyBackend with 3 concurrent workers. [Parallel(n_jobs=-2)]: Done 250 tasks | elapsed: 2.1s [Parallel(n_jobs=-2)]: Done 1450 tasks | elapsed: 11.5s
```

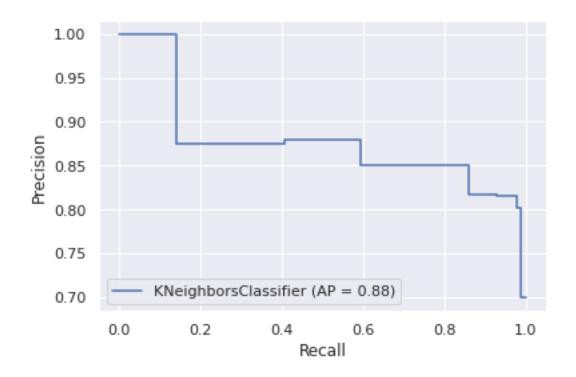
Best parameters: {'algorithm': 'auto', 'leaf\_size': 10, 'n\_neighbors': 12, 'p': 2, 'weights': 'uniform'}, with F1 score of 0.83
[Parallel(n\_jobs=-2)]: Done 1680 out of 1680 | elapsed: 12.8s finished

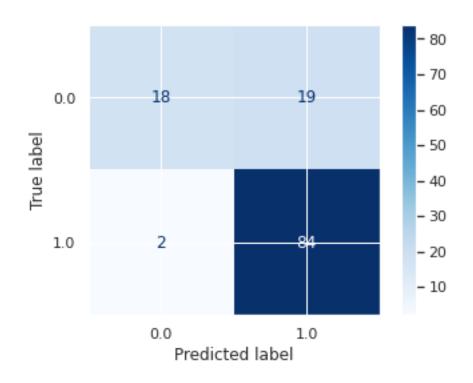
[30]: evaluate(knn\_clf, test\_X, test\_y)
 roc(knn\_clf, test\_X, test\_y)
 prc(knn\_clf, test\_X, test\_y)
 confusion(knn\_clf, test\_X, test\_y)
 plt.show()

RMSE: 0.4132

Accuracy:  $0.803 \pm 0.189$ 







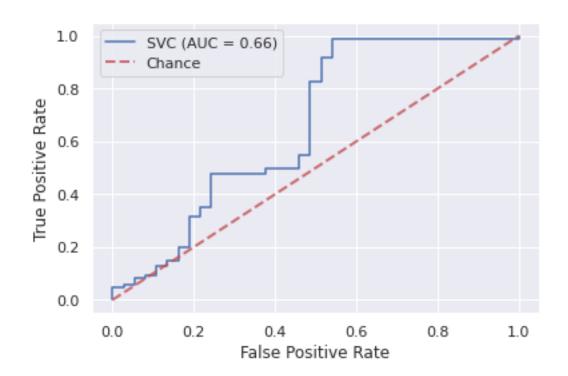
## 0.6 6. Support Vector Machine

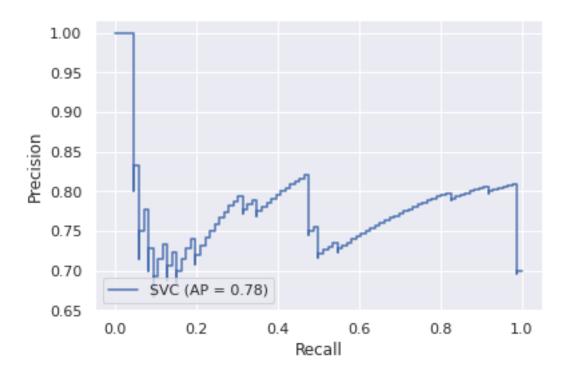
Support Vector Machines, abbr. SVM, is a supervised-learning algorithm used mainly for binary classification, although it is possible to use for multi-class classification by combing several SVMs. It creates hyperplanes in a multi-dimensional feature space, which are then used for generalization and classifications of data points. The best performing hyperplanes are those having the biggest maximum margin, i.e. the closest data points from both classes are as far as possible. In order to transform input data into a desired form, SVM uses so called kernel functions, which return the inner product between two points in a suitable feature space.

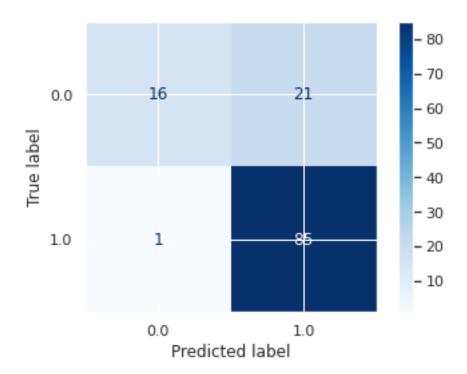
```
[33]: evaluate(svm_clf, test_X, test_y)
   roc(svm_clf, test_X, test_y)
   prc(svm_clf, test_X, test_y)
   confusion(svm_clf, test_X, test_y)
   plt.show()
```

RMSE: 0.4229

Accuracy:  $0.819 \pm 0.198$ 







### 0.7 7. Deep Neural Network

Deep neural networks (DNNs) are artificial neural (ANNs) networks with several hidden layers. Each layer is a fixed number of artificial neurons, which accept an input, process it, and send it to the next layer. The layers are organized followingly:

input layer  $\rightarrow$  hidden layers  $\rightarrow$  output layer.

Each layer has an activation function, whose choice greatly influences the overall performance. In classification tasks, the output layer yields the final class labels. We will use Sequential model from Keras as our DNN.

For the activation functions we will stick with ReLU or Recrified Linear Units. These are nearly linear functions commonly used in DNNs and provide the best results. Leaky ReLU may be used as well.

We will be choosing either Adam, Stochastic Gradient Descent or RMSProp optimizer.

Batch size will remain constant 32 and epochs 10-15, since these numbers offer the best results for the time spent learning.

We have experimented with dropout a bit, but found little to no difference when using it, so it will be kept at 0

```
[34]: import tensorflow as tf import itertools import itertools
```

```
import gc
import keras.backend as K
from keras.optimizers import Adam, SGD, RMSprop
from keras.models import Sequential
from keras.callbacks import EarlyStopping
from keras.layers import Dense, Dropout
from sklearn.metrics import classification_report, confusion_matrix
from keras.wrappers.scikit_learn import KerasClassifier
```

Using TensorFlow backend.

```
net_clf = KerasClassifier(build_fn=build_net, verbose=0)
layer_sizes = [[[32, 64, 128] for _ in range(size)] for size in range(3, 5)]
layer_combinations = list(itertools.chain.from_iterable(map(lambda sublist: list(itertools.product net_values = {"optim": [Adam, SGD, RMSprop], "epochs": [10], "batch_size": [32], "layers": layers = EarlyStopping(monitor='loss', min_delta=0, patience=2, verbose=0, mode='auto')
dnn_clf = get_gscv(net_clf, net_values, callbacks=[es])
Fitting 3 folds for each of 2880 candidates, totalling 8640 fits
```

- 1. Best parameters: {'batch\_size': 32, 'dropout': 0.1, 'epochs': 10, 'layers': (32, 64, 32, 64), 'lr': 0.004, 'optim': <class 'keras.optimizers.RMSprop'>}, with F1 score of 0.78
- 2. Best parameters: {'batch\_size': 32, 'dropout': 0.0, 'epochs': 15, 'layers': (8, 32, 8, 32), 'lr': 0.001, 'optim': <class 'keras.optimizers.RMSprop'>}, with F1 score of 0.77
- 3. Best parameters: {'batch\_size': 32, 'dropout': 0.1, 'epochs': 12, 'layers': (64, 64, 64, 64, 32, 16), 'lr': 0.0003, 'optim': <class 'keras.optimizers.Adam'>}, with F1 score of 0.85

```
[]: ohe = OneHotEncoder()

nn_train_y = ohe.fit_transform(y_train.to_numpy().reshape(-1, 1))
nn_test_y = ohe.transform(y_test.to_numpy().reshape(-1, 1))
```

```
[38]: # best_args = {'batch_size': 32, 'dropout': 0.1, 'epochs': 15, 'layers': (32, \( \omega \) 32, 8), 'lr': 0.0004, 'optim': RMSprop}

# best_args = {'batch_size': 32, 'dropout': 0.1, 'epochs': 12, 'layers': (64, \( \omega \) 46, 64, 64, 32, 16), 'lr': 0.0003, 'optim': Adam}

# best_args = {'batch_size': 32, 'dropout': 0.0, 'epochs': 15, 'layers': (32, \( \omega \) 32, 16, 8), 'lr': 0.0003, 'optim': Adam}

# best_args = {'batch_size': 32, 'dropout': 0.0, 'epochs': 12, 'layers': (64, \( \omega \) 46, 64, 16, 32, 64), 'lr': 0.0003, 'optim': Adam}

best_args = {'batch_size': 32, 'dropout': 0.0, 'epochs': 20, 'layers': (256, \( \omega \) 4128, 64, 64, 32), 'lr': 0.0003, 'optim': Adam}

dnn_clf = KerasClassifier(build_fn=build_net, verbose=0, **best_args)

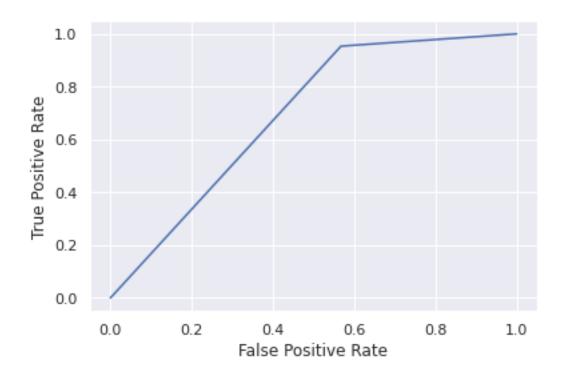
data = dnn_clf.fit(train_X, train_y, epochs=15, batch_size=32)

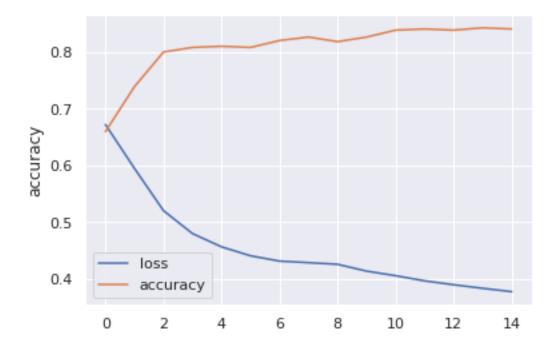
dnn_clf.model.summary()
```

#### Model: "sequential 1"

Layer (type)	Output Shape	Param #
dense_1 (Dense)	(None, 256)	5376
dropout_1 (Dropout)	(None, 256)	0
dense_2 (Dense)	(None, 128)	32896
dropout_2 (Dropout)	(None, 128)	0
dense_3 (Dense)	(None, 64)	8256
dropout_3 (Dropout)	(None, 64)	0

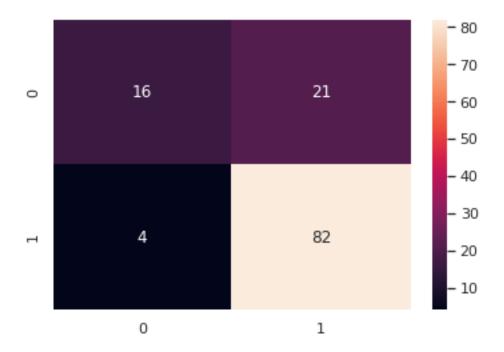
```
dense_4 (Dense) (None, 64)
                                      4160
    _____
    dropout_4 (Dropout)
                         (None, 64)
    dense 5 (Dense)
                         (None, 32)
                                              2080
      -----
    dropout_5 (Dropout)
                     (None, 32)
    ______
    dense 6 (Dense) (None, 2)
                                              66
    _____
    Total params: 52,834
    Trainable params: 52,834
    Non-trainable params: 0
     _____
[55]: from sklearn.metrics import roc_curve
    true_y_labels = np.argmax(nn_test_y, axis=1)
    predicted_y = dnn_clf.predict(test_X)
    roc_curve(true_y_labels, predicted_y)
    fpr, tpr, thresholds = roc_curve(true_y_labels, predicted_y)
    roc_data = pd.DataFrame({"False Positive Rate": fpr, "True Positive Rate": tpr})
    sns.lineplot(x="False Positive Rate", y="True Positive Rate", data=roc_data)
    plt.show()
    history_df = pd.DataFrame(data=data.history, columns=data.history.keys())
    sns.lineplot(legend='full', y=history_df['loss'], x=range(len(data.
     ⇔history['loss'])), label='loss')
    sns.lineplot(legend='full', y=history_df['accuracy'], x=range(len(data.
     ⇔history['accuracy'])), label='accuracy')
    plt.show()
    evaluate(dnn_clf, test_X, test_y)
    sns.heatmap(confusion_matrix(true_y_labels, predicted_y), annot=True)
    plt.show()
    print('\nClassification Report')
    target names = ["Y", "N"]
    print(classification_report(true_y_labels, predicted_y,__
     →target_names=target_names))
```





RMSE: 0.4508

Accuracy:  $0.812 \pm 0.214$ 



### 0.8 8. Evaluation

It is easy to see, that we have moved far beyond the performance of the baseline model. Therefore, we could assume our project reached its goal.

From the evaluation metrics it seems, that *deep neural network*, *KNN*, and *SVM* performed nearly equally. Their accuracy exceeded 80%. This is quite surprising as *KNN* can be considered as the most simple from all 4 models and yet it kept pace with them. On the other side of the spectrum is *decision tree classifier*, which had the worst evaluation metrics from all 4 models.

And finally, the winner's podium:

- 1. Deep Neural Network, KNN Classifier, Support Vector Machine
- 2. Decision Tree Classifier
- 3. Dummy classifier

Though keep in mind that with such small dataset the performance of all models may be influenced by the random state quite a bit.

The performance of all models could be improved in certain models (such as the DNN classifier) by using weighted samples as the dataset is quite imbalanced.

The accuracy has quite a large differences between positive and negative samples. This is most likely caused by the fact that sampling for model training is not stratified whereas accuracy is computed using stratified cross validation.

All models seemed to have problems with recognising true negatives. In all cases the number of false negatives was greater than the number of true negatives. Though this could be due to imbalanced dataset as well.

# 0.9 9. Conclusion

We have explored and preprocessed the dataset. From the computational side, training of the models and tuning of their hyperparameters did not take too long, in average about 35sec per model, with neural network being an exception, as it was trained with several epochs for each parameter search. Even though the dataset did not offer many records, we can conclude that the models performed overall quite well.