# 

#### October 3, 2023

```
import pandas as pd
     import numpy as np
     import seaborn as sns
     import matplotlib.pyplot as plt
[2]: df=pd.read_csv('Placement_Data_Full_Class.csv')
     df=df.drop(columns='sl_no',axis=1)
[3]:
     df.head(10)
[3]:
       gender
               ssc_p
                         ssc_b
                                hsc_p
                                         hsc_b
                                                    hsc_s
                                                           degree_p
                                                                       degree_t
     0
               67.00
                                91.00
            М
                        Others
                                        Others
                                                 Commerce
                                                              58.00
                                                                       Sci&Tech
               79.33
                      Central 78.33
     1
            М
                                        Others
                                                  Science
                                                              77.48
                                                                       Sci&Tech
     2
            М
               65.00
                      Central 68.00
                                       Central
                                                     Arts
                                                              64.00
                                                                      Comm&Mgmt
     3
               56.00
                      Central 52.00
                                       Central
                                                  Science
                                                              52.00
                                                                       Sci&Tech
     4
               85.80
                      Central 73.60
                                                 Commerce
                                       Central
                                                              73.30
                                                                      Comm&Mgmt
     5
               55.00
                       Others 49.80
                                        Others
                                                  Science
                                                              67.25
                                                                       Sci&Tech
     6
            F
               46.00
                        Others 49.20
                                        Others Commerce
                                                              79.00
                                                                      Comm&Mgmt
     7
               82.00
                      Central
                                64.00
                                       Central
                                                  Science
                                                              66.00
                                                                       Sci&Tech
     8
               73.00
                                79.00
                                                              72.00
            Μ
                      Central
                                       Central
                                                 Commerce
                                                                      Comm&Mgmt
               58.00
     9
                      Central
                                70.00
                                       Central
                                                 Commerce
                                                              61.00
                                                                      Comm&Mgmt
       workex
               etest_p specialisation
                                        mba_p
                                                    status
                                                              salary
     0
           No
                 55.00
                                Mkt&HR
                                        58.80
                                                    Placed
                                                            270000.0
     1
          Yes
                 86.50
                               Mkt&Fin
                                        66.28
                                                    Placed
                                                            200000.0
     2
                 75.00
                               Mkt&Fin
                                        57.80
                                                            250000.0
           No
                                                    Placed
     3
           No
                 66.00
                                Mkt&HR
                                       59.43
                                                Not Placed
                                                                 NaN
     4
                               Mkt&Fin 55.50
                 96.80
                                                    Placed
                                                            425000.0
           No
     5
                 55.00
                               Mkt&Fin 51.58
                                                Not Placed
          Yes
                                                                  NaN
     6
                 74.28
                               Mkt&Fin 53.29
                                                Not Placed
           No
                                                                  NaN
     7
                 67.00
                               Mkt&Fin 62.14
                                                    Placed
          Yes
                                                            252000.0
     8
           No
                 91.34
                               Mkt&Fin 61.29
                                                    Placed
                                                            231000.0
     9
                 54.00
                               Mkt&Fin 52.21
                                               Not Placed
                                                                 NaN
           No
```

## 1 1 Data Preprocessing

```
[4]: df.shape
[4]: (215, 14)
     df.select_dtypes(include='object').nunique()
[5]: gender
                        2
                        2
     ssc_b
                        2
    hsc_b
                       3
    hsc_s
                       3
     degree_t
                       2
     workex
                       2
     specialisation
                        2
     status
     dtype: int64
[6]: df.isna().sum()
                         0
[6]: gender
                         0
     ssc_p
                         0
     ssc_b
                         0
    hsc_p
                         0
    hsc_b
    hsc_s
                         0
                         0
     degree_p
     degree_t
                         0
                         0
     workex
                         0
     etest_p
     specialisation
                         0
                         0
    mba_p
                         0
     status
     salary
                       67
     dtype: int64
[7]: df.isna().mean()
[7]: gender
                       0.000000
                       0.000000
     ssc_p
     ssc_b
                       0.000000
    hsc_p
                       0.000000
                       0.000000
    hsc_b
    hsc_s
                       0.000000
     degree_p
                       0.000000
     degree_t
                       0.000000
                       0.000000
     workex
                       0.000000
     etest_p
```

 specialisation
 0.000000

 mba\_p
 0.000000

 status
 0.000000

 salary
 0.311628

dtype: float64

### [8]: df.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 215 entries, 0 to 214
Data columns (total 14 columns):

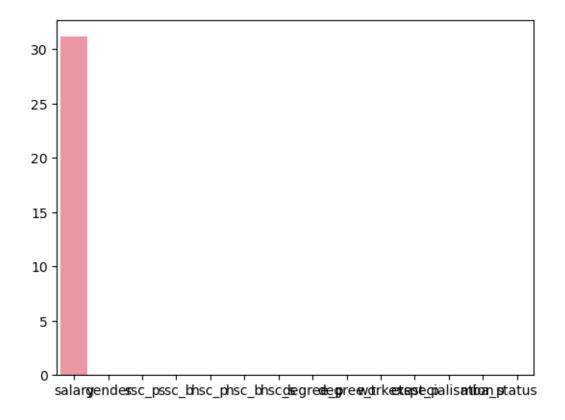
#	Column	Non-Null Count	Dtype
0	gender	215 non-null	object
1	ssc_p	215 non-null	float64
2	ssc_b	215 non-null	object
3	hsc_p	215 non-null	float64
4	hsc_b	215 non-null	object
5	hsc_s	215 non-null	object
6	degree_p	215 non-null	float64
7	degree_t	215 non-null	object
8	workex	215 non-null	object
9	etest_p	215 non-null	float64
10	specialisation	215 non-null	object
11	mba_p	215 non-null	float64
12	status	215 non-null	object
13	salary	148 non-null	float64
_			

dtypes: float64(6), object(8)

memory usage: 23.6+ KB

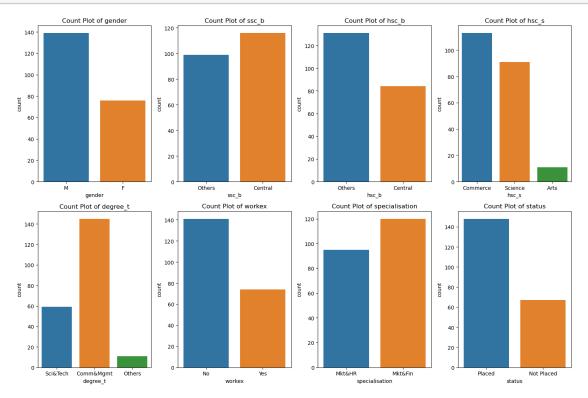
#### 2 EDA

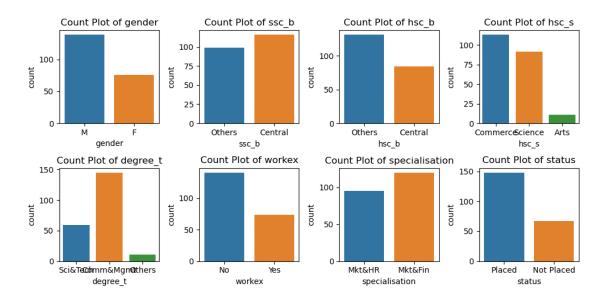
```
[9]: dfcat=df.select_dtypes(include='object')
[10]: cat_col=df.select_dtypes(include='object').columns
[11]: j=(df.isna().mean()*100).sort_values(ascending=False)
[12]: sns.barplot(x=j.index,y=j.values)
[12]: <Axes: >
```



```
[13]: def fun(col):
          fig, ax = plt.subplots(figsize=(7, 5))
          sns.countplot(data=df, x=col, ax=ax)
          ax.set_title(f'Count Plot of {col}')
          plt.tight_layout()
          plt.close() # Close the figure to avoid displaying the individual plots
       →immediately
      # Create two figures side by side (1 row and 2 columns)
      fig, axes = plt.subplots(2, 4, figsize=(15, 10))
      # Call the function for each categorical column in 'cat_col' and plot it in the_
       ⇔respective figure
      for i, col in enumerate(cat_col):
          row_index = i // 4
          col_index = i \% 4
          fun(col)
          sns.countplot(data=df, x=col, ax=axes[row_index, col_index])
          axes[row_index, col_index].set_title(f'Count Plot of {col}')
```

```
plt.tight_layout()
plt.show()
```

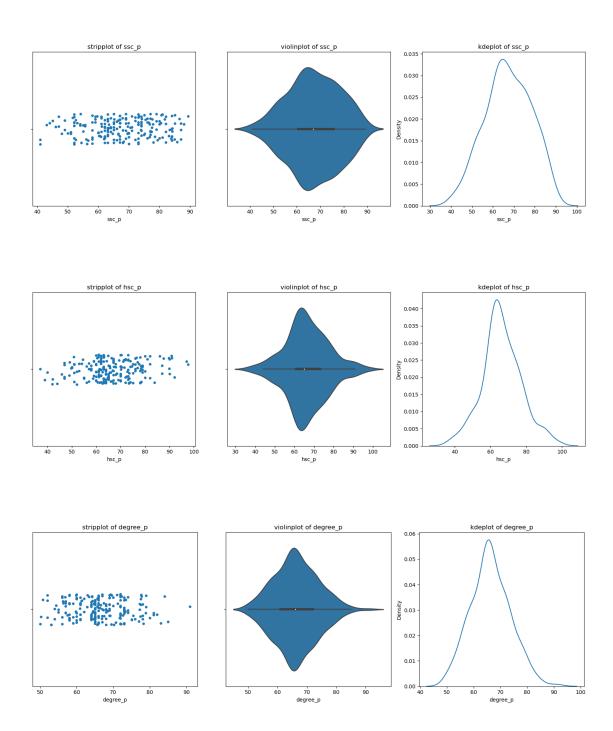


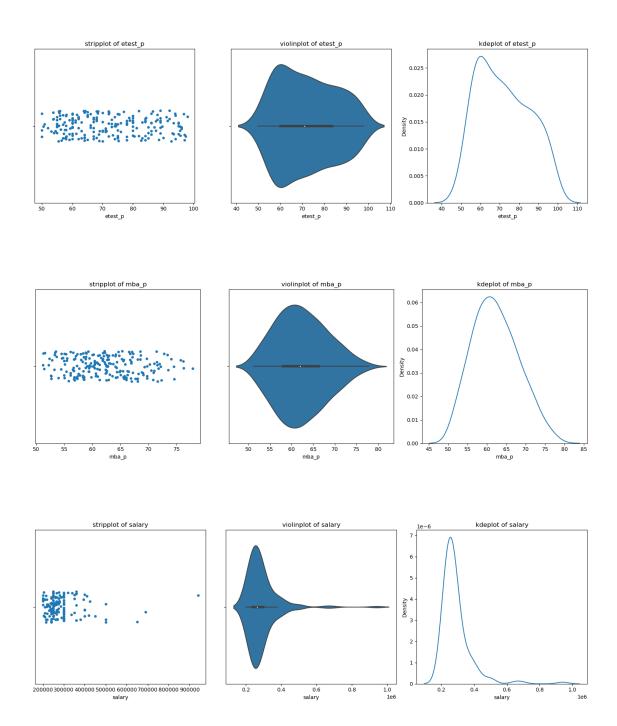


```
[15]: dfnum=df.drop(dfcat.columns,axis=1)
```

[16]: dfnum num\_col=dfnum.columns

```
[17]: #numerica; columns distribution
      def numfunc(col):
          fig, axes = plt.subplots(1, 3, figsize=(15, 5))
          plots = [
              ('stripplot', sns.stripplot),
              ('violinplot', sns.violinplot),
              ('kdeplot', sns.kdeplot)
          ]
          for i, (plot_title, plot_func) in enumerate(plots):
              plot_func(data=dfnum, x=col, ax=axes[i])
              axes[i].set_title(f'{plot_title} of {col}')
          plt.tight_layout()
          plt.show()
      # Call the function for each numerical column in the DataFrame 'DFNUM'
      for col in dfnum.columns:
          numfunc(col)
```



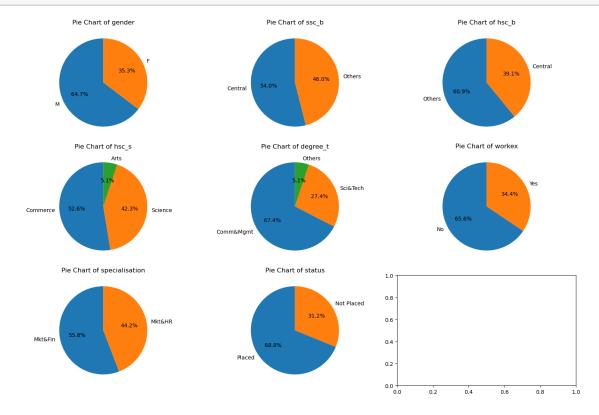


```
[18]: def funccatcol_pie(df,cat_col):
    fig,axes =plt.subplots(3,3,figsize=(15,10))

    for i,col in enumerate(cat_col):
        r=i//3
        c=i%3
        pp=df[col].value_counts()
```

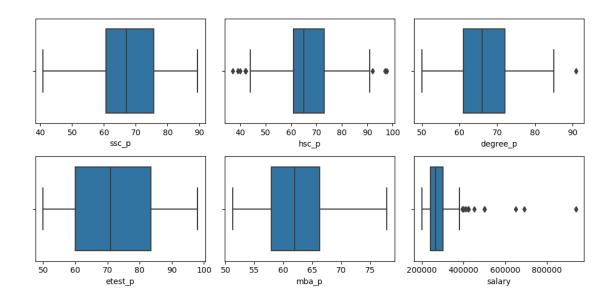
```
axes[r,c].pie(pp.values,labels=pp.index,autopct='%1.1f%%',
startangle=90, textprops={'fontsize': 10})
    axes[r,c].set_title(f'Pie Chart of {col}')
plt.tight_layout()
plt.show()
```

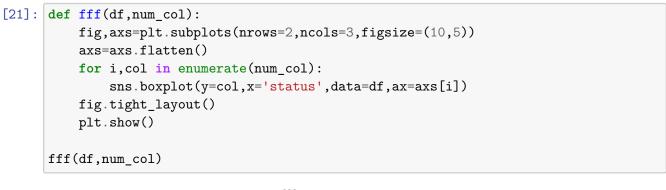
#### [19]: funccatcol\_pie(df,cat\_col)

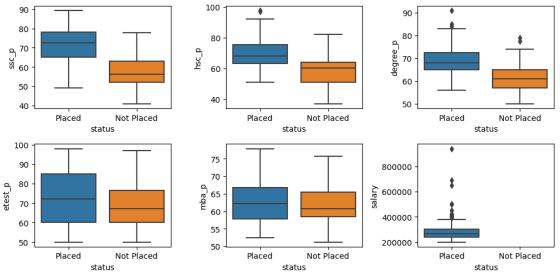


```
[20]: def fff(dfnum,num_col):
    fig,axs=plt.subplots(nrows=2,ncols=3,figsize=(10,5))
    axs=axs.flatten()
    for i,col in enumerate(num_col):
        sns.boxplot(x=col,data=dfnum,ax=axs[i])
    fig.tight_layout()
    plt.show()

fff(dfnum,num_col)
```

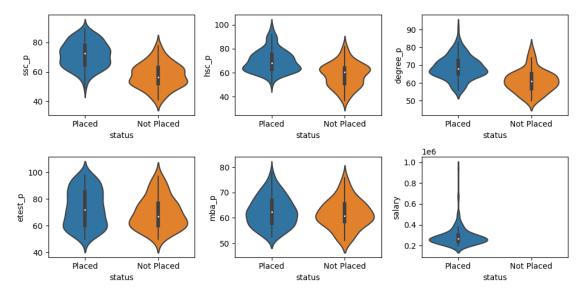






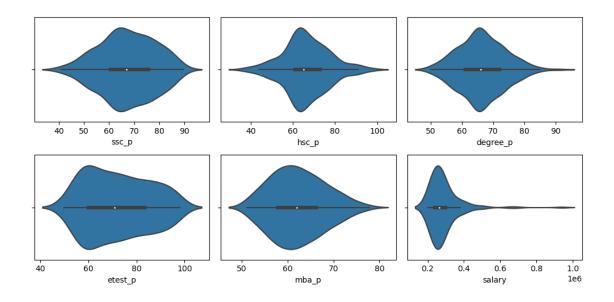
```
[22]: def fff(df,num_col):
    fig,axs=plt.subplots(nrows=2,ncols=3,figsize=(10,5))
    axs=axs.flatten()
    for i,col in enumerate(num_col):
        sns.violinplot(y=col,x='status',data=df,ax=axs[i])
    fig.tight_layout()
    plt.show()

fff(df,num_col)
```



```
[23]: def fff(df,num_col):
    fig,axs=plt.subplots(nrows=2,ncols=3,figsize=(10,5))
    axs=axs.flatten()
    for i,col in enumerate(num_col):
        sns.violinplot(x=col,data=dfnum,ax=axs[i])
    fig.tight_layout()
    plt.show()

fff(df,num_col)
```



## 3 2 Data Preprocessing

## 4 Categoury in each categorical column

```
[28]: for i in cat_col:
        print(f'{i}:{df[i].unique()}')

gender:['M' 'F']
ssc_b:['Others' 'Central']
hsc_b:['Others' 'Central']
hsc_s:['Commerce' 'Science' 'Arts']
degree_t:['Sci&Tech' 'Comm&Mgmt' 'Others']
workex:['No' 'Yes']
```

```
specialisation:['Mkt&HR' 'Mkt&Fin']
status:['Placed' 'Not Placed']
```

### 5 Label Encoding

```
[29]: import pandas as pd
      from sklearn.preprocessing import LabelEncoder
      dfcat1=pd.DataFrame()
      for col in df.select_dtypes(include=['object']).columns:
          label_encoder = LabelEncoder()
          dfcat1[col] = label_encoder.fit_transform(dfcat[col])
          print(f'{col}:{dfcat1[col].unique()}')
     gender:[1 0]
     ssc_b:[1 0]
     hsc b:[1 0]
     hsc_s:[1 2 0]
     degree_t:[2 0 1]
     workex:[0 1]
     specialisation:[1 0]
     status:[1 0]
[30]: import pandas as pd
      from sklearn.preprocessing import LabelEncoder
      for col in df.select_dtypes(include=['object']).columns:
          label_encoder = LabelEncoder()
          df[col] = label_encoder.fit_transform(dfcat[col])
          print(f'{col}:{df[col].unique()}')
     gender:[1 0]
     ssc_b:[1 0]
     hsc b:[1 0]
     hsc_s:[1 2 0]
     degree_t:[2 0 1]
     workex:[0 1]
     specialisation:[1 0]
     status:[1 0]
[31]: dfnum
[31]:
                                                     salary
           ssc_p hsc_p
                         degree_p etest_p
                                            mba_p
      0
           67.00 91.00
                            58.00
                                      55.0 58.80 270000.0
          79.33 78.33
                            77.48
      1
                                      86.5 66.28
                                                   200000.0
      2
          65.00 68.00
                            64.00
                                      75.0 57.80
                                                   250000.0
      3
          56.00 52.00
                            52.00
                                      66.0 59.43
                                                        NaN
                                      96.8 55.50 425000.0
          85.80 73.60
                            73.30
      4
                                      91.0 74.49 400000.0
      210 80.60 82.00
                            77.60
```

```
72.00
211 58.00
           60.00
                               74.0
                                     53.62
                                            275000.0
212 67.00
                     73.00
                                59.0
                                     69.72
                                            295000.0
           67.00
                      58.00
213 74.00
           66.00
                                70.0
                                     60.23
                                            204000.0
214 62.00 58.00
                     53.00
                                89.0
                                     60.22
                                                 NaN
```

[215 rows x 6 columns]

```
[32]: df
                                                                       degree_t
[32]:
                            ssc_b hsc_p hsc_b
            gender
                    ssc_p
                                                   hsc s
                                                           degree_p
                                                                                  workex
                 1
                    67.00
                                 1
                                    91.00
                                                1
                                                        1
                                                               58.00
                                                                              2
                                                                                       0
      0
      1
                 1
                    79.33
                                    78.33
                                                1
                                                        2
                                                               77.48
                                                                              2
                                                                                       1
                                 0
      2
                 1
                    65.00
                                 0
                                    68.00
                                                0
                                                        0
                                                               64.00
                                                                              0
                                                                                       0
                                                        2
                                                                              2
      3
                 1
                    56.00
                                 0
                                    52.00
                                                0
                                                               52.00
                                                                                       0
      4
                    85.80
                                    73.60
                                                        1
                                                                              0
                 1
                                 0
                                                0
                                                               73.30
                                                                                       0
                                                                              0
                                                                                       0
      210
                 1
                    80.60
                                 1
                                    82.00
                                                 1
                                                        1
                                                               77.60
                    58.00
                                    60.00
                                                               72.00
                                                                              2
      211
                 1
                                 1
                                                1
                                                        2
                                                                                       0
      212
                    67.00
                                    67.00
                                                        1
                                                               73.00
                                                                              0
                                                                                       1
                 1
                                 1
                                                1
      213
                    74.00
                                    66.00
                                                        1
                                                               58.00
                                                                              0
                                                                                       0
                 0
                                 1
                                                1
      214
                 1 62.00
                                    58.00
                                                1
                                                        2
                                                               53.00
                                                                              0
                                                                                       0
                      specialisation
            etest_p
                                       mba_p
                                               status
                                                          salary
                                                        270000.0
      0
               55.0
                                       58.80
                                                     1
      1
               86.5
                                       66.28
                                                        200000.0
      2
               75.0
                                    0
                                       57.80
                                                     1
                                                        250000.0
      3
               66.0
                                    1
                                       59.43
                                                     0
                                                        265000.0
      4
               96.8
                                    0
                                       55.50
                                                     1
                                                        425000.0
                •••
                                       74.49
                                                        400000.0
      210
               91.0
                                    0
                                                     1
                                                        275000.0
      211
               74.0
                                       53.62
                                    0
                                                     1
                                       69.72
      212
               59.0
                                                        295000.0
               70.0
                                       60.23
                                                        204000.0
      213
                                    1
                                                     1
      214
               89.0
                                       60.22
                                                        265000.0
```

[215 rows x 14 columns]

hsc\_s\_Commerce:[1 0]

# 6 One - Hot Encoding

```
[33]: DF_encoded = pd.get_dummies(dfcat, columns=cat_col, drop_first=True)
for i in DF_encoded:
    print(f'{i}:{DF_encoded[i].unique()}')

gender_M:[1 0]
ssc_b_Others:[1 0]
hsc_b_Others:[1 0]
```

```
hsc_s_Science:[0 1]
degree_t_Others:[0 1]
degree_t_Sci&Tech:[1 0]
workex_Yes:[0 1]
specialisation_Mkt&HR:[1 0]
status_Placed:[1 0]
```

### [34]: DF\_encoded

[34]:	gender_M	ssc_b_Others	hsc_b_Others	hsc_s_Commerce	hsc_s_Science '	\
0	1	1	1	1	0	
1	1	0	1	0	1	
2	1	0	0	0	0	
3	1	0	0	0	1	
4	1	0	0	1	0	
		•••	•••	•••	•••	
2	10 1	1	1	1	0	
2	11 1	1	1	0	1	
2	12 1	1	1	1	0	
2	13 0	1	1	1	0	
2	14 1	0	1	0	1	

	degree_t_Others	degree_t_Sci&Tech	$workex\_Yes$	specialisation_Mkt&HR	\
0	0	1	0	1	
1	0	1	1	0	
2	0	0	0	0	
3	0	1	0	1	
4	0	0	0	0	
	•••	•••	•••	<b></b>	
210	0	0	0	0	
211	0	1	0	0	
212	0	0	1	0	
213	0	0	0	1	
214	0	0	0	1	

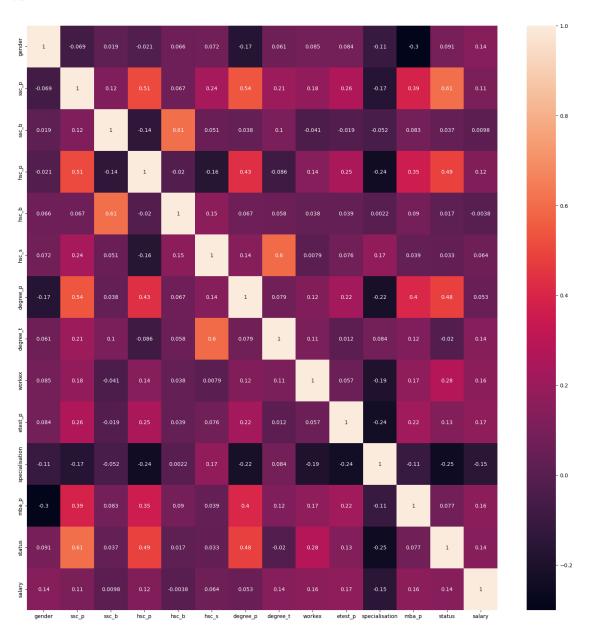
### status\_Placed

0	1
1	1
2	1
3	0
4	1
• •	•••
210	 1
210 211	 1 1
211	1

## 7 Hear Map

```
[35]: plt.figure(figsize=(20,20)) sns.heatmap(df.corr(),fmt='.2g',annot=True)
```

[35]: <Axes: >



```
[36]: df
           gender
[36]:
                   ssc_p ssc_b hsc_p hsc_b hsc_s
                                                        degree_p
                                                                  degree_t
                                                                             workex
      0
                1
                   67.00
                               1
                                  91.00
                                              1
                                                     1
                                                           58.00
                                                                          2
                                                                                  0
                1 79.33
                               0 78.33
                                                     2
                                                           77.48
                                                                          2
      1
                                             1
                                                                                  1
      2
                1 65.00
                                 68.00
                                             0
                                                     0
                                                           64.00
                                                                          0
                                                                                  0
                               0
                                  52.00
                                                     2
                                                                          2
      3
                1
                   56.00
                                             0
                                                           52.00
                                                                                  0
      4
                1 85.80
                                  73.60
                                             0
                                                     1
                                                           73.30
                                                                          0
                                                                                  0
      210
                   80.60
                                  82.00
                                                     1
                                                           77.60
                                                                          0
                                                                                  0
                1
                               1
                                              1
                1 58.00
                                  60.00
                                                     2
                                                           72.00
                                                                          2
                                                                                  0
      211
                               1
                                              1
                1 67.00
                                  67.00
                                                           73.00
                                                                          0
      212
                               1
                                              1
                                                     1
                                                                                  1
      213
                0 74.00
                                  66.00
                                              1
                                                     1
                                                           58.00
                                                                          0
                                                                                  0
                               1
      214
                1 62.00
                                  58.00
                                              1
                                                     2
                                                           53.00
                                                                          0
                                                                                  0
           etest_p specialisation mba_p
                                            status
                                                       salary
      0
              55.0
                                     58.80
                                                     270000.0
      1
              86.5
                                     66.28
                                                  1
                                                     200000.0
      2
              75.0
                                  0 57.80
                                                     250000.0
                                                  1
      3
              66.0
                                  1 59.43
                                                  0
                                                     265000.0
      4
              96.8
                                  0 55.50
                                                  1 425000.0
                                  0 74.49
                                                  1 400000.0
      210
              91.0
      211
              74.0
                                  0 53.62
                                                     275000.0
      212
              59.0
                                  0 69.72
                                                  1
                                                     295000.0
      213
              70.0
                                  1 60.23
                                                     204000.0
                                                  1
      214
              89.0
                                  1 60.22
                                                     265000.0
```

[215 rows x 14 columns]

#### 8 Train Test Split

```
[40]: from sklearn.model_selection import train_test_split
    x=df.drop('status',axis=1)
    y=df['status']

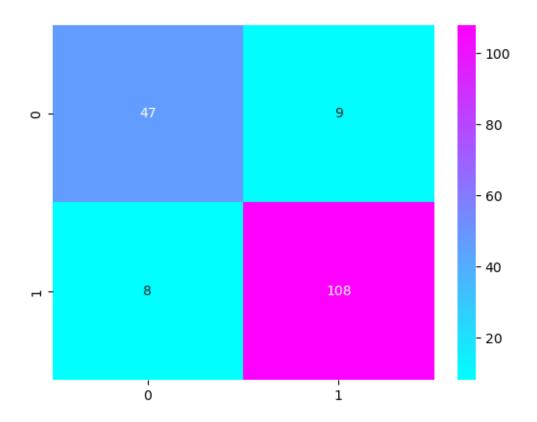
[41]: xtrn,xtst,ytrn,ytst=train_test_split(x,y,train_size=0.2)
```

#### 9 Remove Outlier drom data

```
[39]: from scipy.stats import zscore
z_scores = zscore(df[num_col])
df_no_outliers = df[(z_scores < 3).all(axis=1)]</pre>
```

#### 10 Decision Tree

```
[41]: from sklearn.tree import DecisionTreeClassifier
      from sklearn.model_selection import GridSearchCV
      dt=DecisionTreeClassifier(class_weight='balanced')
      param_grid={
          'max_depth': [2,5,7,11,13],
          'min_samples_split': [2,3,5,7],
          'min_samples_leaf':[2,3,4],
          #'max_feature':[0.2,0.3,0.5,0.7]
      }
      dt_grid=GridSearchCV(dt,param_grid,cv=4)
      dt_grid.fit(xtrn,ytrn)
[41]: GridSearchCV(cv=4, estimator=DecisionTreeClassifier(class_weight='balanced'),
                   param_grid={'max_depth': [2, 5, 7, 11, 13],
                               'min_samples_leaf': [2, 3, 4],
                               'min_samples_split': [2, 3, 5, 7]})
[42]: dt_grid.best_params_
[42]: {'max_depth': 7, 'min_samples_leaf': 2, 'min_samples_split': 3}
[43]: print("Accuracy Score: ", round(dt_grid.best_score_ * 100, 2), "%")
     Accuracy Score: 78.86 %
[44]: ypred=dt_grid.predict(xtst)
     11
           Confusion Matrix
[45]: from sklearn.metrics import confusion_matrix
      cm=confusion_matrix(ytst,ypred)
[46]: sns.heatmap(data=cm,annot=True,fmt='d',cmap='cool')
[46]: <Axes: >
```



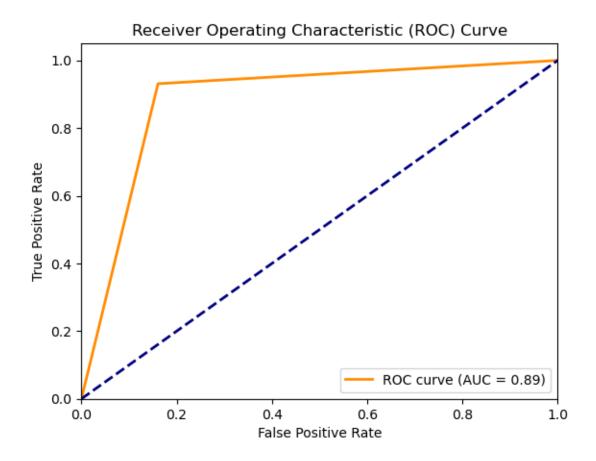
### 12 ROC Curve

```
from sklearn.metrics import roc_curve, auc

fpr, tpr, thresholds = roc_curve(ytst, ypred)

roc_auc = auc(fpr, tpr)

plt.figure()
plt.plot(fpr, tpr, color='darkorange', lw=2, label='ROC curve (AUC = %0.2f)' %u oroc_auc)
plt.plot([0, 1], [0, 1], color='navy', lw=2, linestyle='--')
plt.xlim([0.0, 1.0])
plt.ylim([0.0, 1.05])
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver Operating Characteristic (ROC) Curve')
plt.legend(loc="lower right")
plt.show()
```



### 13 Random Forest

```
[48]: from sklearn.ensemble import RandomForestClassifier
from sklearn.model_selection import GridSearchCV

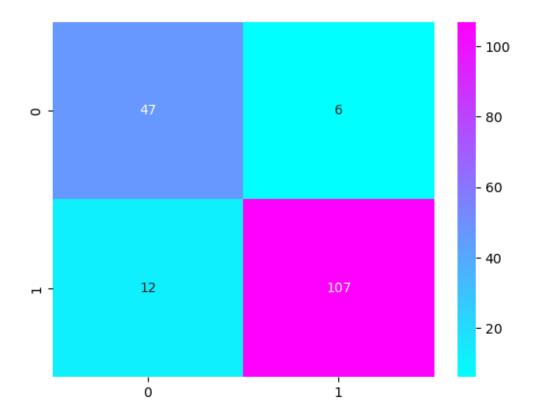
# Assuming you have your training data in 'xtrn' and labels in 'ytrn'

rf = RandomForestClassifier(class_weight='balanced')
param_grid = {
    'n_estimators': [10, 15, 17],
    'max_depth': [2, 5, 7, 11, 13, None],
    'min_samples_split': [2, 3, 5, 7],
    'min_samples_leaf': [2, 3, 4],
    'max_features': [0.2, 0.3, 0.5, 0.7]
}

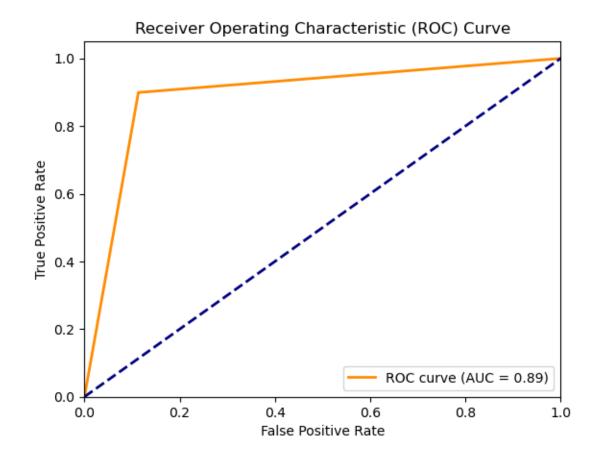
rf_grid = GridSearchCV(rf, param_grid, cv=4)
rf_grid.fit(xtrn, ytrn)
```

```
[48]: GridSearchCV(cv=4, estimator=RandomForestClassifier(class_weight='balanced'),
                   param_grid={'max_depth': [2, 5, 7, 11, 13, None],
                               'max_features': [0.2, 0.3, 0.5, 0.7],
                               'min_samples_leaf': [2, 3, 4],
                               'min_samples_split': [2, 3, 5, 7],
                               'n_estimators': [10, 15, 17]})
[49]: rf_grid.best_params_
[49]: {'max_depth': 7,
       'max_features': 0.2,
       'min_samples_leaf': 2,
       'min_samples_split': 5,
       'n_estimators': 17}
[50]: print("Accuracy Score: ", round(rf_grid.best_score_ * 100, 2), "%")
     Accuracy Score: 95.45 %
[51]: ypred=rf_grid.predict(xtst)
     14
          Confusion Matrix
[57]: from sklearn.metrics import confusion_matrix
      cm=confusion matrix(ytst,ypred)
      sns.heatmap(data=cm,annot=True,fmt='d',cmap='cool')
```

[57]: <Axes: >



### 15 ROC Curve



# 16 Logistic regression

```
[48]: from sklearn.linear_model import LogisticRegression
    from sklearn.metrics import accuracy_score
    lg=LogisticRegression()

lg.fit(xtrn, ytrn)
    ypred=lg.predict(xtst)
    accuracy=round(accuracy_score(ytst, ypred),2)*100
    print("Accuracy:", accuracy)
```

Accuracy: 84.0

C:\Users\Kundan Mourya\anaconda3\lib\sitepackages\sklearn\linear\_model\\_logistic.py:458: ConvergenceWarning: lbfgs failed to converge (status=1): STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.

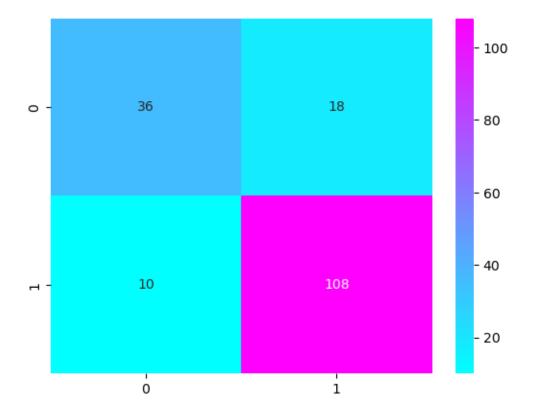
Increase the number of iterations (max\_iter) or scale the data as shown in:
 https://scikit-learn.org/stable/modules/preprocessing.html

```
Please also refer to the documentation for alternative solver options:
    https://scikit-learn.org/stable/modules/linear_model.html#logistic-
regression
    n_iter_i = _check_optimize_result(
```

#### 17 Confusion Matrix

```
[49]: from sklearn.metrics import confusion_matrix cm=confusion_matrix(ytst,ypred) sns.heatmap(data=cm,annot=True,fmt='d',cmap='cool')
```

[49]: <Axes: >



```
[51]: from sklearn.metrics import roc_curve, auc
fpr, tpr, thresholds = roc_curve(ytst, ypred)

roc_auc = auc(fpr, tpr)

plt.figure()
```

```
plt.plot(fpr, tpr, color='darkorange', lw=2, label='ROC curve (AUC = %0.2f)' %_\( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \)
```



