

# Tutorial on Topological Data Analysis

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## Contents

1	Tutorial on $\text{\LaTeX}$	1
2	Metric Space	2

### Abstract

This is for the first tutorial of topological data analysis.

## 1 Tutorial on $\text{\LaTeX}$

This is a **bold text**.

This is a underlined text.

This is a *italic text*.

This could also be ***combined***.

If you don't want to choose manually, you could use *emphsize*.

emphsize *under italic text*. ***emphasize*** under **bold text**.

Take a look at the Figure 1 .

- List one

- List two

1. Number one

2. Number two

Metric: (i)  $d(x, y) \geq 0$  for all  $x, y \in X$ .

$$d(x, y) = \begin{cases} 0000000 & \text{if } x = y, \\ 1 & \text{if } x \neq y, \end{cases} \quad (1)$$

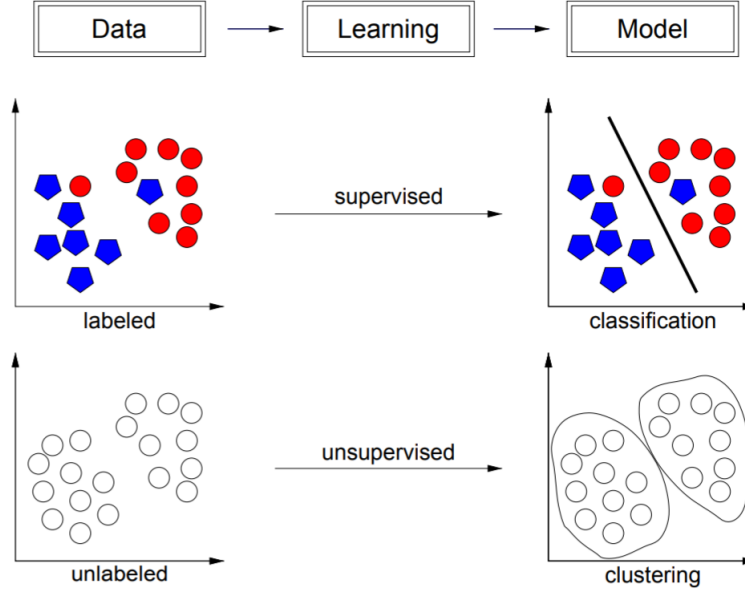


Figure 1: The introduction of xxx

## 2 Metric Space

Definition: Let  $X$  be a set and  $d : X^2 \rightarrow \mathbb{R}$  a function with the follow properties:

- (i)  $d(x, y) \geq 0$  for all  $x, y \in X$ .
- (ii)  $d(x, y) = 0$  if only if  $x = y$ .
- (iii)  $d(x, y) = d(y, x)$  for all  $x, y \in X$ .
- (iv)  $d(x, y) + d(y, z) \geq d(x, z)$  for all  $x, y, z \in X$ . (This is called the *triangle inequality*).

Then we say that  $d$  is a *metric* on  $X$  and that  $(X, d)$  is a *metric space*.

Take away:

- ‘(i) Distances are always positive.
- (ii) Two points are zero distance part if and only if they are the same point.
- (iii) The distance form  $A$  to  $B$  is the same as the distance from  $B$  to  $A$ .
- (iv) The distance form  $A$  to  $B$  via  $C$  is at least as great as the distance from  $A$  to  $B$  directly. ’