

a).

- ① For  $li_1$ :  $LR = -2 \times (-149.521 - (-134.178)) = 30.7 > 3.8$ ;
- ② For  $li_2$ :  $LR = -2 \times (-139.747 - (-134.178)) = 11.1 > 3.8$ ;
- ③ For  $li_1$  and  $li_2$  jointly:  $LR = -2 \times (-152.763 - 134.178) = 37.2 > 6.0$ .

All of the above are significant.

b).

① When the models to be compared share the same dependent variable and same number of explanatory variables, we can use McFadden  $R^2$ .

② The optimal model according to this criterion is:

$$GDPIMPR_t = 0.746 - 0.429li_{1t}(-2) - 0.131li_{2t}(-1) + \varepsilon_t$$

| Explanatory Variables | McFadden $R^2$ |
|-----------------------|----------------|
| $li_1(-2), li_2(-1)$  | 0.1468         |
| $li_1(-2), li_2(-2)$  | 0.1460         |
| $li_1(-1), li_2(-2)$  | 0.1220         |
| $li_1(-1), li_2(-1)$  | 0.1217         |

c).

| Date   | Predicted Prob. | GDPIMPR   |        | Hit |
|--------|-----------------|-----------|--------|-----|
|        |                 | Predicted | Actual |     |
| 2011Q1 | 0.24            | 0         | 1      |     |
| 2011Q2 | 0.22            | 0         | 0      | ○   |
| 2011Q3 | 0.08            | 0         | 0      | ○   |
| 2011Q4 | 0.08            | 0         | 0      | ○   |
| 2012Q1 | 0.16            | 0         | 1      |     |
| 2012Q2 | 0.23            | 0         | 0      | ○   |
| 2012Q3 | 0.38            | 0         | 1      |     |
| 2012Q4 | 0.56            | 1         | 1      | ○   |
| 2013Q1 | 0.60            | 1         | 1      | ○   |
| 2013Q2 | 0.52            | 1         | 1      | ○   |
| 2013Q3 | 0.56            | 1         | 1      | ○   |
| 2013Q4 | 0.71            | 1         | 0      |     |
| 2014Q1 | 0.74            | 1         | 0      |     |
| 2014Q2 | 0.65            | 1         | 1      | ○   |
| 2014Q3 | 0.76            | 1         | 1      | ○   |
| 2014Q4 | 0.85            | 1         | 1      | ○   |
| 2015Q1 | 0.85            | 1         | 1      | ○   |
| 2015Q2 | 0.83            | 1         | 1      | ○   |
| 2015Q3 | 0.71            | 1         | 1      | ○   |
| 2015Q4 | 0.35            | 0         | 0      | ○   |

Hit rate = 0.75

d).

As  $GROWTHRATE = \Delta \text{LOGGDP}$ ,

then  $GROWTHRATE(-1) = D(\text{LOGGDP}(-1))$ ;

T denotes the trend.

Dependent Variable: GROWTHRATE  
Method: Least Squares  
Date: 05/13/17 Time: 15:43  
Sample (adjusted): 1951Q1 2010Q4  
Included observations: 240 after adjustments

| Variable       | Coefficient | Std. Error | t-Statistic | Prob.  |
|----------------|-------------|------------|-------------|--------|
| C              | 0.089935    | 0.037476   | 2.399775    | 0.0172 |
| GROWTHRATE(-1) | 0.612861    | 0.050087   | 12.23584    | 0.0000 |
| LOGGDP(-1)     | -0.019278   | 0.008130   | -2.371164   | 0.0185 |
| T              | 6.23E-05    | 2.59E-05   | 2.406563    | 0.0169 |

As observed, t-statistic of LOGGDP(-1) = -2.371164 > -3.7;

Conclusion: LOGGDP is non-stationary.

e).

② Suggested model:

| Variable           | Coefficient | Std. Error         | t-Statistic | Prob.    |
|--------------------|-------------|--------------------|-------------|----------|
| C                  | 0.001737    | 0.000320           | 5.432574    | 0.0000   |
| GROWTHRATE(-1)     | 0.461579    | 0.048302           | 9.556130    | 0.0000   |
| LI1(-1)            | -0.001023   | 0.000130           | -7.880028   | 0.0000   |
| LI2(-1)            | -0.000149   | 6.42E-05           | -2.326183   | 0.0209   |
| R-squared          | 0.507975    | Mean dependent var |             | 0.003406 |
| Adjusted R-squared | 0.501720    | S.D. dependent var |             | 0.005817 |

①

| Explanatory Variables | R <sup>2</sup> |
|-----------------------|----------------|
| li1(-1), li2(-1)      | 0.5080         |
| li1(-1), li2(-2)      | 0.5077         |
| li1(-2), li2(-1)      | 0.4772         |
| li1(-2), li2(-2)      | 0.4771         |

f).

| Variable           | Coefficient | Std. Error         | t-Statistic | Prob.     |
|--------------------|-------------|--------------------|-------------|-----------|
| C                  | -0.000100   | 0.000384           | -0.261442   | 0.7940    |
| GROWTHRATE(-1)     | 0.029135    | 0.079152           | 0.368094    | 0.7131    |
| RESID01(-1)        | -0.049992   | 0.103221           | -0.484322   | 0.6286    |
| LI1(-1)            | 3.14E-05    | 0.000149           | 0.210114    | 0.8338    |
| LI2(-1)            | 2.77E-06    | 6.50E-05           | 0.042611    | 0.9660    |
| R-squared          | 0.001002    | Mean dependent var |             | -6.65E-07 |
| Adjusted R-squared | -0.016075   | S.D. dependent var |             | 0.004089  |

Breusch-Godfrey test:  $nR^2 = 240 \times 0.001002 = 0.24 < 3.8$

Conclusion: there is no serial correlation

g).

RMSE=0.008156

