## Bioinformatics III

## Fifth Assignment

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## Exercise 5.1: Cliques and Network Evolution

(a) Listing 1 shows source code.

```
Listing 1: Listing of source code
```

```
o import random
  from os.path import exists
  from AbstractNetwork import AbstractNetwork
  import matplotlib.pyplot as plt
  class CliqueNetwork(AbstractNetwork):
      function that computes the number of cliques of sizes 3, 4 and 5 in a network
      def __createNetwork__(self , filename , dummy):
10
           Create a network from a file
           if exists(filename):
              # "with" closes the file again after reading
15
               with open(filename) as openfile:
                   for line in openfile:
                       # get entries of a line as list
                       content = line [0:(len(line)-1)]. split ("\t")
20
                       # and store them
                       if len(content) == 2:
                           n1 = self.getNode(content[0])
                           n2 = self.getNode(content[1])
                           n1.addLinkTo(n2)
                           n2.addLinkTo(n1)
25
           else:
               print(filename, "does_not_exist")
      def findCliques(self):
30
           function that computes the number of cliques of sizes 3, 4 and 5 in a network.
          :return: list of cliques
          for node1 in self.nodes.values():
35
               for node2 in node1.nodelist:
                   candidates = list()
                   candidates.append(node1)
                   \verb|candidates|.append(\verb|node2|)
                   clique = set(self.extendClique(candidates, 3))
40
                   #only consider cliques of size 3-5
                   if clique not in cliques and len(clique) > 2:
                       cliques.append(clique)
          return cliques
```

```
45
       def extendClique(self, candidates, depth):
           try to extend clique to larger cliques
            : param\ candidates:\ smaller\ clique
           :param depth: clique size; maximal 5
50
           :return: largest clique possible
           if depth <= 5:
                for nextnode in candidates [0]. nodelist:
55
                    if nextnode not in candidates:
                        #check if node is connected to all nodes in clique
                        if all(nextnode.hasLinkTo(x) for x in candidates):
                             candidates.append(nextnode)
                            self.extendClique(candidates, depth+1)
                        else:
60
                            return candidates
                return candidates
           else:
                return candidates
       def evolve (self, t):
           function that takes a parameter t representing the number of time steps, as well as a
           step, randomly insert or delete one edge in the network
            : param \ t: \ number \ of \ time \ steps
70
           cliques = list()
           for c in range (3):
                cliques.append(t * [0])
               i in range(t):
75
                clique = cn. findCliques()
                r = random.random()
                nodelid = random.choice(list(self.nodes))
                node1 = self.nodes[node1id]
               \#decide if edge gets removed or new edge added
80
                if r <= 0.5:
                    #try to find two nodes without edge
                    while True:
                        node2id = random.choice(list(self.nodes))
                        node2 = self.nodes[node2id]
85
                        if not node1.hasLinkTo(node2):
                            node1.addLinkTo(node2)
                            node2.addLinkTo(node1)
                            break
                else:
90
                    #search for edge
                    while len(node1.nodelist) == 0:
                        nodelid = random.choice(list(self.nodes))
                        node1 = self.nodes[node1id]
                    node2 = random.choice(node1.nodelist)
                    node1.removeLinkTo(node2)
               #plot number of cliques of size 3, 4 and 5 at the beginning and after each time ste
               \# with t = 100
                cliques = self.plot(clique, i, cliques)
           for index , item in enumerate(cliques):
100
                plt.plot(range(len(item)), item, marker='x')
                plt.xlabel('t')
plt.ylabel('amount_of_cliques')
                plt.title('Evolving_Networks')
                plt.legend('345')
105
                plt.tight_layout()
           plt.show()
       def printClique(self, clique):
110
            print cliques to check result
```

```
:param clique: clique to print
            for line in clique:
                s = 0
115
                for c in line:
                    s += str(c)
                print(s)
       \mathbf{def} plot(self, clique, t, cliques):
120
            count amount of cliques of size i at time step t
            :param\ clique:\ cliques\ in\ current\ time\ step
            :param \ t: \ time \ step
            :param cliques: matrix to store count
125
            :return: matrix with counts
            for c in clique:
                cliques[len(c)-3][t] = cliques[len(c)-3][t] + 1
            return cliques
130
   cn = CliqueNetwork("rat_network.tsv", "dummy")
   clique = cn.findCliques()
135 cn. evolve (1000)
   clique = cn.findCliques()
```

- (b) Listing 1 shows source code.
- (c) Listing 1 shows source code.
- (d) The number of cliques stays approximately the same independent of the time step because approximately the same amount of edges are added which are removed as shown in figure 1, table 4 and table 4. The amount of cliques of size 3 increases rather than the one of larger cliques because a less edges added may result in a small clique.

clique size	number of cliques before evolution	number of cliques after evolution
3	294	300
4	33	33
5	3	3

Table 1: Number of cliques of size 3, 4 and 5 at the beginning and after letting it evolve for 100 time steps

clique size	number of cliques before evolution	number of cliques after evolution
3	294	327
4	33	27
5	3	3

Table 2: Number of cliques of size 3, 4 and 5 at the beginning and after letting it evolve for 1000 time steps

(e) The goal of randomising networks this way is to create random permutations of a network. In this way the behaviour of similar networks may be studied and the networks quality may be rated.

Listing 2 shows source code.

Listing 2: Listing of source code

 $\begin{array}{ll} \textbf{0} & \textbf{from} & AbstractNetwork & \textbf{import} & AbstractNetwork \\ \textbf{import} & random \end{array}$ 

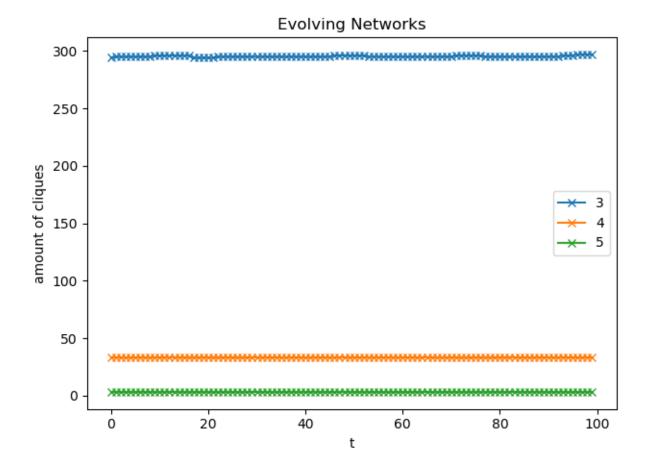


Figure 1: Number of cliques of size 3, 4 and 5 at the beginning and after each time step as a function of time with t=100

from CliqueNetwork import CliqueNetwork

```
class RandomizedNetwork(AbstractNetwork):
       function that takes a network with m edges and returns a randomised version of that network
       def __createNetwork__(self , network , m):
 10
            for 2m iterations, randomly select two edges e1 = (n1; n2) and e2 = (n3; n4) from the
            such \ that \ the \ start \ and \ end \ nodes \ are \ swapped
            :param\ network:\ network
            :param m: number of edges
 15
            self.nodes = network.nodes
            for i in range (2*m):
                node1 = self.chooseNode()
                node2 = random.choice(node1.nodelist)
 20
                node3 = self.chooseNode()
                node4 = random.choice(node3.nodelist)
                node1.addLinkTo(node4)
                node3.addLinkTo(node2)
                node1.removeLinkTo(node2)
 25
                node3.removeLinkTo(node4)
       def chooseNode(self):
            choose random node with edges
 30
            : return: \ random \ node \ with \ at \ least \ one \ edge \\"""
            nodeid = random.choice(list(self.nodes))
            node = self.nodes[nodeid]
            if len(node.nodelist) != 0:
 35
                return node
            else:
                self.chooseNode()
   cn = RandomizedNetwork(CliqueNetwork("test.tsv", "dummy"), 10)
(f) Assuming a p-value of 0.05, none of the clique sizes were significantly enriched, see table 6.
   Listing 3 shows source code.
                            Listing 3: Listing of source code
 o import random
   from CliqueNetwork import CliqueNetwork
   class MotifNetworks:
 5
        class that takes a parameter n and a network and computes if cliques of size 3, 4 and 5 are
        enriched in that network
       network = CliqueNetwork("", "")
       clique = list()
 10
       def __init__(self , network , n):
            self.network = network
            #compute number of cliques in original network
            self.clique = self.network.findCliques()
 15
            #perform n switches
            cliques = self.__createNetwork__(n)
            c_i = dict()
```

#initilize dict
for i in range(3, 6):

 $c_i[i] = 0$ 

20

```
#count cliques of size i
for i in self.clique:
                c_i[len(i)] = c_i.get(len(i), 0) + 1
           \#\ count\ cliques\ of\ size\ of\ at\ least\ i
25
            for i in range (4, 2, -1):
                    c_i [i] += c_i [i+1]
           \#compute p_{-i}
            extremes = list()
            for key, item in c_i.items():
30
                extremes.append((key, self.count(cliques, key, item)))
            print(extremes)
       def __createNetwork__(self , n):
35
            for 2m iterations, randomly select two edges e1 = (n1; n2) and e2 = (n3; n4) from the
            such that the start and end nodes are swapped
            :param n: number of swaps
40
            cliques = list()
            for i in range(n):
                node1 = self.chooseNode()
                node2 = random.choice(node1.nodelist)
45
                node3 = self.chooseNode()
                node4 = random.choice(node3.nodelist)
                node1.addLinkTo(node4)
                node3.addLinkTo(node2)
                node1.removeLinkTo(node2)
50
                node3.removeLinkTo(node4)
                clique = self.network.findCliques()
                cliques.append(clique)
           return cliques
       \mathbf{def} count(self, cliques, i, c_i):
55
            count \ cliques \ of \ size \ of \ at \ least \ i
            : param \>\>\> cliques: \>\>\> randomized \>\>\>\> cliques
            :param\ i:\ clique\ size
            :param c_i: number of cliques with clique size of at least i in original network
:return: number of networks with at least as many cliques of size of at least i over no
60
                     networks
            extremes = 0
            for network in cliques:
65
                count = 0
                for clique in network:
                     if len(clique) >= i:
                         count += 1
                if count >= c_i:
70
                     extremes += 1
            extremes /= float(len(cliques))
            return extremes
       def chooseNode(self):
            choose\ random\ node\ with\ edges
            :return: random node with at least one edge
            nodeid = random.choice(list(self.network.nodes))
            node = self.network.nodes[nodeid]
            if len(node.nodelist) != 0:
                return node
            else:
                self.chooseNode()
85
  cn = CliqueNetwork("rat_network.tsv", "dummy")
```

MotifNetworks (cn, 100)

clique size i	$p_i$
3	0.38
4	0.27
5	1.0

Table 3: Number of randomised networks in which the number of cliques is at least as high as in the original network divided by the number of randomised networks for each clique size

## Exercise 5.2: Annotations in Protein Protein Interaction Networks

- (a)
- (b)
- (c)
- (d)
- (e)