

1.

FIR: $H(z) = b_0 + b_1z^{-1} + b_2z^{-2} + \dots + b_nz^{-n}$

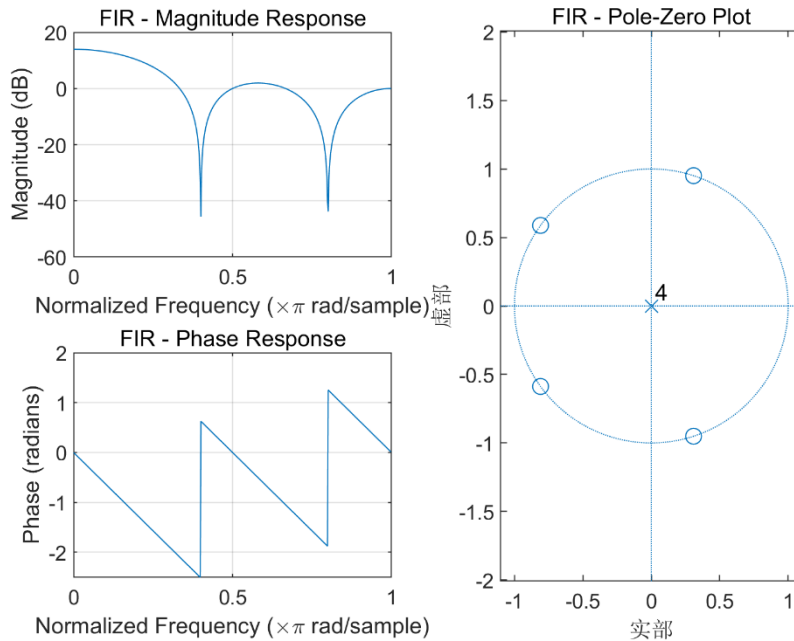
IIR: $H(z) = (b_0 + b_1z^{-1} + b_2z^{-2} + \dots + b_nz^{-n}) / (1 + a_1z^{-1} + a_2z^{-2} + \dots + a_mz^{-m})$:

In 1-b, the first one is FIR filter, the second one is IIR filter. Below are the frequency response and zplane plots.

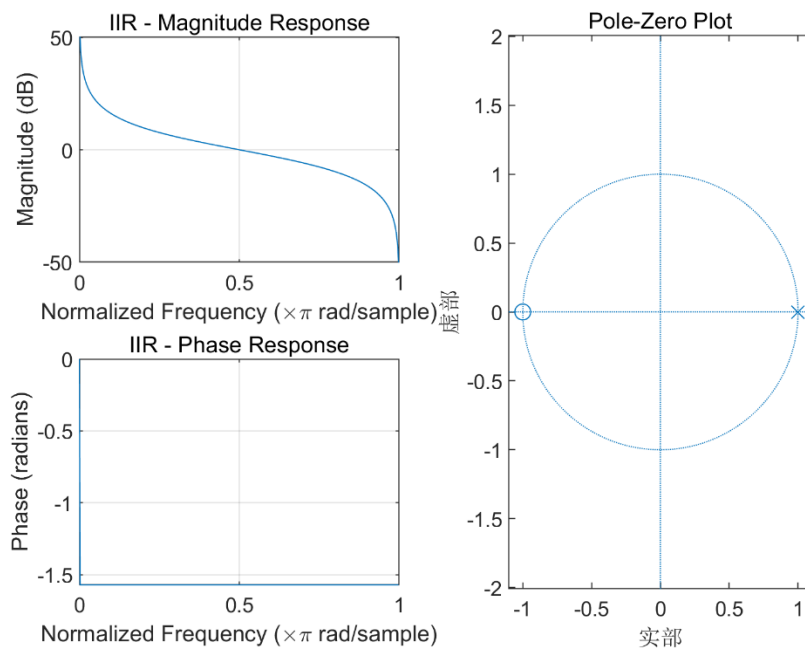
For FIR filter, it has pole 0, and 4 zero located on unit circle equally distributed.

For IIR filter, it has 1 pole at 1, 1 zero at -1.

FIR Response



IIR Response

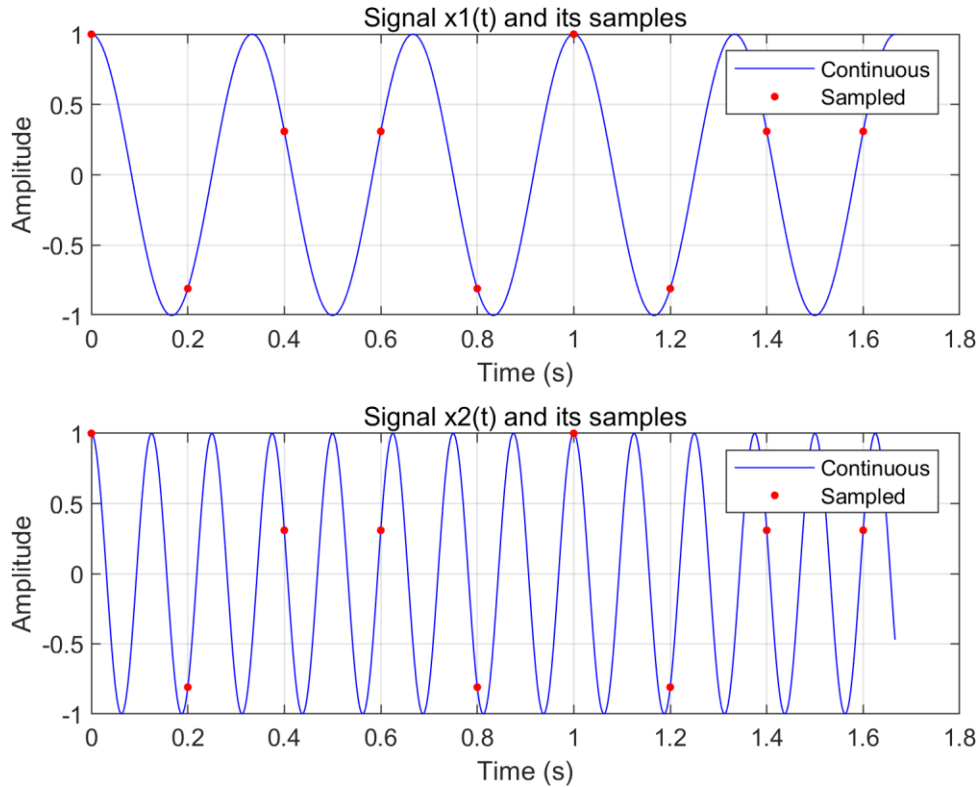


For stability, FIR is always stable because it has no pole. When your input is finite, your output is always finite.

IIR one is not stable, because when your input is $[1 \ 0 \ 0 \ \dots \ 0]$, your output is infinite.

2.

a+b: According to Nyquist Sampling theorem, x_1 can be well reconstructed while x_2 will be aliased to 200MHz. As those red points shows, the 2 signal have the same $x(n)$ after sampling. You should increase your sampling rate higher than 1600MHz.



C: its' given as below

$$x_r(t) = \sum_{n=-\infty}^{\infty} x(nT) * \text{rect}((t-nT)/W - 1)$$

where

$$\text{rect}(t) = 1 \text{ for } 0 \leq t \leq 1$$

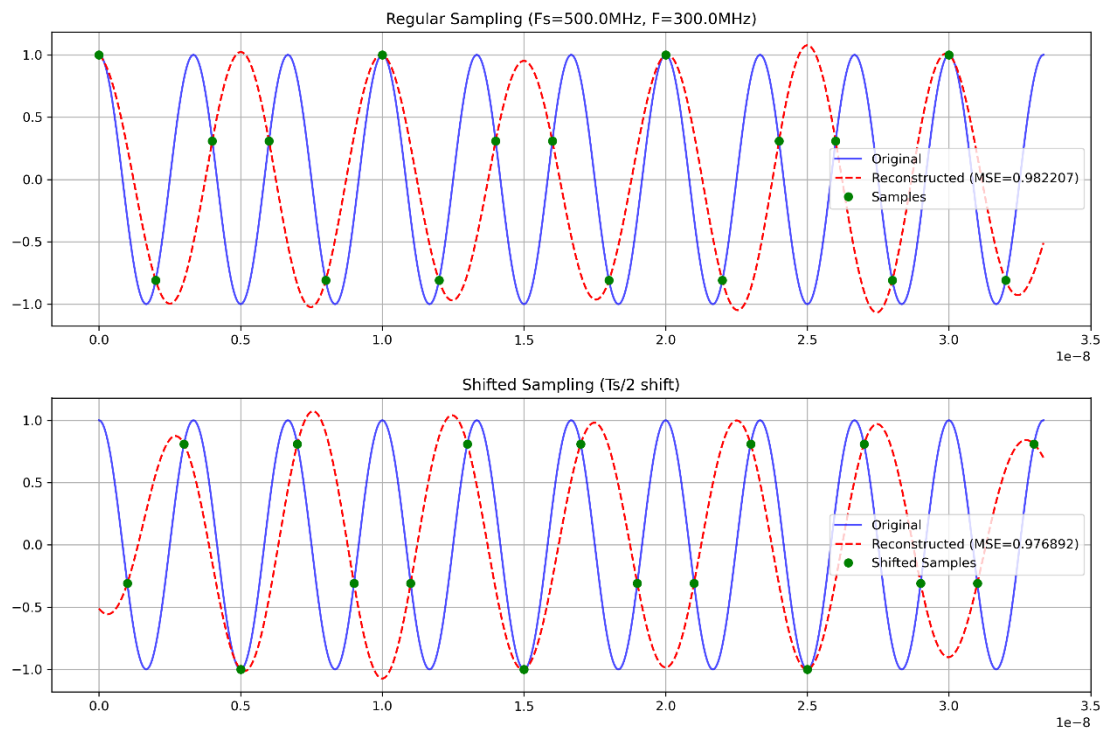
$$\text{rect}(t) = 0 \text{ otherwise}$$

d+e: Here is the result reconstructing x_1 sampled by 3 F_s . As you can see, for $f_s > 2f_1$, it can reconstruct with almost no error. However, when $f_s = 500\text{Hz}$, it can't be reconstructed, as plot given. And shifting doesn't influence reconstruction.

Results for $F_s = 500.0\text{MHz}$:
Regular sampling MSE: 0.982207
Shifted sampling MSE: 0.976892

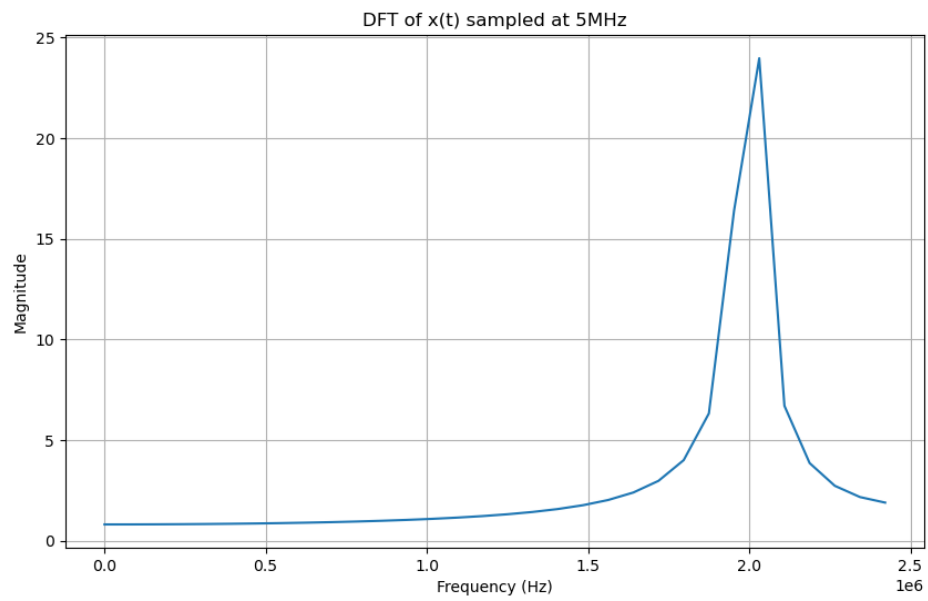
Results for $F_s = 800.0\text{MHz}$:
Regular sampling MSE: 0.008953
Shifted sampling MSE: 0.003850

Results for $F_s = 1000.0\text{MHz}$:
Regular sampling MSE: 0.001476
Shifted sampling MSE: 0.002645



3

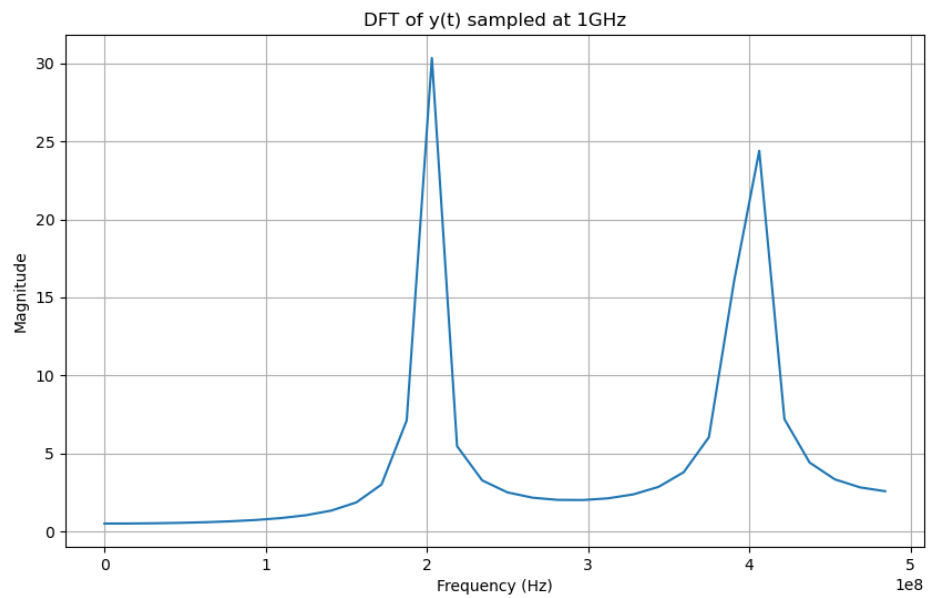
a.



You can detect the 2M signal peak. Due to leakage it looks like this.

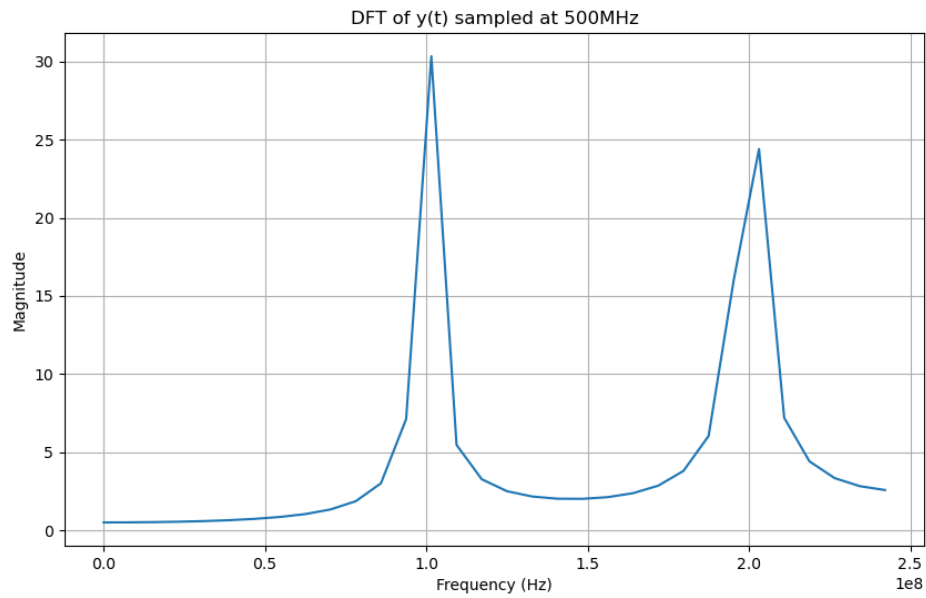
3.b

As shown in the plot, it's easy to identify the 2 tones from the 2 peaks.



3.c

Due to alias, F2 is aliased to $500\text{M} - 400\text{M} = 100\text{M}$, while F1 stays at 200M , as shown in plot.



3.d

As shown in plot, the 2 main lobes get wider comparing to results before.

