2-)Probability & Random Variables $h(x_i) = f_i/n \rightarrow relative frequency$

- $h(x_i) = f_i/n*(c_i c_{i-1}) \rightarrow density height$
- fi: frequency
- n: sample size
 - $P(A) \ge 0$
 - P(S) = 1
 - Mutually Exclusive Events
 - $P(A1UA2U\cdots)=P(A1)+P(A2)+\cdots$
- nPr=n! / (n-r)!
- nCr=n! / r! * (n-r)!
- MR (Multiplication Rule)
 - $P(A \cap B) = P(A \mid B) \times P(B)$
 - $P(A \cap B) = P(B \mid A) \times P(A)$
- **EMR**
 - $P(A \cap B \cap C) = P((A \cap B) \mid C) \times P(C \mid (A \cap B)) \times P(A \cap B)$
 - $P(A \cap B) = P(B \mid A) \times P(A)$
- $P(A \cap B \cap C) = P((A \cap B) \mid C) \times P(C \mid (A \cap B)) \times P(B \mid A) \times P(A)$ 0
- **VENN**
 - $P(A_1 \cap B) \cup P(A_2 \cap B) \cup \dots P(A_k \cap B)$ 0 P(B)
- ME

$$\frac{P(A_1 \cap B) + P(A_2 \cap B) + \cdots P(A_k \cap B)}{P(B)}$$

CP

$$\circ$$
 $P(A_1 \mid B) + P(A_2 \mid B) + \dots P(A_k \mid B)$
Independent Events

0

0

- $P(A \cap B) = P(A) \times P(B)$
- Conditional Probability

$$O \qquad P(T^+ \mid D) = \frac{N(T + \cap D)/N(S)}{N(D)/N(S)}$$

- $P(T^+ \mid D) \neq P(D \mid T^+)$
- $P(A \mid B) = \frac{P(A \cap B)}{P(B)} != P(c \mid X) = \frac{p(x \mid c) p(c)}{p(x) \rightarrow total \ demek}$
- Hyper Geometric Distribution

o P (X = x) = f(x) =
$$\frac{\binom{m}{x}\binom{N-m}{n-x}}{\binom{N}{n}}$$

- select n items without replacement from a set of N items
- m of the items are of one type 0
- and N m of the items are of a second type
- Expected Value & Variance & Standard Deviation
 - E(X) = 3(0.3) + 4(0.4) + 5(0.3) = 4
 - E(Y) = 1(0.4) + 2(0.1) + 6(0.3) + 8(0.2) = 4
 - $\sigma = E(\mu(x)) = E((X \mu)^2) \rightarrow \text{Standard Deviation}$
 - $\sigma^2 = E(\mu(x)) = E((X \mu)^2) \rightarrow \text{Variance} = \sqrt{\sigma^2}$

3-) Bayes & Naïve Bayes

Bayesian Rule

$$P(c \mid \mathbf{X}) = \frac{p(x \mid c) \, p(c)}{p(x)} = Posterior = \frac{likelihood \times prior}{evidence} = \frac{joint}{normalizer}$$

$$\bigcirc \quad \text{Updates the probability of an event}$$

- - Based new evidence
- Run Out Of Space & Time (modelling problem) Tons Of Data (modelling problem)
- Learning Joint Probability is infeasible (modelling problem)
- Posterior Probability ($P(\omega_j/x)$)
 - o hypothesis is true or not in the light of relevant observations
- Joint Probability
 - o $\mathbf{x} = (x_1, x_2), P(\mathbf{x}) = P(x_1, x_2)$
 - $P(x_1, x_2) = P(x_2|x_1)P(x_1) = P(x_1|x_2)P(x_2)$
 - $P(C,x) = P(x|C)P(C) \rightarrow Joint Probability$
 - $P(\neg C, x) = P(x|\neg C)P(\neg C) \rightarrow Joint Probability$
 - Sensitivity: "", Specificity: "¬" {Maximum A Posterior}
- Normalized Histogram (3-1 Page 21, 3-2 Page 8)
 - $P(x) = P(C, x) + P(\neg C, x)$

 - Total or Evidence 0
- Posterior

$$P(C \mid x) = \frac{P(C, x)}{Normalizer}$$

$$P(C \mid x) = \frac{P(C, x)}{P(\neg C, x)}$$

- $P(\neg C \mid x) = \frac{P(\neg C, x)}{Normalizer}$
- $P(C) \rightarrow Prior$ \circ
 - $P(Pos \mid C) \rightarrow Sensitivity$
- $P(Neg \mid \neg C) \rightarrow Specificity$

Naïve Bayes Normal Distribution (independent →y)

$$\hat{P}(x_j|c_i) = \frac{1}{\sqrt{2\pi}\sigma_{ji}} exp\left(-\frac{(x_j - \mu_{ji})^2}{2\sigma_{ji}^2}\right)$$

 μ_{ii} : mean (avearage) of feature values x_i of examples for which $c = c_i$ σ_{ji} : standard deviation of feature values x_j of examples for which $c = c_i$

$$\mu = \frac{1}{N} \sum_{n=1}^{N} x_n, \quad \sigma^2 = \frac{1}{N} \sum_{n=1}^{N} (x_n - \mu)^2$$
KNN 8 Pagrassian

4-) KNN & Regression

$$L_p(\mathbf{x}, \mathbf{y}) = \left(\sum_{i=1}^{d} |\mathbf{x}_i - \mathbf{y}_i|^p\right)^{1/p} L_2(\mathbf{x}, \mathbf{y}) = \left(\sum_{i=1}^{d} |\mathbf{x}_i - \mathbf{y}_i|^2\right)^{1/2} L_1(\mathbf{x}, \mathbf{y}) = \sum_{i=1}^{d} |\mathbf{x}_i - \mathbf{y}_i|$$

- Lp Norm(Minkowski), Euclidian Distance, Manhattan Distance
- y = mx + b (y \rightarrow dependent & x \rightarrow independent)
- $y = mx*b_1 + b_0$
- $Q = \sum_{i=1}^{n} (yi \hat{y}_i)^2 \rightarrow \text{Square Error}$
- Regression Line
- $\hat{y} = b_0 + b_1 x$
- Sum of Squared Errors Point Estimation of Mean
- $SSE = \sum_{i=1}^{n} (y_i \hat{y}_i)^2 = \sum_{i=1}^{n} (y b_0 b_1 x)^2$ $n = 10 \quad \sum_{i=1}^{n} x = 564 \quad \sum_{i=1}^{n} x^2 = 32604$
- $\sum y = 14365$ $\sum xy = 818755$
- $b_1 = \frac{n\sum xy \sum x\sum y}{n\sum x^2 (\sum x)^2} = 10.8$
- $b_0 = \frac{\hat{y}}{n} b_1 \frac{x}{n}$
- $b_0 = 1436.5 10.8(56.4) = 828$
- $cov(x,y) = \frac{\sum_{i=1}^{n} (x_i \bar{X})(y_i \bar{Y})}{n}$ (relation whenever one changes)
- $\sum_{i=1}^{n} (x_i \bar{X})(y_i \bar{Y})$
- $\hat{r} = \frac{cov \, ariance(x,y)}{=} -$ (Relative strength) $\sqrt{var x} \sqrt{var y}$
- $\hat{\beta} = \frac{cov(x,y)}{}$ Var(x)
- Intercept = Calculate: $\bar{\alpha} = \bar{y} \hat{\beta}\bar{x}$
- $\hat{r} = \hat{\beta} \frac{\dot{S}D_{\chi}}{SD_{\chi}}$
- $e_i = Y_i \hat{Y}_i \rightarrow \text{Residual} = \text{Observed} \text{Predicted}$
- Observed = Real Dot (Ground Root)
- Predicted = Value of Y in Line Correspond to X
- $s_{y.x}^2 = \frac{1}{n-2} \sum e_i^2 = \frac{1}{n-2} \sum (y_i \hat{y}_i)^2$

5-) Clustering & PCA

Euclidian, Manhattan, Infinity

$$d(\mathbf{x}, \mathbf{y}) = \sqrt{\sum_{i=1}^{d} (x_i - y_i)^2} \qquad d(\mathbf{x}, \mathbf{y}) = |\mathbf{x} - \mathbf{y}| = \sum_{i=1}^{d} |x_i - y_i| \qquad d(\mathbf{x}, \mathbf{y}) = \max_{1 \le i \le d} |x_i - y_i|$$

- K-Means: Initial Centre Distance Matrix -
 - Object Clustering New Centre Distance
 - Matrix Object Clustering New Centre -
- Recompute Until No Change

6-) Decision Tree & Linear Classification

- $\begin{aligned} &Entropy(S) = -p_{+}\log_{2}p_{+} p_{-}\log_{2}p_{-} \\ &H(Y) = -\sum_{i=1}^{k} P(Y = y_{i})\log_{2} P(Y = y_{i}) \\ &H(Y \mid X) = -\sum_{j=1}^{k} P(X = x_{j}) \sum_{i=1}^{k} P(Y = y_{i} \mid X = x_{j})\log_{2} P(Y = y_{i} \mid X = x_{j}) \end{aligned}$
 - x = true iken y'nin true ve false olma olasılıklarını topla
 - x = false iken y'nin true ve false olma olasılıklarını topla
 - iki toplamında eksisini al dıştan
- $IG(X_i) = H(Y) \dot{H}(Y \mid X_i)$ $\operatorname{argmax} IG(X_i) = \operatorname{argmax} H(Y) - H(Y \mid X_i)$
- $H(Y \mid X:t) = P(X < t)H(Y \mid X < t) + P(X \ge t)H(Y \mid X \ge t)$
- $IG(Y \mid X:t) = H(Y) H(Y \mid X:t)$
- $IG^{\bullet}(Y \mid X) = max_{t}IG(Y \mid X:t)$
- $E = \frac{1}{2}(y f(\sum w_i x_i))^2$
- $\mathbf{w}_{j}^{r}(\text{ new }) = \mathbf{w}_{j}^{r}(\text{ old }) \mu \sum_{i=1}^{N} \frac{\partial \varepsilon(i)}{\partial \mathbf{w}_{j}^{r}} \text{ where } \frac{\partial \varepsilon(i)}{\partial \mathbf{w}_{j}^{r}} = \delta_{j}^{r}(i)\mathbf{y}^{r-1}(i) = \textit{Batch Learning}$
- $\mathbf{w}_{j}^{r}(\text{ new }) = \mathbf{w}_{j}^{r}(\text{ old }) \mu \frac{\partial \varepsilon(i)}{\partial \mathbf{w}_{i}^{r}} \text{ where } \frac{\partial \varepsilon(i)}{\partial \mathbf{w}_{i}^{r}} = \delta_{j}^{r}(i)\mathbf{y}^{r-1}(i) = \textit{Online Learning}$

3-) Bayes & Naïve Bayes

- Zero Conditional Probability
- $\hat{P}(a_{jk}|c_i) = \frac{n_c + mp}{n_c}$
- n_c : number of training examples for which $x_j = a_{jk}$ and $c = c_i$ n: number of training examples for which $c = c_i$
- p: prior estimate (usually, p = 1/t for t possible values of x_i) m: weight to prior (number of "virtual" examples, $m \ge 1$)

```
7-) SVM
        f(x) = w^T x_i + w_0 , (w_0 = bias), bias corresponds to the output of an CNN when it has zero input
        Cycle Through \{x,y\}
        If x is misclassified w \leftarrow w + \alpha sign(f(x))x
        Continue Until Data is Correctly Classified
       Linear SVM
       f(x) = \sum_{i} \alpha_i x_i \left( x_i^T x \right) + b
r = \frac{w x_i + b}{\|w\|} \text{ where } \|w\| = \sqrt{w_1^2 + \dots + w_n^2}
        margin = \frac{2}{\|w\|} \rightarrow minimize weight vector, it will maximize margin
        wx_i + b \ge 1 \ if \ y_i = +1
                                             wx_i + b \le 1 if y_i = -1
        y_i(wx_i + b) \ge 1) for all i
        \varphi = \frac{1}{2}(w^t w), find unique minimum by using training data
        rac{1}{2} w * w + C \sum_{k=1}^R arepsilon_k C is the Slack Variables
        \max(0,1-yif(xi)) uses hinge loss approximates 0-1 loss
        Small C Allows constraints easily ignored → Large Margin – Wider (Soft) (c=1 e.g.)
        Large C Allows constraints hard to ignored \rightarrow Narrow Margin (100) – Close to Hard (c=100) Infinite C enforces all constraints \rightarrow Hard Margin (c=\infty)
              Linear SVM'de W Vektörünü ve S Değişkenlerini minimize edecek çözüm aradım.
Non-Linear SVM'de higher dimension yapıyorum. (Polar Coordinates + Higher dimension)
             \varphi(\chi_2^{\chi_1}) \rightarrow \binom{r}{\theta} R^2 \rightarrow R^2
             f(x) = w^T x_i + w_0 \rightarrow f(x) = w^T \boldsymbol{\varphi}(x) + b
             Classifier: f(x) = w^T \varphi(x) + b
             RBF SVM
                     0 	 f(x) = \sum_{i} \alpha_{i} y_{i} exp(-\|x - x_{i}\|^{2}/2\sigma^{2}) + b
                            \sigma \rightarrow Seperate Data

    Hyper Parameter for Slack Variable
    Decide our data by C & σ

                           Decrease \sigma , it moves towards NN Classifie
              Kernel Trick : Classifier can be learnt and applied without explicitly compute oldsymbol{arphi}
                            RBF
                   0
9-) Deep Learning
     f(x, W) = Wx
     L_i = \sum_{j \neq y_i} max \left( 0, s_j - s_{y_i} + 1 \right)
                     \circ s_j \rightarrow Others
                    \circ \quad s_{y_i} \to Target
   L_i = \frac{1}{N} \sum_{i=1}^{N} L_i
    MSE, Quadratic, L2 = \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{n}
     Mean Absolute Error, L1 = \sum_{i=1}^{n} |y_i - \hat{y}_i|
     \text{Mean Bias Error} = \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)}{n}
      Cross Entropy Loss = -(y_i \log(\hat{y}_i) + (1 - y_i) \log(1 - \hat{y}_i))
     Activations Functions: Sigmoid, tanh, ReLU, LReLU, Maxout, ELU
                          \sigma(x) = \frac{1}{1 - e^{-x}}
                     0
                     0
                           tanh (x)
                     0
                           max (0, x)
                           \max(0.1x.x)
                     0
                           f[n,m] * h[n,m] = \sum_{k=-\infty}^{\infty} \sum_{l=-\infty}^{\infty} f[k,l]h[n-k,m-l]
             Details of CNN
                            Output Size:
                                          O: (N-F)/Stride + 1
                                          N - Input Size
                                          F - Frame Size
                                          The O value can't be float.
                            Generally, Output Sizes
                                          Stride: 1
                                          Filters: FxF
                                          Zero Padding with: (F-1)/2
                                                        Will preserve size stability
                                                        F= 3 → P=1
                                                        F= 5 → P=2
                                                        F= 7 → P=3
                            Output Volume Size:
                                          OVS: (N+2*P-F)/Stride+1
                                          2 is double sided padding coefficient
                            Output Volume:
                                          OV: OVS x OVS x Feature_Size
                            Number of Parameters:
                                          Each Filter Has Parameters: F * F * Input_Depth + Bias
                                          Total → NOP: Parameters * Feature_Size(new)
```

- NOP: Parameters * Feature_Size -poolingde degisim olmaz
- Bias: 0 or +1
- Pooling Layers doesn't consist parameters

Summary

- $\bullet W_1 * H_1 * D_1$
- K: Number of Filter
- F: Spatial Extent
- S: Stride
- P: Amount of Zero Padding
- $W_2 * H_2 * D_2$
- $W_2 = (W_1 F + 2P)/S + 1 W_2 = (W_1 F)/S + 1$
- $H_2 = (H_1 F + 2P)/S + 1_{H_2} = (H_1 F)/S + 1$
- $D_2 = K D_2 = D_1$