

1> Write the formula for computing a two's complement number representation. (3)

$$2^n \text{Neg } n+1$$

2> Describe the implementation of two's complement number representation. (3)

you take the binary number  
and flip the 1's to 0's  
and 0's to 1's, Once that's  
done add 1 to the new number.

The purpose of this is to make  
representing signed integers.

3> Write the (entire) list (in both binary and decimal) signed integers, using 2's complement numbers to represent negative numbers, given a four bit cell. (8)

Decimal	Binary
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

4> Write the polynomial representation of 31047 octal: (5)

$$3 \cdot 8^4 + 1 \cdot 8^3 + 0 \cdot 8^2 + 4 \cdot 8^1 + 7 \cdot 8^0$$

5> In a 9 bit cell what is the range of values, binary and decimal, that can be stored in an unsigned representation. (5)

Decimal: 511 to 0

Binary: 11111111 to 0000 0000

6> In a 9 bit cell what is the range of values, binary and decimal, that can be stored in a signed representation, assuming 2's complement? (5)

Decimal: 255 to -256

Binary: 01111111 to 110000 0000

7> List and briefly define the three flow of control methods used in programming: (12)

1. Selection - will only run if a condition is met
2. repetition - will repeat as long as condition is met
3. Recursion - solving a problem by reducing it to smaller versions of itself

8> Perform the following operations, assuming seven bit two's complement representation and show the values of the status bits after the operation is complete. (4)

$$\begin{array}{r} 011\ 0100 \quad N = 1 \\ \text{ADD } 010\ 0110 \\ \hline 101\ 1010 \end{array} \quad Z = 0 \quad V = 1 \quad C = 0$$

a) Describe and diagram the internal form of an 8-bit floating point number which uses 1 bit for the sign and three for the exponent. Make sure you not only label, but also explain how the value is determined.

$$\begin{array}{r} 100\ 1001 \quad N = 1 \\ \text{ADD } 000\ 1100 \\ \hline 101\ 0101 \end{array} \quad Z = 0 \quad V = 1 \quad C = 0$$

9&gt; Convert from decimal to binary: (4)

3.09375

11.

11.00011

0.09375

-0.06250

0.03125

-0.03125

0

0.68

0.1010110000

0

$$\begin{array}{r} 0.02375 \\ - 0.015625 \\ \hline 0.008125 \\ - 0.0078125 \\ \hline 0.0003125 \end{array}$$

0.68

-0.50

0.18

-0.125

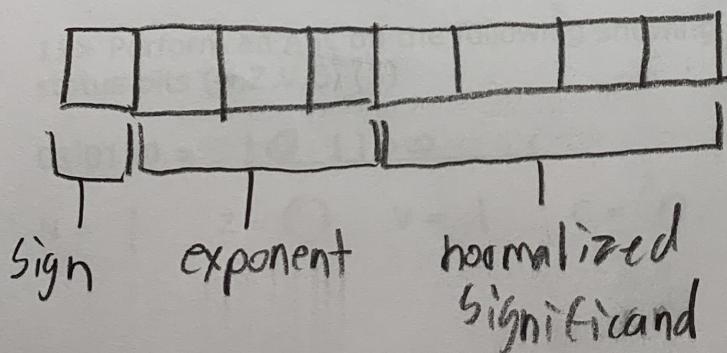
0.05500

-0.03125

0.02375

10&gt; (a-8;b-4;c-4)

a) Describe and diagram the internal form of an 8-bit floating point number which uses 1 bit for the sign and three for the exponent. Make sure you not only label, but also explain how the value is determined.



sign - determined by whether the number is negative or not

exponent - determined by what exponent the number uses

normalized significand - determined by the exponent minus 3 in binary

b) Represent the following value (base 10) in the format from a) using excess 3: -12.5

$$\begin{array}{r} 12 \quad 1100 \\ -12 \quad 0011 \\ + \quad \underline{0100} \\ 0001 \end{array}$$

$$\begin{array}{r} 0.5 \\ -0.5 \\ \hline 0 \end{array}$$

c) repeat b with this value (base 10): 0.03125

$$\begin{array}{r} 0.03125 \\ -0.3125 \\ \hline 0 \end{array}$$

$$0.00001$$

11> Perform an ASL on the following showing the bit setting for the status bits (N,Z,V,C) (5)

$$01\ 0110 = \underline{010}\ 1100$$

$$N = | \quad Z = 0 \quad V = 1 \quad C = 0$$

12> Perform an ASR on the following showing the bit setting for the status bits (N,Z,V,C) (5)

$$\underbrace{11\ 0101}_{\leftarrow} = \underline{\underline{11\ 1010}}$$

N = 1    Z = 0    V = 0    C = 1

DR: 0101100  
SR: 1101010  
N = 1  
Z = 0

13> Perform an ROL on the following showing the bit setting the carry bit after the operation, given the carry bit setting before the operation. (5)

$$C = 1 \text{ ROL } 01\ 1101 = \underline{\underline{11\ 1011}} \quad C = 0$$

14> Perform an ROR on the following showing the bit setting the carry bit after the operation, given the carry bit setting before the operation. (5)

$$C = 1 \text{ ROR } 01\ 1101 = \underline{\underline{10\ 1110}} \quad C = 1$$

15> Perform the following logical operations, assuming a seven-bit cell: (9)

$$\begin{array}{r} 010\ 1100 \\ \text{AND} \quad 110\ 1010 \\ \hline 010\ 1000 \end{array}$$

$$\begin{array}{l} N = 0 \\ Z = 0 \end{array}$$

$$\begin{array}{r} 010\ 1100 \\ \text{OR} \quad 110\ 1010 \\ \hline 110\ 1110 \end{array}$$

$$\begin{array}{l} N = 1 \\ Z = 0 \end{array}$$

$$\begin{array}{r} 010\ 1100 \\ \text{XOR} \quad 110\ 1010 \\ \hline 011\ 1001 \end{array}$$

$$\begin{array}{l} N = 0 \\ Z = 0 \end{array}$$

f. 722

$$\begin{array}{r} 110 \\ \underline{-16} \\ 94 \\ \underline{-16} \\ 78 \\ \underline{-16} \\ 62 \\ \underline{-16} \\ 46 \\ \underline{-16} \\ 30 \\ \underline{-16} \\ 14 \end{array}$$

$\frac{110}{16}$

$\frac{16}{94}$

$\frac{16}{190}$

$\frac{16}{78}$

$\frac{16}{174}$

$\frac{16}{62}$

$\frac{16}{158}$

$\frac{16}{-16}$

$\frac{16}{142}$

$\frac{16}{16}$

$\frac{16}{126}$

16> Show the representations of the following **unsigned** numbers in the indicated base. (6)

a)  $1011\ 1101_2$  in base 10

$$189$$

b)  $F7_{16}$  in base 2

$$1111\ 0111$$

c)  $1433_{10}$  in base 16

$$599$$

d)  $BA2_{16}$  in base 10

$$2478$$

e)  $512_{10}$  in base 2

$$100000000000$$

f)  $1101\ 1110_2$  in base 16

$$DE$$

f. 14

$\frac{1}{13}$

$\frac{1}{12}$

$\frac{1}{11}$

$\frac{1}{10}$

$\frac{1}{9}$

$\frac{1}{8}$

$\frac{1}{7}$

$\frac{1}{6}$

$\frac{1}{5}$

$\frac{1}{4}$

$\frac{1}{3}$

$\frac{1}{2}$

a.  $1011\ 1101$

b.  $F7$

$$11110111$$

c.  $1433$

$$- 256$$

$$\hline 1177$$

$$- 256$$

$$\hline 921$$

$$- 256$$

$$\hline 665$$

$$- 256$$

$$\hline 409$$

$$- 256$$

$$\hline 153$$

$$- 16$$

$$\hline 137$$

$$- 16$$

$$\hline 121$$

$$- 16$$

$$\hline 105$$

$$- 16$$

$$\hline 1$$

d.  $BA2$

$$\begin{array}{r} 128 \\ 64 \\ 16 \\ 8 \\ 4 \\ + 1 \\ \hline 189 \end{array}$$

$$+ 1$$

$$\hline 722$$

$$(256 \cdot 11) + (16 \cdot 15) + (1 \cdot 2)$$

$$= 2478$$