

✓ Assignment 3.2 Practice Problem 2 (Split the Bill)

Problem

In the Splitwise app, people form groups and add the expenses of members of the group. This is especially useful for vacations, where people traveling in a group can maintain an account of their expenses and who paid the bills.

All people in the group are assigned distinct IDs between 1 and N, where N is the size of the group.

In addition to keeping a record of the expenditure, Splitwise also calculates the list of shortest-path transfers (defined later) that will settle up all dues.

Each transaction has the following parameters:

- transaction_id - It is a string representing the unique ID by which the transaction is identified.
- paid_by - It is a list of lists, where each element of the list is another list having the form [x, y]. Here, x and y denote that person having ID x paid Rs. y.
- split_as - It is a list of lists, where each element of the list is another list having the form [x, y]. Here, x and y denote that after all dues are settled, a person having ID x will ultimately contribute Rs. y to the transaction.

For any given transaction, the following condition holds true:-

Total_Amt_Paid = Sum_of_all_splits

In other words, the sum total of all amounts in list paid_by equals the sum total of all amounts in list split_as.

Following is the example of a transaction in a group of size N=64:-

- transaction_id : "#f1230"
- paid_by : [[1, 30], [4, 100], [63, 320]]
- split_as : [[1, 120], [2, 20], [3, 40], [4, 40], [37, 100], [51, 40], [53, 90]]

Shortest-Path Transfers: Shortest-path transfers lead to a reduction in the number of transfers.

Specifically, for a group having multiple transactions, the shortest-path transfers will be a list of payments to be made such that:-

- Each payment can be represented by a list of the following form:- [payer_id, payee_id, amount]. There is only 1 payer, and 1 payee in each payment, which are distinct from each other. So, payer_id != payee_id, for any payment.
- Each person (out of the N people) can only either be the payer (in all payments involving him), or the payee, but not both.
- The total amount of money that each person should receive/spend, must be equal to the total amount he would receive/spend according to the given list of transactions. Clearly, there can be several shortest-path transfers for a particular list of transactions.

Specifically, the lexicographically smallest shortest path has the following:-

- Arrange people who have borrowed money in ascending order of their IDs. Do the same for people who have lent money.
- Now, construct payments so that the least borrower ID has to pay the least lender ID. Continue this process, till all debts have been settled.

Task

Given N members in a group, and lists representing the transactions(expenses), print the payments involved in the lexicographically smallest shortest-path transfers for the group.

Example

Input:

- N = 4
- 5 transactions, that can be represented as follows:-
transaction_id = "#a1234", paid_by = [[1, 60]], split_as = [[2, 60]].
transaction_id = "#a2142", paid_by = [[2, 40]], split_as = [[3, 40]].
transaction_id = "#b3310", paid_by = [[3, 30]], split_as = [[4, 30]].
transaction_id = "#b2211", paid_by = [[4, 30]], split_as = [[3, 30]].
transaction_id = "#f1210", paid_by = [[3, 20]], split_as = [[1, 20]].

Output:

- 2 payments (of the form [payer_id, payee_id, amount]) are to be made, represented by the list:-
 - [[1, 2, 20], [1, 3, 20]]

Approach:

- The given list of payments satisfies all three necessary conditions. Hence, it is a Shortest-Path Transfer.

Function description

Complete the function solve. This function takes the following 2 parameters and returns the required answer:

- N: An integer, representing the number of people in the group.
- transaction_list: A list (vector) of transactions. Each transaction is a dictionary, having keys “transaction_id”, “paid_by” and “split_as”. (The contents of each transaction are explained above)

Input format

Note: This is the input format that you must use to provide custom input (available above the Compile and Test button).

- The first line contains two space-separated integers N and M, the number of people in the group, and the number of transactions recorded.
- The next lines describe the M transactions as follows:-
- Each new transaction begins from a new line.
- The first line of each transaction contains a string, representing the transaction_id of the transaction.
- The 2nd line of each transaction contains 2 space-separated integers n_payers and n_splits.
- n_payers denotes the number of people in the paid_by list. n_splits denotes the number of people in the split_as list.
- The next n_payers lines contain two space-separated integers, the payer and the amount paid.
- The next n_splits lines contain two space-separated integers, the borrower and the amount borrowed.

Output format

Print the answer in the given format.

- In the first line, print a single integer K, denoting the number of payments involved in the Shortest Path Transfer.

- The next K lines should represent the K payments. Each payment should be printed in a single line as 3 space-separated integers payer_id, payee_id, and amount. Here, payer_id is the ID of the person who needs to pay the amount of money to the person with ID payee_id.

Constraints

- $2 \leq N \leq 2 * 10^5$
- $1 \leq M \leq 5000$
- $1 \leq len(transaction[i][paid_by]) + len(transaction[i][split_as]) \leq 50$
- $1 \leq total_money_exchanged_in_each_transaction \leq 10^7$

*SAMPLE *

Input	Output
<pre>6 5 #itsmylife 2 3 1 25 3 15 4 10 5 25 6 5 #itsnow 1 4 4 100 1 25 2 25 3 25 4 25 #ornever 2 2 5 30 3 10 1 25 4 15 #iaintgonna 1 3 2 150 1 50 2 50 3 50 #liveforever 2 2 5 13 6 25 4 25 1 13</pre>	<pre>1 2 75 1 4 13 3 4 12 3 5 18 3 6 20</pre>

ANSWER

- for this problem, i suppose that i can solve it by creating a dictionary. But since we aim for an optimized solution, I think the use of arrays are cool.
- Using the sample input/output as a guide. I think the implementation of graphs are not really needed but since this problem is a set of ordered pairs, this can be theoretically a representation of graphs

ALGORITHM

START

1. Get user Input for Transaction ID
 2. Get the User input for payer and payee
 3. split the the string inputs
 4. transform to be int
 5. Create balance array
 6. edit the Balance array per iterations
 7. Make the values inside the array 0 --> (HOW??)
 8. Present Output
- END

- With this guided now so algo we can create an pseudocode

PSEUDOCODE

user input --> numberOfPeople, numberOfTransactions

balance[base of noOfPeople]

- loop through numberOfTransactions
 - input transactionID
 - input noOfPayer, noOfPayee
 - input peopleId, price
 - if payer, add to balance
 - if payee, negate to balance
- loop through balance[]
 - if positive number
 - make it zero by adding negative numbers in the balance[]
- print result

✓ CODING

- with that we can do some codes. this line allows the user for double integer inputs that seperated with whitespace

```
1 group , transactions = input().split()

6 5
```

- For the recording/noting purposes I include a dictionary that shows the transaction data neatly

```
1 dictTransactions = {} # for recording/representation purposes
```

- Based on the number of members of the group, I made a Balance array. this will be useful for tracking the money lent(positive) and the money need to be paid(negative)

```
1 balance = [0 for i in range(int(group))] # for storing balances in just one array
```

- This part of the asks for the inputs of the following: Transaction ID(string), number of payers and payees (both integers), id's of the payer or payees and their corresponding price of their contribution(which also the integers processed to balance array).

```
1 for i in range(int(transactions)):
2     transacID = input() # The transaction ID
3     dictTransactions[transacID] = [["paid_by"], ["split_by"]] # added for representation purposes
4     payers, payees = input().split()
5
6     for k in range(int(payers)):
7         payerId, price1 = input().split() # The transaction ID
8         dictTransactions[transacID][0].append([payerId, price1]) # added for representation purposes
9         balance[int(payerId)-1] += int(price1)
10
11     for l in range(int(payees)):
12         payeeId, price2 = input().split()
13         dictTransactions[transacID][1].append([payeeId, price2]) # added for representation purposes
14         balance[int(payeeId)-1] -= int(price2)
```

```
#NeverGonnaGiveyouUp
2 3
1 25
3 15
4 10
5 25
6 5
#NeverGonnaLetYouDown
1 4
4 100
1 25
2 25
3 25
4 25
#NeverGonnaRunAround
2 2
5 30
3 10
1 25
```

```
4 15
#AndDessertYou
1 3
2 150
1 50
  2 50
3 50
# NeverGonnaMakeYouCry
2 2
5 13
6 25
4 25
1 13
```

- Lets check the transactions first:

```
1 print(dictTransactions)

{'#NeverGonnaGiveyouUp': [['paid_by', ['1', '25']], ['3', '15']], ['split_by', ['4', '10'], ['5', '25'], ['6', '5']]], '#NeverGonnaLetYouDown': [['paid_by', ['4', '100']], ['split_by', ['1', '25'], ['2', '25'], ['3', '15']]]}
```

✓ LOGIC FOR THE BALANCE ARRAY

- Recall of the balance array, this array uses its index to record the price the members lent or paid

noOfPeople = 6

BALANCE = [0, 0, 0, 0, 0, 0]

0 1 2 3 4 5 ← ID - 1

- for example, if id=1 is the one who pays, index 0 (since id - 1) will have an additional price

If id = 1 paid 100:

BALANCE = [100, 0, 0, 0, 0, 0]

0 1 2 3 4 5 ← ID - 1

- but if the id/person is one of the one who split, it will be negated in the array

If id = 6 split 100:

BALANCE = [100, 0, 0, 0, 0, -100]

0 1 2 3 4 5

- With these we can easily record the prices in Faster way.For reference,we can see here the balance array after n iterations.

```
1 print(balance)

[-88, 75, -50, 25, 18, 20]
```

✓ Lexicographically Smallest Shortest Path

- ths section process the balance array and record the processes for the output showing the shortest way to pay all the balance.

Finding the positive number , use the negative numbers to make it equal to 0

BALANCE = [-88, 75, -50, 25, 18, 20]

0 1 2 3 4 5

remaining negative numbers will
be used until it is zero

-13

75 to 0 means it is paid

Record every movement and payment

index + 1 = ID

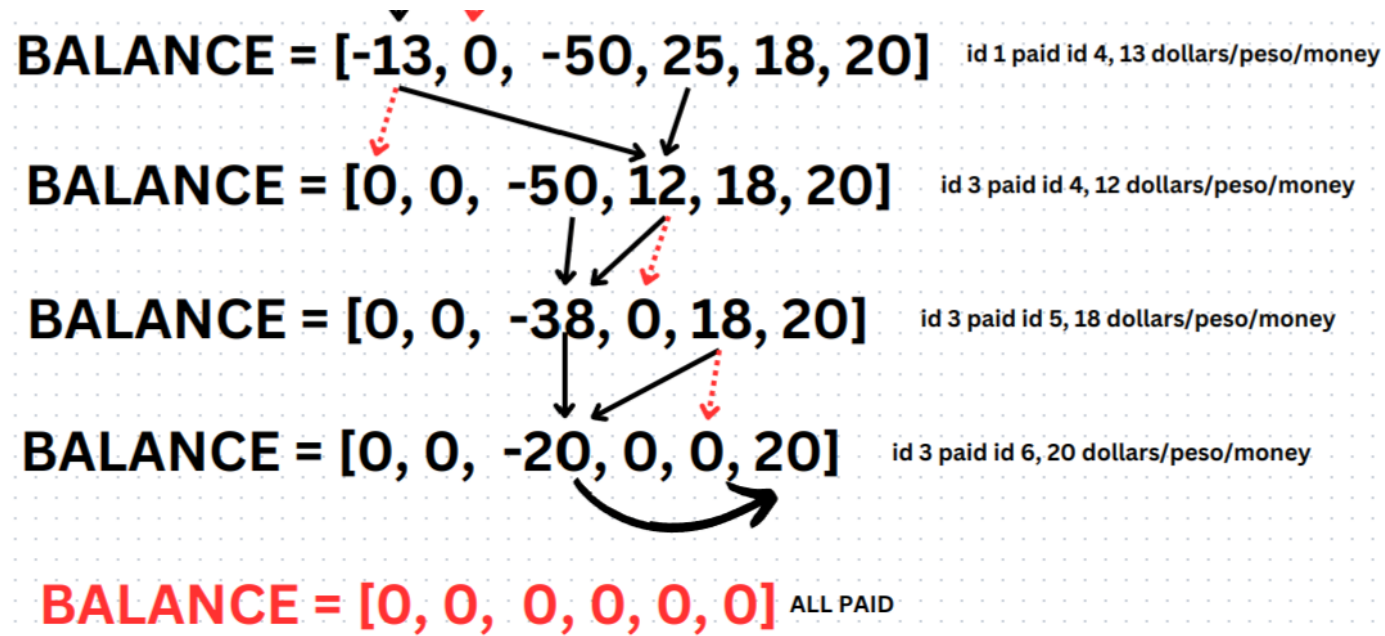
so id 1 paid id 2, 75 dollars/peso/money

BALANCE = [-13, 0, -50, 25, 18, 20]

- this representation how the balance array is processed.

✓ ALGORITHM:

1. FIND POSITIVE NUM
2. FIND NEGATIVE NUM
3. ADD NEGATIVE TO POSITIVE NUM
4. RECORD
5. REPEAT 3
6. IF POSITIVE NUM = 0:
7. BACK TO 1



- If balance array elements are all 0 again, then all are paid.

```
1 # CODE
2 answer = []
3 for bal in range(len(balance)):
4     index = 0
5     if balance[bal] > 0: # gets only positives
6         while balance[bal] != 0:
7             if index == bal: # disregards same index
8                 index += 1
9                 continue
10            if balance[index] < 0:
11                min_balance = min(balance[bal], abs(balance[index]))
12                balance[bal] -= min_balance
13                balance[index] += min_balance
14                answer.append([index+1, bal+1, min_balance])
15            index += 1
```


▼ **OUTPUT**

```
id 1 paid id 2, 75 dollars/peso/money
```

```
id 1 paid id 4, 13 dollars/peso/money
```

```
id 3 paid id 4, 12 dollars/peso/money
```

```
id 3 paid id 5, 18 dollars/peso/money
```

```
id 3 paid id 6, 20 dollars/peso/money
```

```
1 print(answer)

   [[1, 2, 75], [1, 4, 13], [3, 4, 12], [3, 5, 18], [3, 6, 20]]

1 for i in answer: # SAME FOR THE REQUIRED OUTPUT
2   for j in i:
3     print(j, end = " ")
4   print()

   1 2 75
   1 4 13
   3 4 12
   3 5 18
   3 6 20
```

END