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Practical 2

Aim:- Basics of R Software

- 1) R is a software for Statistical analysis & Data computing
- 2) It is an effective data handling Software outcome storage is possible
- 3) It is capable of graphical display
- 4) It is a free Software

Q1) Solve the following

$$4+6+8 \div 2 - 5$$

$$4+6+8/2 - 5$$

[2] 9



2)

$$2^0 + 1 - 3 + \sqrt{45}$$

$$2^0 + 1 - 3 + \sqrt{45} = (-3) + \sqrt{45}$$

[2] 13.7082

3)

$$5^3 + 7 \times 5 \times 8 + 46/5$$

$$5^3 + 7 \times 5 \times 8 + 46/5 = 125 + 280 + 9.2$$

[2] 414.2

$$1) \sqrt{4x^2 + 9x^3 + 7x^6}$$
$$\text{sqrt}(4x^2 + 9x^3 + 7x^6)$$
$$[1] 5 \cdot 671567$$

$$\text{round off}$$
$$46 \div 7 + 9 \times 8$$

$$\text{round}(46 \div 7 + 9 \times 8)$$
$$[1] 79$$

$$2) \text{cc}((2,3,5,7)) * 2$$
$$[1] 4, 6, 10, 14$$

$$\text{cc}((2,3,5,7)) * \text{cc}((2,3,6,2))$$
$$[1] 4, 9, 30, 14$$

$$\text{cc}((2,3,5,7))^2$$
$$[1] 4 \quad 9 \quad 25 \quad 49$$

$$\text{cc}((5,2,7,5)) / \text{cc}((4,5))$$
$$[1] 1.90 \quad 0.40 \quad 1.75 \quad 1.00$$

$$3) \text{if } x=20 \rightarrow y=30 \rightarrow z=1$$
$$\text{if } x^2 + y^3 + z$$

$$[1] 27402$$
$$\text{sqrt}(x^2 + y^3 + z)$$

$$[1] 20.73644$$

$$\text{if } x^2 + y^2$$

1.7 .0 - .

$$\rightarrow \text{cc}((2,3,5,7)) * \text{cc}((5,2,3))$$
$$[1] 4 \cdot 9 \cdot 1021$$

$$\rightarrow \text{cc}((1,6,2,3)) * \text{cc}((-2,-3,-4,-1))$$
$$[1] -2, -18, -8, -3$$
$$\text{cc}((4,6,8,9,4,5)) * \text{cc}((1,1,3))$$
$$[1] 4 \cdot 36 \cdot 512 \cdot 918 \cdot 125$$

✓

Q4) `> x <- matrix(x, nrow = 4, ncol = 2, data = c(1, 2, 3, 4, 5, 6, 7, 8))`

`x`

[1,1]	[1,2]
[2,1]	[2,2]
[3,1]	[3,2]
[4,1]	[4,2]

Q5) Find $x+y$ and $2x+3y$ where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$

 $y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$

`> x <- matrix(x, nrow = 3, ncol = 3, data = c(4, 7, 9, 10, 12, 15))`

`> x[,1] [,2] [,3]`

[1,1]	4	-2	6
[2,1]	7	0	7
[3,1]	9	-5	3

`> t <- matrix(t, nrow = 3, ncol = 3, data = c(10, 12, 15, 11, 13, 16))`

`> y [,1] [,2] [,3]`

[1,1]	10	-5	7
[2,1]	12	-4	9
[3,1]	15	6	5

`> x + t [,1] [,2] [,3]`

[1,1]	14	-3	13
[2,1]	19	-4	16
[3,1]	24	-11	8

Marks of Statistics of CS Batch B

$x = c(58, 35, 20, 24, 34, 96, 56, 55, 54, 27, 12, 24, 47, 19, 54, 40, 50, 36, 29, 35, 39)$

$\triangleright x = c(\text{data})$

$\triangleright \text{breaks} = \text{seq}(20, 60, 5)$

$\triangleright a = \text{cut}(x, \text{breaks}, \text{right} = \text{FALSE})$

$\triangleright b = \text{table}(a)$

$\triangleright c = \text{transform}(b)$

$\triangleright c$

Practical-2

TOP IC:- Probability Distribution

1) Check whether the following are p.m.f or not

x	$p(x)$
0	0.1
1	0.2
2	0.9
3	0.4
4	0.3
5	0.5

If the given data is p.m.f then $\sum p(x) = 1$

$$\begin{aligned} \therefore P(0) + P(1) + P(2) + P(3) + P(4) + P(5) &= P(x) \\ = 0.1 + 0.2 + 0.9 + 0.4 + 0.3 + 0.5 & \\ = 2.0 & \end{aligned}$$

$P(2) = -0.5$ it can't be probability mass function.

~~∴ $P(x) \geq 0 \forall x$~~

x	$P(x)$
1	0.2
2	0.3
3	0.3
4	0.2
5	0.2

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The condition for P.m.f is $\sum P(x) = 1$

$$\begin{aligned}\text{So } \sum P(x) &= P(1) + P(2) + P(3) + P(4) + P(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \\ &= 1.1\end{aligned}$$

\therefore The given data is not a p.m.f because the $P(x) \neq 1$

x	$P(x)$
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1



The condition for P.m.f is

1) $P(x) \geq 0 \forall x$ satisfy

2) $\sum P(x) = 1$

$$\begin{aligned}\sum P(x) &= P(10) + P(20) + P(30) + P(40) + P(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1\end{aligned}$$

\therefore The given data is a p.m.f

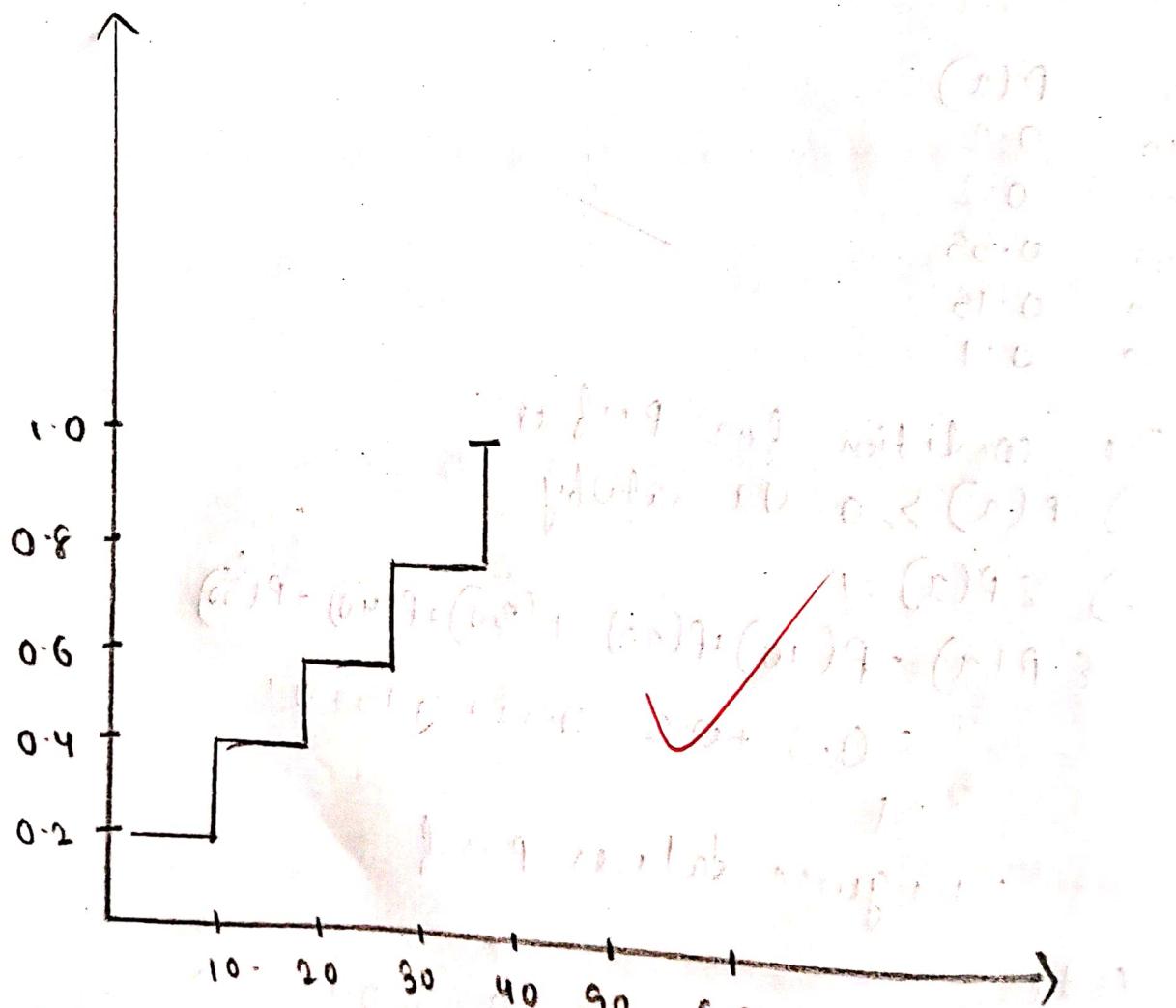
Code

> Prob = c(0.2, 0.2, 0.35, 0.15, 0.1)
[1] 1

Q2) Find the C.F. for the following P.M.F and draw its graph.

	10	20	30	40	50
x	0.2	0.2	0.35	0.15	0.1
$p(x)$	0.2	0.2	0.35	0.15	0.1

$$F(x) = \begin{cases} 0 & x < 10 \\ 0.2 & 10 \leq x < 20 \\ 0.4 & 20 \leq x < 30 \\ 0.75 & 30 \leq x < 40 \\ 0.9 & 40 \leq x < 50 \\ 1.0 & x \geq 50 \end{cases}$$



$\gg X = c(10, 20, 30, 40, 50)$
 $\gg \text{plot}(X, \text{cumsum}(p(x)), "s")$

01) Find
 x
 $P(x)$

1.	2	3	4	5	6
0.5	0.25	0.1	0.2	0.2	0.1

$$f(x) = 0$$

$$x < 1$$

$$= 0.15$$

$$1 \leq x < 2$$

$$= 0.40$$

$$2 \leq x < 3$$

$$= 0.50$$

$$3 \leq x < 4$$

$$= 0.70$$

$$4 \leq x < 5$$

$$= 0.90$$

$$5 \leq x < 6$$

$$= 1.00$$

$$x \geq 6$$

↳ prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

↳ sum(prob)

[1] 1

↳ cumsum(prob)

[2] 0.15, 0.40, 0.50, 0.10, 0.90, 1.00

↳ x = c(1, 2, 3, 4, 5, 6)

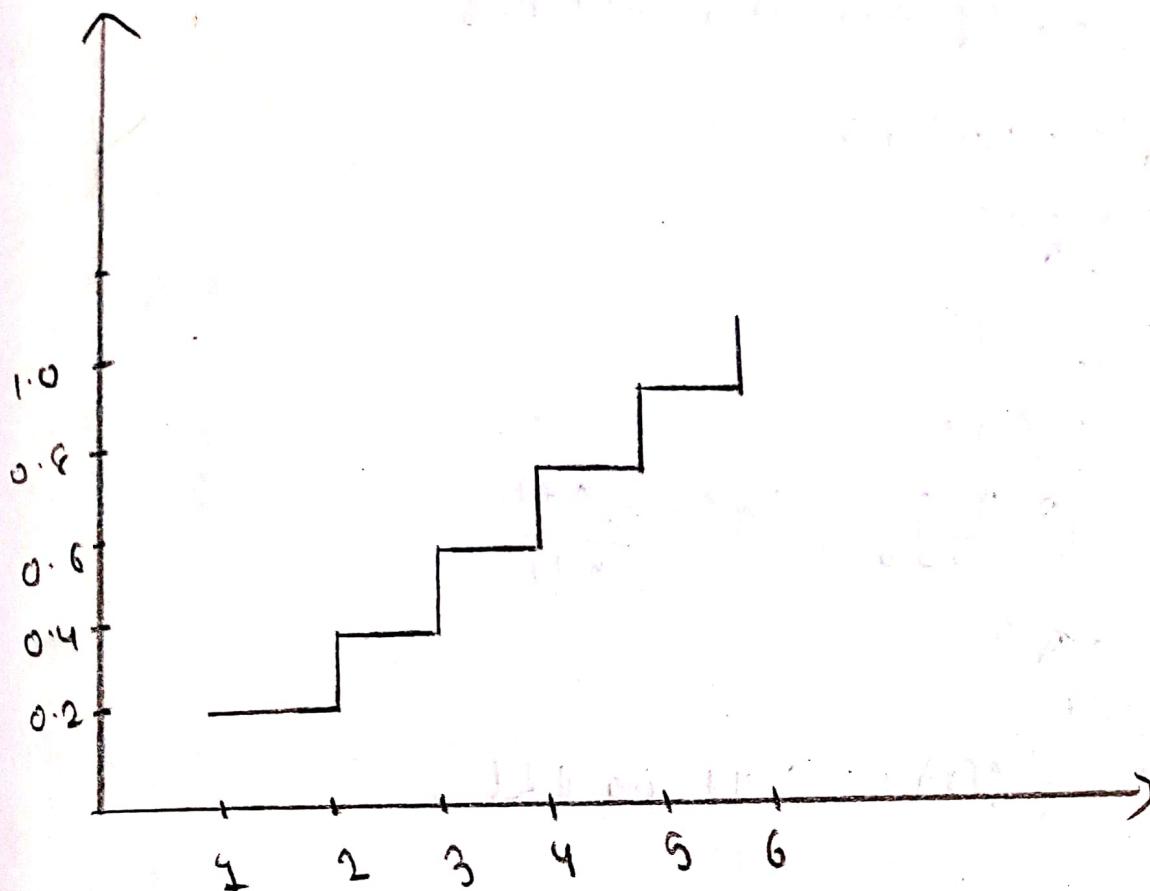
↳ plot(x, cumsum(prob), "S" xlab = "value"

ylab = "Cumulative probability"

main = "CDF graph", "o" (= "brown")

CDF Graph

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3) Check that whether the following is R.F or not

$$1) f(x) = 3 - 2x ; 0 \leq x \leq 1$$

$$2) f(x) = 3x^2 ; 0 < x < 1$$

$$1) f(x) = 3 - 2x$$

$$= \int_0^1 f(x) dx$$

$$= \int_0^1 (3 - 2x) dx$$

$$= \int_0^1 3dx - \int_0^1 2xdx$$

∴ $[3x^2 - x^3]_0^1 = 2$
∴ The $\int f(x) dx = 1$. ∵ It is not a b/w

2) $f(x) = 3x^2 ; 0 < x < 1$

$$\begin{aligned} & \int_0^1 f(x) dx \\ &= \int_0^1 3x^2 dx \\ &= 3 \int_0^1 x^2 dx \\ &= \left[3 \frac{x^3}{3} \right]_0^1 \quad \because x^n = \frac{x^{n+1}}{n+1} \\ &= x^3 \\ &= 1 \end{aligned}$$

The $\int f(x) dx = 1$. ∵ It is a b/w

1) $x = \text{binom}(10, 100, 0.1)$

∴ x

(i) 0.1318693

2) i) $\text{binom}(4, 12, 0.2)$

(i) 0.1328756

(ii) $\text{binom}(4, 12, 0.2)$

(i) 0.4224445

(iii) $\text{binom}(5, 12, 0.2)$

(i) 0.01940528

(a)

Practical 3

TOPIC:- Binomial distribution

$P(X=x) = \text{Binom}(x, n, p)$

$P(X \leq x) = P_{\text{Binom}}(x, n, p)$

$P(X > x) = 1 - P_{\text{Binom}}(x, n, p)$

If X is unknown or free random

$$P_{\text{I}} = P(X \leq x) = \text{Binom}(P_1, n, p)$$

- 1) Find the probability of exactly 10 success in hundred trials with $p=0.4$.
- 2) Suppose there are 12 mcq. Each question has 5 options out of which 1 is correct. Find the probability of having exactly 4 correct answers.
 - i) at most 4 correct answers.
 - ii) more than 5 correct answers.
- 3) Find the complete distribution when $n=5$ and $p=0.1$
- 4) $n=12, p=0.25$ find the following probabilities.
 - i) $P(X=5)$
 - ii) $P(X \leq 5)$

- 52
- 6.
- 9) The probability of a Salesman making a sale to customer 0.15. Find the probability of
- No sales out of 10 customer
 - more than 3 sales out of 10 customer.
- 6) A Salesman has 20% probability of making a sale to customer out of 30 customers. What minimum number of sales he can make with 88% of probability?
- 7) X follows binomial distribution with $n=10$, $p=0.3$ plot the graph of P.M.F & C.F.
- 5) Binom $(0, 10, 0.15)$
- 0.1968744
 - $1 - \text{Binom } (3, 10, 0.15)$

D) $\text{dbinom}(0.88, 130, 0.7)$

(i) 9

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$$\rightarrow n = 130$$

$$\rightarrow p = 0.7$$

$$\rightarrow x = 0.88$$

$\rightarrow \text{prob} = \text{dbinom}(x, n, p)$

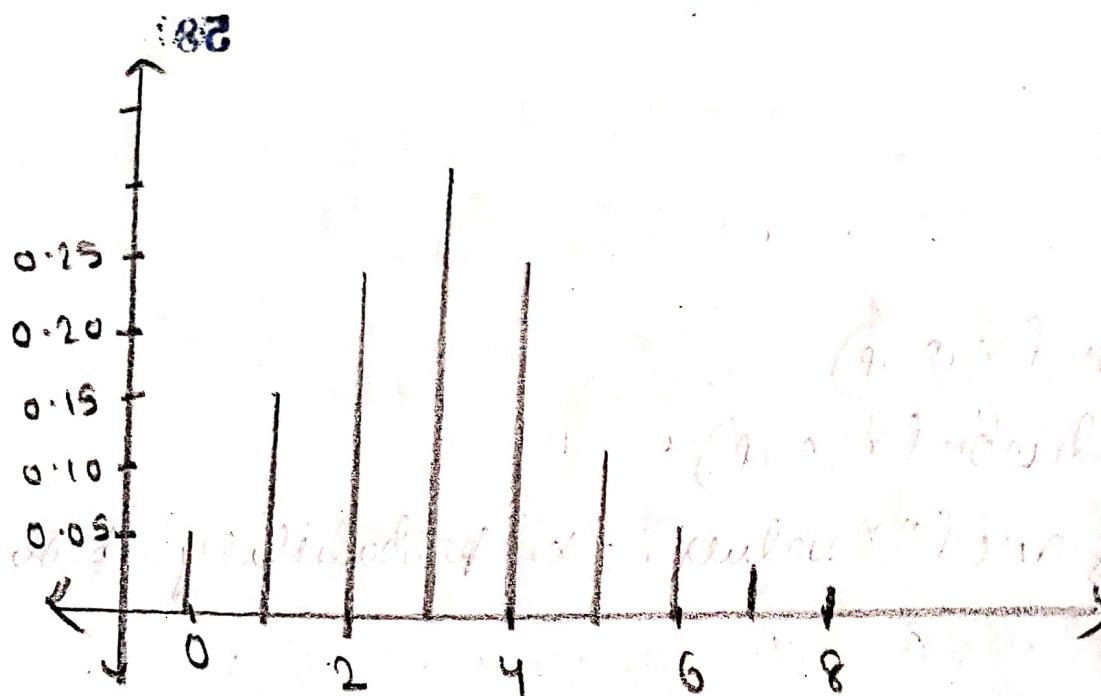
$\rightarrow \text{cumprob} = \text{Pbinom}(x, n, p)$

$\rightarrow d = \text{data.frame("X values": } x, \text{"probability": prob}$

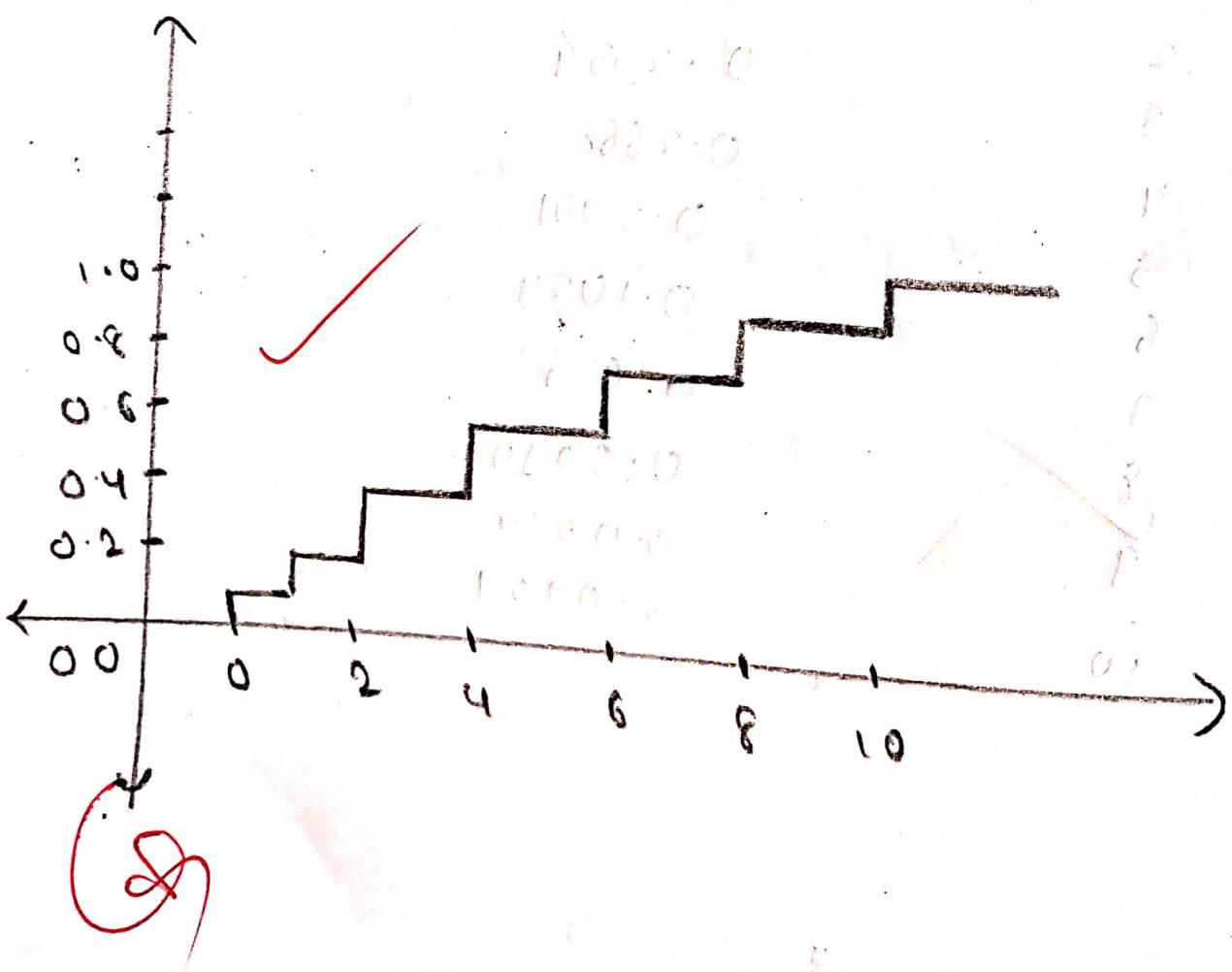
$\rightarrow \text{print}(d)$

	X values	Probability
1	0	0.0282
2	1	0.1210
3	2	0.2534
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.0367
8	7	0.0090
9	8	0.0014
10	9	0.0001
	10	

$\rightarrow \text{plot}(x, \text{krob}, "h")$



$\rightarrow \text{plot}(x, \text{curkrob}, "s")$



i) To generate random numbers from a normal distribution (n random variables) the R code is
 $\text{rnorm}(n, \mu, \sigma)$

A random variable X follows normal distribution with mean = $\mu = 12$ and $S.D = \sigma = 3$. Find

$$\begin{aligned} & P(X \leq 15) \\ & P(10 \leq X \leq 13) \\ & P(X > 14) \end{aligned}$$

CODE:-

$P1 = \text{pnorm}(15, 12, 3)$

$P1$

[1] 0.8413442

$\text{cat("P(X \leq 15) = ", P1)}$

$$(i) \quad 0.1574915 \\ \text{Ans: } P(X > 14) = 0.2924925 \\ P(X < 14) = 0.707575 \\ \text{Ans: } (9, 12, 15)$$

$$(ii) \quad 15.154725 \quad 16.548505 \quad 11.250515, 6.419312 \\ \text{Ans: } 15.154725 \quad 16.548505 \quad 11.250515, 6.419312$$

- (i) X follows normal distribution with $\mu = 10, \sigma^2 = 1$
 find i) $P(X < 7)$ ii) $P(5 < X < 12)$ iii) $P(X > 12)$
 iv) generate 10 observations $\sim N(10, 1)$ such that
 $P(X < 12) = 0.4$

(Ans)

$$\gamma_{q_1} = \text{preru}(7, 10, 1)$$

$$(i) = 0.666027$$

$$\gamma_{q_2} = \text{preru}(5, 10, 1) - \text{preru}(12, 10, 1)$$

$$(i) = 0.431551$$

$$\gamma_{q_3} = 1 - \text{preru}(12, 10, 1)$$

$$(i) = 0.1546555$$

$$\gamma_{q_4} = \text{preru}(10, 10, 1)$$

$$(i) = 0.504951$$

$$(i) \quad 9.721380 \quad 9.193216 \quad 9.031510$$

$$\gamma_{q_5} = \text{preru}(0.4, 10, 1) \\ (i) \quad 9.531564 \quad 10.715006 \quad 9.366824 \quad 11.10$$

$$(i) = 5.4533306$$

(b) Generate 5 random numbers from a normal distribution $\mu = 5$, $\sigma = 4$. Find sample mean, median, S.D and standard deviation.

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Code: (15, 15, 15)

(1) 10.4649 7.193249 9.455944 13.345904
17.509668

$\bar{x}_{\text{sample}} = \text{mean} (\text{b})$

\bar{x}_{sample}

(1) 11.87345

$\bar{x}_{\text{sample}} \leftarrow \text{"sample mean is: "}, \bar{x}_{\text{sample}}$

sample mean is: 11.87345

$\bar{x}_{\text{sample}} = \text{median} (\text{b})$

\bar{x}_{sample}

(1) 11.09969

$\bar{x}_{\text{sample}} = \text{median} (\text{b})$

\bar{x}_{sample}

(1) 3.33163

$\bar{x}_{\text{sample}} = \text{S.D. of: "150")$

$\bar{x}_{\text{sample}} = 3.33163$

6. (001, 001) 22x²y²

10(2)

2) $(x > 35)$

(g) $P(25 < X < 35)$

u) Ein Buch

YF1 = program [40,30,10]

Y F1 10.04.1947

$\gamma \lambda_2 = 1 - \text{norm}(99, 100)$

5765306.001

$$Y_{13} = \text{pnorm}(25, 30, 10) - \text{pnorm}(35, 30, 10)$$

188

$$[1] = 0.3829749$$

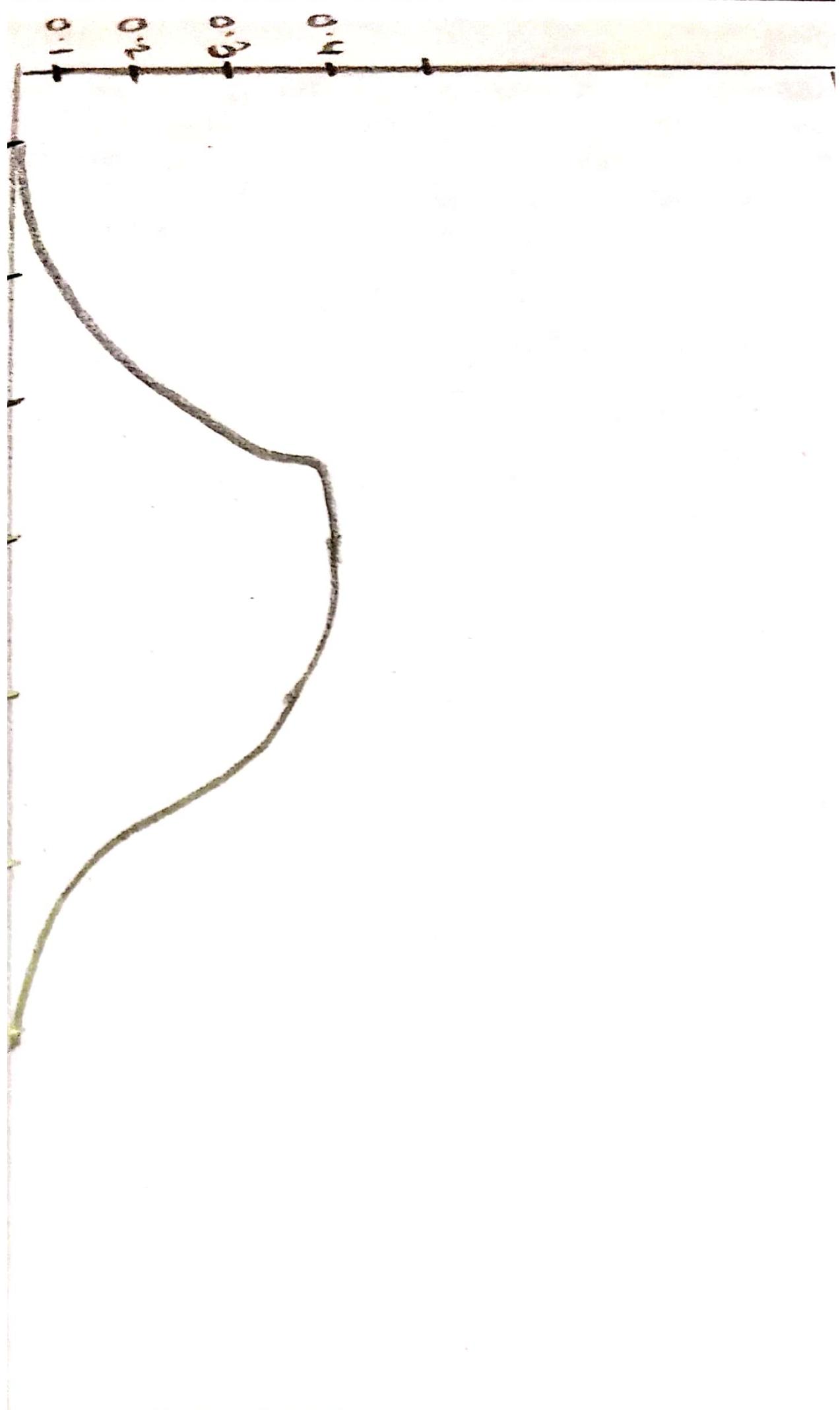
~~Y = 0.613010~~

1784-93347

Plot the stand and regression.

$$C_1 = \text{diag}(-3, 3, -3, 3) = \begin{pmatrix} -3 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 \\ 0 & 0 & -3 & 0 \\ 0 & 0 & 0 & 3 \end{pmatrix}$$

```
plot(x1,y,xlab="x values",ylab="probability")
```



Topic - Normal and t-test

$$H_0 : \mu = 15 \quad H_1 : \mu \neq 15$$

Test the hypothesis

A random sample of size 400 is drawn and its calculated the sample mean is 14 and S.D. is 5. Test the hypothesis at 5% level of significance.

0.05 > Accept the values

0.05 < less than reject

$$\mu_0 = 15$$

$$\bar{X} = 14$$

$$S.D. = 3$$

$$n = 400$$

$$\chi^2_{\text{cal}} = (\bar{X} - \mu_0) / (S.D / \sqrt{n})$$

$$\chi^2_{\text{cal}}$$

$$= 6.66667$$

> Cal (" calculated value of χ^2 is " χ^2_{cal})

calculated value of χ^2 is $= 6.66667$

> p-value = $2 * (1 - \text{prob}(\chi^2(\text{df})))$

> p-value

$$[1] 2.616796e-11$$

: The value is less than 0.05 we will reject the value of $H_0 : \mu = 15$

test the hypothesis $H_0: \mu = 10$ against $H_1: \mu < 10$
A random sample size of 400 is drawn
Sample mean = 10.2 and $S.D = 2.25$. Test the null
hypothesis at

$$H_0: \mu = 10$$

$$H_1: \mu < 10$$

$$n = 400$$

$$\bar{x} = 10.2$$

$$S.D = 2.25$$

$$H_0: \mu = 10$$

$$H_1: \mu < 10$$

$$z_{\text{cal}} = 1.77728$$

$$p\text{-value} = 2 * (1 - \text{norm.pdf}(z_{\text{cal}}))$$

$$p\text{-value} = 2 * (1 - \text{norm.pdf}(1.77728))$$

$$= 0.07544036$$

\checkmark The value of p-value is greater than 0.05

The value is accepted

Test the hypothesis $H_0: p = 0.2$: Proportion of sick
in college is 0.2
A Sample is collected and calculated the proportion
proportional to 0.125. Test of hypothesis of
less of significance (Sample size is 900)

$$H_0: p = 0.2$$

$$H_1: p < 0.2$$

$$n = 900$$

$$\alpha = 1 - p$$

$$r_{cal} = (P - p) / \sqrt{P * q * n}$$

"Calculated value of r is -0.2000"

64

Calculated value of r is -0.325

$$(a) p-value = 2 * (1 - \text{pnorm}(|abs(r)|))$$

$p-value$

$$[1] 0.0001768346 \quad (\text{pnorm})$$

Last year farmers had 20% of their crops A random sample of 60 fields are collected and it is found that 9 fields crops are insect polluted. Test the hypothesis at 1% level of significance.

$$y_p = 0.2$$

$$y_p = 9/60$$

$$n = 60$$

$$r_{cal} = ((P - p) / \sqrt{P * q * n})$$

$$r_{cal}$$

$$[1] -0.5612456$$

$$p-value = 2 * (1 - \text{pnorm}(|abs(r)|))$$

kw
 $p-value$

$$[2] 0.3339216$$

The value is 0.1 so values is accepted

Test the hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance.

$$x = [12.15, 11.97, 12.15, 12.05, 12.31, 12.18, 11.94, 11.89, 12.16,$$

$$12.04]$$

$$n = \text{length}(x)$$

$$[1] 20$$

$\bar{m}_X = \text{mean}(x)$

$\hat{\sigma}_X^2 = 2.102$

$\text{variance} = (n-1) * \text{var}(x) / n$

variance

[2] 0.019621

$\text{sd} = \sqrt{\text{variance}}$

[2] 0.1394176

$m_0 = 12.5$

$t = (m_X - m_0) / (\text{sd} / \sqrt{n})$

[2] -8.94909

$p\text{value} = 2 * (1 - \text{norm}(abs(t)))$

$p\text{value}$

[2] 0

\therefore the value is less than 0.05 the value is accepted

Q1) In a large sample test of the population mean (the amount spent by customers in a restaurant) is 250. A sample of 100 customers selected. The sample mean is calculated as 245 and S.D. is 0. Test the hypothesis that the population mean is 250 at 5% level of significance.

In a random sample of 1000 students it was found that 750 were blue pen test the hypothesis that the population proportion is 0.8 at 1% level of significance.

$$\begin{aligned} \text{Solution:} \\ n &= 1000 \\ m_0 &= 250 \\ m_k &= 245 \\ z_{sd} &= 3.0 \\ n &= 100 \\ z_{cal} &= (m_k - m_0) / (\text{Sqrt}(n)) \\ &\rightarrow \text{Calculated value of } z_{cal} = 1.25 \\ \text{(a) Calculated value of } z &= 1.33333 \\ \text{p-value} &= 2 * (1 - \text{Pr}(z > 1.33333)) \\ \text{p-value} &= 0 \end{aligned}$$

The value is less than 0.05 and will reject the value of $m_0 = M = 250$

2)

Soln:

$$P = 0.8$$

$$Q = 1 - P$$

$$n = 1000$$

$$Z_{\text{cal}} = \frac{(P - Q)}{\sqrt{PQ/n}}$$

$$= \frac{(0.8 - 0.2)}{\sqrt{0.8 \times 0.2 / 1000}}$$

$$= \frac{0.6}{\sqrt{0.16 / 1000}} = 4.74$$

$$\text{Calculated value of } Z_{\text{cal}} = 4.74$$

$$\text{Value of } Z_{\text{tab}} = 1.96$$

$$(2) 4.74 > 1.96 = 0.05$$

The value is less than 0.01 is rejected.

- 3) To random samples of size 1000 & 2000 are drawn from two populations with SD 2.5. The sample means are 67.5 and 68. Test the hypothesis $H_0: \mu_1 = \mu_2$ at 5% significance.

- 4) A study of noise level in 2 hospitals is given below. Test the claim that 2 hospital have same level of noise at 1% level of significance.

HOS A

84

HOS B

61.2

34

7.9

59.4

7.5

Sample of 600 students in city out of 400 used blue ink were blue ink. Test the hypothesis that the proportion of students using blue ink in the city is not at 1% level of significance.

$$n_1 = 1000$$

$$n_2 = 2000$$

$$m_1 = 67.9$$

$$m_2 = 68$$

$$x_1 = 0.9$$

$$x_2 = 2.5$$

$$Z_{\text{test}} = \frac{(m_1 - m_2)}{\sqrt{\frac{m_1}{n_1} + \frac{m_2}{n_2}}} \left(\text{Zstat} \left(\frac{(m_1 - m_2) / \sqrt{\frac{m_1}{n_1} + \frac{m_2}{n_2}}}{\sqrt{\frac{m_1}{n_1} + \frac{m_2}{n_2}}} \right) \right)$$

$$\text{real}$$

$$[1] - 5.163978$$

$$\text{p value} = 2 \times (1 - \text{pnorm}(\text{abs}(z_{\text{test}})))$$

$$\text{pvalue}$$

$$[1] 0.4175648 - 0.7 \quad \text{: (rejected)}$$

$$n_1 = 84$$

$$n_2 = 94$$

$$m_1 = 51.2$$

$$m_2 = 55.9$$

$$x_1 = 7.9$$

$$x_2 = 7.5$$

$$Z_{\text{test}} = \frac{(m_1 - m_2)}{\sqrt{\frac{m_1}{n_1} + \frac{m_2}{n_2}}} \left(\text{Zstat} \left(\frac{(m_1 - m_2) / \sqrt{\frac{m_1}{n_1} + \frac{m_2}{n_2}}}{\sqrt{\frac{m_1}{n_1} + \frac{m_2}{n_2}}} \right) \right)$$

$$[1] -1.62928$$

γ p-value = $2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

p-value

[2] 0.2450211

The value is greater than 0.01 we accept H_0 .

g) $H_0: p_1 = p_2$ againt $H_1: p_1 \neq p_2$

$n_1 = 600$

$n_2 = 400$

$p_1 = 400/600$

$p_2 = 450/900$

$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

p

[2] 0.5666667

$q = 1 - p$

q

[2] 0.4333333

$z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

z_{cal}

[2] 6.3815339

γ p-value = $2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

γ p-value

[2] 1.1753227e-10

Value is less than 0.01 the value is rejected

Statistical Test

part

Small Sample Test

n marks of 10 students are given say 65, 63, 66,
67, 68, 69, 70, 71, 72 test the hypothesis that
the sample comes from the population with
average 66

$$H_0 : \mu = 66$$

$$H_A = \{ 66, 63, 66, 67, 68, 69, 70, 71 \}$$

t-test (T)

one sample test

$$\text{data : } X = [66, 63, 66, 67, 68, 69, 70, 71]$$

alternative hypothesis

true mean is not equal to 66

95 percent confidence interval

$$65.171 \leq \bar{x} \leq 68.729$$

sample estimates

mean of X

$$67.9$$

The p-value is less than 0.05 we reject
the hypothesis at 5% level of significance.

2) Two groups of students to record the marks under the hypothesis that there is no significance difference between the 2 groups

GR1 = [18, 22, 21, 17, 20, 17, 12, 20, 20, 21]
GR2 = [16, 12, 14, 21, 20, 18, 15, 19, 17, 21]

H₀: There is no difference b/w the 2 groups

> d = c(18, 22, 21, 17, 20, 17, 12, 20, 20, 21)
> y = c(16, 12, 14, 21, 20, 18, 15, 19, 17, 21)
> t.test(x, y)

with ~~Two Sample t-test~~

data : x, y

t = 2.2345 df = 16.376 p-value = 0.03796

alternative hypothesis:

New difference in means is not equal to 0 95 percent confidence interval
0.1629005 5.031795
Sample estimates
mean of x mean of y
20.1 17.9

> p-value

= 0.03796

if (p-value > 0.05) cat ("accept H0")
else cat ("reject H0")

(i) Sales data of 6 stores before & after advertising campaign are given below

68

before : 53, 28, 31, 48, 50, 42
after : 58, 29, 30, 55, 56, 49

∴ Ques
No
says

test the hypothesis that the campaign is effective or not.

H₀ : There is no significance difference of sales before & after campaign

u/s

$\gamma_{X=C}$ (Before)

$\gamma_{Y=C}$ (After)

t-test (X, Y , paired) = T, alternative = "greater."

paired + test

data : $X \geq Y$

$t = -2.4815$ df = 5, p-value = 0.9806

alternative hypothesis.

True difference in means is greater than 0

95 per cent confidence interval

paired

all

-6.0395 < μ < 1.11

Sample estimated
mean of the difference

-3.9

∴ p value is greater than 0.05, we accept the hypothesis at 5% level of significance.

(ii) Following are the weights before & after the diet program Is the diet program effective.

before : 120, 125, 115, 130, 123, 118

After : 100, 114, 95, 90, 115, 99

Sol : H₀: There is no significance difference

> x=c
> y=g
> t-test(x,y,paired=T, alternative="less")
paired t-test

data : n=8
 $t = 4.3458$, df = 6, p-value = 0.9963

Alternative hypothesis : true difference in mean is less than 0

99 percent confidence interval

10.795 29.0295

Sample estimates
mean of the difference

19.8333

(g) If value is greater than 0.05 we accept the hypothesis at 5% level of significance.

Practical No 8

Topic :- Large and Small Test

$$H_0 : \mu = 5.5, H_1 : \mu \neq 5.5$$

$$n_0 = 100$$

$$n_1 = 50$$

$$\sigma = 1$$

$$z_{\text{cal}} = (\bar{x} - \mu_0) / (\sigma / \sqrt{n})$$

$\rightarrow z_{\text{cal}}$

$$(1) -4.285 + 14$$

$$z_{\text{value}} = -2.74 \quad \cancel{\text{not in tabular values}} \quad (\text{abs } z_{\text{cal}})$$

$$(2) 1.532 - 0.5 = 0.81$$

As p-value is less than 0.05 we reject H_0 at 5% level of significance.

$$H_0 : P = 0.50 \text{ against } H_1 : P \neq 0.5$$

$$\rightarrow P = 0.5$$

$$\rightarrow Q = 1 - P$$

$$\rightarrow n = 100$$

$$\rightarrow z_{\text{cal}} = (P - \bar{P}) / (\sigma / \sqrt{n})$$

$\rightarrow z_{\text{cal}}$

$$(1) 0$$

$$\rightarrow \text{p-value} = 2 * (1 - \text{prob}(Z > |z_{\text{cal}}|))$$

$\rightarrow \text{p-value}$

e)

As p-value is greater than 0.05 we can't reject H_0 at level of significance.

$H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

$$\text{Sol. } (3) \quad n_1 = 1000$$

$$n_2 = 1500$$

$$p_1 = 2/1000$$

$$p_2 = 1/1500$$

$$p = (n_1 p_1 + n_2 p_2) / (n_1 + n_2)$$

$$p = 0.0012$$

$$q = 1 - p$$

$$(1) \quad 0.9988$$

$$n_{\text{cal}} = (p_1 - p_2)^2 / (p_1 * q_1 * (n_1 + n_2))$$

$$(2) \quad 0.9433 + 52$$

$$\text{p-value} = 2 * (1 - \text{norm}(\text{abs}(n_{\text{cal}})))$$

$$(2) \cdot 0.3454 \approx 0.6908$$

∴ p-value is greater than 0.05 we accept H_0 and 5% level of significance

$$H_0: \mu = 100 \text{ against } H_1: \mu \neq 100$$

$$n = 64$$

$$n = 400$$

$$x = 60$$

$$x = 80$$

$$p = \text{sqrt}(n \sigma^2)$$

> zcal

zcal (n=10) | (sd 1.897 (n))

70

> zcal

(1) 2.5
pvalue : $\alpha + (1 - \text{pnorm}(\text{abs}(zcal)))$

pvalue

0.01241933

since pvalue is less than 0.05 we reject H_0 at 5% level of significance.

③ $H_0 : \mu = 66$ against $H_1 : \mu \neq 66$

> x = c(63, 63, 64, 69, 71, 71, 72)

> t.test(x)

one sample t-test

Data: x

t = 4.794, df = 6, p-value = 0.002222

alternative hypothesis: true mean is not equal to 66
95 percent confidence interval

66.479 71.62092

sample estimates:

mean of x

68.19286

since pvalue is less than 0.05 we reject H_0 at

Soln @ Q. No. 1) $H_0: \sigma_1^2 = \sigma_2^2$ against $H_1: \sigma_1^2 \neq \sigma_2^2$

$\Rightarrow x = \{66, 67, 75, 76, 82, 88, 90, 92\}$
 $\Rightarrow y = \{64, 66, 74, 78, 82, 85, 87, 88, 93, 95\}$
 $\Rightarrow \text{var. lens} (x, y)$

F test to compare two variances
 data : x and y

F : 0.78803, num. df = 7, denom. df = 10, p-value = 0.4761601
 alternative hypothesis: true ratio of variance is not equal to 1

95 percent confidence interval

$$0.19950973 - 0.51881$$

Sample estimates

ratio of variance

$$0.7770288$$

\therefore p-value is greater than 0.05 we accept H_0 at 5% level of significance

Q. 2) $H_0: \mu = 1150$ against $H_1: \mu \neq 1150$

$$\Rightarrow n = 100$$

$$\Rightarrow \bar{x} = 1150$$

$$\Rightarrow \sigma_0 = 1200$$

$$\Rightarrow z_{\text{cal}} = (\bar{x} - \mu_0) / (\sigma_0 / \sqrt{n})$$

$$[2] - 4$$

$$\Rightarrow \text{pvalue} = 2 * (1 - \text{norm}(z_{\text{cal}}))$$

71

value is less than 0.05 we reject H_0

$H_0 : p_1 = p_2$ against $H_1 : p_1 \neq p_2$

$$\gamma n_1 = 200$$

$$\gamma n_2 = 300$$

$$\gamma p_1 = 44 / 200$$

$$\gamma p_2 = 56 / 300$$

$$\gamma p = (n_1 \times p_1 + n_2 \times p_2) / (n_1 + n_2)$$

$$\gamma p$$

$$[2] 0.2$$

$$\gamma q = 1 - p$$

$$\{ 0.8$$

$$\gamma z_{\text{cal}} = (p_1 - p_2) / \sqrt{p \cdot q \cdot (1/n_1 + 1/n_2)}$$

$$\gamma z_{\text{cal}}$$

$$[2] 0.9128709$$

$$\gamma p \text{ value} = 2 * (1 - \text{norm}(\text{abs}(z_{\text{cal}})))$$

$$\gamma p \text{ value}$$

$$[1] 0.3613104$$

$\therefore p \text{ value is greater than } 0.9$ we accept H_0 at
1% level of significance.

Topic: Non-parametric testing of hypothesis using R environment

The following data represent earnings (in dollar) for a random sample of five common stocks listed on the New York Stock Exchange. Whether median earnings is as follows
Data : 1.68, 3.35, 1.96, 6.25, 3.24

$\gamma_{n-k} = \{ 1.68, 3.35, 1.96, 6.25, 3.24 \}$,
 $\gamma_{nk} = \text{length } (\gamma)$,

$\gamma_{[1]} = 5$

$\gamma_{[2]} = 5$

$\gamma_{[3]} = 4$

$\gamma_{[4]} = 1$

$\gamma_{[5]} = 1$

$\gamma_{[6]} = 1$

$\gamma_{[7]} = 1$

$\gamma_{[8]} = 1$

$\gamma_{[9]} = 1$

$\gamma_{[10]} = 1$

$\gamma_{[11]} = 1$

$\gamma_{[12]} = 1$

$\gamma_{[13]} = 1$

$\gamma_{[14]} = 1$

$\gamma_{[15]} = 1$

$\gamma_{[16]} = 1$

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$\gamma_{[222]} = 1$

$\gamma_{[223]} = 1$

$\gamma_{[224]} = 1$

$\gamma_{[225]} = 1$

$\gamma_{[226]} = 1$

$\gamma_{[227]} = 1$

$\gamma_{[228]} = 1$

$\gamma_{[229]} =$

The Scores of 8 students in reading before & after lesson are as follows
test whether there is effect of reading

Students	1	2	3	4	5	6	7
Score Before	10	15	16	14	09	07	11
Score After	13	16	15	13	09	10	13

CODE:-

```

> b <- c(10, 15, 16, 12, 09, 07, 11, 12);
> a <- c(13, 16, 15, 13, 08, 10, 13, 10);
> D <- b - a;
> wilcox.test(D, alternative = "greater");

```

wilcoxon signed rank test with

continuity correction data: D
 $\nu = 10.9$, p-value = 0.8722

alternative hypothesis: true location is greater than 0

warning message

In wilcox.test default (P), alternative = "great"
 cannot compute exact p-value with ties
 \therefore p-value is greater than 0.05 was accepted

the diameter of a ball bearing was measured by 5 inspectors each using two different kinds of calipers. The results were as follows: average ball bearing size for

Durchmesser	1	2	3	4	5	6
Caliper 1	0.165	0.166	0.165	0.167	0.169	0.166
Caliper 2	0.163	0.162	0.170	0.161	0.171	0.160

Caliper 1 and caliper 2 are same

St:

K-C ($0.165, 0.169, 0.166, 0.167, 0.169, 0.164$)

K-C ($0.163, 0.162, 0.170, 0.161, 0.171, 0.160$)

wilcoxon-test ($X > Y$, alternative = "greater")

wilcoxon rank sum test

Data: X and Y

$$W = 24, p = 0.197$$

2nd

Alternative hypothesis: true location shift is greater than 0

1st
p-value is greater than 0.05 we accept H₀



Practical-10

Ques:- Chi Square tests & ANOVA

(Analysis of variances)

- (i) Use the following data to test whether the condition of home & condition of child are independent or not.

cond child	cond Home	Clear	Dirty	Light
clean	70	35	50	10
Fairy	80	60	20	10
dirty	35	45	45	10

H0:- condition of Home & child are independent

$$\chi^2 = \sum (O - E)^2 / E$$

$$M = 3$$

$$N = 2$$

$$\chi^2 = \text{matrix}(x, \text{row} = M, \text{ncol} = N)$$

$$Y$$

	[1, 1]	[1, 2]	[2, 1]	[2, 2]
[1, 1]	70	80	20	45
[1, 2]				
[2, 1]	35			
[2, 2]				

$\Rightarrow \text{p-value} = \text{chi-squared test (+)}$

Pearson's Chi-squared test

Data : 4

$$\chi^2 - \text{Squared} = 25.646$$

$$df = 2$$

$$p - \text{value} = 2.698 \times 10^{-6}$$

They are dependent

$\because p$ value is less than 0.05 we reject the hypothesis at 95% level of significance.

Q) Test the hypothesis that vaccination & disease are independent or not

Vaccine

Disease
Affect
Non-affected

Affected

70

35

Not Affected

46

37

H_0 : Disease & vaccine are independent

$x = c(70, 35, 46, 37)$

$m = 2$ $y = \text{matrix}(x, \text{row} = m, \text{ncol} = n)$

$y = \text{matrix}(x, \text{row} = m, \text{ncol} = n)$

$y = \begin{bmatrix} 70 & 35 \\ 46 & 37 \end{bmatrix}$

$\begin{bmatrix} 70 \\ 46 \end{bmatrix}$ $\begin{bmatrix} 35 \\ 37 \end{bmatrix}$

$\chi^2 = \text{chisq.test}(y)$

χ^2 test for independence of row and column

pearson's chi-squared test with Yates' continuity correction

data : y

$\chi^2 = 2.0275$

$df = 1$

$p\text{-value} = 0.1549$

$\therefore p\text{-value is more than } 0.05$ we accept the hypothesis at 5% level of significance

|| They are INDEPENDENT

Q3) Perform a ANOVA for the following data.

<u>TYPE</u>	<u>OBSERVATION</u>
A	50, 52
B	53, 55, 53
C	50, 58, 57, 56
D	52, 54, 54, 55

H_0 : The mean's are equal for A, B, C, D.

```

> X1 = c(50, 52)
> X2 = c(53, 55, 53)
> X3 = c(50, 58, 57, 56)
> X4 = c(52, 54, 54, 55)
> f = stack(list(b1 = X1, b2 = X2, b3 = X3, b4 = X4))
> mnames(f)
[1] "value" "end"

```

one way test (value wind, data=f, var.equal=T)

one-way analysis of means

data: values and end.

F = 11.735 df = 3, from kf = 9,

P value = 0.00183

P-value is less than 0.05 we reject the hypothesis.

`anova = anova (values windata = d)`
`>summary (anova)`

	Df	Sum	mean Sq	F value	Pr(>F)
id	3	71.06	23.688	11.73	6.00185**
residuals	9	18.17	2.019		

`signif. codes : 0 *** 0.001 ** 0.01 *
 0.05 . 0.1 ' ' 1`

QG