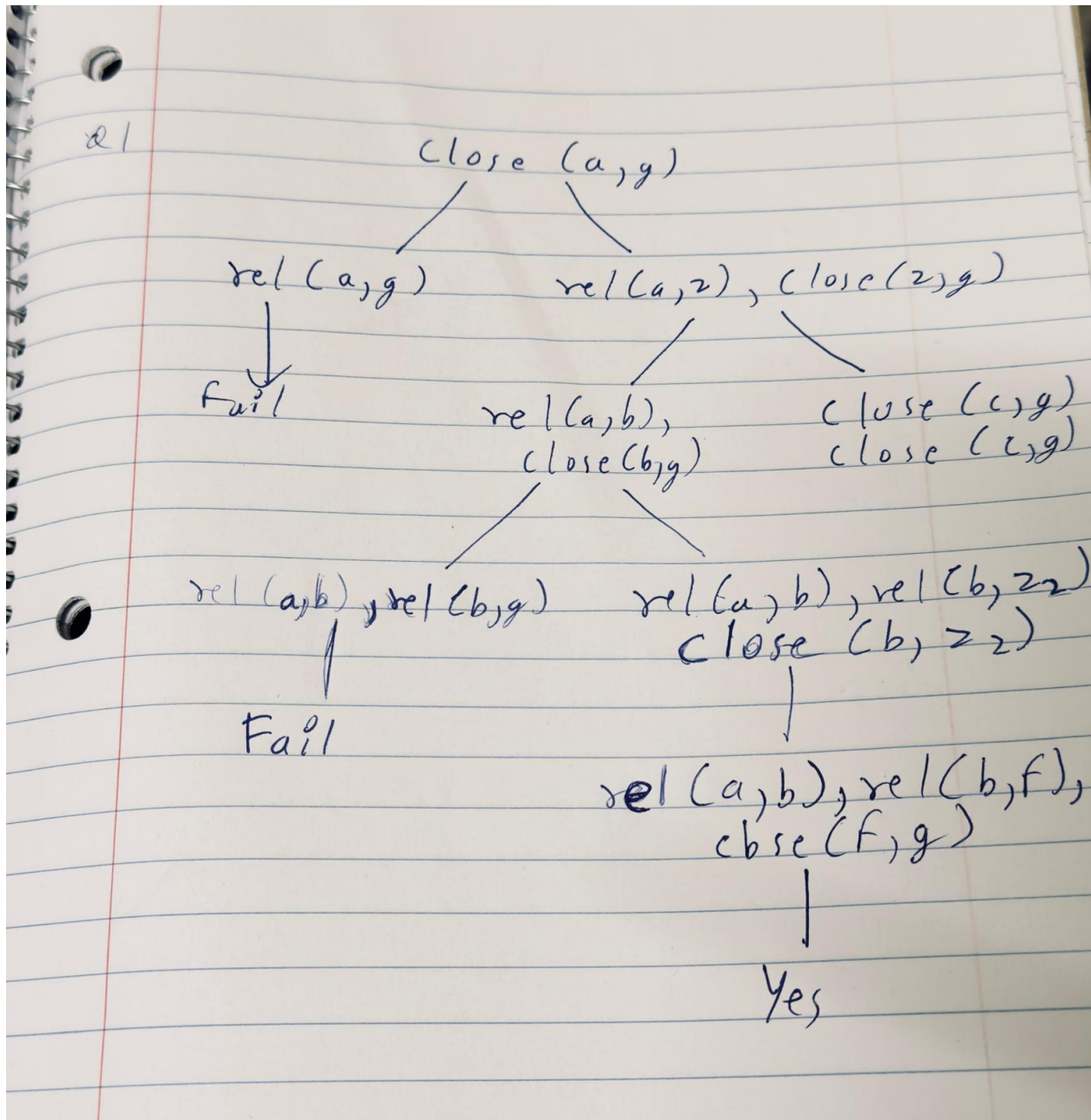


HW-6

Ans-1



Ans-2:

1. $p(X, Y) = p(Y, X) \rightarrow$ Succeeds: $X = Y$
2. $q(X, X) = q(1, 2) \rightarrow$ Fails: X cannot both be 1 and 2
3. $m(f(X), Y) = m(f(a), b) \rightarrow$ Succeeds: $X = a, Y = b$
4. $k(X, Y) = k(a) \rightarrow$ Fails: Arity mismatch
5. $[A, B | X] = [1, 2] \rightarrow$ Succeeds: $A = 1, B = 2, X = []$

Ans-3:

In Peano arithmetic, we can formally define the predicate of exponentiation as:

% Base case: any number raised to the power 0 equals 1.

`exp(_, 0, s(0)).`

% Recursive case: `exp(X, Y, Z)` if $Y = s(Y1) \Rightarrow Z = X * \text{exp}(X, Y1)$

`exp(X, s(Y), Z) :-`

`exp(X, Y, Z1), mult(X, Z1, Z).`

Ans-4:

Rotate left and right predicates for a BST:

`rotateRight(tree(Z, KZ, tree(Y, KY, A, B), C), tree(Y, KY, A, tree(Z, KZ, B, C))).`

`rotateLeft(tree(X, KX, A, tree(Y, KY, B, C)), tree(Y, KY, tree(X, KX, A, B), C)).`

`ltree(tree(3, c, tree(2, b, tree(1, a, empty, empty), empty), empty)).`

`rtree(tree(1, a, empty, tree(2, b, empty, tree(3, c, empty, empty)))).`