HPC Lab Assignment No: 4

Title: Two large vectors Addition/Subtraction/Multiplication

Aim: Design and implement a parallel algorithm to add/subtract/multiply two large vectors using C programming language.

Objective:

- 1. Write sequential vector addition/subtraction/multiplication program.
- 2. Calculate complexity of the program.
- 3. Measure time taken by the sequential program.
- 4. Write program for Parallel vector addition/subtraction/multiplication
- 5. Measure time taken by the parallel program.
- 6. Measure and compare time taken by the parallel vs serial program.

Theory:

1. Write about the serial vector addition/subtraction/multiplication.

ANS:

• Vector addition can be done by sequentially accessing the elements of both the

large vectors and adding them and store result in result vector(array).

• The following v_add function inside v_add.c performs an element-byelement

addition of two vectors x and y and places the result in a third vector z;

```
void\ v\_add(double*\ x,\ double*\ y,\ double*\ z) { for(int\ i=0;\ i<ARRAY\_SIZE;\ i++) z[i]=x[i]+y[i]; }
```

2. Write about the parallel vector addition/subtraction/multiplication.

ANS:

- Vector addition is inherently a very parallel computation.
- The v_add function inside v_add.c performs an element-by-element addition of two vectors x and y and places the result in a third vector z parallely, as shown below:

```
void v_add(double* x, double* y, double* z)
{
    # pragma omp parallel
    {
        for(int i=0; i<ARRAY_SIZE; i++)
            z[i] = x[i] + y[i];
        }//end_pragma section
}</pre>
```

3. Write which constructs of OPENMP are used for parallel vector addition, subtraction, multiplication.

ANS:

The 'for' construct of openMP is used for parallel openMP addition.

```
#pragma omp parallel for for(i=0;\ i< n;\ i++) { c[i] = a[i]+b[i]; printf("Thread %d works on element%d\n", omp_get_thread_num(), i);} }
```

Test on data set of sufficiently large size.

Compute Total cost and Efficiency as: -

Total Cost = Time complexity \times Number of processors used

Efficiency = Execution time of sequential algorithm/Execution time of the parallel algorithm

Efficiency = 0.76

Mention the number of processors / processor cores of your machine: 8

Consider data points as follows: -

| Sr no | Data points/Data | Time Taken for | Time Taken for |
|-------|--------------------|-----------------|-------------------|
| | values for vectors | serial approach | parallel approach |
| 1 | 500 | 0.000002 | 0.0042441 |
| 2 | 1000 | 0.000007 | 0.002412 |
| 3 | 10000 | 0.000091 | 0.001008 |
| 4 | 30000 | 0.000253 | 0.000915 |
| 5 | 50000 | 0.000416 | 0.001801 |

| 6 | 70000 | 0.000572 | 0.001650 |
|---|--------|----------|----------|
| 7 | 100000 | 0.000719 | 0.000946 |

Auto Generate the data points/values through:-

a) Giving a specific pattern of data value generation

b) Randomizing the data points/values

(Also a file may be maintained for reading the values stored)

Input: Two large vectors.

Output: Addition/multiplication/subtraction of two large vectors.

Platform: Windows

Conclusion: Thus, successfully studied, analyzed addition/subtraction/multiplication of two

large vectors.

FAQs:

1. What is the Complexity of Strassen's Matrix Multiplication?

ANS: Time complexity of Strassen's Matrix Multiplication is:

$$O(n^{\log 2(7)}) = O(n^{2.81})$$

2. What do you understand by Speedup and Efficiency?

<u>ANS:</u> The speedup is defined as the ratio of the serial runtime of the best sequential algorithm for solving a problem to the time taken by the parallel algorithm to solve the same problem on p processors. The efficiency is defined as the ratio of speedup to the number of processors.

Code:

```
#include <stdio.h>
#include <stdlib.h>
#include <omp.h>
#define NUM_THREADS 4
double addVector(double *a, double *b, double *ans, int n)
    double start = omp_get_wtime();
    for(int i=0; i<n; i++)</pre>
        ans[i] = a[i] + b[i];
    double end = omp_get_wtime();
    printf("Time Taken for Serial : %f\n", end-start);
    double T1 = end-start;
    return T1;
double addVectorPar(double *a, double *b, double *ans, int n)
    double start = omp_get_wtime();
    #pragma omp parallel for
   for(int i=0; i<n; i++)</pre>
        ans[i] = a[i] + b[i];
        //printf("Addition%lf + %lf = %lf performed by thread %d \n", a[i], b[i],
ans[i], omp_get_thread_num());
    double end = omp_get_wtime();
    printf("Time Taken for Parallel : %f\n", end-start);
    double Tp = end-start;
    return Tp;
int main()
    int n = 700000000;
    printf("\nFor vector of size %d\n",n);
    double *array1 = (double *) malloc(sizeof(double) * n), *array2 = (double *)
malloc(sizeof(double) * n), *array3 = (double *) malloc(sizeof(double) * n), *array4
= (double *) malloc(sizeof(double) * n);
    for (int i=0; i<n; i++)
        array1[i] = rand() % 1000;
```

```
array2[i] = rand() % 1000;
}

omp_set_num_threads(NUM_THREADS);
// addVector(array1, array2, array3, n);
// addVectorPar(array1, array2, array4, n);
double a = addVector(array1, array2, array3, n);
double b = addVectorPar(array1, array2, array4, n);
double cores = omp_get_num_procs();
double speedup = a/b;
double efficiency = (1/cores)*speedup;
printf("Speedup = %f",speedup);
printf("\nEfficiency = %lf",efficiency);
}
```

Output:

```
For vector of size 100000000
Time Taken for Serial: 1.362000
Time Taken for Parallel: 1.228000
Speedup = 1.109121
Efficiency = 0.138640
PS D:\HPC> gcc -fopenmp -o vector hpcvector.c
PS D:\HPC> ./vector.exe
For vector of size 50000000
Time Taken for Serial: 0.157000
Time Taken for Parallel: 0.079000
Speedup = 1.987343
Efficiency = 0.248418
PS D:\HPC> gcc -fopenmp -o vector hpcvector.c
PS D:\HPC> ./vector.exe
For vector of size 70000000
Time Taken for Serial: 0.254000
Time Taken for Parallel: 0.129000
Speedup = 1.968989
Efficiency = 0.246124
PS D:\HPC>
```