## **Assignment 1**

## AI1110: Probability and Random Variables

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**12.13.6.15**: **Question.** An electronic assembley consists of two subsystems,say A and B.From previous testing procedures, the following probabilities are assumed to be known:

$$Pr(A fails) = 0.20 (1)$$

$$Pr(B \text{ alone fails}) = 0.15$$
 (2)

$$Pr(A \text{ and } B \text{ fails}) = 0.15 \tag{3}$$

Evaluate the following probabilities

- 1) Pr (A fails given B has failed)
- 2) Pr (A fails alone)

ans:

1)

$$Pr(A \text{ fails given B has failed}) = 0.50$$
 (4)

2)

$$Pr(A \text{ fails alone}) = 0.05$$
 (5)

Solution: Given,

$$\Pr(A') = 0.20$$
 (6)

$$\Pr(AB') = 0.15$$
 (7)

$$\Pr(A'B') = 0.15$$
 (8)

1) to find, Pr(A'|B') we use

$$\Pr(A'|B') = \frac{\Pr(A'B')}{\Pr(B')} \tag{9}$$

to obtain Pr(B')

$$B'(1) = B'(A + A') \tag{10}$$

$$= B'A + B'A' \text{ since}((B'A)(B'A')) = 0$$
(11)

$$Pr(B') = Pr(AB') + Pr(A'B')$$
 (12)

we use,

$$Pr(B') = Pr(AB') + Pr(A'B') (from (12))$$

(13)

$$= 0.15 + 0.15 \text{ (from } (7), (8))$$

(14)

$$\implies \Pr(B') = 0.30 \tag{15}$$

2) to find Pr(A'|B')

$$Pr(A'|B') = 0.15/0.30 \text{ (from } (15), (8), (9))$$

(16)

1

$$\implies \Pr(A'|B') = 0.50 \tag{17}$$

similarly, to obtain Pr(BA')

$$BA' + B'A' = BA' + B'A'$$
 (18)

$$BA' + B'A' = A'(B' + B)$$
 (19)

$$BA' + B'A' = A' \tag{20}$$

$$A' = BA' + B'A' \text{ since}((A'B)(B'A')) = 0$$
(21)

$$Pr(A') = Pr(BA') + Pr(A'B')$$
 (22)

$$Pr(BA') = Pr(A') - Pr(A'B')$$
 (23)

we use

$$Pr(BA') = Pr(A') - Pr(A'B')$$
 from (23)  
(24)

$$= 0.20 - 0.15$$
 from eq:(6),(8)

(25)

$$\implies \Pr(BA') = 0.05 \tag{26}$$