



HEAP DATA STRUCTURE

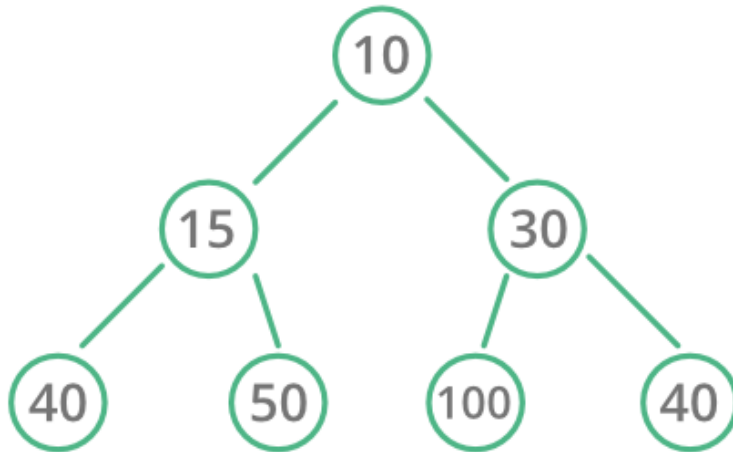


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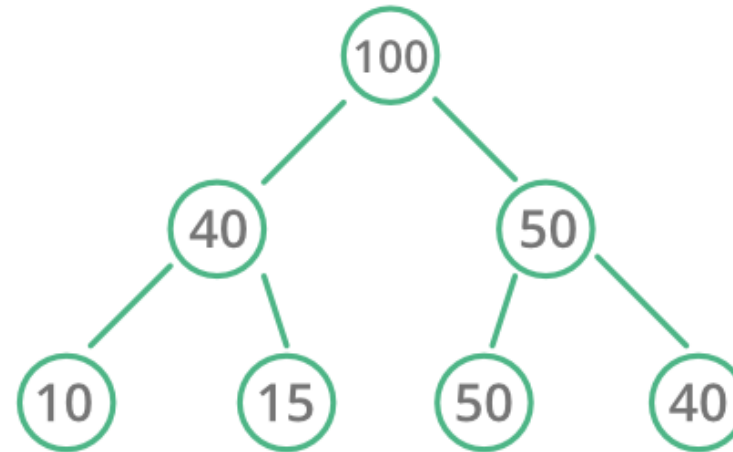
- A heap is a **complete binary tree** that satisfies the **heap property**.
 - For each node, the value of its children is (less than or equal) to its own value.
- **Max Heap**
 - The root node contains the **maximum** value.
 - For each node C, the value of its parent P is **greater than or equal to** its own value.
- **Min Heap**
 - The root node contains the **minimum** value.
 - For each node C, the value of its parent P is **less than or equal** to its own value.

Heap Data Structure

Heap is not a sorted structure.



Min Heap



Max Heap



HEAP OPERATIONS

- **heapify**: Rearrange the heap in order to maintain the heap property
- **insert**: Add a new key to the heap
- **extract**: Delete the root node and return its value
- **buildHeap**: Build a heap from the given array

APPLICATIONS OF HEAP DATA STRUCTURE

- Priority Queues
- Heap Sort
- Graph Algorithms (e.g. Dijkstra's algorithm and Prim's algorithm)
 - Finding the shortest paths
 - Minimum spanning trees

PRIORITY QUEUE

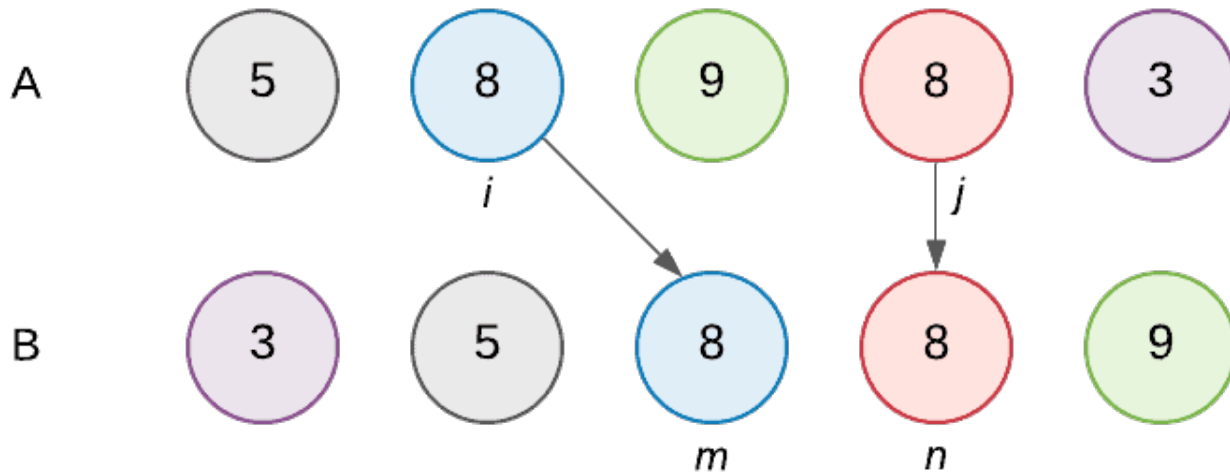
- An abstract data type
- Each element in a priority queue is associated with a **priority**.
- A queue whose elements are arranged based on their priorities.
 - Elements with higher priority are retrieved before elements with lower priority.

HEAPSORT

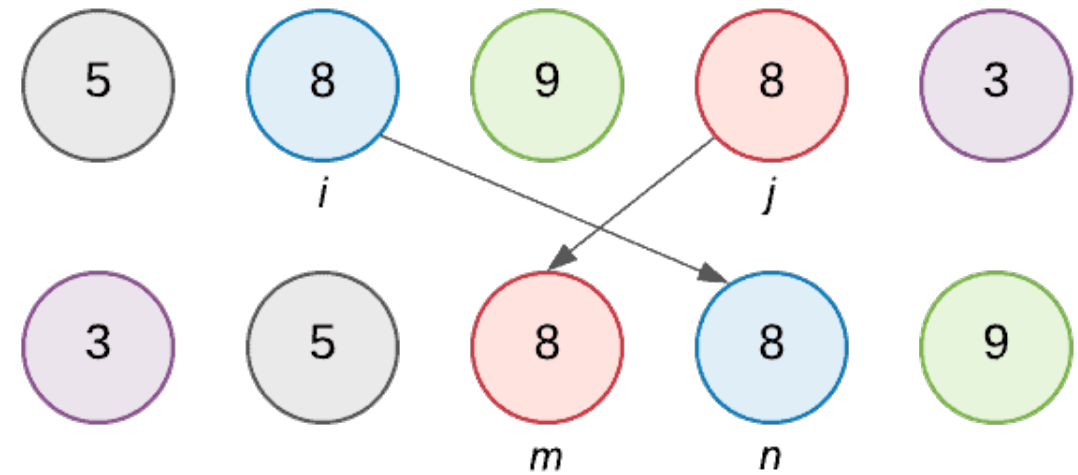
- Heapsort is similar to selection sort *i.e.*, repeated choosing the largest item and moving it to the end of the array.
- It utilizes the heap data structure in sorting.
- It is an in-place but unstable sorting algorithm
 - The order of elements of equal keys is **not** preserved after sorting.

STABLE VS. UNSTABLE SORTING

STABLE SORTING



UNSTABLE SORTING



HEAPSORT ALGORITHM

■ Steps:

1. Transform the array into a binary tree.
2. Convert the binary tree into a max heap.
3. Swap the root node (largest element) with the last node in the heap.
4. Heapify to maintain the heap property.
5. Repeat step 3 and 4 until there is no element left in the heap.