



# Evaluating Recurring Traffic Congestion Using Change Point Regression and Random Variation Markov Structured Model

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# Presentation Overview

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- Introduction
- Research objective
- Study site
- Data
- Methodology
- Results and Discussion
- Conclusions
- Future Work

# Introduction

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## Mobility

- Travel delay of nearly 7 billion hours
- Total cost of congestion was \$ 160 billion

## Environment

- Wasted more than 3 billion gallons of fuel

Urban Mobility Scorecard report (Schrank, *et al.*, 2015)



# Introduction

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- Success of alleviating traffic congestion through operation efficiency depends on:
    - Quality of the data used for evaluation and prediction
    - Predictive capability of the model
    - Dissemination of the accurate and timely traffic information to road users
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# Research Objective

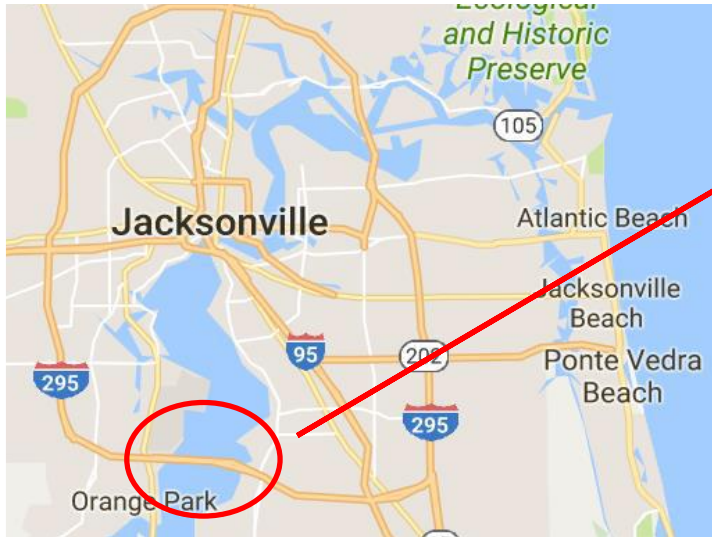
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- The study proposes a probabilistic framework to evaluate the dynamic evolution process of recurring traffic congestion on a basic freeway segment
  - Bayesian change point regression to estimate speed threshold
  - Markov Chain Structure regression to estimate the dynamic evolution of recurring congestion

# Study site

## A section of Interstate 295 in Jacksonville

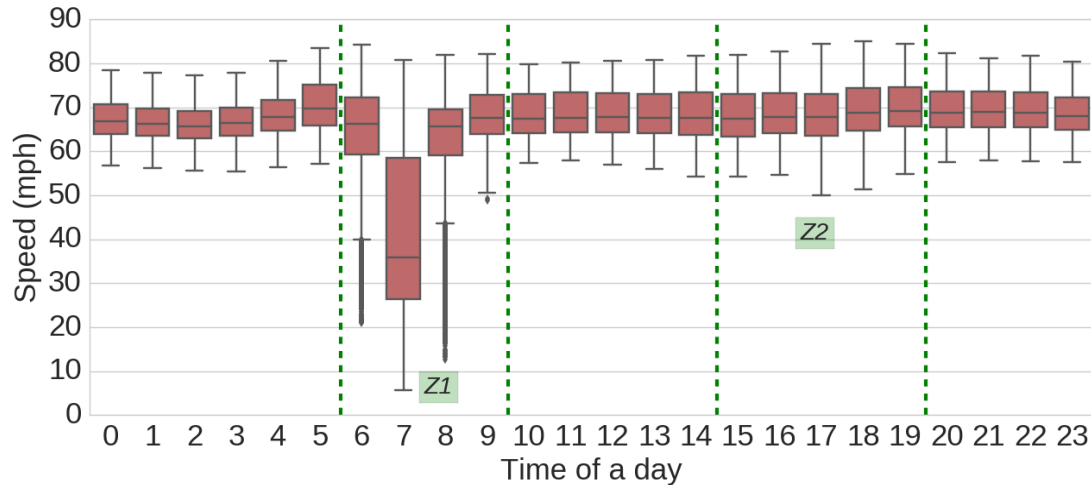
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- 4.8-miles basic freeway segment
- 65 mph posted speed limit
- One year traffic data were used in the analysis (2015)

# Data

- Hourly speed profile for the study segment

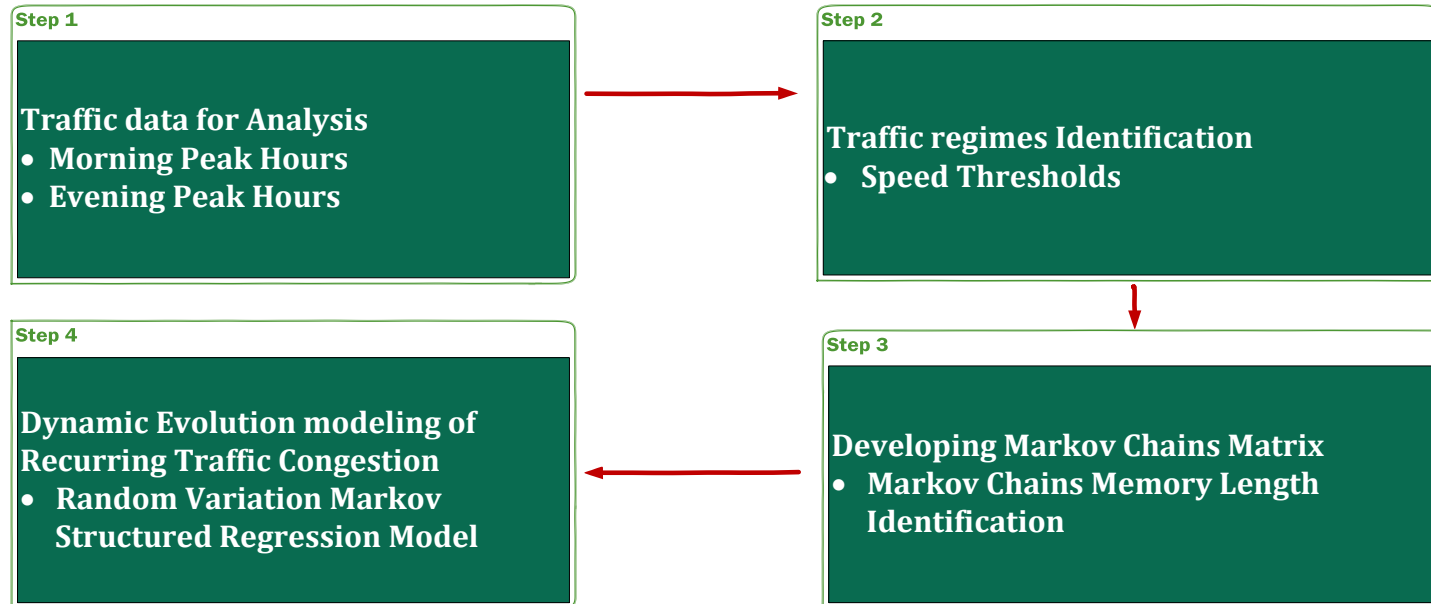


- Morning peak period (6am – 9am)
- Evening peak period (3pm – 7pm)

# Methodology

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- To evaluate the dynamic evolution of recurring traffic congestion, four steps were applied in the modeling process;

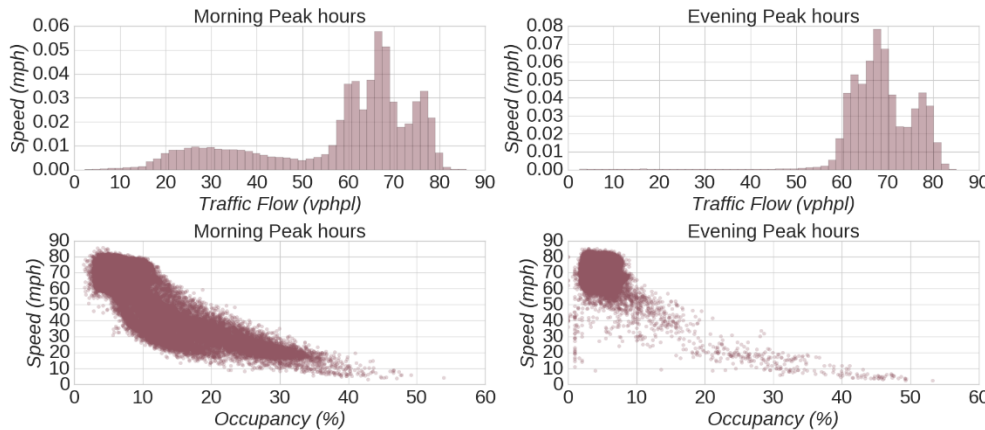




# Methodology

## Bayesian change point regression model

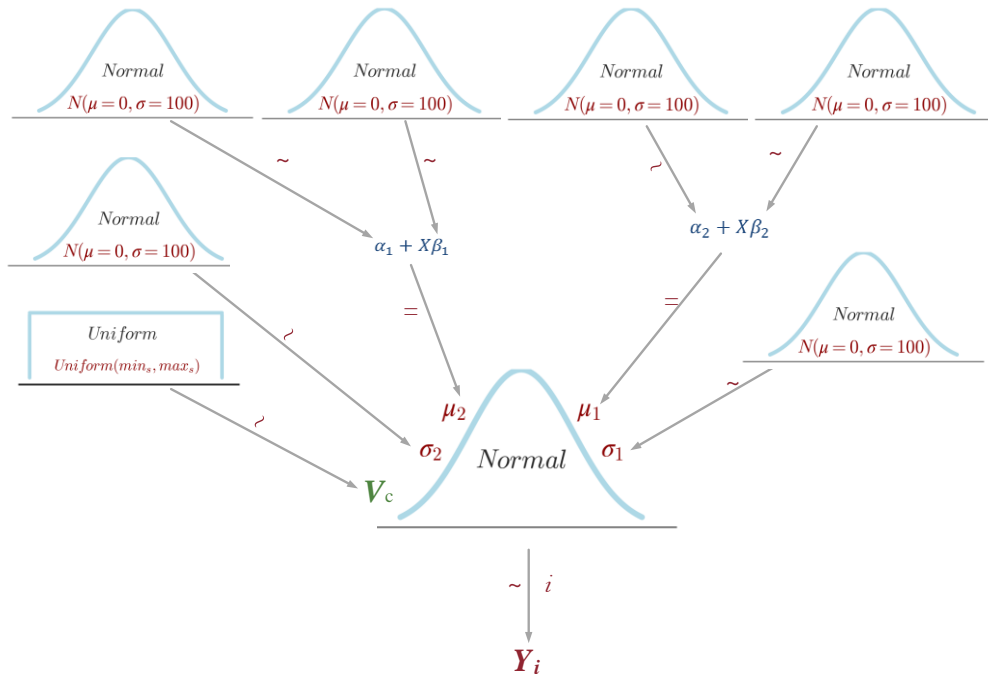
- A model that was used to estimate a speed threshold where patterns before and after the threshold are significantly different



- Non-linear relationship between speed and occupancy
- The two regressions are separated by the critical point called critical speed threshold

# Methodology

## Bayesian change point regression model



$$Y \sim \text{Normal}(\alpha_1 + X\beta_1, \sigma_2) \text{ if } X \leq V_c$$
$$Y \sim \text{Normal}(\alpha_2 + X\beta_2, \sigma_2) \text{ if } X > V_c$$

# Methodology

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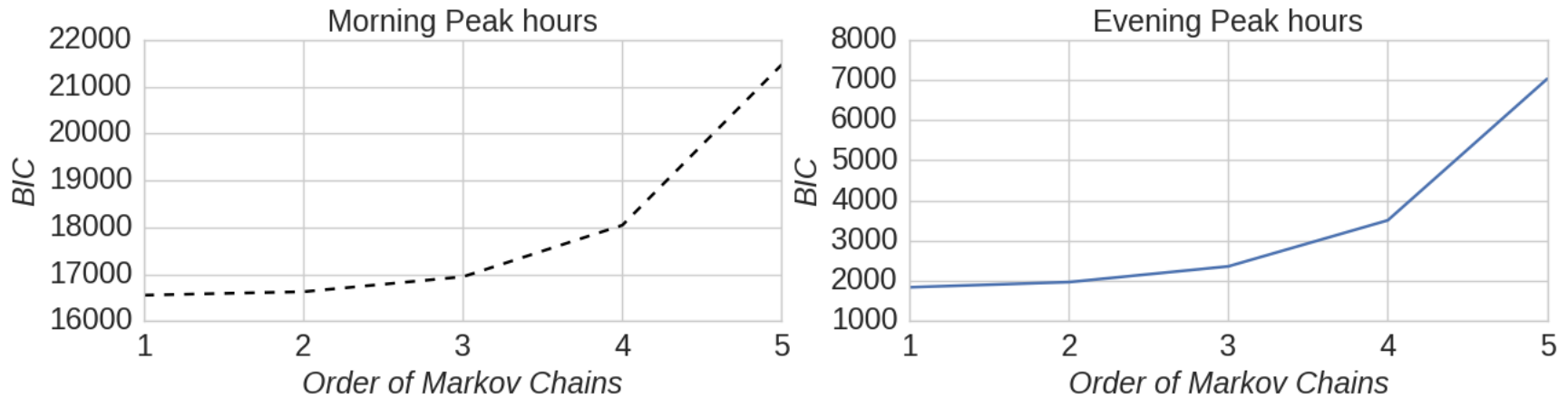
## Investigation of the Markov Chains Order

- Order of the Markov Chains was investigated using the Bayesian Information Criterion (BIC) approach
- The approach penalizes higher order models to balances the model complexity and the predictive accuracy to avoid the overfitting problem

$$BIC = -2 * \ln(L) + (|S|^m - |S|^{\ell})(|S| - 1) * \ln(n)$$

# Methodology

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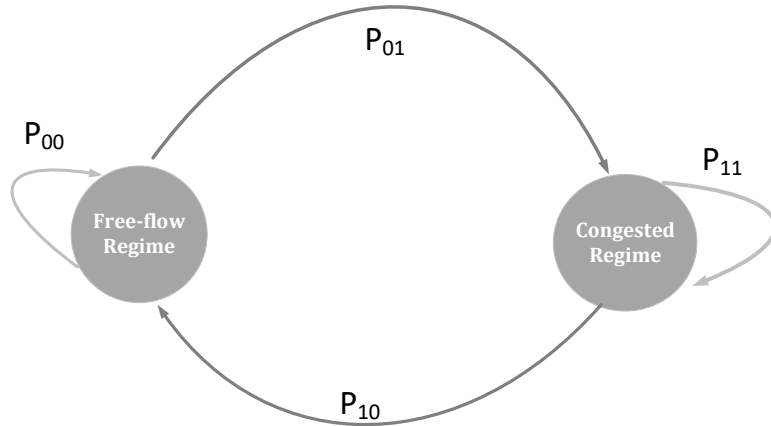


- The BIC approach favors lower order compared to higher order Markov Chains models

# Methodology

## Random Variation Markov Structured Model

- Discrete-time first-order Markov Chains models were developed for both the evening and the morning peak periods



The transition processes can be presented in the matrix format below;

$$P_{ij} = \begin{pmatrix} P_{00} & P_{01} \\ P_{10} & P_{11} \end{pmatrix}$$

# Methodology

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## Random Variation Markov Structured Model

$$P_{ij} = \begin{pmatrix} P_{00} & P_{01} \\ P_{10} & P_{11} \end{pmatrix}$$

$$P_{01} = Pr(Y_t = 1 | Y_{t-1} = 0, X_{t-1} = x) = \Phi(\beta_0 + \beta X_{i,t-1})$$

$$P_{11} = P(Y_t = 1 | Y_{t-1} = 1, X_{t-1} = x) = \Phi(\beta_0 + \beta X_{i,t-1})$$

$$P_{00} = 1 - P_{01} \text{ and } P_{11} = 1 - P_{10}$$

# Methodology

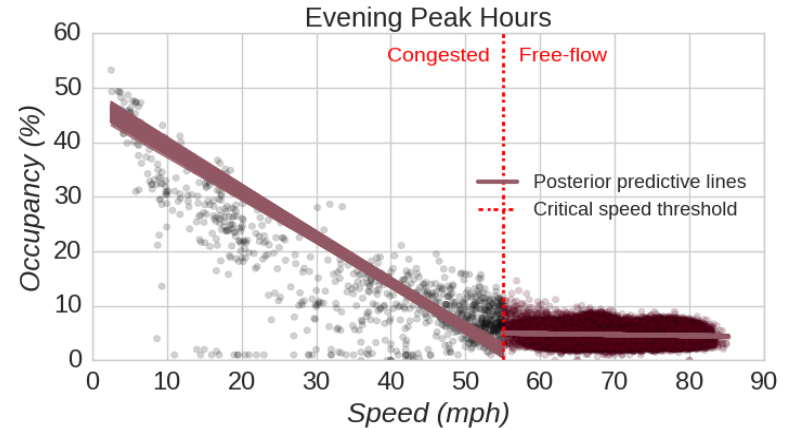
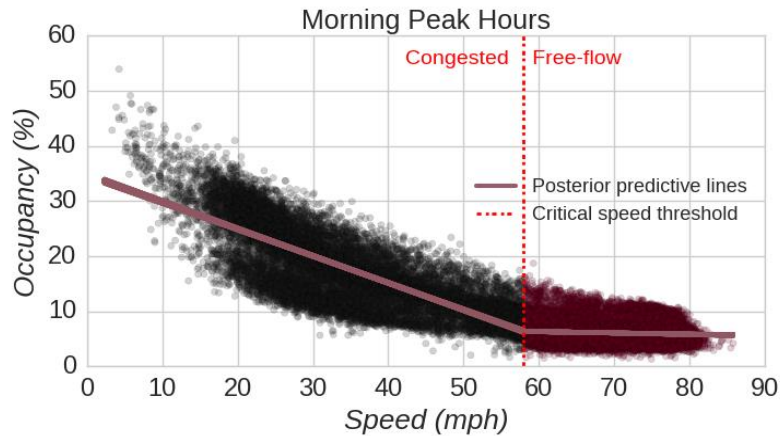
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## Bayesian Parameter Estimations

- The posterior distribution of the unknown parameters were estimated via the Markov Chain Monte Carlo simulations
- Two chains of 20,000 iterations were run (first 10,000 as burn-in)
- Gelman-Rubin statistic was used to assess the convergence of chains

# Results and Discussion

## Bayesian change point regression model

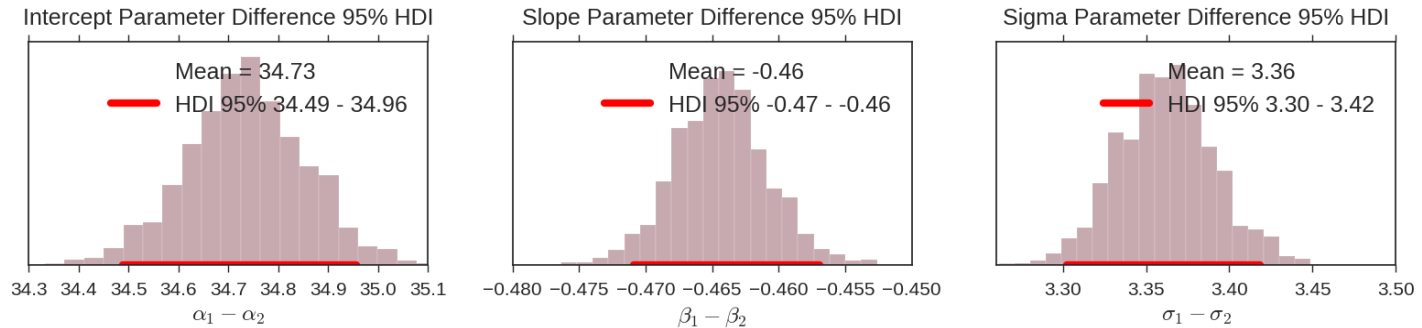


- Speed threshold during the morning and evening peak periods are 58 mph and 55 mph, respectively



# Results and Discussion

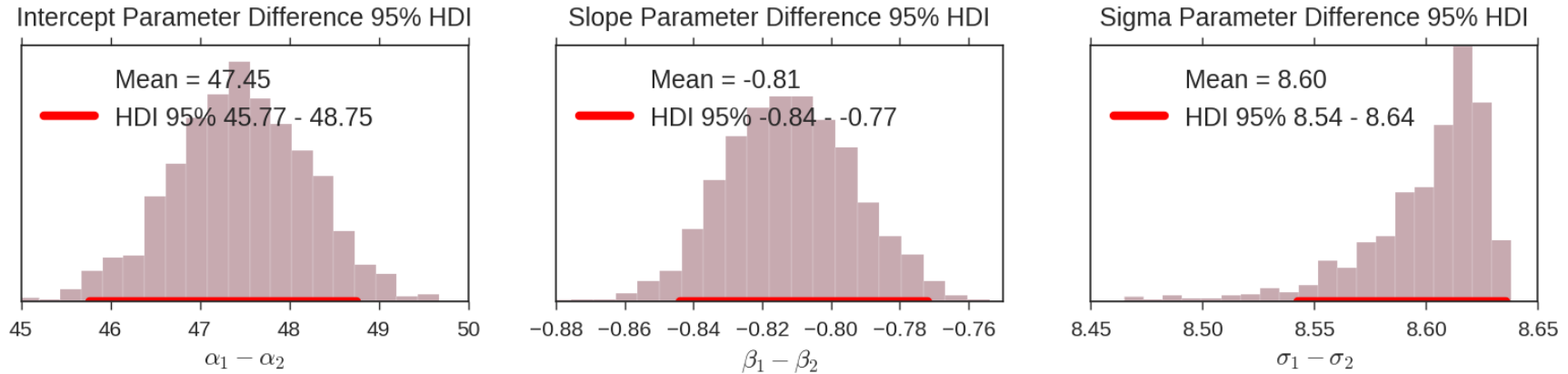
- The hypothesis test was conducted to verify if traffic patterns in the congested and free-flow regime are the same or credibly different.



Parameter posterior distributions differences for the morning peak period

- There is a statistically significant difference between the regression in free-flow and congested regime at 95% HDI

# Results and Discussion



Parameter posterior distributions differences for the evening peak period

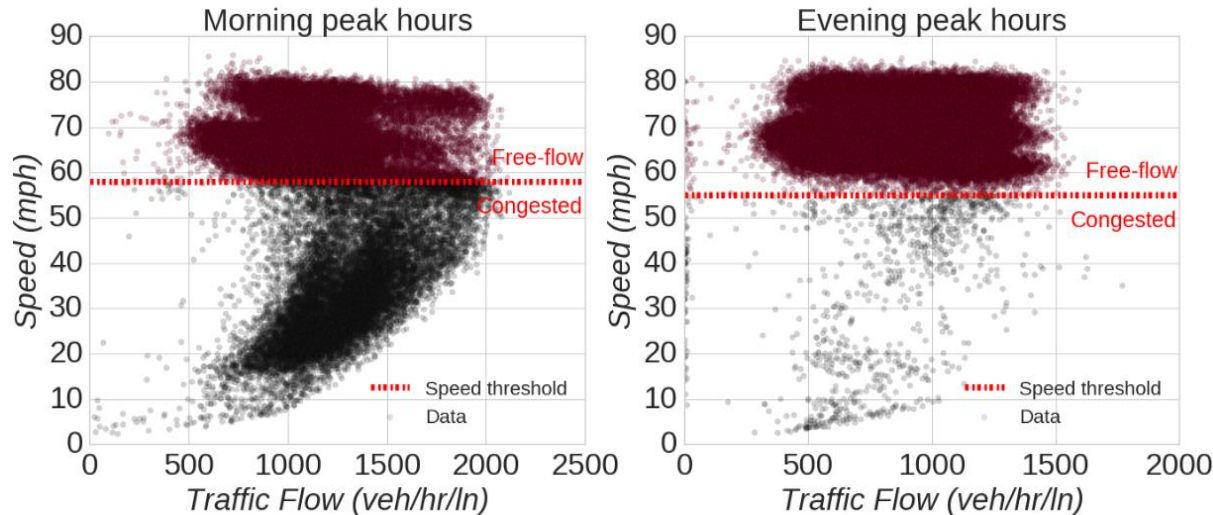
- There is a statistically significant difference between the regression in free-flow and congested regime at 95% HDI

# Results and Discussion

Variable	Posterior Mean	Posterior Std.	95% Credible Interval	
			lower	upper
<b>Morning Peak Period</b>				
<b>Remaining in a congested regime</b>				
Intercept	1.24	0.078	1.085	1.387
Flow rate ( <i>veh/hr/lane</i> )	0.00016*	0.00006	0.00004	0.00028
<b>Breakdown process</b>				
Intercept	-3.794	0.063	-3.914	-3.669
Flow rate ( <i>veh/hr/lane</i> )	0.00145*	0.00005	0.00136	0.00154
<b>Evening Peak Period</b>				
<b>Remaining in a congested regime</b>				
Intercept	2.066	0.197	1.688	2.464
Flow rate ( <i>veh/hr/lane</i> )	-0.0001	0.00021	-0.00153	0.00006
<b>Breakdown process</b>				
Intercept	-2.761	0.003	-2.970	-2.537
Flow rate ( <i>veh/hr/lane</i> )	-0.00021	0.00012	-0.00047	0.00001

- Traffic flow significantly influence the evolution process of traffic regime at 95% CI during the morning peak period
- For evening peak period, traffic flow was insignificant in influencing the evolution process of traffic regime at 95% CI

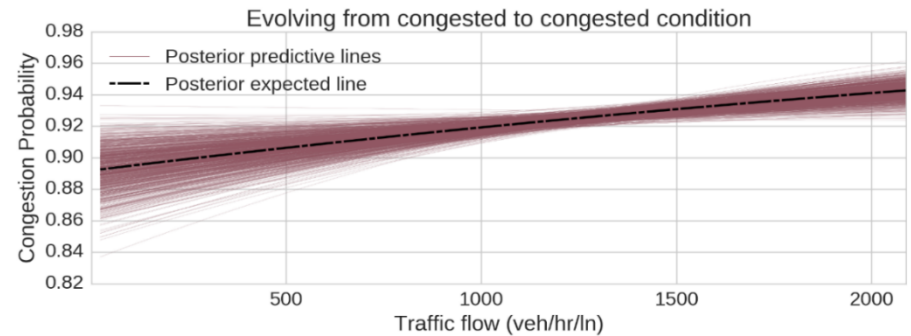
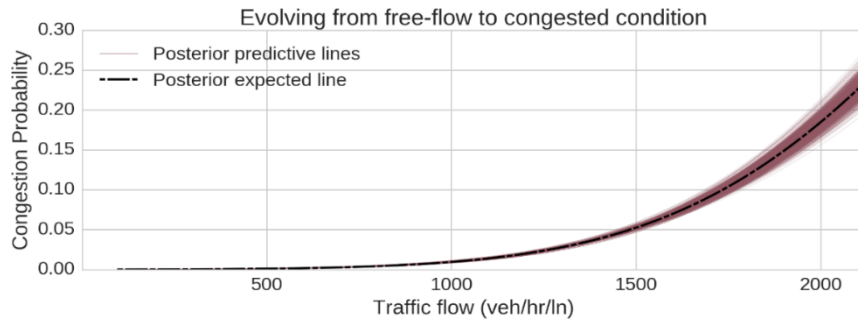
# Results and Discussion



- For evening peak period, the insignificance of traffic flow may be associated with few sample data in the congested regime
- Highly scattered data characteristic below the speed threshold may have also contributed

# Results and Discussion

## Posterior predictive line of transition probability



- The probabilities of remaining in the congested state are higher than those of breakdown process at the same traffic flow

# Conclusions

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- The morning peak congested state occurs once speed is below 58 (mph) while the evening peak period occurs at a speed below 55 mph
- The Information Criterion favored that first-order Markov Chains assumption was sufficient to characterize the evolution of traffic congestion
- Results of Bayesian change point and Markov model can be useful to traffic operators and planners in managing recurring traffic congestion

# Future Work

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- Bayesian change point regression can be modified to account for more than two traffic regimes as congested, free-flow, congestion onset/dissipation
- Additional work is needed to evaluate the influence of spatial location, vehicle mix, and weather conditions on the evolution of traffic congestion
- It will be beneficial to test the proposed approaches in different locations and different types of bottlenecks



**Thank you!**

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