

HomeWork 2

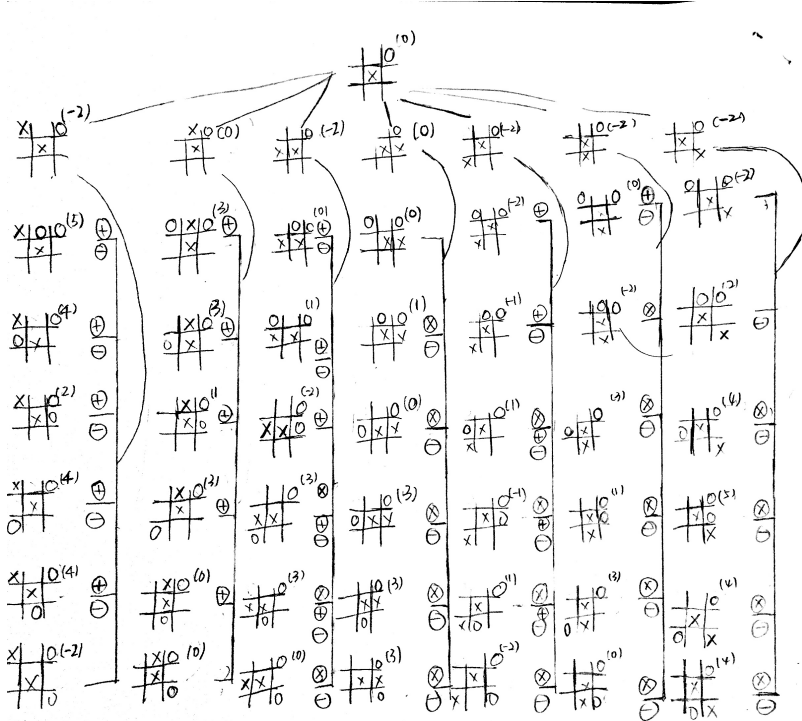
Name: *Liangjian Chen*

ID: #52006933

October 24, 2016

Problem 1 **Solution:**

- (a) $3^9 = 19683$, every cell would have 3 possible state(X,O,empty). But it may contains some illegal positions.
- (b) Maximum depth is 9(if the depth of root is 0). It does not contain all the board positions I counted in (a), but it does not contain additional board position.
- (c) The graph is below

Left to Right marked as \otimes Right to left marked as \oplus Optimal order marked as \ominus

Problem 2 Solution:

Yes, consider the following evaluation function f , $f(x) = 1$, if x is a winning state, $f(x) = -1$ if x is a lost state, and $f(x) = 0$ if x is a tie state. Applied $f(x)$ into this game, then we can use min-max algorithm in this game tree. Thus alpha-beta pruning can correctly applied in this problem.

Problem 3 Solution:

Let's name the node in each layer by the order from left to right.

- (a) move to first black circle.
- (b) In third layer (black square), $5^{th}, 8^{th}, 9^{th}, 11^{th}$ nodes with their subtree, would not be examined. In fourth layer, $4^{th}, 6^{th}$ nodes would not be examined.

Problem 4 Solution:

Assume $f(x) = 5ax + b$ where $a > 0$.

Because $f(x)$ monotonic increasing, $\forall x_1, x_2, x_1 > x_2, f(x_1) > f(x_2)$. So, the larger value remains relatively larger after transforming. Thus choice remains unchanged.

Problem 5 Solution:

Yes, the average over all n executions means the expectation of Min-Max value of this chance node. In every chance node, we can not calculate the deterministic Min-Max value, but we can use the Min-Max expectation to approximate how valuable this move is. Thus it is a good way to determining the best move.