

HomeWork 6

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Problem 1 **Solution:**

Define cost function as how many constraints are violated. At beginning the cost is 4.

- (a) In original expression, x and y could be same. Thus it should be revised as following:

$$\neg \exists x, y, n \text{ Person}(x) \wedge \text{Person}(y) \wedge \neg(x = y) \wedge \text{HasSS}\#(x, n) \wedge \text{HasSS}\#(y, n)$$

- (b) Yes, it is correct.

- (c) No. In original expression, it said that everyone has every different SSN, which obviously incorrect.

$$\forall x, n \text{ Person}(x) \wedge \text{HasSS}\#(x, n) \Rightarrow \text{Digits}(n, 9)$$

- (d) Assume $\text{SS}\#(x)$ means x 's social security number.

$$\neg \exists x, y \text{ Person}(x) \wedge \text{Person}(y) \wedge (\text{SS}\#(x) = \text{SS}\#(y))$$

$$\text{SS}\#(\text{Jhon}) = \text{SS}\#(\text{Mary})$$

$$\forall x \text{ Person}(x) \Rightarrow \text{Digits}(\text{SS}\#(x), 9)$$

Problem 2 **Solution:**

- (a) No
- (b) $x = A, y = B, z = B$
- (c) $x = \text{David}, \text{father}(x) = \text{George}$
- (d) $x = g(u) = g(f(v))$
- (e) $x = y = z = B$

Problem 3 **Solution:**

$$Alpine(Tony), Alpine(Mike), Alpine(John). \quad (1)$$

$$\forall x, Alpine(x) \Rightarrow (skier(x) \wedge \neg climber(x)) \vee (\neg skier(x) \wedge climber(x)) \quad (2)$$

$$\forall x, climber(x) \Rightarrow \neg like(x, Rain) \quad (3)$$

$$\forall x, skier(x) \Rightarrow like(x, snow) \quad (4)$$

$$\forall x, like(Jhon, x) \Rightarrow \neg like(Mike, x) \quad (5)$$

$$\forall x, \neg like(Jhon, x) \Rightarrow like(Mike, x) \quad (6)$$

$$\neg like(John, rain) \quad (7)$$

$$\neg like(John, snow) \quad (8)$$

Problem 4 **Solution:**

Problem 5 **Solution:**

Problem 6 **Solution:**

Problem 7 **Solution:**

Problem 8 **Solution:**