

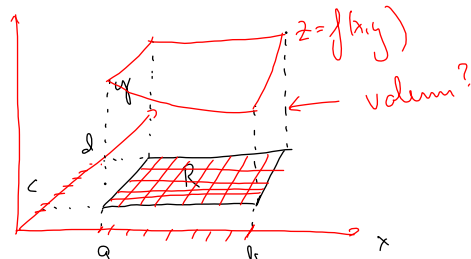
Kapittel 6

Omfangte: Onsdag: forelesning

Neste uke
Mandag: Plenum
Onsdag: Forelesning

Dobbelintegraler:

Idé:



$$z = f(x, y)$$

Sammenheng



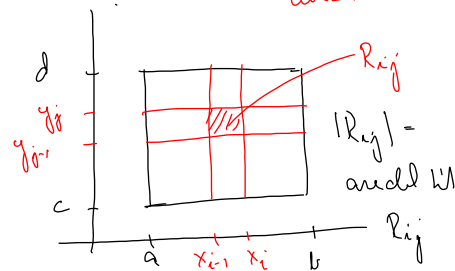
Π en partisjon av R

$$a = x_0 < x_1 < x_2 < \dots < x_n = b$$

$$c = y_0 < y_1 < y_2 < \dots < y_n = d$$

$$m_{ij} = \inf \{ f(x, y) : (x, y) \in R_{ij} \}$$

$$M_{ij} = \sup \{ f(x, y) : (x, y) \in R_{ij} \}$$



$$N(\Pi) = \sum_{ij} m_{ij} |R_{ij}| \quad \text{neder kraggesum}$$

Bør ha:

$$N(\Pi) \leq V \leq \Phi(\Pi)$$

$$\Phi(\Pi) = \sum_{ij} M_{ij} |R_{ij}| \quad \text{øvre kraggesum}$$

Neder integral: $\iint_R f(x, y) dx dy = \sup \{ N(\Pi) : \Pi \text{ en partisjon} \}$

Øvre integral: $\overline{\iint_R f(x, y) dx dy} = \inf \{ \Phi(\Pi) : \Pi \text{ en partisjon} \}$

Definisjon: Hvis $\iint_R f(x, y) dx dy = \overline{\iint_R f(x, y) dx dy}$, så sier vi at f er integrerbar over R og i så fall definerer vi (dobbel)integral til f over R ved

$$\iint_R f(x, y) dx dy = \iint_R f(x, y) dx dy = \overline{\iint_R f(x, y) dx dy}$$