

Q-1

$$S(x+1, y) + S(x-1, y)$$

In $S(x+1, y)$ is defined at $x=N-1, y=0$, Taking mod
Final function is.

$$S(x-(N-1), y) + S(x-1, y)$$

$$F(k, L) = \sum_{n=0}^{N-1} \sum_{m=0}^{M-1} \left(S(x-(N-1), y) + S(x-1, y) \right) e^{-j \frac{2\pi k n}{N}} e^{-j \frac{2\pi L m}{M}}$$

only defined at $x=N-1$ & $x=1, y=0$

using sifting property we get.

$$F(k, L) = e^{-j \frac{2\pi k}{N} (N-1)} e^0 + e^{-j \frac{2\pi k}{N}} e^0$$

$$F(k, L) = e^{-j \frac{2\pi k}{N} (N-1)} + e^{-j \frac{2\pi k}{N}}$$

Checking value at different point k, L in above equation.

① $(k, L) = (0, 0)$

$$F(0, 0) = e^0 + e^0 = 1 + 1 = 2$$

② $(k, L) = (N/2, M/2)$

$$F\left(\frac{N}{2}, \frac{M}{2}\right) = e^{-j \frac{2\pi k}{N} (N-1)} + e^{-j \frac{2\pi k}{N}}$$

$$F\left(\frac{N}{2}, \frac{M}{2}\right) = e^{-j \pi (N-1)} + e^{-j \pi}$$

We can see that \rightarrow High frequency, blocked.

value at $k = \frac{N}{2}, M = \frac{M}{2}$ is low which means

it block DC value, whereas Top left

~~allow DC value to pass~~

corner value ~~allow DC value to pass~~

so it's Low pass filter. $k=0, M=0$ \rightarrow low frequency

DC value passing through center are blocked.

whereas DC value can pass through top left + corner, which are

If $N \rightarrow$ even

$N-1 \rightarrow$ odd.

$$F\left(\frac{N}{2}, \frac{M}{2}\right) = e^{-j \pi} (-1)^{N-1} - 1 = -2$$

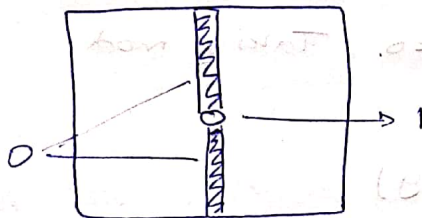
If $N \rightarrow$ odd

$(N-1) \rightarrow$ even

$$F\left(\frac{N}{2}, \frac{M}{2}\right) = (-1)^{N-1} - 1 = 1 - 1 = 0$$

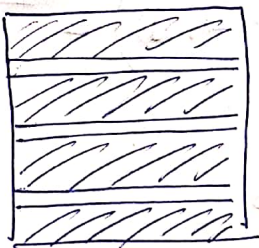
Q-2 Given an image having strong periodic lines.

For eliminating these lines, we can have a filter like the
In frequency domain, we can use Notch reject filter
In frequency domain.



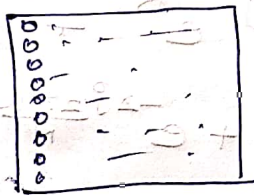
Black vertical strip with DC value at the center strip in frequency domain.

For a periodic image like this, (Below steps without shifting)



Taking 2DFFT of this image we get vertical column on the left with non-zero values.

In order to suppress them we can take Hadamard product with a filter having zero value at left vertical column in frequency domain.



On taking product this will remove those periodic lines.