

## **Recursive function of Fibonacci Function:**

```
int fibRec (int n) {  
    //Base Case  
    if(n<=0) return 0;  
    if(n==1) return 1;  
    //Recursive Representation  
    return fibRec(n-1) +fibRec(n-2);  
}
```

The function calls itself 2 times for each non-base case. This creates a recursion tree where:

- Each node branches into 2 more recursive calls
- The depth of the tree is n
- The total number of function calls is approximately  $2^n$

So, the Big O notation for this is  $O(2^n)$ . The time complexity is  $O(2^n)$  for recursive function

## **Non-Recursive Function for Fibonacci Function:**

```
int fibLoop (int n){  
    //Base Case  
    if(n<=0) return 0;  
    if(n==1) return 1;  
    int fim1=1, fim2=0, fi=fim1+fim2;  
    for (int i=2; i<n; i++) {  
        fim2=fim1;  
        fim1=fi;  
        fi=fim1+fim2;  
    }  
    return fi;  
}
```

This function uses one loop that runs n-2 times. Each step inside the loop takes  $O(1)$  time. This means it takes the same amount of time regardless of n. The other operations outside the loop also take  $O(1)$  time.

Time complexity =  $O(n) + O(1) = O(n)$

We only keep  $O(n)$  in the final answer because when n gets large, the  $O(1)$  part becomes insignificant compared to  $O(n)$ . Therefore, the non-recursive Fibonacci function has a time complexity of  $O(n)$ .