

CS590 homework 3 – Binary-Search, and Red-black Trees

The due date for this assignment is **Friday, April 9th, at 11.59pm**. This assignment is worth 10% of your final grade.

Any sign of collaboration will result in a 0 and being reported to the Graduate Academic Integrity Board. Late submission policy described in the syllabus will be applied.

(100 points)

We can use binary-search and red-black trees in order to sort an array of n integers by inserting them into an empty tree, and using a modified INORDER-TREE-WALK algorithm to copy the elements back to the array sorted.

1. You are given an implementation of red-black trees. Implement a binary-search tree with the corresponding functionality. You can omit the delete functionality for binary-search and red-black trees, but you have to modify the insertion routine of the binary-search and red-black tree to not allow duplicate values. The insertion functions should not insert a value if the value is already in the tree.

2. Modify the INORDER-TREE-WALK algorithm for binary-search and red-black trees such that it traverses the tree in order to copy its elements back to an array, in a sorted ascending order. The number of elements in the tree might be less than n due to the elimination of key duplicates. The function should therefore return the number n' of elements that were copied into the array (number of tree elements).

Notes: The algorithm relies only on the binary-search tree properties which also red-black trees satisfy. Keep in mind that only the first n' elements of your array are afterwards sorted. This should be implemented in the method `convert()` provided in the skeleton code.

3. Modify your insertion routine for binary-search and red-black trees such that it counts the following occurrences over the sequence of insertions.

- Counter for the number of duplicates.
- Counter for each of the insertion cases (case 1, case 2, and case 3) (red-black tree only).
- Counter for left rotate and for right rotate (red-black tree only).

You should have 1 counter for binary-search trees and 6 counters for red-black trees altogether.

4. Develop a test function for red-black trees such that, given a node of the red-black tree, traverses to each of the accessible leaves and counts the number of black nodes on the path to the leaf.

Notes: You could use your test function to verify whether or not your red-black tree implementation satisfies red-black property 5.

5. Measure the runtime performance of your "Binary-Search Tree Sort" and "Red-Black Tree Sort" for random, sorted, and inverse sorted inputs of size $n = 50000; 65000; 80000; 95000; 110000; 125000$. You can use the provided functions *create random*, *create sorted*, *create reverse sorted*.

Repeat each test a number of times (usually at least 7 times) and compute the average running time and the average counter values for each combination of input and size n . Report and comment on your results. How do the counters change in comparison to how the running time behaves.

(You might have to adjust the value for n dependent on your computers speed, but allow each test to take up to a couple of minutes. Start with smaller values of n and stop if one instance of the algorithm takes more than 3 min to complete).

Remarks:

- You are not allowed to use code from online resources. Your submission will be tested against that, and will receive a 0, and a report to the Graduate Academic Integrity Board if it is detected.
- Your report has to be typed, and submitted in a pdf file. You should provide figures that plot the running times in relation to the input size parameters.
- No additional libraries are allowed to be used
- A Makefile is provided for both problems to build the code in the Virtual Box
- Your code has to compile, and will be graded on the Virtual Box.
- The programming, and testing will take some time. Start early.
- Feel free to use the provided source code for your implementation. You have to document your code.