EDA Capstone

Capstone 2021: Exploratory Time Series Forecasting

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1 Data Set-up

```
download.file(
   "https://github.com/Kydoimos97/CapstoneMSBA2020/raw/main/Data/CapstoneProjectInfoRevised.rds",
   destfile = "CapstoneProjectInfoRevised.rds")

download.file(
   "https://github.com/Kydoimos97/CapstoneMSBA2020/raw/main/Data/CapstoneProjectProducts.rds",
   destfile= "CapstoneProjectProducts.rds")

df <- readRDS("CapstoneProjectInfoRevised.rds")
products <- readRDS("CapstoneProjectProducts.rds")</pre>
```

1.1 Setting Data Types

```
# Factorization
df$Site_ID <- as.factor(df$Site_ID)</pre>
df$Location_ID <- as.factor(df$Location_ID)</pre>
df$Locale <- as.factor(df$Locale)</pre>
df$Fiscal_Period <- as.factor(df$Fiscal_Period)</pre>
df$MPDS <- as.factor(df$MPDS)</pre>
df$Project <- as.factor(df$Project)</pre>
# Numeration
df$Quantity_Sold <- as.numeric(df$Quantity_Sold)</pre>
df$SQ_Footage <- as.numeric(df$SQ_Footage)# Shows Factor like tendencies
df$Periodic GBV <- as.numeric(df$Periodic GBV)</pre>
df$Current_GBV <- as.numeric(df$Current_GBV)</pre>
# Re-origin of Dates at 06/22/1998
x <- min(df$Open_Date)</pre>
df$Open_Date <- as_date(df$Open_Date, origin = x)</pre>
df$DATE <- as_date(df$DATE, origin = x)</pre>
rm(x)
# enables DATE to be used in prediction algorithms
```

A Date format in R is based on epoch time and thus easily convert to a number. The origin is reset to the earliest date present in the data set. Setting the origin allows us to work with an origin point that holds value [06/22/1998] instead of the arbitrary origin point of epoch [1/1/1970]

```
candy_vector <- c(products$Item_Desc)
id_vector <- c(products$Item_ID)

df$Item_desc <- df$Item_ID
df$Item_desc <- plyr::mapvalues(df$Item_desc, id_vector, candy_vector)</pre>
```

```
df$Item_ID <- as.factor(df$Item_ID)

# Reodering Data
df <- df[, c(1,2,6,17,7,3,12,13,14,10,11,8,9,15,16,4,5)]

#Rename Variables
names(df) <- tolower(make.names(names(df)))

rm(products, candy_vector, id_vector)</pre>
```

1.1.1 Removal and Creation of variables

```
# creation of tempdiff
df$temp_diff <- as.numeric(df$maxtemp-df$mintemp)

# Creation of cgbv_sqf
df$cgbv_sqf <- as.numeric(df$current_gbv/df$sq_footage)

# creation of diff_gbv
df$diff_gbv <- df$current_gbv - df$periodic_gbv

#Days open
x <- min(df$open_date)
df$days_open <- as.numeric(df$date-df$open_date)

rm(x)

df <- df[, c(1,2,3,4,21,6,7,19,20,10,18,12,13,14,15,16,17,8,9,11,5)]

df <- df[,-c(12,18,19,20,21)]</pre>
```

2 Time Series Model

2.1 Reshape Data Set

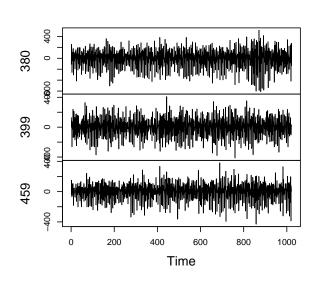
3 Dickey Fuller Test

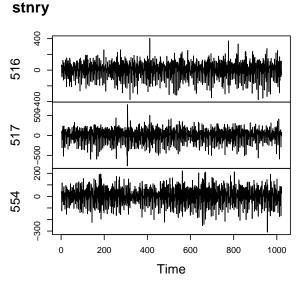
```
apply(mymts, 2, tseries::adf.test)
## Registered S3 method overwritten by 'quantmod':
##
    method
                       from
##
     as.zoo.data.frame zoo
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## $\380\
##
   Augmented Dickey-Fuller Test
##
##
## data: newX[, i]
## Dickey-Fuller = -4.3177, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
## $\399\
##
   Augmented Dickey-Fuller Test
##
## data: newX[, i]
## Dickey-Fuller = -5.3014, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
## $`459`
##
   Augmented Dickey-Fuller Test
##
##
## data: newX[, i]
## Dickey-Fuller = -5.1798, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
## $\\ 516\\
##
## Augmented Dickey-Fuller Test
## data: newX[, i]
```

```
## Dickey-Fuller = -5.2071, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
##
   $`517`
##
    Augmented Dickey-Fuller Test
##
##
## data: newX[, i]
  Dickey-Fuller = -5.7121, Lag order = 10, p-value = 0.01
   alternative hypothesis: stationary
##
##
## $`554`
##
##
    Augmented Dickey-Fuller Test
##
## data: newX[, i]
## Dickey-Fuller = -5.3323, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
```

3.1 Stationary Time Series

```
stnry <- MTS::diffM(mymts)
plot.ts(stnry)</pre>
```





apply(stnry, 2, tseries::adf.test)

Warning in FUN(newX[, i], ...): p-value smaller than printed p-value

```
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## Warning in FUN(newX[, i], ...): p-value smaller than printed p-value
## $\380\
##
   Augmented Dickey-Fuller Test
##
##
## data: newX[, i]
## Dickey-Fuller = -11.839, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
## $\399\
##
   Augmented Dickey-Fuller Test
##
## data: newX[, i]
## Dickey-Fuller = -12.31, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
## $`459`
##
## Augmented Dickey-Fuller Test
##
## data: newX[, i]
## Dickey-Fuller = -13.095, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
## $`516`
## Augmented Dickey-Fuller Test
##
## data: newX[, i]
## Dickey-Fuller = -12.635, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
##
##
## $\517\
##
## Augmented Dickey-Fuller Test
## data: newX[, i]
## Dickey-Fuller = -11.493, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
```

```
##
##
## $`554`
##
## Augmented Dickey-Fuller Test
##
## data: newX[, i]
## Dickey-Fuller = -11.738, Lag order = 10, p-value = 0.01
## alternative hypothesis: stationary
```

3.2 Variable Selection

```
vars::VARselect(stnry,
          type = "none", #type of deterministic regressors to include. We use none becasue the time ser
          lag.max = 10) #highest lag order
## $selection
## AIC(n)
          HQ(n) SC(n) FPE(n)
##
              7
                     6
##
## $criteria
## AIC(n) 5.418079e+01 5.343327e+01 5.291415e+01 5.244901e+01 5.187072e+01
## HQ(n) 5.424726e+01 5.356622e+01 5.311358e+01 5.271492e+01 5.220310e+01
## SC(n) 5.435579e+01 5.378329e+01 5.343918e+01 5.314905e+01 5.274576e+01
## FPE(n) 3.391692e+23 1.606117e+23 9.557279e+22 6.002610e+22 3.366753e+22
## AIC(n) 5.144295e+01 5.132462e+01 5.130901e+01 5.130398e+01 5.131036e+01
## HQ(n) 5.184181e+01 5.178996e+01 5.184083e+01 5.190227e+01 5.197513e+01
## SC(n) 5.249300e+01 5.254968e+01 5.270908e+01 5.287905e+01 5.306044e+01
## FPE(n) 2.195171e+22 1.950400e+22 1.920467e+22 1.911168e+22 1.923838e+22
```

3.3 Time Series Regression

Sample size: 1009

Log Likelihood: -33954.634

Roots of the characteristic polynomial:

```
## 0.9924 0.9924 0.9888 0.9888 0.9634 0.9634 0.91 0.91 0.8946 0.8946 0.8926 0.8926 0.8891 0.8891 0.88
## Call:
## vars::VAR(y = stnry, type = "none", lag.max = 25, ic = "AIC")
## Estimation results for equation X380:
## X380 = X380.11 + X399.11 + X459.11 + X516.11 + X517.11 + X554.11 + X380.12 + X399.12 + X459.12 + X51.11 + X516.11 
##
##
                    Estimate Std. Error t value Pr(>|t|)
## X380.11 -0.820314 0.035843 -22.886 < 2e-16 ***
                 0.020621
                                     0.043840
                                                    0.470 0.638201
## X399.11
## X459.11 0.083120 0.048072
                                                    1.729 0.084129 .
                0.236692 0.050018
                                                    4.732 2.57e-06 ***
## X516.11
## X517.11
                                                    3.747 0.000190 ***
                 0.119967
                                     0.032013
## X554.11
                  0.184782
                                     0.064116 2.882 0.004043 **
## X380.12 -0.814940 0.046932 -17.364 < 2e-16 ***
## X399.12
                  0.036705 0.057047
                                                    0.643 0.520110
## X459.12 -0.023213 0.062658 -0.370 0.711115
## X516.12
                  0.193050 0.066606
                                                     2.898 0.003839 **
## X517.12
                 ## X554.12
                  0.256324 0.084875
                                                    3.020 0.002596 **
## X380.13 -0.788871
                                     0.055636 -14.179 < 2e-16 ***
## X399.13 -0.027826 0.064784 -0.430 0.667646
## X459.13 -0.050483 0.074635 -0.676 0.498961
## X517.13
                 0.166867
                                                    3.657 0.000270 ***
                                     0.045632
## X554.13
                 ## X380.14 -0.676470 0.062457 -10.831 < 2e-16 ***
## X399.14 -0.109080 0.070287 -1.552 0.121021
## X459.14 -0.072893
                                     0.082003 -0.889 0.374285
## X517.14 0.181993
                                     0.049161 3.702 0.000227 ***
## X554.14
                                     0.105706 3.596 0.000341 ***
                  0.380074
## X380.15 -0.553224 0.067351 -8.214 7.11e-16 ***
## X399.15 -0.080972 0.074776 -1.083 0.279149
## X459.15 -0.086616 0.087259 -0.993 0.321151
## X516.15
                  0.033956 0.090193 0.376 0.706641
## X517.15
                  0.117044 0.051911
                                                    2.255 0.024384 *
## X554.15
                  ## X380.16 -0.484846 0.070187 -6.908 9.10e-12 ***
                  0.049733 0.077372
                                                    0.643 0.520530
## X399.16
## X459.16 -0.095784 0.091785 -1.044 0.296957
                 0.016053 0.093434
                                                   0.172 0.863624
## X516.16
## X517.16
                  0.086444
                                     0.053095
                                                    1.628 0.103843
                                                   2.260 0.024057 *
## X554.16
                  0.258509
                                     0.114389
## X380.17 -0.274257
                                     0.072248 -3.796 0.000157 ***
## X399.17
                  0.011893
                                     0.078123 0.152 0.879030
## X459.17
                  0.016815
                                     0.093902 0.179 0.857921
## X516.17
                    0.158358
                                     0.094451
                                                     1.677 0.093954 .
                    ## X517.17
## X554.17
                   0.239117
                                     0.115588 2.069 0.038849 *
## X380.18 -0.296701
                                     0.070826 -4.189 3.07e-05 ***
```

X399.18 -0.005366 0.077397 -0.069 0.944743

```
## X459.18 -0.114866
                                           0.091441 -1.256 0.209367
## X516.18 -0.023302
                                           0.093331 -0.250 0.802894
## X517.18
                    0.144392
                                           0.053256
                                                            2.711 0.006826 **
## X554.18
                                                              1.287 0.198368
                     0.146708
                                           0.113981
## X380.19
                    -0.258018
                                           0.067609 -3.816 0.000144 ***
## X399.19 -0.013091
                                           0.074977 -0.175 0.861433
## X459.19 -0.039215
                                           0.087065 -0.450 0.652518
## X516.19
                     0.057495
                                           0.090357
                                                              0.636 0.524728
## X517.19
                       0.079280
                                           0.052102
                                                              1.522 0.128443
## X554.19
                       0.110622
                                           0.111376
                                                            0.993 0.320857
## X380.110 -0.194026
                                           0.063055 -3.077 0.002152 **
## X399.110 -0.027636
                                           0.070322 -0.393 0.694410
## X459.110 -0.002541
                                           0.081581 -0.031 0.975154
## X516.110 0.113912
                                           0.086277
                                                            1.320 0.187056
## X517.110 0.021603
                                           0.049498
                                                            0.436 0.662617
## X554.110 0.125336
                                           0.106662
                                                              1.175 0.240265
## X380.111 -0.156532
                                           0.056044 -2.793 0.005329 **
## X399.111 -0.064758
                                           0.064869 -0.998 0.318403
## X459.111 -0.092814
                                           0.074131 -1.252 0.210875
## X516.111 0.089479
                                           0.078548
                                                             1.139 0.254925
## X517.111 0.064517
                                           0.046070
                                                            1.400 0.161725
## X554.111 0.136345
                                           0.099665
                                                             1.368 0.171634
## X380.112 -0.110712
                                           0.047462 -2.333 0.019880 *
## X399.112 0.005470
                                           0.056688
                                                             0.096 0.923145
## X459.112 -0.024618
                                           0.062663 -0.393 0.694510
## X516.112 0.094042
                                           0.066645
                                                             1.411 0.158553
## X517.112 -0.003106
                                           0.041323 -0.075 0.940092
## X554.112 -0.037024
                                           0.087610 -0.423 0.672684
## X380.113 -0.106708
                                           0.035053 -3.044 0.002398 **
                                                            0.120 0.904237
## X399.113 0.005146
                                           0.042758
## X459.113 -0.065729
                                           0.048583 -1.353 0.176414
## X516.113 -0.087617
                                           0.050962 -1.719 0.085900
## X517.113 -0.042804
                                           0.032326 -1.324 0.185779
## X554.113 -0.062817
                                           0.066161 -0.949 0.342635
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 90.73 on 931 degrees of freedom
## Multiple R-Squared: 0.7277, Adjusted R-squared: 0.7049
## F-statistic: 31.9 on 78 and 931 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation X399:
## X399 = X380.11 + X399.11 + X459.11 + X516.11 + X517.11 + X554.11 + X380.12 + X399.12 + X459.12 + X51.11 + X516.11 
##
##
                       Estimate Std. Error t value Pr(>|t|)
## X380.11
                       0.041821
                                           0.028599
                                                            1.462 0.143993
## X399.11
                    -0.844503
                                           0.034980 -24.142 < 2e-16 ***
## X459.11
                       0.037969
                                           0.038357
                                                              0.990 0.322491
## X516.11
                       0.113499
                                           0.039909
                                                            2.844 0.004553 **
## X517.11
                       0.096169
                                           0.025543 3.765 0.000177 ***
## X554.11
                       0.211341
                                           0.051158 4.131 3.93e-05 ***
```

```
## X380.12
             0.034520
                         0.037447
                                   0.922 0.356858
## X399.12
            -0.749873
                         0.045518 -16.474 < 2e-16 ***
## X459.12
            -0.036664
                         0.049995
                                   -0.733 0.463524
## X516.12
             0.100330
                         0.053145
                                    1.888 0.059355
## X517.12
             0.057463
                         0.032569
                                    1.764 0.078001 .
## X554.12
             0.294162
                         0.067721
                                    4.344 1.55e-05 ***
## X380.13
             0.010974
                         0.044392
                                    0.247 0.804806
## X399.13
            -0.683751
                         0.051691 -13.228 < 2e-16 ***
## X459.13
            -0.089669
                         0.059552
                                   -1.506 0.132474
## X516.13
             0.170178
                         0.062270
                                    2.733 0.006397 **
## X517.13
             0.069921
                         0.036410
                                    1.920 0.055115 .
## X554.13
             0.250576
                         0.078204
                                    3.204 0.001401 **
## X380.14
             0.027425
                         0.049835
                                    0.550 0.582227
                         0.056082 -11.829 < 2e-16 ***
## X399.14
            -0.663422
## X459.14
            -0.057798
                                   -0.883 0.377278
                         0.065430
## X516.14
             0.141625
                         0.068779
                                    2.059 0.039760 *
## X517.14
             0.113773
                         0.039226
                                    2.900 0.003814 **
## X554.14
             0.296864
                         0.084343
                                    3.520 0.000453 ***
## X380.15
             0.032413
                         0.053739
                                    0.603 0.546554
## X399.15
            -0.585207
                         0.059664
                                   -9.808 < 2e-16 ***
## X459.15
            -0.042167
                         0.069624
                                   -0.606 0.544902
## X516.15
             0.031744
                         0.071965
                                    0.441 0.659235
## X517.15
             0.070580
                         0.041420
                                    1.704 0.088711 .
## X554.15
             0.150172
                         0.088519
                                    1.697 0.090125
## X380.16
             0.086024
                         0.056002
                                    1.536 0.124858
## X399.16
            -0.459272
                         0.061735
                                   -7.439 2.30e-13 ***
## X459.16
            -0.042983
                         0.073236
                                   -0.587 0.557406
## X516.16
             0.013743
                         0.074551
                                    0.184 0.853784
## X517.16
             0.067934
                         0.042365
                                    1.604 0.109151
## X554.16
             0.011633
                         0.091271
                                    0.127 0.898610
## X380.17
             0.091852
                         0.057647
                                    1.593 0.111418
## X399.17
            -0.357511
                         0.062334
                                   -5.735 1.31e-08 ***
## X459.17
            -0.031142
                         0.074924
                                   -0.416 0.677762
## X516.17
             0.103486
                         0.075363
                                    1.373 0.170028
## X517.17
             0.105590
                         0.042694
                                    2.473 0.013570 *
## X554.17
             0.185800
                         0.092227
                                    2.015 0.044235 *
## X380.18
             0.052200
                         0.056512
                                    0.924 0.355885
## X399.18
            -0.329857
                                   -5.341 1.16e-07 ***
                         0.061755
## X459.18
            -0.062196
                         0.072961
                                   -0.852 0.394175
## X516.18
             0.106614
                         0.074469
                                    1.432 0.152578
## X517.18
             0.061329
                         0.042493
                                    1.443 0.149283
## X554.18
                         0.090945
             0.166792
                                    1.834 0.066976
                                    1.287 0.198242
## X380.19
             0.069454
                         0.053945
## X399.19
            -0.288786
                         0.059824
                                   -4.827 1.62e-06 ***
## X459.19
            -0.075186
                         0.069469
                                   -1.082 0.279403
             0.124822
## X516.19
                         0.072096
                                    1.731 0.083722 .
## X517.19
             0.032072
                         0.041572
                                    0.771 0.440618
## X554.19
             0.078657
                         0.088867
                                    0.885 0.376325
## X380.110 0.033469
                         0.050312
                                    0.665 0.506069
## X399.110 -0.271502
                         0.056110
                                   -4.839 1.53e-06
## X459.110 -0.081516
                         0.065093
                                   -1.252 0.210778
## X516.110 0.110150
                         0.068840
                                    1.600 0.109920
## X517.110 0.031760
                         0.039495
                                    0.804 0.421510
## X554.110 0.168347
                         0.085106
                                    1.978 0.048213 *
```

```
## X380.111 0.088967
                                           0.044717
                                                            1.990 0.046932 *
## X399.111 -0.250157
                                           0.051759 -4.833 1.57e-06 ***
## X459.111 -0.081887
                                           0.059149 -1.384 0.166562
## X516.111 0.019220
                                                            0.307 0.759166
                                           0.062673
## X517.111 0.009232
                                           0.036759
                                                            0.251 0.801753
## X554.111 0.249865
                                           0.079523
                                                            3.142 0.001731 **
## X380.112 0.051314
                                           0.037870
                                                            1.355 0.175748
## X399.112 -0.169446
                                           0.045231 -3.746 0.000191 ***
## X459.112 -0.100981
                                           0.049999 -2.020 0.043702 *
## X516.112 0.026100
                                           0.053176
                                                            0.491 0.623670
## X517.112 -0.022252
                                           0.032972 -0.675 0.499916
## X554.112 0.107091
                                           0.069904
                                                             1.532 0.125871
## X380.113 -0.001548
                                           0.027969 -0.055 0.955873
                                           0.034117 -1.455 0.146131
## X399.113 -0.049624
                                           0.038765 -0.496 0.620348
## X459.113 -0.019209
## X516.113 0.018700
                                           0.040663
                                                              0.460 0.645712
## X517.113 -0.058679
                                           0.025793 -2.275 0.023131 *
## X554.113 0.002317
                                           0.052790
                                                            0.044 0.964995
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 72.39 on 931 degrees of freedom
## Multiple R-Squared: 0.7026, Adjusted R-squared: 0.6777
## F-statistic: 28.19 on 78 and 931 DF, p-value: < 2.2e-16
##
## Estimation results for equation X459:
## ===============
## X459 = X380.11 + X399.11 + X459.11 + X516.11 + X517.11 + X554.11 + X380.12 + X399.12 + X459.12 + X51.11 + X519.12 + X519.
##
##
                       Estimate Std. Error t value Pr(>|t|)
## X380.11
                       0.032595
                                          0.026592
                                                            1.226 0.220616
                                           0.032525
## X399.11
                       0.014562
                                                           0.448 0.654468
## X459.11
                    -0.829628
                                          0.035665 -23.261 < 2e-16
## X516.11
                    0.042363
                                          0.037109
                                                            1.142 0.253919
## X517.11
                       0.037517
                                           0.023751
                                                            1.580 0.114532
## X554.11
                       0.118925
                                           0.047568
                                                            2.500 0.012587 *
## X380.12
                      0.043028
                                           0.034819
                                                             1.236 0.216866
## X399.12 -0.014007
                                           0.042324 -0.331 0.740763
## X459.12 -0.833370
                                           0.046487 - 17.927 < 2e - 16
                                                            0.614 0.539198
## X516.12
                     0.030354
                                           0.049416
## X517.12
                      0.077048
                                          0.030284
                                                             2.544 0.011113 *
## X554.12
                                           0.062969
                                                           3.702 0.000226 ***
                       0.233121
## X380.13
                      0.058278
                                           0.041277
                                                             1.412 0.158318
## X399.13
                                           0.048064 -1.415 0.157441
                    -0.068004
## X459.13 -0.751488
                                           0.055373 -13.571 < 2e-16 ***
## X516.13
                     0.037060
                                           0.057901
                                                           0.640 0.522293
                                                              3.746 0.000191 ***
## X517.13
                      0.126807
                                           0.033855
## X554.13
                      0.258550
                                           0.072717
                                                               3.556 0.000396 ***
## X380.14
                      0.108651
                                           0.046338
                                                              2.345 0.019249 *
## X399.14 -0.040370
                                           0.052147 -0.774 0.439033
## X459.14 -0.705707
                                           0.060839 -11.600 < 2e-16 ***
## X516.14 -0.001641
                                           0.063953 -0.026 0.979537
```

```
## X517.14
             0.119543
                         0.036473
                                    3.278 0.001086 **
## X554.14
             0.241533
                         0.078424
                                    3.080 0.002132 **
                         0.049968
## X380.15
             0.120380
                                    2.409 0.016184 *
## X399.15
            -0.033599
                                   -0.606 0.544902
                         0.055477
## X459.15
            -0.706675
                         0.064739 -10.916 < 2e-16 ***
            -0.066458
## X516.15
                         0.066915
                                  -0.993 0.320883
## X517.15
             0.094146
                         0.038513
                                    2.445 0.014690 *
## X554.15
             0.236584
                         0.082307
                                    2.874 0.004140 **
## X380.16
             0.122805
                         0.052072
                                    2.358 0.018562 *
## X399.16
            -0.005184
                         0.057403
                                  -0.090 0.928066
## X459.16
            -0.637528
                         0.068097
                                   -9.362 < 2e-16 ***
## X516.16
            -0.022232
                         0.069319
                                   -0.321 0.748501
## X517.16
             0.094603
                         0.039392
                                    2.402 0.016520 *
                                    1.723 0.085274 .
## X554.16
             0.146200
                         0.084866
## X380.17
             0.132482
                         0.053602
                                    2.472 0.013629 *
## X399.17
             0.028441
                         0.057960
                                    0.491 0.623759
## X459.17
            -0.416120
                         0.069667
                                   -5.973 3.31e-09 ***
## X516.17
             0.122317
                         0.070075
                                    1.746 0.081224 .
## X517.17
             0.121558
                         0.039698
                                    3.062 0.002261 **
## X554.17
             0.148685
                         0.085756
                                    1.734 0.083280
## X380.18
             0.039607
                         0.052547
                                    0.754 0.451185
## X399.18
            -0.005007
                         0.057422
                                   -0.087 0.930535
            -0.402643
## X459.18
                         0.067841
                                   -5.935 4.14e-09 ***
## X516.18
             0.066550
                         0.069244
                                    0.961 0.336750
## X517.18
             0.101561
                         0.039511
                                    2.570 0.010312 *
## X554.18
             0.145673
                         0.084564
                                    1.723 0.085284
## X380.19
             0.020591
                         0.050160
                                    0.411 0.681527
## X399.19
            -0.014628
                         0.055626
                                   -0.263 0.792625
            -0.344925
## X459.19
                         0.064594
                                  -5.340 1.17e-07 ***
## X516.19
             0.066307
                         0.067037
                                    0.989 0.322866
## X517.19
             0.089480
                         0.038655
                                    2.315 0.020839 *
## X554.19
             0.074712
                         0.082631
                                    0.904 0.366141
## X380.110 0.004917
                         0.046781
                                    0.105 0.916312
## X399.110 -0.064330
                         0.052173
                                   -1.233 0.217880
## X459.110 -0.329924
                         0.060526
                                   -5.451 6.42e-08
## X516.110 0.071700
                         0.064010
                                    1.120 0.262940
## X517.110 0.061070
                         0.036723
                                    1.663 0.096657 .
## X554.110 0.210168
                         0.079134
                                    2.656 0.008046 **
## X380.111 0.031906
                         0.041579
                                    0.767 0.443072
## X399.111 -0.088924
                         0.048127
                                  -1.848 0.064966
## X459.111 -0.197304
                         0.054999
                                   -3.587 0.000351 ***
## X516.111 0.030586
                         0.058275
                                    0.525 0.599808
## X517.111 0.066310
                         0.034180
                                    1.940 0.052680
## X554.111 0.122320
                         0.073943
                                    1.654 0.098415
## X380.112 0.051465
                         0.035213
                                    1.462 0.144202
## X399.112 -0.042845
                         0.042057
                                   -1.019 0.308595
## X459.112 -0.179789
                         0.046490
                                   -3.867 0.000118 ***
## X516.112 0.027364
                         0.049445
                                    0.553 0.580109
## X517.112 0.035477
                         0.030658
                                    1.157 0.247503
## X554.112
            0.019529
                         0.064999
                                    0.300 0.763905
## X380.113 -0.035524
                         0.026006
                                  -1.366 0.172270
## X399.113 -0.027230
                         0.031723
                                  -0.858 0.390899
## X459.113 -0.079591
                         0.036045
                                  -2.208 0.027478 *
## X516.113 -0.032321
                         0.037810 -0.855 0.392865
```

```
## X517.113 -0.001147
                                           0.023983 -0.048 0.961849
                                           0.049086 -1.425 0.154596
## X554.113 -0.069929
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 67.31 on 931 degrees of freedom
## Multiple R-Squared: 0.6645, Adjusted R-squared: 0.6364
## F-statistic: 23.64 on 78 and 931 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation X516:
## X516 = X380.11 + X399.11 + X459.11 + X516.11 + X517.11 + X554.11 + X380.12 + X399.12 + X459.12 + X510.11 + X510
##
##
                       Estimate Std. Error t value Pr(>|t|)
## X380.11
                       0.043553
                                           0.026287
                                                               1.657 0.097889
## X399.11
                       0.008178
                                           0.032152
                                                               0.254 0.799280
## X459.11
                       0.055703
                                           0.035256
                                                             1.580 0.114451
## X516.11
                    -0.812567
                                           0.036682 -22.151 < 2e-16 ***
## X517.11
                       0.036546
                                           0.023478
                                                             1.557 0.119908
## X554.11
                                                            2.493 0.012843 *
                       0.117222
                                           0.047022
## X380.12
                       0.036171
                                           0.034419
                                                               1.051 0.293587
## X399.12
                       0.001867
                                           0.041837
                                                               0.045 0.964407
## X459.12
                       0.138399
                                          0.045953
                                                             3.012 0.002668 **
## X516.12
                   -0.798701
                                           0.048848 -16.351 < 2e-16 ***
## X517.12
                                                              1.830 0.067495
                      0.054797
                                           0.029936
## X554.12
                       0.145597
                                           0.062246
                                                               2.339 0.019543 *
## X380.13
                       0.022149
                                           0.040802
                                                             0.543 0.587370
## X399.13
                   -0.067083
                                           0.047512 -1.412 0.158305
## X459.13
                       0.110662
                                           0.054737
                                                               2.022 0.043490 *
## X516.13
                    -0.713904
                                           0.057235 -12.473 < 2e-16 ***
## X517.13
                       0.078461
                                           0.033466
                                                             2.344 0.019263 *
## X554.13
                       0.028829
                                           0.071881
                                                               0.401 0.688462
## X380.14
                       0.072435
                                           0.045805
                                                              1.581 0.114134
## X399.14
                   -0.059207
                                           0.051548 -1.149 0.251024
## X459.14
                       0.049555
                                           0.060140
                                                             0.824 0.410157
## X516.14
                    -0.600924
                                           0.063218 -9.506 < 2e-16 ***
## X517.14
                       0.085415
                                           0.036054
                                                               2.369 0.018036 *
## X554.14
                       0.032564
                                           0.077523
                                                             0.420 0.674541
## X380.15
                       0.096407
                                           0.049394
                                                             1.952 0.051263
## X399.15
                    -0.059698
                                           0.054840
                                                           -1.089 0.276611
## X459.15
                      0.054264
                                           0.063995
                                                             0.848 0.396689
## X516.15
                    -0.647086
                                           0.066146 -9.783 < 2e-16 ***
## X517.15
                       0.040668
                                           0.038071
                                                              1.068 0.285693
## X554.15
                       0.097614
                                           0.081362
                                                               1.200 0.230539
## X380.16
                       0.121296
                                           0.051474
                                                               2.356 0.018656 *
## X399.16
                    -0.028713
                                           0.056744 -0.506 0.612972
## X459.16
                      0.019654
                                           0.067314
                                                             0.292 0.770369
## X516.16
                    -0.503584
                                           0.068523
                                                            -7.349 4.36e-13 ***
                                                             1.104 0.270010
## X517.16
                       0.042977
                                           0.038939
## X554.16
                       0.094910
                                           0.083891
                                                              1.131 0.258204
## X380.17
                       0.161444
                                           0.052986
                                                               3.047 0.002377 **
## X399.17
                       0.025023
                                           0.057294 0.437 0.662396
```

```
## X459.17
                     0.088278
                                        0.068867
                                                        1.282 0.200207
## X516.17 -0.320652 0.069270 -4.629 4.19e-06 ***
## X517.17
                   0.108012
                                       0.039242 2.752 0.006030 **
## X554.17
                                                       0.996 0.319537
                     0.084427
                                       0.084771
## X380.18
                    0.099182 0.051943
                                                        1.909 0.056513
## X399.18 -0.009653 0.056762 -0.170 0.865003
## X459.18 -0.047617
                                       0.067061 -0.710 0.477854
## X516.18 -0.377612
                                       0.068448 -5.517 4.48e-08 ***
                   0.071097
## X517.18
                                       0.039057
                                                       1.820 0.069030 .
## X554.18
                  0.047522
                                       0.083592
                                                      0.569 0.569830
## X380.19
                   0.090333
                                       0.049584 1.822 0.068801
## X399.19 -0.039811
                                       0.054987 -0.724 0.469246
## X459.19 -0.054043 0.063852 -0.846 0.397558
## X516.19 -0.278090
                                       0.066266 -4.197 2.97e-05 ***
## X517.19
                   0.043150
                                       0.038211
                                                       1.129 0.259079
## X554.19 -0.019008
                                       0.081682 -0.233 0.816040
## X380.110 0.078677
                                       0.046244
                                                        1.701 0.089212
## X399.110 -0.089081
                                       0.051573 -1.727 0.084451
## X459.110 -0.032776
                                       0.059830 -0.548 0.583952
## X517.110 0.045344 0.036302 1.249 0.211943
                                       0.078225 -0.272 0.785832
## X554.110 -0.021262
## X380.111 0.080284
                                                        1.953 0.051084 .
                                       0.041102
## X399.111 -0.076476
                                       0.047574 -1.608 0.108282
## X459.111 -0.050843
                                       0.054367 -0.935 0.349936
## X516.111 -0.222168
                                       0.057606 -3.857 0.000123 ***
## X517.111 0.061417
                                       0.033787
                                                        1.818 0.069423
## X554.111 -0.015802 0.073093 -0.216 0.828890
## X380.112 0.084503 0.034808 2.428 0.015385 *
## X459.112 -0.037289
                                       0.045956 -0.811 0.417343
## X516.112 -0.152781
                                       0.048877 -3.126 0.001828 **
## X517.112 -0.023780 0.030306 -0.785 0.432861
## X554.112 -0.074043
                                       0.064252 -1.152 0.249463
## X380.113 0.008079 0.025707
                                                         0.314 0.753377
## X459.113 -0.012907
                                       0.035630 -0.362 0.717255
## X516.113 -0.159402
                                       0.037375 -4.265 2.20e-05 ***
## X517.113 -0.029373
                                       0.023707 -1.239 0.215668
## X554.113 -0.102994
                                       0.048522 -2.123 0.034049 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 66.54 on 931 degrees of freedom
## Multiple R-Squared: 0.6732, Adjusted R-squared: 0.6458
## F-statistic: 24.59 on 78 and 931 DF, p-value: < 2.2e-16
##
## Estimation results for equation X517:
## X517 = X380.11 + X399.11 + X459.11 + X516.11 + X517.11 + X554.11 + X380.12 + X399.12 + X459.12 + X51.11 + X517.11 + X519.12 + X519.
##
##
                     Estimate Std. Error t value Pr(>|t|)
```

```
## X380.11
             0.066703
                         0.040753
                                    1.637 0.102017
## X399.11
            -0.037210
                         0.049845
                                   -0.747 0.455544
## X459.11
            -0.040035
                         0.054658
                                   -0.732 0.464068
## X516.11
             0.084205
                                    1.481 0.139030
                         0.056869
## X517.11
            -0.728942
                         0.036398 -20.027 < 2e-16 ***
## X554.11
             0.205193
                         0.072899
                                    2.815 0.004984 **
## X380.12
             0.096142
                         0.053361
                                    1.802 0.071912
## X399.12
            -0.090354
                         0.064861
                                   -1.393 0.163943
## X459.12
            -0.073774
                         0.071241
                                   -1.036 0.300678
## X516.12
            -0.050766
                         0.075730
                                  -0.670 0.502800
## X517.12
            -0.586164
                         0.046410 -12.630 < 2e-16 ***
                                    3.280 0.001078
## X554.12
             0.316491
                         0.096501
## X380.13
             0.020053
                         0.063257
                                    0.317 0.751303
## X399.13
            -0.051439
                         0.073658
                                   -0.698 0.485135
## X459.13
            -0.022717
                                   -0.268 0.788989
                         0.084859
## X516.13
            -0.092779
                         0.088733
                                   -1.046 0.296021
                         0.051883
## X517.13
            -0.488026
                                   -9.406 < 2e-16 ***
## X554.13
             0.249163
                         0.111439
                                    2.236 0.025596
## X380.14
             0.075476
                         0.071013
                                    1.063 0.288127
## X399.14
            -0.065359
                         0.079916
                                   -0.818 0.413653
## X459.14
            -0.098462
                         0.093236
                                   -1.056 0.291219
            -0.080180
                                   -0.818 0.413515
## X516.14
                         0.098009
            -0.452377
## X517.14
                         0.055896
                                   -8.093 1.81e-15 ***
## X554.14
             0.337503
                         0.120186
                                    2.808 0.005087 **
## X380.15
             0.147181
                         0.076577
                                    1.922 0.054910
## X399.15
             0.009597
                         0.085019
                                    0.113 0.910147
## X459.15
                         0.099213
                                   -1.191 0.233867
            -0.118185
            -0.136730
                                   -1.333 0.182749
## X516.15
                         0.102548
## X517.15
            -0.415601
                         0.059022
                                   -7.041 3.69e-12 ***
## X554.15
             0.283324
                         0.126137
                                    2.246 0.024927 *
## X380.16
             0.210882
                         0.079801
                                    2.643 0.008365 **
## X399.16
             0.024368
                         0.087971
                                    0.277 0.781838
## X459.16
            -0.132963
                         0.104359
                                   -1.274 0.202949
## X516.16
            -0.119444
                         0.106233
                                   -1.124 0.261150
## X517.16
            -0.298869
                         0.060369
                                   -4.951 8.77e-07
## X554.16
             0.154304
                         0.130059
                                    1.186 0.235760
## X380.17
             0.201864
                         0.082145
                                    2.457 0.014175 *
## X399.17
             0.102192
                         0.088825
                                    1.150 0.250237
## X459.17
            -0.057930
                         0.106765
                                   -0.543 0.587541
## X516.17
             0.069003
                         0.107390
                                    0.643 0.520677
## X517.17
            -0.161687
                         0.060838
                                   -2.658 0.008003 **
## X554.17
             0.250610
                         0.131421
                                    1.907 0.056839
## X380.18
             0.148232
                         0.080528
                                    1.841 0.065976
## X399.18
             0.072486
                         0.087999
                                    0.824 0.410311
## X459.18
            -0.155726
                         0.103967
                                   -1.498 0.134513
            -0.036021
## X516.18
                         0.106117
                                   -0.339 0.734346
## X517.18
            -0.244961
                         0.060551
                                   -4.046 5.65e-05 ***
## X554.18
             0.340992
                         0.129594
                                    2.631 0.008648 **
## X380.19
             0.057995
                         0.076870
                                    0.754 0.450772
## X399.19
            -0.039778
                         0.085248
                                   -0.467 0.640880
## X459.19
            -0.188434
                         0.098991
                                   -1.904 0.057277
## X516.19
             0.039696
                         0.102734
                                    0.386 0.699289
## X517.19
            -0.273166
                         0.059239
                                   -4.611 4.56e-06 ***
## X554.19
             0.203980
                         0.126633
                                    1.611 0.107562
```

```
## X380.110 0.092786
                                       0.071693
                                                       1.294 0.195914
## X399.110 -0.023919 0.079955 -0.299 0.764890
## X459.110 -0.152917
                                       0.092756 -1.649 0.099569
## X516.110 0.027667
                                       0.098095
                                                       0.282 0.777977
## X554.110 0.337603 0.121273 2.784 0.005481 **
## X380.111 0.115228 0.063721
                                                       1.808 0.070879
## X459.111 -0.160631
                                       0.084286 -1.906 0.056986 .
## X516.111 -0.060184 0.089308 -0.674 0.500545
## X517.111 -0.121120 0.052381 -2.312 0.020979 *
                                                        2.529 0.011610 *
## X554.111 0.286557
                                       0.113318
## X380.112 0.076107
                                       0.053964 1.410 0.158777
## X399.112 -0.085975
                                       0.064453 -1.334 0.182557
                                       0.071247 -0.891 0.373414
## X459.112 -0.063447
## X516.112 -0.050751
                                       0.075775 -0.670 0.503173
## X517.112 -0.178250
                                       0.046984 -3.794 0.000158 ***
## X554.112 0.146847
                                       0.099612 1.474 0.140766
## X399.113 -0.025733 0.048615 -0.529 0.596710
## X459.113 -0.047781
                                       0.055239 -0.865 0.387269
                                       0.057943 -1.182 0.237600
## X516.113 -0.068476
## X517.113 -0.146703
                                       0.036754 -3.992 7.08e-05 ***
## X554.113 -0.081045
                                       0.075224 -1.077 0.281588
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 103.2 on 931 degrees of freedom
## Multiple R-Squared: 0.694, Adjusted R-squared: 0.6684
## F-statistic: 27.07 on 78 and 931 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation X554:
## =============
## X554 = X380.11 + X399.11 + X459.11 + X516.11 + X517.11 + X554.11 + X380.12 + X399.12 + X459.12 + X510.11 + X510
##
##
                       Estimate Std. Error t value Pr(>|t|)
## X380.11 -0.0124982 0.0191951 -0.651 0.515133
## X399.11 0.0041615 0.0234777
                                                         0.177 0.859350
## X459.11 -0.0154257 0.0257442 -0.599 0.549190
## X516.11
                  0.0494785 0.0267860
                                                          1.847 0.065038
## X517.11
                   0.0292346 0.0171440
                                                          1.705 0.088483 .
## X554.11 -0.8130048 0.0343361 -23.678 < 2e-16 ***
## X380.12
                   0.0160017 0.0251336
                                                          0.637 0.524499
## X399.12 -0.0656194 0.0305503 -2.148 0.031978 *
## X459.12 -0.0385315 0.0335553 -1.148 0.251140
## X516.12
                  0.0368231 0.0356695
                                                         1.032 0.302180
## X517.12
                   0.0342247 0.0218596
                                                           1.566 0.117768
## X554.12 -0.6866280 0.0454529 -15.106 < 2e-16 ***
## X380.13
                   0.0443260 0.0297946
                                                          1.488 0.137163
## X399.13 -0.0802001 0.0346937 -2.312 0.021014 *
## X459.13 -0.0613738 0.0399695 -1.536 0.124997
## X516.13
                   0.0006299 0.0417941
                                                          0.015 0.987979
```

```
## X517.13
             0.0498296 0.0244374
                                     2.039 0.041725 *
## X554.13
           -0.5757179
                        0.0524887 -10.968 < 2e-16 ***
## X380.14
             0.1085757
                        0.0334478
                                    3.246 0.001212 **
                        0.0376410
## X399.14
                                   -0.876 0.381254
           -0.0329737
## X459.14
            -0.0399136
                        0.0439153
                                   -0.909 0.363649
           -0.0356659
                        0.0461631
## X516.14
                                   -0.773 0.439952
## X517.14
             0.0352586
                        0.0263274
                                    1.339 0.180821
## X554.14
           -0.4450752
                        0.0566087
                                   -7.862 1.04e-14 ***
## X380.15
             0.0912954
                        0.0360684
                                    2.531 0.011532 *
## X399.15
           -0.0247662
                        0.0400447
                                   -0.618 0.536421
## X459.15
             0.0012593
                        0.0467301
                                    0.027 0.978507
## X516.15
           -0.0610361
                        0.0483010
                                   -1.264 0.206668
## X517.15
           -0.0031863
                        0.0277999
                                   -0.115 0.908776
## X554.15
           -0.4056550
                        0.0594116
                                   -6.828 1.55e-11 ***
## X380.16
            0.0971862
                        0.0375871
                                    2.586 0.009871 **
## X399.16
            -0.0029961
                        0.0414351
                                   -0.072 0.942371
## X459.16
             0.0268542
                        0.0491540
                                    0.546 0.584972
## X516.16
           -0.0095582
                        0.0500366
                                   -0.191 0.848548
## X517.16
            0.0016908
                        0.0284342
                                    0.059 0.952596
## X554.16
           -0.3226461
                        0.0612588
                                    -5.267 1.72e-07 ***
## X380.17
             0.0771029
                        0.0386910
                                    1.993 0.046576 *
## X399.17
           -0.0071996
                        0.0418372
                                    -0.172 0.863408
                                    0.577 0.563812
## X459.17
             0.0290357
                        0.0502873
                        0.0505816
## X516.17
             0.0452319
                                    0.894 0.371427
## X517.17
             0.0339096
                        0.0286552
                                    1.183 0.236966
## X554.17
            -0.1812289
                        0.0619007
                                   -2.928 0.003498 **
## X380.18
             0.0283523
                        0.0379295
                                    0.748 0.454950
## X399.18
           -0.0068859
                        0.0414484
                                   -0.166 0.868090
## X459.18
             0.0237947
                        0.0489693
                                    0.486 0.627145
## X516.18
           -0.0119435
                        0.0499819
                                   -0.239 0.811192
## X517.18
            -0.0231936
                        0.0285202
                                    -0.813 0.416292
## X554.18
           -0.2056310
                        0.0610402
                                   -3.369 0.000786 ***
## X380.19
            0.0177549
                        0.0362067
                                    0.490 0.623983
## X399.19
           -0.0473986
                        0.0401524
                                   -1.180 0.238116
## X459.19
             0.0276102
                        0.0466258
                                    0.592 0.553883
## X516.19
             0.0228944
                        0.0483888
                                    0.473 0.636228
## X517.19
           -0.0270011
                        0.0279023
                                   -0.968 0.333445
## X554.19 -0.2111451
                        0.0596452
                                   -3.540 0.000420 ***
## X380.110 -0.0149370
                        0.0337680
                                    -0.442 0.658344
## X399.110 -0.0538358
                        0.0376595
                                   -1.430 0.153184
## X459.110 0.0267151
                        0.0436890
                                    0.611 0.541029
## X516.110 0.0392456
                        0.0462038
                                    0.849 0.395876
## X517.110 -0.0133468
                        0.0265080
                                   -0.504 0.614730
## X554.110 -0.1744859
                        0.0571209
                                   -3.055 0.002317 **
## X380.111 -0.0148233
                        0.0300131
                                   -0.494 0.621497
## X399.111 -0.0355650
                        0.0347396
                                   -1.024 0.306215
## X459.111 0.0084500
                        0.0396995
                                    0.213 0.831491
## X516.111 -0.0025897
                        0.0420648
                                   -0.062 0.950923
## X517.111 -0.0194530
                        0.0246720
                                   -0.788 0.430624
## X554.111 -0.1669117
                        0.0533739
                                    -3.127 0.001820 **
## X380.112 0.0151653
                        0.0254175
                                    0.597 0.550887
## X399.112 -0.0339409
                        0.0303580
                                   -1.118 0.263845
## X459.112 0.0006901
                        0.0335578
                                    0.021 0.983599
## X516.112 0.0149678 0.0356907
                                    0.419 0.675039
```

```
## X517.112 -0.0600134 0.0221299 -2.712 0.006814 **
## X380.113 0.0002788 0.0187718
                                 0.015 0.988153
## X399.113 0.0071444 0.0228982
                                 0.312 0.755104
## X459.113 -0.0166942 0.0260179
                                -0.642 0.521262
## X516.113 -0.0579600 0.0272919 -2.124 0.033958 *
## X517.113 -0.0388769 0.0173113 -2.246 0.024954 *
## X554.113 -0.1545114 0.0354313 -4.361 1.44e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 48.59 on 931 degrees of freedom
## Multiple R-Squared: 0.6647, Adjusted R-squared: 0.6366
## F-statistic: 23.66 on 78 and 931 DF, p-value: < 2.2e-16
##
##
##
## Covariance matrix of residuals:
         X380 X399 X459
                             X516 X517
                                         X554
## X380 8230.6 1651.4 1804.7 1855.0 2515 750.6
## X399 1651.4 5240.4 912.5 1163.8 1889 742.5
## X459 1804.7 912.5 4530.0 1318.9
                                  1954 544.4
## X516 1855.0 1163.8 1318.9 4425.7
                                  2296 813.8
## X517 2514.9 1889.2 1953.5 2295.6 10637 1278.4
## X554 750.6 742.5 544.4 813.8 1278 2360.6
##
## Correlation matrix of residuals:
                                          X554
         X380
               X399
                      X459
                             X516
                                   X517
## X380 1.0000 0.2515 0.2956 0.3074 0.2688 0.1703
## X399 0.2515 1.0000 0.1873 0.2416 0.2530 0.2111
## X459 0.2956 0.1873 1.0000 0.2946 0.2814 0.1665
## X516 0.3074 0.2416 0.2946 1.0000 0.3346 0.2518
## X517 0.2688 0.2530 0.2814 0.3346 1.0000 0.2551
## X554 0.1703 0.2111 0.1665 0.2518 0.2551 1.0000
```

3.4 Serial Test

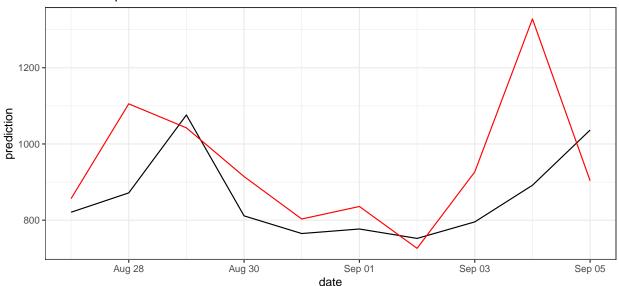
```
##
## Portmanteau Test (asymptotic)
##
## data: Residuals of VAR object var.a
## Chi-squared = 258.87, df = 108, p-value = 2.087e-14
```

3.5 Creating and preparing Predictions

```
# selecting the variables
# Granger test for causality
```

```
vars::causality(var.a, #VAR model
         cause = c("X380"))
## $Granger
##
## Granger causality HO: X380 do not Granger-cause X399 X459 X516 X517
##
   X554
##
## data: VAR object var.a
## F-Test = 1.5941, df1 = 65, df2 = 5586, p-value = 0.001783
##
##
## $Instant
##
## HO: No instantaneous causality between: X380 and X399 X459 X516 X517
##
  X554
##
## data: VAR object var.a
## Chi-squared = 152.99, df = 5, p-value < 2.2e-16
fcast = predict(var.a, n.ahead = 10)
par(mar = c(2.5, 2.5, 2.5, 2.5))
X380 = fcast$fcst[1]; X380
## $X380
##
                                   upper
                                               CI
              fcst
                        lower
          87.66732 -90.15249 265.48712 177.8198
   [1.]
   [2,]
          50.78343 -172.12985 273.69671 222.9133
##
   [3,] 204.46582 -24.88820 433.81984 229.3540
## [4,] -264.70409 -494.95216 -34.45601 230.2481
## [5,] -46.40174 -277.85129 185.04782 231.4496
## [6,]
          11.91893 -220.85695 244.69481 232.7759
## [7,] -24.70974 -258.86780 209.44832 234.1581
## [8,]
         43.29329 -200.08338 286.66996 243.3767
## [9,]
          96.14749 -151.60976 343.90474 247.7572
## [10,] 144.93731 -104.24321 394.11783 249.1805
x = X380$X380[,1]; x
   [1]
         87.66732
                    50.78343 204.46582 -264.70409 -46.40174
                                                                11.91893
   [7]
        -24.70974
                    43.29329
                               96.14749 144.93731
tail(mymts)
                            459
              380
                     399
                                   516
                                           517
                                                   554
##
## [1018,] 867.51 735.65 642.56 740.37 1120.12 312.84
## [1019,] 1114.71 647.80 839.44 685.29 1264.26 399.08
## [1020,] 697.20 603.41 453.36 603.04 973.41 231.36
## [1021,] 591.55 500.77 527.22 607.77 1014.68 265.72
## [1022,] 867.43 532.05 542.22 547.76 994.33 348.15
## [1023,] 733.10 560.13 548.26 662.33 1075.28 374.84
```

Relationship of sales and 380



```
test[,1]
```

```
## [1] 856.45 1105.29 1042.28 914.40 803.06 835.91 726.08 926.60 1328.08 ## [10] 903.53
```

3.6 Calculate Mean Difference

```
listsites <- c(380,399, 459, 516, 517, 554)
counter = 0
plot_list <- list(1)
g <- NULL
result <- NULL</pre>
```

```
for (i in listsites) {
  g <- NULL
  result <- NULL
  counter = counter+1
  x = fcast$fcst[counter]
  x = as.data.frame(x)
  x = unlist(x[1])
  p = as.numeric(tail(mymts,2)[2,counter])
  x = cumsum(x) + p
  par(mar = c(2.5, 2.5, 1, 2.5))
  g <- test[,counter]</pre>
  diff = g-x
  result <- data.frame(test = g,
                     difference = diff,
                     prediction = x,
                     date = datelist)
  o = ggplot(data=result, aes_string(x = "date", y="prediction")) +
      geom_line() + geom_line(aes_string(y="test"), color="red") + geom_line(aes_string(y="diff"), color
      theme_fivethirtyeight() + ggtitle(paste0("Site = ", as.character(i), sep= " ")) + theme(plot.titl
  assign(paste0("plt", i), o)
  plot list <- rlist::list.append(plot list, o)</pre>
  print(paste0("mean error for ",i, " = ", mean(diff)))
}
## [1] "mean error for 380 = 84.4700618869718"
## [1] "mean error for 399 = 14.7058416069735"
## [1] "mean error for 459 = 0.169449221575502"
## [1] "mean error for 516 = 91.68113802353"
## [1] "mean error for 517 = 27.259284097961"
## [1] "mean error for 554 = 33.2970098272065"
3.7 Plot Results
plot_list <- plot_list[-1]</pre>
nCol <- floor(sqrt(length(plot_list)))</pre>
grid.arrange(grobs=plot_list, widths = c(1,1), ncol=2, layout_matrix = rbind(c(1,2),
                                                                                    c(3,4),
                                                                                    c(5,6)),
             top = "Predicted time series")
```

Predicted time series

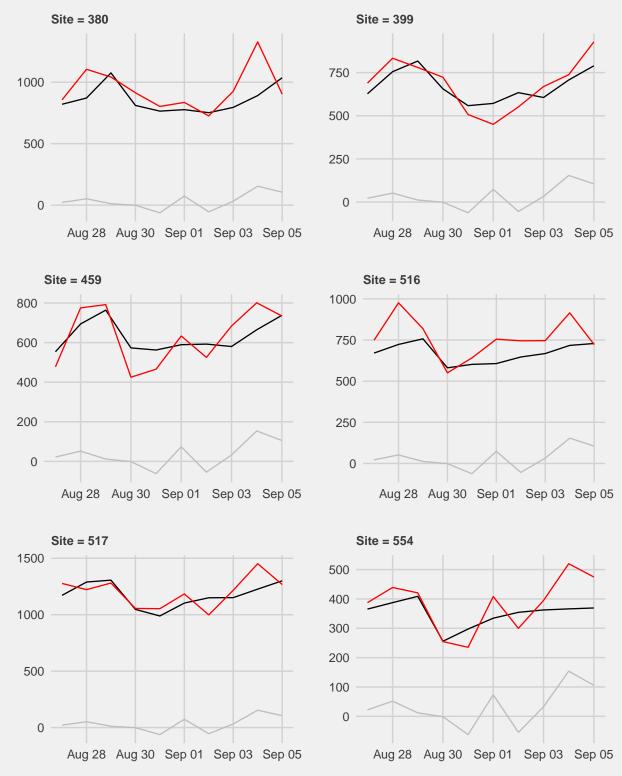


Figure 1: Predictions of Time Series