Stock Market Simulation Using Support Vector Machines

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ABSTRACT

The aim of this research was to analyse the different results that can be achieved using support vector machines (SVM) to forecast the weekly change movement of different simulated markets. The markets are developed by a GARCH model based on the S&P 500. These simulated markets are grouped by a main parameter: high volatility, bearish trend, bullish trend and low volatility. The inputs retained of the SVM are traditional technical trading rules used in quantitative analysis, such as relative strength index (RSI) and moving average convergence divergence (MACD) decision rules. The outputs of the SVM are the degree of set membership and market movement (bullish or bearish). The design of the SVM algorithm has been developed by Matlab and SVM-KM. The configuration for the SVM shows that the best results are achieved in simulated markets with high volatility; also results are good in trend simulated markets. Copyright © 2014 John Wiley & Sons, Ltd.

KEY WORDS support vector machines; stock market simulation; RSI, MACD

INTRODUCTION

Quantitative decision making in financial markets is a topic of constant innovation. Artificial intelligence is helping investors in this decision making. In order to manage money, trading systems are using neural networks (NN), genetic algorithm (GA), fuzzy logic and, more recently, support vector machines (SVMs). In this article, a trading system based on SVMs is developed.

The goal of this study is to understand where the trading system model is working better. In order to know this, different simulated markets are presented. The first simulated market is characterized by high volatility, the second simulated market is characterized by a bullish trend and the last one is characterized by a bearish trend. The different simulated markets are developed by a generalized autoregressive conditional heteroscedasticity (GARCH) model based on the S&P 500. A trading system for the prediction of the directional weekly movement of each kind of market has been developed in order to achieve the aim of the paper.

SVMs are a supervised learning technique used for data analysis and pattern recognition, mainly in classification problems, with an increasing number of real-world applications including finance. The parameters of the SVM such as kernel function and *C* parameter are changed in order to achieve better results.

Technical analysis is widely used by investors (Taylor and Allen, 1992) to make decisions. Owing to this importance, two of the main indicators of this analysis have been considered like inputs of this SVM, such as relative strength index (RSI) and moving average convergence divergence (MACD).

In this paper, we propose an intelligent stock trading system based on SVMs using technical analysis (RSI and MACD). The results demonstrate that this algorithm obtains better profits than buy and hold (BH) and naïve strategy, especially in the simulated markets with high volatility.

The rest of the paper is structured as follows. In the next section the literature review relevant to SVM and technical analysis is presented. The third section explains the simulation markets procedure. The fourth section explains the SVM trading algorithm created. The fifth section shows the empirical results of the trading system. Finally, the sixth section provides some concluding remarks.

LITERATURE REVIEW

In this section, the literature review relevant to the SVM and technical analysis is presented.

Support vector machines

A basic theory of the SVM classifier model is presented. SVMs are specific learning algorithms characterized by the capacity control of the decision function and the use of kernel functions (Vapnik, 1999; Cristianini and Taylor, 2000). The correct selection of the kernel function is very important.

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SVMs were originally developed by Vapnik (1998). For a detailed introduction to the subject, Burges (1998) and Evgeniou et al. (2000) are recommended.

The methods based on kernel functions suggest that instead of attaching an algebraic correspondence to each element of the input domain represented by

$$\Phi: X \to F \tag{1}$$

a kernel function

$$K: X \times X \to R \tag{2}$$

is used to calculate the similarity of each pair of objects in the input set. An example is illustrated in Figure 1 (Huang and Sun, 2001).

The biggest difference between SVMs and other traditional methods of learning is that SVMs do not focus on an optimization protocol that makes minimal errors as with other techniques. Traditionally, most learning algorithms have focused on minimizing errors generated by their models. They are based on what is called the principle of empirical risk minimization (ERM). The goal of SVM is different. It does not seek to reduce the empirical risk of making just a few mistakes, but intends to build reliable models. This principle is called structural risk minimization. The SVM searches a structural model that has little risk of making mistakes with future data.

The main idea of SVMs is to construct a hyperplane as the decision surface so that the margin of separation between positive and negative examples is maximized (Xu et al., 2009); it is called the optimum separation hyperplane (OSH), as shown in Figure 1.

Given a training set of instance-label pairs (\mathbf{x}_i, y_i) , i = 1, ..., m, where $\mathbf{x}_i \in \mathcal{R}^n$ and $y_i \in \{1, -1\}$, y_i indicating the class to which the point x_i belongs, the SVMs require the solution of the following problem:

$$\min_{\mathbf{w}, \xi, b} \left\{ \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{i=1}^n \xi_i \right\}$$
 (3)

subject to

$$y_i(\mathbf{w} \cdot \mathbf{x}_i - b) \ge 1 - \xi_i$$
$$\xi_i \ge 0 \tag{4}$$

where ξ_i are the slack variables introduced by the method which measures the degree of misclassification of the data \mathbf{x}_i ; w is the normal vector to the hyperplane; b is the offset of the hyperplane from the origin along the normal vector w; and C > 0 is the penalty parameter of the error term. Different values of parameter C are tested in order to achieve the best results to forecast the movement.

SVMs can be used in two different ways: for classification or regression. Recently there have been reports of the use of SVMs to solve financial forecasting problems.

Two applications on SVM financial time series forecasting were developed in 2003: in Cao and Tay (2003), SVMs are applied to the problem of forecasting several futures contracts from the Chicago Mercantile Market, showing the superiority of SVMs over back-propagation and regularized radial basis function neural networks; in Kim (2003), SVMs are used to predict the direction of change in the daily Korean composite stock index and they are benchmarked against back-propagation neural networks and case-based reasoning. The experimental results show that SVMs outperform the other methods and that they should be considered as a promising methodology for financial time series forecasting. In Huang et al. (2005), an SVM classifier is used to predict the directional movement

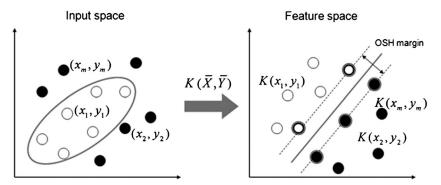


Figure 1. An example of how a kernel function works

of the Nikkei 225 index with extremely promising results. Also Ince and Trafalis (2006) try to solve portfolio problems optimization using SVM.

Lastly, Lee (2009) explains a prediction model based on SVM with a hybrid feature selection to predict the trend of stock markets. It is shown that SVM outperforms back-propagation neural networks in the problem of stock trend prediction. Dunis *et al.* (2013a) show that it is possible to forecast some periods of IBEX-35 index under some chosen risk aversion parameters using the SVM classifier. In Dunis *et al.* (2013b), a genetic algorithm was used to optimize the input selection procedure and the parameters of an SVM model. This methodology was applied to the 1-day-ahead forecasting and trading problem using the FTSE 100 and ASE 20 indexes. A new financial-oriented fitness function plus confirmation filters and leveraging techniques were applied to improve the performance of the overall methodology. Experimental results indicated that this method outperformed more classical techniques such as MACD and ARMA models, Bayesian predictors and higher-order neural networks.

Technical analysis

The main literature review on technical analysis is Menkhoff and Taylor (2007). Four arguments are analysed: technical analysis may exploit the influence of central bank interventions; foreign exchange markets may be characterized by not-fully-rational behaviour; technical analysis may be an efficient form of information processing; and it may provide information on the non-fundamental influences on foreign exchange movements. This study will focus on the last two arguments.

Almost all foreign exchange professional traders use technical analysis as a tool in decision making at least to some degree and the relative weight given to technical analysis as opposed to fundamental analysis rises as the trading or forecast horizon declines, as shown by Menkhoff and Taylor (2007). Technical analysis is used more than fundamental analysis; according to Taylor and Allen (1992), 90% of polled investors use it. Allen and Taylor (1990) and Taylor and Allen (1992) document systematically for the first time that technical analysis is indeed an important tool in decision making in the foreign exchange market.

There are many more recent studies which recommend the use of technical analysis for trading rules. Brock *et al.* (1992) prove that the use of moving averages and the use of supports and resistances as trading tools for the technical analysis of companies of the Dow Jones index from 1897 to 1986 generates better profitability than the buy and hold strategy for the same Index. Mills (1997) shows a similar result to the one considered in the previous article, but for the Financial Times Institute of Actuaries 30 (FT 30 index).

Kwon and Kish (2002) document that technical trading rules achieve better profitability than the buy and hold strategy in the NYSE, while Chong and Ng (2008) recommend the use of technical trading rules using the RSI and MACD indicators for the FT 30 index and they show that the use of both oscillators generates a greater profitability than the buy and hold strategy. Rosillo *et al.* (2013) recommend the use of technical trading rules using the RSI indicator for blue chips and momentum indicator for small caps and they show that the use of both oscillators generates a greater profitability.

Finally, Rodriguez-Gonzalez et al. (2011) develop systems trading with neural networks based on the RSI financial indicator.

As has been described, there are studies that support the validity of technical analysis and stochastic indicators in order to forecast stock markets, and this is the main motivation why RSI and MACD have been used as inputs of the SVM.

SIMULATION PROCEDURE

Financial returns series are mainly characterized by being zero mean, exhibiting high kurtosis and little, if any, correlation. The squares of these returns often present high correlation and persistence, which makes ARCH-type models suitable for characterizing the conditional volatility of such processes; see Engle (1982) for the seminal work, Bollerslev *et al.* (1994) for a survey on market volatility models and Engle and Patton (2001) for several extensions.

GARCH(1,1) model

The GARCH(1,1) model provides a simple representation of the main statistical characteristics of return series for a wide range of assets and, consequently, it is extensively used to model real financial time series. It serves as a natural benchmark for the forecast performance of heteroscedastic models based on ARCH. In the simplest setup, if R_t follows a GARCH(1,1) model then

$$R_t = \mu + \sigma_t \varepsilon_t$$

$$\sigma_t^2 = \omega + \alpha R_{t-1}^2 + \beta \sigma_{t-1}^2$$
(5)

where ε_t is an uncorrelated process with zero mean and unit variance. Following the definition in (equation 5), the conditional variance σ_t^2 is a stochastic process assumed to be a constant plus a weighted average of the last period's

forecast, σ_{t-1}^2 , and the last period's squared observation, R_{t-1}^2 . The parameters ω , α and β must satisfy that $\omega > 0$, α , $\beta \ge 0$ to ensure that the conditional variance is positive. The process R_t is stationary if $\alpha + \beta < 1$.

We can define the unconditional, or long-run average, variance σ^2 , to be

$$\sigma^{2} = E[\sigma_{t}^{2}] = \omega + \alpha E[R_{t-1}^{2}] + \beta E[\sigma_{t-1}^{2}] = \omega + \alpha \sigma^{2} + \beta \sigma^{2}$$
so $\sigma^{2} = \omega/(1 - \alpha - \beta)$ (6)

If we assume $\omega = \sigma^2(1 - \alpha - \beta)$ we get the desirable property that the GARCH model implicitly relies on σ^2 . Substituting in variance equation (5), we obtain

$$\sigma_t^2 = \sigma^2 (1 - \alpha - \beta) + \alpha R_{t-1}^2 + \beta \sigma_{t-1}^2 = \sigma^2 + \alpha (R_{t-1}^2 - \sigma^2) + \beta (\sigma_{t-1}^2 - \sigma^2)$$
(7)

So we can see the GARCH model as a weighted average of the long-run variance. The contemporaneous variance is the long-run average variance with one term added (subtracted) if t-1's squared return is above (below) its longrun average, and another term added (subtracted) if t-1's variance is above (below) its long-run average.

The sum $\alpha + \beta$ is named the persistence of the model. A high persistence, $\alpha + \beta$ close to 1, implies that socks that push variance away from its long-run average will persist for a long time.

The GARCH parameters are usually estimated using maximum likelihood (ML) procedures that are optimal when the data have been drawn from a Gaussian distribution. This model is usually estimated using the (conditionally) Gaussian log-likelihood function and maximizing it through an iterative algorithm such as BHHH (Berndt et al., 1974), because the functional to be maximized is nonlinear in its arguments. The estimates are called ML when the Gaussian distribution is the underlying probability density function the data have been sampled from, or quasi-ML, otherwise. Bollerslev and Wooldridge (1992) have shown the consistency of these estimates in this case, which does not ensure that for a finite sample set it is the best estimate.

The S&P 500 model

The simulated markets will be designed following the main parameters of the S&P 500 index market, in order to reflect as much as possible the real market situation. The daily data of S&P500 index are taken from 2001 to 2010, and its GARCH parameters are estimated. Then, some model parameters will be modified to create new simulated markets, trying to reproduce real market situations.

The empirical unconditional daily return variance is $\sigma_d^2 = 0.00018965$, the annual variance $\sigma_a^2 = 250 \sigma_d^2 = 0.047413$, and the annual volatility $\sigma_a = 0.21775$ (21.775%). The studied period comprises years with high volatility (40% in 2008) and other years with low volatility (10% in 2005 or 2006).

Using maximum likelihood (ML) we estimate the equation (5) GARCH model parameters. The parameter ω is calculated with the constrained condition (6), so the model matches well the unconditional variance. The S&P 500 GARCH(1,1) model in the 2001–2011 period is

$$R_t = \sigma_t \varepsilon_t$$

$$\sigma_t^2 = 3.0 \cdot 10^{-7} + 0.081 R_{t-1}^2 + 0.913 \sigma_{t-1}^2$$
(8)

The mean of the daily financial return can be neglected without significantly degrading the performance of the proposed model. In Figure 2, the original S&P 500 index and the corresponding GARCH simulated series are shown. The innovations used in the model are those corresponding to the original market data.

Simulated markets

The simulation process is based on the previous GARCH model, generating new random innovations ε_t that will determine the particular results for each stochastic process. Different kinds of simulated markets are generated by the changing of some specific parameters model. This is the procedure we are using to generate the different simulated markets.

The simulated markets can be classified in this paper by four kind of markets: bullish trend (Figure 3), bearish trend (Figure 4), high volatility (Figure 5) and low volatility (Figure 6).

Bullish trend

The market is characterized by S&P 500 parameters, but we introduced an annual drift $\mu_a = 4\%$, so the model follows a light bullish trend.

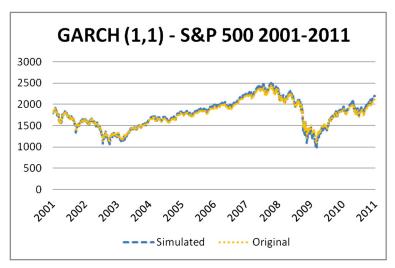


Figure 2. S&P 500 index, original and GARCH(1,1) model simulated, 2001–2011 period.

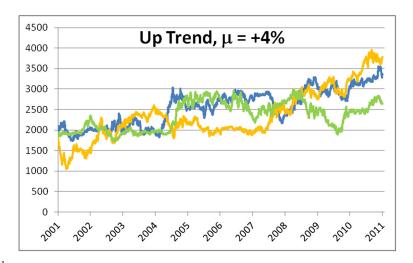


Figure 3. Bullish trend

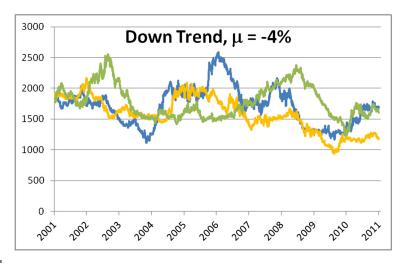


Figure 4. Bearish trend

Bearish trend

The market is characterized by S&P 500 parameters, but we introduced an annual drift $\mu_a = -4\%$, so the model follows a light bearish trend.

High volatility

The market is characterized by S&P 500 parameters, but we introduced a double annual volatility $\sigma_a = 43 \%$.



Figure 5. High volatility

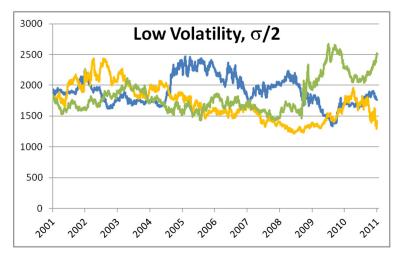


Figure 6. Low volatility

Low volatility

The market is characterized by S&P 500 parameters, but we introduced a half of the annual volatility $\sigma_a = 10.9 \%$.

SVM TRADING RULE

The design of the experiment and the trading rule is presented in this section. The algorithm has been developed in Matlab. An outline of the design of the trading rule is shown in Figure 7.

SVM inputs

The inputs of the SVM are the quantitative analysis indicators RSI and MACD. Rosillo et al. (2013) explain that RSI gets good profits in blue chips and the momentum indicator gets good profits in small caps; MACD and stochastic indicators have also been analysed over the Spanish continuous market.

Relative strength index (RSI)

This was designed by J. Welles Wilder Jr. A brief explanation of this indicator is shown below in equation (9). For further details see Welles Wilder (1978).

The RSI is an oscillator that shows the strength or speed of the asset price by comparing the individual upward or downward movements of the consecutive closing prices.

For each day, an upward change (U_t) or downward change (D_t) is calculated. 'Up days' are characterized by the daily close S_t being higher than the close of previous day S_{t-1} .

¹The software used is MATLAB 7.8.0 (R2009a).

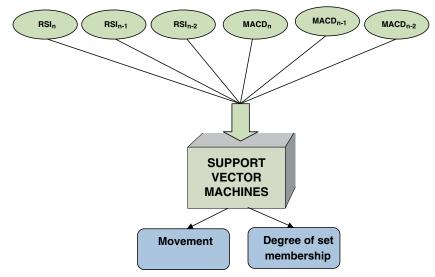


Figure 7. Design of the SVM trading rule

$$U_t = S_t - S_{t-1}$$

$$D_t = 0$$

'Down days' are characterized by the daily close being lower than the close of the previous day:

$$U_t = 0$$

$$D_t = S_{t-1} - S_t$$

The average U_t and D_t are calculated using an *n*-period exponential moving average (EMA_n). Relative strength index at time t (RSI_t) is the following ratio between 0 and 100:

$$RSI_{t} = 100 \frac{EMA_{n}^{U}}{EMA_{n}^{U} + EMA_{n}^{D}}$$

$$(9)$$

The 14-day RSI, a popular length of time utilized by traders, is also applied in this study. The RSI ranges from 0 to 100; however, the range has been normalized between -1 and +1 in order to place it in the SVM.

Moving average convergence divergence (MACD)

The MACD is designed mainly to identify trend changes. It is constructed based on moving averages and is calculated by subtracting a longer exponential moving average (EMA) from a shorter EMA. The MACD is shown in equation (10):

$$MACD(n) = EMA_k(i) - EMA_d(i)$$
(10)

where

$$EMA_n(i) = \alpha * S_i + (1 - \alpha) * EMA_n(i - 1)$$

$$\alpha = \frac{2}{1 + n}$$

where n is the number of days in the exponential average and S_i is the asset price on the ith day.

In this article, k = 12 and d = 26-day EMAs are selected, which are commonly used time spans in order to calculate MACD (Murphy, 1999).

The range of MACD has been normalized between -1 and +1 in order to use it in the SVM.

The SVM trading rule

The SVM trading rule is explained in Rosillo et al. (2014). The best configuration of the SVM is achieved by the cross-validation algorithm. In this paper, we use the SVM trading rule from Rosillo et al. (2014) to analyse which is the best simulated market where it works. The only change that has been made is in the inputs of the trading rule, where VIX is avoided because we are working in this study with simulated markets.

An SVM classifier has been chosen in order to make the quantitative decision. As explained above, SVMs are helping investors in decision making and many experiments demonstrate that SVMs generate better results than other artificial intelligence techniques.

The training period lasts 249 days and the following day (day 250) is tested by the SVM in order to ascertain whether the result is a good decision or not. Other periods such as 200 days, 300 days and 500 days have been tested as well but the best results are achieved with 250. Thus the training period is 249 days and the testing period is 1 day. In total, each experiment consists of 250 days—very similar to the length one of business year.

Although our dataset is daily, the trading strategy relies on a weekly prediction of the simulated market price move. A weekly forecast was selected as the expected price move—up or down—over a week is more significant.

The only problem that has been detected is in the situation where the SVM is being trained and data do not exist to make comparisons in order to take the decision to buy or sell. This situation occurs in the last 5 days of the training period. In this way, the study is more real. In order to fix this, four experiments have been carried out: for example, compare these 5 days with the last day known, delete these 5 days, compare these 5 days with a simple moving average of those 5 days and compare these 5 days with a weighted average of those 5 days. The best results achieved are shown in the Results section.

The following example is presented in order to clarify the previous explanation. Let us start with the following situation.

Training data are from day 1 to day 249. In Table I, data from day 241 to 250 are shown. The sell/buy decision is made by comparing the current-day value with the value 5 days ahead. In the case of days 245–249, the 5-day-ahead value is unknown. Thus, to have a value to compare with, a simple moving average with values of days 245–249 is done.

Table II would be as follows:

Simple moving average :
$$4 + 6 + 10 + 8 + 1 = 29/5 = 5.8$$

In consequence, SVM would be trained using Table II. The day 250 decision would be taken by the SVM. The SVM procedure can be described as follows.

First, the SVM analyses the inputs classified in buy or sell situations.

Second, the SVM tries to separate the different prices of the simulated markets into two classes: buying and selling situations, with the inputs mentioned earlier.

Third, the SVM uses the kernel function 'heavy tailed radial basis function' (HTRBF; equation (11)) in order to make the forecast. HTRBF was developed by Chapelle et al. (1999) and is used by the SVM-KM Matlab toolbox developed by Canu et al. (2005). The parameter C of the SVM is tested in several experiments and its optimal value is 10:

$$e^{-\rho \sum_{j} \left| x_{j}^{a} - y_{j}^{a} \right|^{b}}$$
 with $a \le 1$ and $b \le 2$ (11)

Table I. Training data with unknown values

	Training												
Day	241	242	243	244	245	246	247	248	249	250			
Daily close price	7	5	3	3	4	6	10	8	1	7			
Decision	Sell	Buy	Buy	Sell	?	?	?	?	?	?			

Table II. Training data with known values

	Training												
Day	241	242	243	244	245	246	247	248	249	250			
Daily close price	7	5	3	3	4	6	10	8	1	7			
Decision	Sell	Buy	Buy	Sell	Buy	Sell	Sell	Sell	Buy	SVM decision			

Fourth, the hit ratio is calculated for the different testing periods.

Finally, given a value of the RSI and MACD, the SVM predicts the upward or downward movement for the following week and the intensity of that movement.

SVM outputs

The outputs of the SVM are the up or down movements, expected for the index the following week, and its degree of set membership.

EXPERIMENTS

The main results are shown in this section. The SVM trading rule is benchmarked against a naïve strategy and a buy and hold strategy.

The trading strategy method is explained below. For each day, the simulated market index is bought or sold depending on the trading system recommendation. After 5 days, the reverse operation over the simulated market index is applied in order to be out of the market. This sequence is repeated every day. Five contracts can be accumulated as a maximum in the generated portfolio. Maximum drawdown, standard deviation, daily return and Sharpe ratio are calculated based on the achieved results of this strategy. The daily return is annualized, $R_a = 250 R_d$, and daily volatility is annualized as well, $\sigma_a = \sqrt{250} \sigma_d$.

and daily volatility is annualized as well, $\sigma_a = \sqrt{250}\,\sigma_d$. A simulated market is composed of 2515 days, which is 503 5-day periods (weeks). The SVM needs an initial training period of 250 days, so 440 weeks are analysed in total.

For each kind of simulated market, three different simulated markets are generated. The obtained results are calculated by an average of these three simulated markets. Thus the number of experiments in this study is 1320 in each kind of simulated market.

Benchmark models

In this paper, we benchmark our SVM model with two traditional strategies: a buy and hold strategy (BH) and a naïve strategy (N). For the sake of simplicity, we do not extend the analysis to other forecasting techniques, as autoregressive models or neural networks, because the goal of this paper is to find which kind of simulated market is more predictable with the SVM strategy.

The performance of each strategy is evaluated in terms of trading performance via a simulated trading strategy.

Buy and hold

The BH strategy consists in buying the spot and holding the investment for the specified time without further decisions. In our case the investment period is 5 days. So we buy $S_{t-5}, ..., S_{t-1}$ and sell $S_t, ..., S_{t+4}$.

Naïve strategy

The N strategy takes the most recent period change as the best prediction of future change, i.e. a simple random walk. The model is defined by

$$\hat{R}_{t+1} = R_t$$

where the forecast rate of return \hat{R}_{t+1} is based on the actual rate of return R_t .

As we are trading on a 5-day periods, we have implemented this strategy buying the market S_{t-5} if $S_{t-6} > S_{t-7}$ or selling the market S_{t-5} when $S_{t-6} < S_{t-7}$, and doing the reverse operation 5 days later.

Experimental results

The obtained results are shown in Tables III-VI. Each table corresponds to a kind of simulated market.

In the first set of columns the achieved points are shown with each strategy, in the second set of columns the annualized return is shown, in the third set of columns the annualized standard deviation of daily returns, in the fourth set of columns the Sharpe ratio and in the fifth set of columns the maximum drawdown. On the left side of the table the label of the three simulated markets can be seen, and the last row shows the average of the results.

The highlighted numbers present the best result of each strategy for a determinate indicator.

Table III explains the results for a bullish simulated market. BH achieves 774.8 points, SVM strategy achieves 60.8 points and N strategy -403.9 points. The index points are equivalent in terms of average annual returns: Buy and Hold strategy (6.4%), SVM strategy (0.57%) and Naïve strategy (-3.2%). The annual volatility is not too high in the investments and takes 4.5% for BH, 6% for SVM strategy and 7% for N strategy.

The BH strategy is not a good benchmark in this kind of market because we are analysing a bullish trend, so BH beats the other two strategies. SVM strategy improves the results obtained from the N strategy, particularly; SVM

Table III. Bullish trend results

	SP points (annual)			$R_{\rm a}~(\%)$			$\sigma_{\rm a}\left(\% ight)$			$SR = R_a/\sigma_a$			MDD (%, annual)		
Bullish trend simulations	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N
Exp. 1 Exp. 2 Exp. 3 Mean	337.0 -303.3 148.8 60.8	800.1 1147.3 377.1 774.8	-425.5 -592.5 -193.8 -403.9	2.6 -1.8 0.9 0.57	6.4 9.3 3.4 6.4	-3.6 -4.5 -1.3 -3.2	6.1 6.1 5.8 6.0	4.6 4.4	7.1 7.1 6.9 7.0	0.4 -0.3 0.2 0.10	1.4 2.0 0.8 1.4	-0.5 -0.6 -0.2 -0.5	33.9 36.1 33.2 34.4	36.8 35.6 36.6 36.3	38.1 37.4 35.8 37.1

Note: The bold entries mean the best result achieved for each financial ratio. SP, points achieved with each strategy; Ra, annualized return; $\sigma_{\rm a}$, annualized standard deviation of daily returns, SR, Sharpe ratio; MDD, maximum drawdown.

Table IV. Bearish trend results

	SP points (annual)				$R_{\rm a}~(\%)$		σ	a (%)		SI	$R = R_a/c$	r _a	MDD	D (%, annual)			
Bearish trend simulations	SVM	ВН	N	SVM	ВН	N	SVM	вн	N	SVM	ВН	N	SVM	ВН	N		
Exp. 1 Exp. 2	153.1 104.8	-389.9		3.0	-4.6	-3.5 -1.5	5.8		6.9	0.4 0.1	0.0 -1.0	-0.2	38.2 34.1	44.4 39.7	41.7 35.7		
Exp. 3 Mean	-9.0 83.0	-241.3 -216.1	100.0	1.2 1.63	-2.3 -2.2	-1.8 -2.3	5.3 6.0	4.1 4.6	6.2 7.0	0.2 0.27	-0.5 -0.5	-0.3 -0.3	30.8 34.4	36.3 40.2	33.0 36.8		

Note: The bold entries mean the best result achieved for each financial ratio. SP, points achieved with each strategy; Ra, annualized return; σ_a , annualized standard deviation of daily returns, SR, Sharpe ratio; MDD, maximum drawdown.

Table V. High-volatility results

	SP points (annual)			$R_{\rm a}~(\%)$			σ _a (%)			$SR = R_a/\sigma_a$			MDD (%, annual)		
High-volatility simulations	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N
Exp. 1	-284.8	655.8	297.0	-5.9	7.3	1.1	11.1	8.2	12.9	-0.5	0.9	0.1	65.1	70.1	68.6
Exp. 2	2599.4	22.8	789.5	11.0	2.3	4.3	14.4	10.7	16.8	0.8	0.2	0.3	76.1	92.4	88.8
Exp. 3	288.9	-755.5	-458.1	8.0	-16.8	-10.1	12.5	9.8	14.6	0.6	-1.7	-0.7	66.0	87.5	80.0
Mean	867.8	-25.6	209.5	4.37	-2.4	-1.6	12.6	9.6	14.8	0.35	-0.3	-0.1	69.1	83.3	79.1

Note: The bold entries mean the best result achieved for each financial ratio. SP, points achieved with each strategy; Ra, annualized return; σ_a , annualized standard deviation of daily returns, SR, Sharpe ratio; MDD, maximum drawdown.

Table VI. Low-volatility results

	SP points (annual)				$R_{\rm a}~(\%)$			$\sigma_{\mathrm{a}}\left(\% ight)$			$R = R_a/\sigma$	a	MDD (%, annual)		
Low-volatility simulations	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N	SVM	ВН	N
Exp. 1	145.2	-43.9		1.4		-0.8	2.9	2.2		0.5	-0.2		16.6	19.1	17.9
Exp. 2 Exp. 3	9.1 -111.8	-181.8 143.1	-3.8 33.8	$0.1 \\ -1.4$	-1.9	-0.2 0.3	2.7 2.8		3.2	$0.0 \\ -0.5$	$-1.0 \\ 0.8$	$-0.1 \\ 0.1$	15.5 16.2	18.6 17.8	16.4 17.2
Mean Mean	14.2	-27.5	-18.2	0.05			2.8	2.1			-0.1		16.1	18.5	17.2

Note: The bold entries mean the best result achieved for each financial ratio. SP, points achieved with each strategy; Ra, annualized return; $\sigma_{\rm a}$, annualized standard deviation of daily returns, SR, Sharpe ratio; MDD, maximum drawdown.

strategy has a positive Sharpe ratio, whereas the N strategy has a negative Sharpe ratio. It is worth noting that SVM strategy achieves 60.8 points and N strategy achieves -403.9 points.

In Table IV the results for the bearish simulated markets are shown. On the one hand, the greater annual mean return is 1.63%, which corresponds to the SVM strategy. On the other hand, BH strategy and N strategy obtain a negative annual return. We can also highlight that the best results of maximum drawdown and Sharpe ratio are obtained with the SVM strategy.

In Table V we show the results for the high volatility simulated markets. This kind of market is probably more difficult to forecast. The SVM annual return is 4.37%, which is a better result than the other models. The lowest maximum drawdown is obtained by the SVM strategy, at 69.1%. Rosillo *et al.* (2014) use the volatility index (VIX) to forecast the S&P 500 like an input for the SVM strategy to improve the results. This is a simulated market, so in this situation it is not possible to use other indexes to improve results, although SVM strategy beats the other two strategies (BH and N strategy).

In Table VI we show the results for the low-volatility market. The mean annual return is low in the three strategies, but only SVM strategy achieves profits. The lowest mean annual volatility is achieved by BH with 2.1%, but the best maximum drawdown and the highest Sharpe ratio are achieved by SVM strategy with values of 16.1% and 0.02.

CONCLUSIONS

The aim of this paper was to analyse in which kind of simulated market (bullish trend, bearish trend, high volatility and low volatility) the SVM trading strategy is useful. We have researched the profitability of simple technical trading rules based on SVM models.

An SVM algorithm has been chosen in order to make a quantitative decision. The main inputs of this algorithm are RSI and MACD. The outputs are the up or down movements expected for the index weekly change, and its degree of set membership (bullish or bearish class).

Three trading strategies are compared, holding a maximum of five contracts at the same time in order to analyse the relevance of SVM in the different simulated markets during the quantitative decision making, although the most important thing is to compare the results of the SVM strategy in the four simulated markets.

Overall, this study shows that SVM strategy produces better results than N strategy or BH strategy in bearish markets, high-volatility markets and low-volatility markets. However, BH strategy achieves higher returns in bullish markets; this situation is logical because BH always earns more points in bullish markets, so it is not a good benchmark for bullish movements. If SVM strategy and N strategy are compared for bullish markets, SVM strategy beats N strategy, as can be seen in the results section. These results are in line with Fernández Rodríguez *et al.* (2000) when applying nonlinear predictors to the Spanish Stock Market Index.

It is noteworthy that SVM strategy achieves better results in high-volatility markets than other kinds of markets. These results are in line with Rosillo *et al.* (2014), who use VIX like an input of the SVM to forecast the S&P 500. The SVM strategy allows a reduction in maximum drawdown and a reduction in the annualized standard deviation. Also, the Sharpe ratio is improved using SVMs. Furthermore, SVM trading strategy reduces the global risk of the investment.

The SVM strategy analysed would be useful in high-volatility markets. The use of this algorithm would generate profits during financial crises.

However, some limitations are found in our work. For example, the algorithm is not able to achieve interesting results in low-volatility markets. This could be due to the fact that SVM models works better in markets with high volatility because the price does not change significantly in low-volatility markets.

As further work, it would be advisable to use a trend indicator in order to determine when the market is going to be immersed in a high-volatility movement. Also, it would be interesting to combine this algorithm with an expert system in order to avoid days which are expected to be extremely volatile, such as a political crisis or FED decisions.

Another research possibility would be to use eXtensible Business Reporting Language (XBRL). XBRL is a freely available and global standard for exchanging business information. XBRL allows us to obtain more information and to calculate more ratios in fundamental analysis for indexes and companies. It would be interesting to combine different fundamental analysis indicators to improve the results.

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