Machine Learning

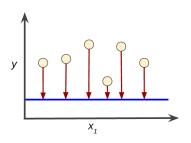
Pawel Wocjan

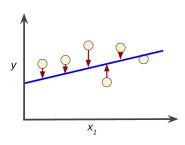
University of Central Florida

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- ➤ **Training** a model simply means determining good values for all the weights and the bias that minimize the loss by examining many examples.
- ► Loss is the penalty for a bad prediction, that it, loss is a number indicating how bad the model's prediction was on a single example.
 - If the model's prediction is perfect, the loss is zero; otherwise, the loss is greater.
- ► The goal of training is to find a set of weights and biases that have low loss, on average, across all examples.
- ► This process is called **empirical risk minimization**.

- ► For example, the figure below shows a high loss model on the left and a low loss model on the right.
 - ► The red arrows represent loss.
 - ► The blue lines represent predictions.





- ▶ Notice that the arrows in the left plot are much longer than their counterparts in the right plot.
- ► Clearly, the line in the right plot is a much better predictive model than the line in the left plot.
- ▶ The linear regression models we examine here use a loss function called **squared loss** (also known as L_2 loss).

► The squared loss for a single example the difference between the label (observation) y and the prediction \hat{y} :

$$(y-\hat{y})^2$$

▶ Mean square error (MSE) is the average squared loss per example over the whole dataset

$$MSE = \frac{1}{m} \sum_{i=1}^{m} (y^{(i)} - \hat{y}^{(i)})^2$$

- ▶ *m* is the number of examples.
- $\mathbf{x}^{(i)} = (x_1^{(i)}, \dots, x_n^{(i)})$ and $y^{(i)}$ are the features and the label of the *i*th example.
- \triangleright $\hat{y}^{(i)}$ is the prediction of the model. More formally,

$$\hat{y}^{(i)} = f_{\theta}(x^{(i)})$$

where $\theta = (w_1, \dots, w_n, b)$ are the parameters (weights and bias) of the model.

► Although MSE is commonly-used in machine learning, it is neither the only practical loss function nor the best loss function for all circumstances.

Key Terms

- ▶ empirical risk minimization
- ► loss
- mean squared error
- squared loss
- ► training